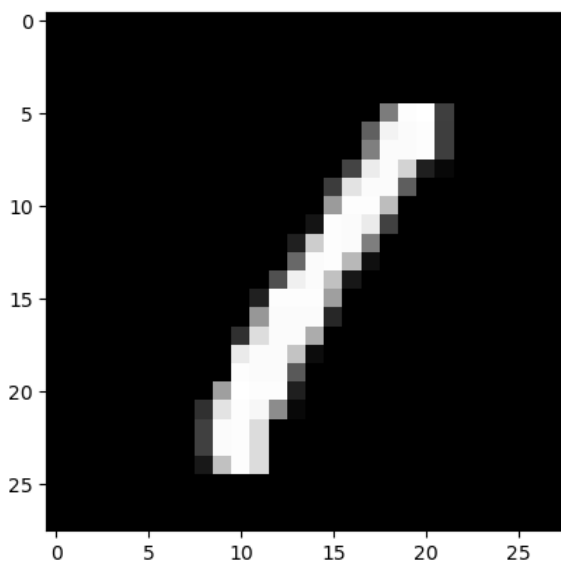


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Registration no:	24MDT0184
Course Name:	Deep Learning Lab
Course Code:	PMDS603P
Experiment:	3
Date:	31 July,2025

**Question1.** Today, we will try to recall the work done in the previous lab first. The second problem attempted in the last lab was to use MNIST dataset which contains handwritten numbers (their images) from 0 to 9 digits. First try to fit a simple neural network model. Let us import the necessary modules required for this along with the dataset. It contains 70000 handwritten images of digits from 0 to 9. So its a 10 class classification problem. Lets try to create a model that can do the classification task.

```
In [1]: import keras
from keras.datasets import mnist
from keras.models import Sequential
from keras.layers import Dense,Dropout,Flatten
from keras.optimizers import SGD
import matplotlib.pyplot as plt

import warnings
warnings.filterwarnings('ignore')
batch_size = 128
num_classes = 10
epochs = 50
(x_train,y_train), (x_test,y_test) = mnist.load_data()
plt.imshow(x_train[3],cmap='gray')
plt.show()
```



```
In [2]: x_train = x_train.reshape(60000,784)
x_test = x_test.reshape(10000,784)
x_train = x_train.astype('float32')
x_test = x_test.astype('float32')
x_train/=255
x_test/=255
print(x_train.shape[0],'train samples')
print(x_test.shape[0],'test samples')
y_train = keras.utils.to_categorical(y_train,num_classes)
y_test_ = keras.utils.to_categorical(y_test,num_classes)
```

60000 train samples  
10000 test samples

### Without dropout with relu activation

```
In [3]: model = Sequential()
model.add(Dense(512, activation = 'relu',input_shape = (784,)))
model.add(Dense(512, activation = 'relu'))
```

```
model.add(Dense(10, activation = 'softmax'))
model.summary()
sgd1 = SGD(learning_rate=0.01)
model.compile(loss = 'categorical_crossentropy', optimizer = sgd1, metrics = ['accuracy'])
history = model.fit(x_train,y_train,batch_size=batch_size,epochs=epochs,verbose=1,validation_data=(x_test,y_test_))
```

Model: "sequential"

Layer (type)	Output Shape	Param #
dense (Dense)	(None, 512)	401,920
dense_1 (Dense)	(None, 512)	262,656
dense_2 (Dense)	(None, 10)	5,130

Total params: 669,706 (2.55 MB)

Trainable params: 669,706 (2.55 MB)

Non-trainable params: 0 (0.00 B)

Epoch 1/50  
469/469 ————— 2s 4ms/step - accuracy: 0.6002 - loss: 1.6090 - val\_accuracy: 0.8730 - val\_loss: 0.5244  
Epoch 2/50  
469/469 ————— 2s 3ms/step - accuracy: 0.8790 - loss: 0.4862 - val\_accuracy: 0.9014 - val\_loss: 0.3686  
Epoch 3/50  
469/469 ————— 2s 3ms/step - accuracy: 0.8980 - loss: 0.3731 - val\_accuracy: 0.9117 - val\_loss: 0.3183  
Epoch 4/50  
469/469 ————— 2s 3ms/step - accuracy: 0.9079 - loss: 0.3255 - val\_accuracy: 0.9185 - val\_loss: 0.2891  
Epoch 5/50  
469/469 ————— 2s 4ms/step - accuracy: 0.9167 - loss: 0.2995 - val\_accuracy: 0.9244 - val\_loss: 0.2702  
Epoch 6/50  
469/469 ————— 2s 4ms/step - accuracy: 0.9215 - loss: 0.2764 - val\_accuracy: 0.9267 - val\_loss: 0.2539  
Epoch 7/50  
469/469 ————— 2s 4ms/step - accuracy: 0.9277 - loss: 0.2582 - val\_accuracy: 0.9320 - val\_loss: 0.2401  
Epoch 8/50  
469/469 ————— 2s 4ms/step - accuracy: 0.9337 - loss: 0.2403 - val\_accuracy: 0.9344 - val\_loss: 0.2297  
Epoch 9/50  
469/469 ————— 2s 4ms/step - accuracy: 0.9353 - loss: 0.2265 - val\_accuracy: 0.9387 - val\_loss: 0.2193  
Epoch 10/50  
469/469 ————— 2s 4ms/step - accuracy: 0.9371 - loss: 0.2223 - val\_accuracy: 0.9406 - val\_loss: 0.2085  
Epoch 11/50  
469/469 ————— 2s 4ms/step - accuracy: 0.9402 - loss: 0.2089 - val\_accuracy: 0.9426 - val\_loss: 0.2010  
Epoch 12/50  
469/469 ————— 2s 4ms/step - accuracy: 0.9436 - loss: 0.2028 - val\_accuracy: 0.9454 - val\_loss: 0.1931  
Epoch 13/50  
469/469 ————— 2s 3ms/step - accuracy: 0.9456 - loss: 0.1934 - val\_accuracy: 0.9459 - val\_loss: 0.1884  
Epoch 14/50  
469/469 ————— 2s 3ms/step - accuracy: 0.9469 - loss: 0.1909 - val\_accuracy: 0.9480 - val\_loss: 0.1795  
Epoch 15/50  
469/469 ————— 2s 3ms/step - accuracy: 0.9503 - loss: 0.1800 - val\_accuracy: 0.9504 - val\_loss: 0.1750  
Epoch 16/50  
469/469 ————— 2s 3ms/step - accuracy: 0.9528 - loss: 0.1709 - val\_accuracy: 0.9507 - val\_loss: 0.1692  
Epoch 17/50  
469/469 ————— 2s 3ms/step - accuracy: 0.9532 - loss: 0.1643 - val\_accuracy: 0.9525 - val\_loss: 0.1653  
Epoch 18/50  
469/469 ————— 2s 3ms/step - accuracy: 0.9539 - loss: 0.1617 - val\_accuracy: 0.9554 - val\_loss: 0.1599  
Epoch 19/50  
469/469 ————— 2s 3ms/step - accuracy: 0.9575 - loss: 0.1556 - val\_accuracy: 0.9555 - val\_loss: 0.1544  
Epoch 20/50  
469/469 ————— 2s 3ms/step - accuracy: 0.9570 - loss: 0.1519 - val\_accuracy: 0.9563 - val\_loss: 0.1502  
Epoch 21/50  
469/469 ————— 2s 3ms/step - accuracy: 0.9601 - loss: 0.1456 - val\_accuracy: 0.9566 - val\_loss: 0.1495  
Epoch 22/50  
469/469 ————— 2s 3ms/step - accuracy: 0.9608 - loss: 0.1404 - val\_accuracy: 0.9590 - val\_loss: 0.1433  
Epoch 23/50  
469/469 ————— 2s 3ms/step - accuracy: 0.9634 - loss: 0.1343 - val\_accuracy: 0.9592 - val\_loss: 0.1394  
Epoch 24/50  
469/469 ————— 2s 3ms/step - accuracy: 0.9629 - loss: 0.1343 - val\_accuracy: 0.9588 - val\_loss: 0.1374  
Epoch 25/50  
469/469 ————— 2s 3ms/step - accuracy: 0.9645 - loss: 0.1277 - val\_accuracy: 0.9607 - val\_loss: 0.1341  
Epoch 26/50  
469/469 ————— 2s 3ms/step - accuracy: 0.9654 - loss: 0.1244 - val\_accuracy: 0.9610 - val\_loss: 0.1301  
Epoch 27/50  
469/469 ————— 2s 3ms/step - accuracy: 0.9661 - loss: 0.1199 - val\_accuracy: 0.9625 - val\_loss: 0.1289  
Epoch 28/50  
469/469 ————— 2s 3ms/step - accuracy: 0.9672 - loss: 0.1170 - val\_accuracy: 0.9617 - val\_loss: 0.1262  
Epoch 29/50  
469/469 ————— 2s 3ms/step - accuracy: 0.9689 - loss: 0.1140 - val\_accuracy: 0.9636 - val\_loss: 0.1239  
Epoch 30/50  
469/469 ————— 2s 3ms/step - accuracy: 0.9685 - loss: 0.1148 - val\_accuracy: 0.9638 - val\_loss: 0.1207  
Epoch 31/50  
469/469 ————— 2s 3ms/step - accuracy: 0.9708 - loss: 0.1069 - val\_accuracy: 0.9641 - val\_loss: 0.1195  
Epoch 32/50  
469/469 ————— 2s 3ms/step - accuracy: 0.9717 - loss: 0.1042 - val\_accuracy: 0.9650 - val\_loss: 0.1164  
Epoch 33/50  
469/469 ————— 2s 3ms/step - accuracy: 0.9725 - loss: 0.1000 - val\_accuracy: 0.9664 - val\_loss: 0.1135  
Epoch 34/50  
469/469 ————— 2s 3ms/step - accuracy: 0.9715 - loss: 0.1018 - val\_accuracy: 0.9662 - val\_loss: 0.1129  
Epoch 35/50  
469/469 ————— 2s 3ms/step - accuracy: 0.9734 - loss: 0.0983 - val\_accuracy: 0.9667 - val\_loss: 0.1102  
Epoch 36/50  
469/469 ————— 2s 3ms/step - accuracy: 0.9731 - loss: 0.0988 - val\_accuracy: 0.9671 - val\_loss: 0.1090  
Epoch 37/50  
469/469 ————— 2s 3ms/step - accuracy: 0.9729 - loss: 0.0969 - val\_accuracy: 0.9667 - val\_loss: 0.1085  
Epoch 38/50  
469/469 ————— 2s 3ms/step - accuracy: 0.9748 - loss: 0.0924 - val\_accuracy: 0.9679 - val\_loss: 0.1065  
Epoch 39/50  
469/469 ————— 2s 3ms/step - accuracy: 0.9748 - loss: 0.0902 - val\_accuracy: 0.9694 - val\_loss: 0.1048  
Epoch 40/50  
469/469 ————— 2s 3ms/step - accuracy: 0.9766 - loss: 0.0863 - val\_accuracy: 0.9691 - val\_loss: 0.1043  
Epoch 41/50  
469/469 ————— 2s 3ms/step - accuracy: 0.9767 - loss: 0.0853 - val\_accuracy: 0.9695 - val\_loss: 0.1031  
Epoch 42/50  
469/469 ————— 2s 3ms/step - accuracy: 0.9776 - loss: 0.0841 - val\_accuracy: 0.9696 - val\_loss: 0.1002  
Epoch 43/50  
469/469 ————— 2s 3ms/step - accuracy: 0.9774 - loss: 0.0822 - val\_accuracy: 0.9701 - val\_loss: 0.0997

Epoch 44/50  
 469/469 ————— 2s 3ms/step - accuracy: 0.9778 - loss: 0.0818 - val\_accuracy: 0.9705 - val\_loss: 0.0974  
 Epoch 45/50  
 469/469 ————— 2s 3ms/step - accuracy: 0.9788 - loss: 0.0764 - val\_accuracy: 0.9717 - val\_loss: 0.0967  
 Epoch 46/50  
 469/469 ————— 2s 3ms/step - accuracy: 0.9797 - loss: 0.0754 - val\_accuracy: 0.9715 - val\_loss: 0.0957  
 Epoch 47/50  
 469/469 ————— 2s 3ms/step - accuracy: 0.9799 - loss: 0.0731 - val\_accuracy: 0.9710 - val\_loss: 0.0944  
 Epoch 48/50  
 469/469 ————— 2s 3ms/step - accuracy: 0.9794 - loss: 0.0758 - val\_accuracy: 0.9724 - val\_loss: 0.0925  
 Epoch 49/50  
 469/469 ————— 2s 3ms/step - accuracy: 0.9797 - loss: 0.0748 - val\_accuracy: 0.9719 - val\_loss: 0.0932  
 Epoch 50/50  
 469/469 ————— 2s 3ms/step - accuracy: 0.9817 - loss: 0.0674 - val\_accuracy: 0.9723 - val\_loss: 0.0914

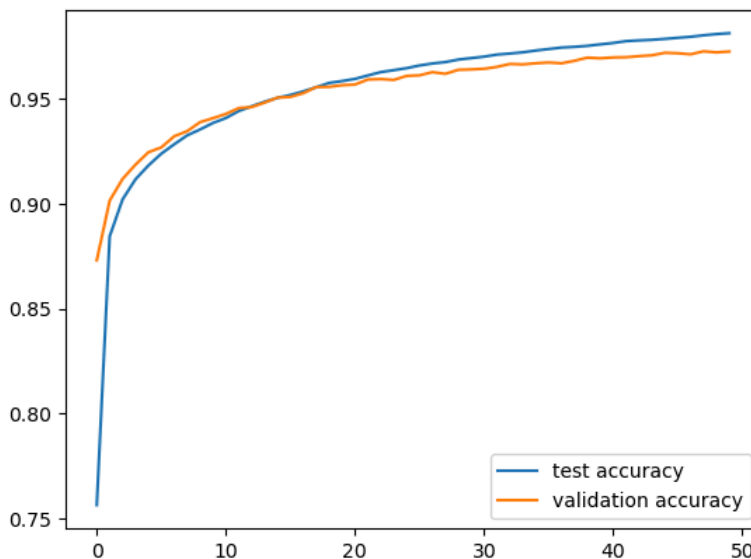
```
In [4]: y_prob = model.predict(x_test)
y_pred = y_prob.argmax(axis = 1)
from sklearn.metrics import accuracy_score
print(f"Accuracy:{accuracy_score(y_test,y_pred)*100:.2f}%")
```

313/313 ————— 0s 1ms/step  
 Accuracy:97.23%

```
In [5]: score = model.evaluate(x_test,y_test_, verbose = 1)
print("Test loss:", score[0])
print(f"Test Accuracy:{score[1]*100:.2f}%")
```

313/313 ————— 0s 1ms/step - accuracy: 0.9669 - loss: 0.1094  
 Test loss: 0.09142811596393585  
 Test Accuracy:97.23%

```
In [6]: plt.plot(history.history['accuracy'],label='test accuracy')
plt.plot(history.history['val_accuracy'],label='validation accuracy')
plt.legend()
plt.show()
```



## Without dropout using sigmoid activation

```
In [7]: model = Sequential()
model.add(Dense(512, activation = 'sigmoid',input_shape = (784,)))
model.add(Dense(512, activation = 'sigmoid'))
model.add(Dense(10, activation = 'softmax'))
model.summary()
sgd1 = SGD(learning_rate=0.01)
model.compile(loss = 'categorical_crossentropy', optimizer = sgd1, metrics = ['accuracy'])
history = model.fit(x_train,y_train,batch_size=batch_size,epochs=epochs,verbose=1,validation_data=(x_test,y_test_))
score = model.evaluate(x_test,y_test_, verbose = 1)
print("Test loss:", score[0])
print(f"Test Accuracy:{score[1]*100:.2f}%")
```

Model: "sequential\_1"

Layer (type)	Output Shape	Param #
dense_3 (Dense)	(None, 512)	401,920
dense_4 (Dense)	(None, 512)	262,656
dense_5 (Dense)	(None, 10)	5,130

Total params: 669,706 (2.55 MB)  
Trainable params: 669,706 (2.55 MB)  
Non-trainable params: 0 (0.00 B)

Epoch 1/50  
469/469 ————— 2s 4ms/step - accuracy: 0.1514 - loss: 2.3069 - val\_accuracy: 0.2339 - val\_loss: 2.2321  
Epoch 2/50  
469/469 ————— 2s 3ms/step - accuracy: 0.3451 - loss: 2.2118 - val\_accuracy: 0.4213 - val\_loss: 2.1418  
Epoch 3/50  
469/469 ————— 2s 3ms/step - accuracy: 0.4897 - loss: 2.1128 - val\_accuracy: 0.4130 - val\_loss: 2.0063  
Epoch 4/50  
469/469 ————— 2s 3ms/step - accuracy: 0.5633 - loss: 1.9659 - val\_accuracy: 0.5803 - val\_loss: 1.8083  
Epoch 5/50  
469/469 ————— 2s 3ms/step - accuracy: 0.6322 - loss: 1.7591 - val\_accuracy: 0.6437 - val\_loss: 1.5656  
Epoch 6/50  
469/469 ————— 2s 3ms/step - accuracy: 0.6756 - loss: 1.5155 - val\_accuracy: 0.6589 - val\_loss: 1.3284  
Epoch 7/50  
469/469 ————— 2s 3ms/step - accuracy: 0.7187 - loss: 1.2881 - val\_accuracy: 0.7564 - val\_loss: 1.1290  
Epoch 8/50  
469/469 ————— 2s 3ms/step - accuracy: 0.7550 - loss: 1.1044 - val\_accuracy: 0.7752 - val\_loss: 0.9824  
Epoch 9/50  
469/469 ————— 2s 3ms/step - accuracy: 0.7742 - loss: 0.9683 - val\_accuracy: 0.8056 - val\_loss: 0.8730  
Epoch 10/50  
469/469 ————— 2s 3ms/step - accuracy: 0.7956 - loss: 0.8654 - val\_accuracy: 0.8137 - val\_loss: 0.7864  
Epoch 11/50  
469/469 ————— 2s 3ms/step - accuracy: 0.8099 - loss: 0.7868 - val\_accuracy: 0.8183 - val\_loss: 0.7203  
Epoch 12/50  
469/469 ————— 2s 4ms/step - accuracy: 0.8194 - loss: 0.7253 - val\_accuracy: 0.8313 - val\_loss: 0.6665  
Epoch 13/50  
469/469 ————— 2s 3ms/step - accuracy: 0.8328 - loss: 0.6662 - val\_accuracy: 0.8413 - val\_loss: 0.6221  
Epoch 14/50  
469/469 ————— 2s 3ms/step - accuracy: 0.8393 - loss: 0.6276 - val\_accuracy: 0.8474 - val\_loss: 0.5851  
Epoch 15/50  
469/469 ————— 2s 4ms/step - accuracy: 0.8457 - loss: 0.5921 - val\_accuracy: 0.8542 - val\_loss: 0.5548  
Epoch 16/50  
469/469 ————— 2s 3ms/step - accuracy: 0.8512 - loss: 0.5665 - val\_accuracy: 0.8595 - val\_loss: 0.5290  
Epoch 17/50  
469/469 ————— 2s 3ms/step - accuracy: 0.8597 - loss: 0.5322 - val\_accuracy: 0.8650 - val\_loss: 0.5060  
Epoch 18/50  
469/469 ————— 2s 3ms/step - accuracy: 0.8651 - loss: 0.5139 - val\_accuracy: 0.8680 - val\_loss: 0.4884  
Epoch 19/50  
469/469 ————— 2s 3ms/step - accuracy: 0.8695 - loss: 0.4909 - val\_accuracy: 0.8726 - val\_loss: 0.4701  
Epoch 20/50  
469/469 ————— 2s 3ms/step - accuracy: 0.8703 - loss: 0.4848 - val\_accuracy: 0.8771 - val\_loss: 0.4561  
Epoch 21/50  
469/469 ————— 2s 3ms/step - accuracy: 0.8742 - loss: 0.4635 - val\_accuracy: 0.8792 - val\_loss: 0.4429  
Epoch 22/50  
469/469 ————— 2s 3ms/step - accuracy: 0.8756 - loss: 0.4547 - val\_accuracy: 0.8814 - val\_loss: 0.4321  
Epoch 23/50  
469/469 ————— 2s 3ms/step - accuracy: 0.8795 - loss: 0.4461 - val\_accuracy: 0.8842 - val\_loss: 0.4213  
Epoch 24/50  
469/469 ————— 2s 3ms/step - accuracy: 0.8800 - loss: 0.4385 - val\_accuracy: 0.8853 - val\_loss: 0.4126  
Epoch 25/50  
469/469 ————— 2s 3ms/step - accuracy: 0.8838 - loss: 0.4228 - val\_accuracy: 0.8874 - val\_loss: 0.4051  
Epoch 26/50  
469/469 ————— 2s 3ms/step - accuracy: 0.8880 - loss: 0.4116 - val\_accuracy: 0.8891 - val\_loss: 0.3973  
Epoch 27/50  
469/469 ————— 2s 4ms/step - accuracy: 0.8880 - loss: 0.4082 - val\_accuracy: 0.8923 - val\_loss: 0.3904  
Epoch 28/50  
469/469 ————— 2s 4ms/step - accuracy: 0.8882 - loss: 0.4033 - val\_accuracy: 0.8950 - val\_loss: 0.3835  
Epoch 29/50  
469/469 ————— 2s 4ms/step - accuracy: 0.8911 - loss: 0.3952 - val\_accuracy: 0.8946 - val\_loss: 0.3789  
Epoch 30/50  
469/469 ————— 2s 4ms/step - accuracy: 0.8910 - loss: 0.3904 - val\_accuracy: 0.8954 - val\_loss: 0.3732  
Epoch 31/50  
469/469 ————— 2s 4ms/step - accuracy: 0.8928 - loss: 0.3825 - val\_accuracy: 0.8967 - val\_loss: 0.3691  
Epoch 32/50  
469/469 ————— 2s 4ms/step - accuracy: 0.8932 - loss: 0.3835 - val\_accuracy: 0.8969 - val\_loss: 0.3647  
Epoch 33/50  
469/469 ————— 2s 3ms/step - accuracy: 0.8961 - loss: 0.3772 - val\_accuracy: 0.9002 - val\_loss: 0.3610  
Epoch 34/50  
469/469 ————— 2s 4ms/step - accuracy: 0.8963 - loss: 0.3767 - val\_accuracy: 0.8990 - val\_loss: 0.3560  
Epoch 35/50  
469/469 ————— 2s 3ms/step - accuracy: 0.8957 - loss: 0.3730 - val\_accuracy: 0.9001 - val\_loss: 0.3533  
Epoch 36/50  
469/469 ————— 2s 3ms/step - accuracy: 0.8957 - loss: 0.3672 - val\_accuracy: 0.9004 - val\_loss: 0.3501  
Epoch 37/50  
469/469 ————— 2s 3ms/step - accuracy: 0.8993 - loss: 0.3581 - val\_accuracy: 0.8995 - val\_loss: 0.3481  
Epoch 38/50  
469/469 ————— 2s 3ms/step - accuracy: 0.8993 - loss: 0.3598 - val\_accuracy: 0.9015 - val\_loss: 0.3437  
Epoch 39/50  
469/469 ————— 2s 3ms/step - accuracy: 0.8979 - loss: 0.3590 - val\_accuracy: 0.9019 - val\_loss: 0.3415  
Epoch 40/50  
469/469 ————— 2s 3ms/step - accuracy: 0.9009 - loss: 0.3501 - val\_accuracy: 0.9016 - val\_loss: 0.3387  
Epoch 41/50  
469/469 ————— 2s 3ms/step - accuracy: 0.8989 - loss: 0.3580 - val\_accuracy: 0.9028 - val\_loss: 0.3360  
Epoch 42/50  
469/469 ————— 2s 3ms/step - accuracy: 0.9012 - loss: 0.3505 - val\_accuracy: 0.9043 - val\_loss: 0.3331  
Epoch 43/50  
469/469 ————— 2s 3ms/step - accuracy: 0.9002 - loss: 0.3478 - val\_accuracy: 0.9042 - val\_loss: 0.3321

Epoch 44/50  
 469/469 ————— 2s 3ms/step - accuracy: 0.9023 - loss: 0.3449 - val\_accuracy: 0.9041 - val\_loss: 0.3292  
 Epoch 45/50  
 469/469 ————— 2s 3ms/step - accuracy: 0.9025 - loss: 0.3400 - val\_accuracy: 0.9053 - val\_loss: 0.3275  
 Epoch 46/50  
 469/469 ————— 2s 3ms/step - accuracy: 0.9044 - loss: 0.3356 - val\_accuracy: 0.9059 - val\_loss: 0.3253  
 Epoch 47/50  
 469/469 ————— 2s 3ms/step - accuracy: 0.9032 - loss: 0.3348 - val\_accuracy: 0.9059 - val\_loss: 0.3228  
 Epoch 48/50  
 469/469 ————— 2s 3ms/step - accuracy: 0.9061 - loss: 0.3352 - val\_accuracy: 0.9070 - val\_loss: 0.3213  
 Epoch 49/50  
 469/469 ————— 2s 3ms/step - accuracy: 0.9042 - loss: 0.3342 - val\_accuracy: 0.9069 - val\_loss: 0.3201  
 Epoch 50/50  
 469/469 ————— 2s 4ms/step - accuracy: 0.9038 - loss: 0.3339 - val\_accuracy: 0.9077 - val\_loss: 0.3187  
 313/313 ————— 0s 1ms/step - accuracy: 0.8962 - loss: 0.3621  
 Test loss: 0.3186941146850586  
 Test Accuracy:90.77%

## Q2- Regularization Techniques

### Using dropout(0.2)

```
In [8]: model = Sequential()
model.add(Dense(512, activation = 'relu',input_shape = (784,)))
model.add(Dropout(0.2))
model.add(Dense(512, activation = 'relu'))
model.add(Dropout(0.2))
model.add(Dense(10, activation = 'softmax'))
model.summary()
sgd1 = SGD(learning_rate=0.01)
model.compile(loss = 'categorical_crossentropy', optimizer = sgd1, metrics = ['accuracy'])
history = model.fit(x_train,y_train,batch_size=batch_size,epochs=epochs,verbose=1,validation_data=(x_test,y_test_))
score = model.evaluate(x_test,y_test_, verbose = 1)
print("Test loss:", score[0])
print(f"Test Accuracy:{score[1]*100:.2f}%")
```

Model: "sequential\_2"

Layer (type)	Output Shape	Param #
dense_6 (Dense)	(None, 512)	401,920
dropout (Dropout)	(None, 512)	0
dense_7 (Dense)	(None, 512)	262,656
dropout_1 (Dropout)	(None, 512)	0
dense_8 (Dense)	(None, 10)	5,130

Total params: 669,706 (2.55 MB)

Trainable params: 669,706 (2.55 MB)

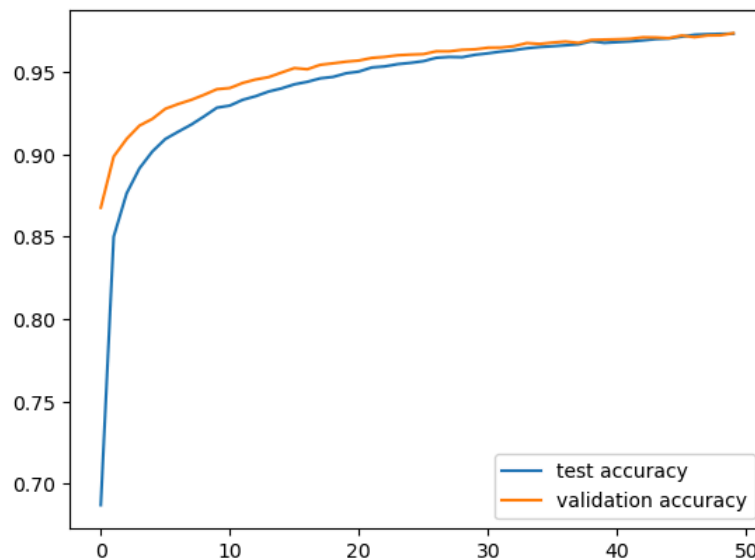
Non-trainable params: 0 (0.00 B)

Epoch 1/50  
469/469 ————— 2s 4ms/step - accuracy: 0.5206 - loss: 1.6797 - val\_accuracy: 0.8676 - val\_loss: 0.5445  
Epoch 2/50  
469/469 ————— 2s 4ms/step - accuracy: 0.8382 - loss: 0.5817 - val\_accuracy: 0.8986 - val\_loss: 0.3766  
Epoch 3/50  
469/469 ————— 2s 4ms/step - accuracy: 0.8708 - loss: 0.4441 - val\_accuracy: 0.9093 - val\_loss: 0.3227  
Epoch 4/50  
469/469 ————— 2s 4ms/step - accuracy: 0.8873 - loss: 0.3887 - val\_accuracy: 0.9174 - val\_loss: 0.2939  
Epoch 5/50  
469/469 ————— 2s 4ms/step - accuracy: 0.8993 - loss: 0.3489 - val\_accuracy: 0.9215 - val\_loss: 0.2720  
Epoch 6/50  
469/469 ————— 2s 4ms/step - accuracy: 0.9082 - loss: 0.3207 - val\_accuracy: 0.9276 - val\_loss: 0.2553  
Epoch 7/50  
469/469 ————— 2s 4ms/step - accuracy: 0.9113 - loss: 0.3112 - val\_accuracy: 0.9305 - val\_loss: 0.2415  
Epoch 8/50  
469/469 ————— 2s 4ms/step - accuracy: 0.9156 - loss: 0.2882 - val\_accuracy: 0.9330 - val\_loss: 0.2300  
Epoch 9/50  
469/469 ————— 2s 4ms/step - accuracy: 0.9206 - loss: 0.2746 - val\_accuracy: 0.9361 - val\_loss: 0.2184  
Epoch 10/50  
469/469 ————— 2s 4ms/step - accuracy: 0.9277 - loss: 0.2577 - val\_accuracy: 0.9395 - val\_loss: 0.2090  
Epoch 11/50  
469/469 ————— 2s 4ms/step - accuracy: 0.9286 - loss: 0.2444 - val\_accuracy: 0.9402 - val\_loss: 0.2000  
Epoch 12/50  
469/469 ————— 2s 4ms/step - accuracy: 0.9318 - loss: 0.2353 - val\_accuracy: 0.9433 - val\_loss: 0.1915  
Epoch 13/50  
469/469 ————— 2s 4ms/step - accuracy: 0.9356 - loss: 0.2217 - val\_accuracy: 0.9454 - val\_loss: 0.1854  
Epoch 14/50  
469/469 ————— 2s 4ms/step - accuracy: 0.9381 - loss: 0.2136 - val\_accuracy: 0.9468 - val\_loss: 0.1782  
Epoch 15/50  
469/469 ————— 2s 4ms/step - accuracy: 0.9403 - loss: 0.2064 - val\_accuracy: 0.9496 - val\_loss: 0.1711  
Epoch 16/50  
469/469 ————— 2s 4ms/step - accuracy: 0.9431 - loss: 0.1969 - val\_accuracy: 0.9523 - val\_loss: 0.1658  
Epoch 17/50  
469/469 ————— 2s 4ms/step - accuracy: 0.9441 - loss: 0.1914 - val\_accuracy: 0.9516 - val\_loss: 0.1613  
Epoch 18/50  
469/469 ————— 2s 4ms/step - accuracy: 0.9457 - loss: 0.1857 - val\_accuracy: 0.9543 - val\_loss: 0.1556  
Epoch 19/50  
469/469 ————— 2s 4ms/step - accuracy: 0.9468 - loss: 0.1805 - val\_accuracy: 0.9552 - val\_loss: 0.1508  
Epoch 20/50  
469/469 ————— 2s 4ms/step - accuracy: 0.9490 - loss: 0.1763 - val\_accuracy: 0.9562 - val\_loss: 0.1466  
Epoch 21/50  
469/469 ————— 2s 4ms/step - accuracy: 0.9490 - loss: 0.1746 - val\_accuracy: 0.9569 - val\_loss: 0.1432  
Epoch 22/50  
469/469 ————— 2s 4ms/step - accuracy: 0.9535 - loss: 0.1637 - val\_accuracy: 0.9585 - val\_loss: 0.1391  
Epoch 23/50  
469/469 ————— 2s 4ms/step - accuracy: 0.9519 - loss: 0.1635 - val\_accuracy: 0.9591 - val\_loss: 0.1363  
Epoch 24/50  
469/469 ————— 2s 4ms/step - accuracy: 0.9528 - loss: 0.1609 - val\_accuracy: 0.9601 - val\_loss: 0.1324  
Epoch 25/50  
469/469 ————— 2s 4ms/step - accuracy: 0.9549 - loss: 0.1533 - val\_accuracy: 0.9605 - val\_loss: 0.1298  
Epoch 26/50  
469/469 ————— 2s 4ms/step - accuracy: 0.9557 - loss: 0.1536 - val\_accuracy: 0.9608 - val\_loss: 0.1271  
Epoch 27/50  
469/469 ————— 2s 4ms/step - accuracy: 0.9589 - loss: 0.1423 - val\_accuracy: 0.9625 - val\_loss: 0.1235  
Epoch 28/50  
469/469 ————— 2s 4ms/step - accuracy: 0.9596 - loss: 0.1388 - val\_accuracy: 0.9625 - val\_loss: 0.1213  
Epoch 29/50  
469/469 ————— 2s 4ms/step - accuracy: 0.9588 - loss: 0.1374 - val\_accuracy: 0.9634 - val\_loss: 0.1188  
Epoch 30/50  
469/469 ————— 2s 4ms/step - accuracy: 0.9596 - loss: 0.1365 - val\_accuracy: 0.9637 - val\_loss: 0.1164  
Epoch 31/50  
469/469 ————— 2s 4ms/step - accuracy: 0.9611 - loss: 0.1331 - val\_accuracy: 0.9647 - val\_loss: 0.1141  
Epoch 32/50  
469/469 ————— 2s 4ms/step - accuracy: 0.9634 - loss: 0.1264 - val\_accuracy: 0.9648 - val\_loss: 0.1125  
Epoch 33/50  
469/469 ————— 2s 4ms/step - accuracy: 0.9643 - loss: 0.1255 - val\_accuracy: 0.9656 - val\_loss: 0.1101  
Epoch 34/50  
469/469 ————— 2s 4ms/step - accuracy: 0.9635 - loss: 0.1249 - val\_accuracy: 0.9675 - val\_loss: 0.1084  
Epoch 35/50  
469/469 ————— 2s 4ms/step - accuracy: 0.9657 - loss: 0.1194 - val\_accuracy: 0.9670 - val\_loss: 0.1068  
Epoch 36/50  
469/469 ————— 2s 4ms/step - accuracy: 0.9653 - loss: 0.1209 - val\_accuracy: 0.9678 - val\_loss: 0.1045  
Epoch 37/50  
469/469 ————— 2s 4ms/step - accuracy: 0.9650 - loss: 0.1174 - val\_accuracy: 0.9684 - val\_loss: 0.1029  
Epoch 38/50  
469/469 ————— 2s 4ms/step - accuracy: 0.9675 - loss: 0.1122 - val\_accuracy: 0.9676 - val\_loss: 0.1015  
Epoch 39/50  
469/469 ————— 2s 4ms/step - accuracy: 0.9689 - loss: 0.1106 - val\_accuracy: 0.9694 - val\_loss: 0.0999  
Epoch 40/50  
469/469 ————— 2s 4ms/step - accuracy: 0.9684 - loss: 0.1090 - val\_accuracy: 0.9696 - val\_loss: 0.0990  
Epoch 41/50  
469/469 ————— 2s 4ms/step - accuracy: 0.9676 - loss: 0.1087 - val\_accuracy: 0.9698 - val\_loss: 0.0976  
Epoch 42/50  
469/469 ————— 2s 4ms/step - accuracy: 0.9673 - loss: 0.1103 - val\_accuracy: 0.9701 - val\_loss: 0.0963  
Epoch 43/50  
469/469 ————— 2s 4ms/step - accuracy: 0.9692 - loss: 0.1053 - val\_accuracy: 0.9710 - val\_loss: 0.0945



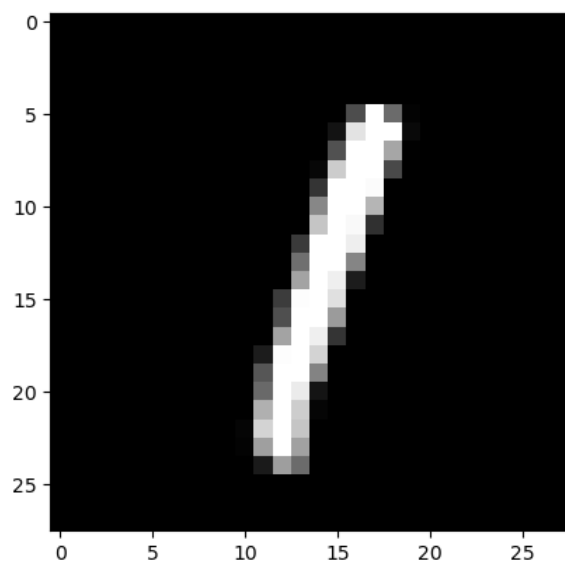
Epoch 44/50  
 469/469 — 2s 4ms/step - accuracy: 0.9709 - loss: 0.1008 - val\_accuracy: 0.9709 - val\_loss: 0.0937  
 Epoch 45/50  
 469/469 — 2s 4ms/step - accuracy: 0.9696 - loss: 0.1059 - val\_accuracy: 0.9705 - val\_loss: 0.0928  
 Epoch 46/50  
 469/469 — 2s 4ms/step - accuracy: 0.9713 - loss: 0.0994 - val\_accuracy: 0.9721 - val\_loss: 0.0917  
 Epoch 47/50  
 469/469 — 2s 4ms/step - accuracy: 0.9720 - loss: 0.0974 - val\_accuracy: 0.9711 - val\_loss: 0.0904  
 Epoch 48/50  
 469/469 — 2s 3ms/step - accuracy: 0.9723 - loss: 0.0933 - val\_accuracy: 0.9721 - val\_loss: 0.0894  
 Epoch 49/50  
 469/469 — 2s 4ms/step - accuracy: 0.9732 - loss: 0.0949 - val\_accuracy: 0.9722 - val\_loss: 0.0885  
 Epoch 50/50  
 469/469 — 2s 4ms/step - accuracy: 0.9724 - loss: 0.0956 - val\_accuracy: 0.9735 - val\_loss: 0.0870  
 313/313 — 0s 1ms/step - accuracy: 0.9687 - loss: 0.1040  
 Test loss: 0.08701445907354355  
 Test Accuracy:97.35%

```
In [9]: plt.plot(history.history['accuracy'],label='test accuracy')
plt.plot(history.history['val_accuracy'],label='validation accuracy')
plt.legend()
plt.show()
```



## Checking the image and output

```
In [10]: plt.imshow(x_test[5].reshape(28, 28),cmap = 'gray')
plt.show()
print(f"Label:{model.predict(x_test[5].reshape(-1,784),verbose=0).argmax(axis = 1)}")
```



Label:[1]

## Early stopping

```
In [11]: from sklearn.model_selection import train_test_split
(x_train,y_train),(x_test,y_test) = mnist.load_data()
x_subtrain,x_valid,y_subtrain,y_valid = train_test_split(x_train,y_train,test_size = 0.10, random_state = 1)
```

```
In [12]: x_train = x_train/255
x_test = x_test/255
x_subtrain = x_subtrain/255
x_valid=x_valid/255
```

## making the ANN

```
In [13]: model = Sequential()
model.add(Flatten(input_shape = (28,28)))
model.add(Dense(512, activation = 'relu'))
model.add(Dense(512, activation = 'relu'))
model.add(Dense(10, activation = 'softmax'))
model.summary()
sgd1 = SGD(learning_rate=0.01)
```

Model: "sequential\_3"

Layer (type)	Output Shape	Param #
flatten (Flatten)	(None, 784)	0
dense_9 (Dense)	(None, 512)	401,920
dense_10 (Dense)	(None, 512)	262,656
dense_11 (Dense)	(None, 10)	5,130

Total params: 669,706 (2.55 MB)

Trainable params: 669,706 (2.55 MB)

Non-trainable params: 0 (0.00 B)

```
In [14]: from keras.callbacks import EarlyStopping
model.compile(loss= 'sparse_categorical_crossentropy',optimizer = sgd1,metrics = ['accuracy'])
estop = EarlyStopping(monitor = 'val_loss', min_delta = 1e-3, mode = 'min', patience = 4, verbose = 1, restore_best_weight
history = model.fit(x_subtrain,y_subtrain, batch_size=batch_size, epochs = 50, verbose = 1, validation_data=(x_valid,y_val
```

Epoch 1/50  
422/422 ————— 2s 3ms/step - accuracy: 0.6003 - loss: 1.6514 - val\_accuracy: 0.8655 - val\_loss: 0.5795  
Epoch 2/50  
422/422 ————— 1s 3ms/step - accuracy: 0.8713 - loss: 0.5177 - val\_accuracy: 0.8895 - val\_loss: 0.4065  
Epoch 3/50  
422/422 ————— 1s 3ms/step - accuracy: 0.8961 - loss: 0.3824 - val\_accuracy: 0.9010 - val\_loss: 0.3513  
Epoch 4/50  
422/422 ————— 1s 3ms/step - accuracy: 0.9060 - loss: 0.3383 - val\_accuracy: 0.9092 - val\_loss: 0.3187  
Epoch 5/50  
422/422 ————— 1s 3ms/step - accuracy: 0.9122 - loss: 0.3079 - val\_accuracy: 0.9167 - val\_loss: 0.2962  
Epoch 6/50  
422/422 ————— 1s 3ms/step - accuracy: 0.9177 - loss: 0.2860 - val\_accuracy: 0.9205 - val\_loss: 0.2813  
Epoch 7/50  
422/422 ————— 1s 3ms/step - accuracy: 0.9239 - loss: 0.2685 - val\_accuracy: 0.9252 - val\_loss: 0.2681  
Epoch 8/50  
422/422 ————— 1s 3ms/step - accuracy: 0.9296 - loss: 0.2497 - val\_accuracy: 0.9263 - val\_loss: 0.2562  
Epoch 9/50  
422/422 ————— 1s 3ms/step - accuracy: 0.9323 - loss: 0.2398 - val\_accuracy: 0.9297 - val\_loss: 0.2469  
Epoch 10/50  
422/422 ————— 1s 3ms/step - accuracy: 0.9340 - loss: 0.2308 - val\_accuracy: 0.9325 - val\_loss: 0.2388  
Epoch 11/50  
422/422 ————— 1s 3ms/step - accuracy: 0.9382 - loss: 0.2194 - val\_accuracy: 0.9350 - val\_loss: 0.2292  
Epoch 12/50  
422/422 ————— 1s 3ms/step - accuracy: 0.9410 - loss: 0.2101 - val\_accuracy: 0.9390 - val\_loss: 0.2204  
Epoch 13/50  
422/422 ————— 1s 3ms/step - accuracy: 0.9420 - loss: 0.2071 - val\_accuracy: 0.9412 - val\_loss: 0.2138  
Epoch 14/50  
422/422 ————— 1s 3ms/step - accuracy: 0.9462 - loss: 0.1918 - val\_accuracy: 0.9418 - val\_loss: 0.2087  
Epoch 15/50  
422/422 ————— 1s 3ms/step - accuracy: 0.9470 - loss: 0.1845 - val\_accuracy: 0.9447 - val\_loss: 0.2025  
Epoch 16/50  
422/422 ————— 1s 3ms/step - accuracy: 0.9483 - loss: 0.1800 - val\_accuracy: 0.9450 - val\_loss: 0.1982  
Epoch 17/50  
422/422 ————— 1s 3ms/step - accuracy: 0.9516 - loss: 0.1732 - val\_accuracy: 0.9457 - val\_loss: 0.1909  
Epoch 18/50  
422/422 ————— 1s 3ms/step - accuracy: 0.9526 - loss: 0.1666 - val\_accuracy: 0.9473 - val\_loss: 0.1876  
Epoch 19/50  
422/422 ————— 1s 3ms/step - accuracy: 0.9540 - loss: 0.1627 - val\_accuracy: 0.9470 - val\_loss: 0.1852  
Epoch 20/50  
422/422 ————— 1s 3ms/step - accuracy: 0.9562 - loss: 0.1584 - val\_accuracy: 0.9497 - val\_loss: 0.1784  
Epoch 21/50  
422/422 ————— 1s 3ms/step - accuracy: 0.9566 - loss: 0.1539 - val\_accuracy: 0.9498 - val\_loss: 0.1737  
Epoch 22/50  
422/422 ————— 1s 3ms/step - accuracy: 0.9580 - loss: 0.1478 - val\_accuracy: 0.9500 - val\_loss: 0.1733  
Epoch 23/50  
422/422 ————— 1s 3ms/step - accuracy: 0.9604 - loss: 0.1444 - val\_accuracy: 0.9518 - val\_loss: 0.1676  
Epoch 24/50  
422/422 ————— 1s 3ms/step - accuracy: 0.9593 - loss: 0.1439 - val\_accuracy: 0.9532 - val\_loss: 0.1661  
Epoch 25/50  
422/422 ————— 1s 3ms/step - accuracy: 0.9632 - loss: 0.1323 - val\_accuracy: 0.9542 - val\_loss: 0.1621  
Epoch 26/50  
422/422 ————— 1s 3ms/step - accuracy: 0.9641 - loss: 0.1322 - val\_accuracy: 0.9560 - val\_loss: 0.1579  
Epoch 27/50  
422/422 ————— 1s 3ms/step - accuracy: 0.9646 - loss: 0.1268 - val\_accuracy: 0.9555 - val\_loss: 0.1562  
Epoch 28/50  
422/422 ————— 1s 3ms/step - accuracy: 0.9646 - loss: 0.1224 - val\_accuracy: 0.9575 - val\_loss: 0.1519  
Epoch 29/50  
422/422 ————— 1s 3ms/step - accuracy: 0.9664 - loss: 0.1233 - val\_accuracy: 0.9573 - val\_loss: 0.1506  
Epoch 30/50  
422/422 ————— 1s 3ms/step - accuracy: 0.9663 - loss: 0.1198 - val\_accuracy: 0.9587 - val\_loss: 0.1487  
Epoch 31/50  
422/422 ————— 1s 3ms/step - accuracy: 0.9682 - loss: 0.1165 - val\_accuracy: 0.9597 - val\_loss: 0.1453  
Epoch 32/50  
422/422 ————— 1s 3ms/step - accuracy: 0.9691 - loss: 0.1111 - val\_accuracy: 0.9603 - val\_loss: 0.1436  
Epoch 33/50  
422/422 ————— 1s 3ms/step - accuracy: 0.9707 - loss: 0.1085 - val\_accuracy: 0.9612 - val\_loss: 0.1413  
Epoch 34/50  
422/422 ————— 1s 3ms/step - accuracy: 0.9702 - loss: 0.1091 - val\_accuracy: 0.9610 - val\_loss: 0.1397  
Epoch 35/50  
422/422 ————— 1s 3ms/step - accuracy: 0.9713 - loss: 0.1033 - val\_accuracy: 0.9617 - val\_loss: 0.1375  
Epoch 36/50  
422/422 ————— 1s 3ms/step - accuracy: 0.9729 - loss: 0.1000 - val\_accuracy: 0.9625 - val\_loss: 0.1363  
Epoch 37/50  
422/422 ————— 1s 3ms/step - accuracy: 0.9714 - loss: 0.1013 - val\_accuracy: 0.9622 - val\_loss: 0.1363  
Epoch 38/50  
422/422 ————— 1s 3ms/step - accuracy: 0.9733 - loss: 0.0973 - val\_accuracy: 0.9635 - val\_loss: 0.1316  
Epoch 39/50  
422/422 ————— 1s 3ms/step - accuracy: 0.9741 - loss: 0.0950 - val\_accuracy: 0.9637 - val\_loss: 0.1311  
Epoch 40/50  
422/422 ————— 1s 3ms/step - accuracy: 0.9743 - loss: 0.0938 - val\_accuracy: 0.9642 - val\_loss: 0.1282  
Epoch 41/50  
422/422 ————— 1s 3ms/step - accuracy: 0.9757 - loss: 0.0895 - val\_accuracy: 0.9640 - val\_loss: 0.1270  
Epoch 42/50  
422/422 ————— 1s 3ms/step - accuracy: 0.9751 - loss: 0.0902 - val\_accuracy: 0.9638 - val\_loss: 0.1263  
Epoch 43/50  
422/422 ————— 1s 3ms/step - accuracy: 0.9756 - loss: 0.0883 - val\_accuracy: 0.9652 - val\_loss: 0.1239

```

Epoch 44/50
422/422 ————— 1s 3ms/step - accuracy: 0.9768 - loss: 0.0870 - val_accuracy: 0.9655 - val_loss: 0.1237
Epoch 45/50
422/422 ————— 1s 3ms/step - accuracy: 0.9776 - loss: 0.0832 - val_accuracy: 0.9637 - val_loss: 0.1224
Epoch 46/50
422/422 ————— 1s 3ms/step - accuracy: 0.9781 - loss: 0.0803 - val_accuracy: 0.9660 - val_loss: 0.1212
Epoch 47/50
422/422 ————— 1s 3ms/step - accuracy: 0.9788 - loss: 0.0792 - val_accuracy: 0.9658 - val_loss: 0.1189
Epoch 48/50
422/422 ————— 1s 3ms/step - accuracy: 0.9791 - loss: 0.0784 - val_accuracy: 0.9657 - val_loss: 0.1188
Epoch 49/50
422/422 ————— 1s 3ms/step - accuracy: 0.9797 - loss: 0.0757 - val_accuracy: 0.9670 - val_loss: 0.1160
Epoch 50/50
422/422 ————— 1s 3ms/step - accuracy: 0.9794 - loss: 0.0759 - val_accuracy: 0.9670 - val_loss: 0.1162
Restoring model weights from the end of the best epoch: 49.

```

```

In [15]: score = model.evaluate(x_test,y_test, verbose = 1)
print("Test loss:", score[0])
print(f"Test Accuracy:{score[1]*100:.2f}%")

```

```

313/313 ————— 0s 1ms/step - accuracy: 0.9654 - loss: 0.1168
Test loss: 0.09891818463802338
Test Accuracy:97.10%

```

**Challenging Question:** Try for a scratch code for this case where you can create a custom neural network without using any inbuilt classes like sequential etc. Where you need to define a class neural network which has methods like forwardpass, backwardpass, and train. Figure out how we can do this. This model has inputs as [0, 0, 1], [0, 1, 1], [1, 0, 1], [1, 1, 1] and the expected output as [0], [1], [1], [0] in each case. So there are three features in our dataset as you see above. The activation function is to be taken as sigmoid. The architecture is like we have only one hidden layer and an output layer with one neuron. Take the error function as  $(1/2)(y - \hat{y})^2$

```

In [17]: import numpy as np

# sigmoid activation function
def sigmoid(x):
    return 1 / (1 + np.exp(-x))

# derivative of sigmoid function
def sigmoid_derivative(x):
    return x*(1-x)

# mean squared error Loss
def mse_loss(y_true,y_pred):
    return 0.5*np.mean((y_true-y_pred)**2)

# Input dataset (XOR gate inputs with bias term)
x = np.array([[0,0,1],
[0,1,1],
[1,0,1],
[1,1,1]])

# output Labels
y = np.array([[0],
[1],
[1],
[0]])

# seed for reproducibility
np.random.seed(1)

# Initialize weights randomly with mean 0
input_size = 3 # 3 input features
hidden_size = 2 # 2 hidden layers
output_size = 1 # 1 output neuron

# Weights
w1 = 2 * np.random.random((input_size, hidden_size))-1
w2 = 2 * np.random.random((hidden_size, output_size))-1

# Biases
b1 = np.zeros((1, hidden_size))
b2 = np.zeros((1, output_size))

# Learning rate
lr = 0.1

# Training Loop

```

```

for epoch in range(10000):

    ##----- Forward pass -----
    a1 = np.dot(x,w1) + b1
    h1 = sigmoid(a1) # activation of hidden layer
    a2 = np.dot(h1,w2) + b2
    output = sigmoid(a2) # final prediction
    # Loss calculation
    loss = mse_loss(y,output)
    ##----- Back propagation -----
    # output layer error
    output_error = output - y
    output_delta = output_error * sigmoid_derivative(output)
    ## hidden layer error
    hidden_error = np.dot(output_delta, w2.T)
    hidden_delta = hidden_error * sigmoid_derivative(h1)
    ##-----Updating weights and biases -----
    w2 -= lr * np.dot(h1.T,output_delta)
    b2 -= lr * np.sum(output_delta, axis = 0, keepdims = True)
    w1 -= lr * np.dot(x.T, hidden_delta)
    b1 -= lr * np.sum(hidden_delta, axis = 0, keepdims = True)
    # Print Loss every 1000 epochs
    if epoch % 1000 == 0:
        print(f"Epoch {epoch}, Loss: {loss:.4f}")

# ----- Final Output -----
print("\nFinal predictions after training:")
print(output.round(3))

```

```

Epoch 0, Loss: 0.1267
Epoch 1000, Loss: 0.1215
Epoch 2000, Loss: 0.1029
Epoch 3000, Loss: 0.0905
Epoch 4000, Loss: 0.0828
Epoch 5000, Loss: 0.0433
Epoch 6000, Loss: 0.0105
Epoch 7000, Loss: 0.0049
Epoch 8000, Loss: 0.0031
Epoch 9000, Loss: 0.0022

```

Final predictions after training:

```

[[0.049]
 [0.945]
 [0.945]
 [0.071]]

```

```

In [18]: y_pred_binary = (output > 0.5).astype(int)
print("Predicted labels:", y_pred_binary.ravel())
print("True labels: ", y.ravel())

```

```

Predicted labels: [0 1 1 0]
True labels:  [0 1 1 0]

```