

# Package ‘pomp’

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**Type** Package

**Title** Statistical Inference for Partially Observed Markov Processes

**Version** 1.16.4.1

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**URL** <https://kingaa.github.io/pomp/>

**Description** Tools for working with partially observed Markov process (POMP) models (also known as stochastic dynamical systems, hidden Markov models, and nonlinear, non-Gaussian, state-space models). The package provides facilities for implementing POMP models, simulating them, and fitting them to time series data by a variety of frequentist and Bayesian methods. It is also a versatile platform for implementation of inference methods for general POMP models.

**Depends** R(>= 3.1.2), methods

**Imports** stats, graphics, digest, mvtnorm, deSolve, coda, subplex, nloptr

**Suggests** magrittr, plyr, reshape2, ggplot2, knitr

**SystemRequirements** For Windows users, Rtools (see <https://cran.r-project.org/bin/windows/Rtools/>).

**License** GPL-3

**LazyData** true

**Contact** kingaa at umich dot edu

**BugReports** <https://github.com/kingaa/pomp/issues/>

**Collate** aaa.R authors.R bake.R generics.R eulermultinom.R  
csnippet.R safecall.R pomp\_fun.R plugins.R builder.R  
parmat.R logmeanexp.R slice\_design.R  
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pfilter.R pfilter\_methods.R minim.R traj\_match.R  
bsmc.R bsmc2.R  
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mif.R mif\_methods.R mif2.R mif2\_methods.R  
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 nlf\_funes.R nlf\_guts.R nlf\_objfun.R nlf.R  
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## Description

The **pomp** package provides facilities for inference on time series data using partially-observed Markov process (POMP) models. These models are also known as state-space models, hidden Markov models, or nonlinear stochastic dynamical systems. One can use **pomp** to fit nonlinear, non-Gaussian dynamic models to time-series data. The package is both a set of tools for data analysis and a platform upon which statistical inference methods for POMP models can be implemented.

## Data analysis using pomp

The first step in using **pomp** is to encode one's model(s) and data in objects of class `pomp`. One does this via a call to [pomp constructor function](#). Details on this are given in the documentation ([pomp](#)).

**pomp** version 1.16.3.2 provides algorithms for

1. simulation of stochastic dynamical systems; see [simulate](#)
2. particle filtering (AKA sequential Monte Carlo or sequential importance sampling); see [pfilter](#)
3. the iterated filtering methods of Ionides et al. (2006, 2011, 2015); see [mif2](#)
4. the nonlinear forecasting algorithm of Kendall et al. (2005); see [nlf](#)
5. the particle MCMC approach of Andrieu et al. (2010); see [pmcmc](#)
6. the probe-matching method of Kendall et al. (1999, 2005); see [probe.match](#)
7. a spectral probe-matching method (Reuman et al. 2006, 2008); see [spect.match](#)
8. synthetic likelihood a la Wood (2010); see [probe](#)
9. approximate Bayesian computation (Toni et al. 2009); see [abc](#)
10. the approximate Bayesian sequential Monte Carlo scheme of Liu & West (2001); see [bsmc2](#)
11. ensemble and ensemble adjusted Kalman filters; see [enkf](#)
12. simple trajectory matching; see [traj.match](#).

The package also provides various tools for plotting and extracting information on models and data.

## Developing inference tools on the pomp platform

**pomp** provides a very general interface to the components of POMP models. All the inference algorithms in **pomp** interact with the models and data via this interface. One goal of the **pomp** project has been to facilitate the development of new algorithms in an environment where they can be tested and compared on a growing body of models and datasets.

## Comments, bug reports, feature requests

Contributions are welcome, as are comments, feature requests, and bug reports. Please submit these via the [issues page](#). See the [package website](#) for more information, access to the package new RSS feed, links to the authors' websites, references to the literature, and up-to-date versions of the package source and documentation. Help requests are welcome, but please read the [FAQ](#) before sending requests.

We are very interested in improving the documentation and the package error and warning messages. If you find a portion of the documentation impenetrable, please let us know, preferably with suggestions for improvement. If you find an error message that is uninformative or misleading, please be sure to let us know. The best way to do so is via the [package issues page](#). Please do read the [FAQ](#) before reporting an issue.

## Documentation

A number of tutorials, demonstrating the construction of pomp objects and the application of various inference algorithms, are available on the [package webpage](#). Examples are given in the tutorials on the [package website](#), in the demos, and via the `pompExample` function. See a list of the demos via

```
demo(package="pomp")
```

and a list of the included examples via

```
pompExample()
```

## History

Much of the groundwork for **pomp** was laid by a working group of the National Center for Ecological Analysis and Synthesis (NCEAS), "Inference for Mechanistic Models".

## License

**pomp** is provided under the GNU Public License (GPL).

## Author(s)

Aaron A. King

## References

A. A. King, D. Nguyen, and E. L. Ionides (2016) Statistical Inference for Partially Observed Markov Processes via the R Package **pomp**. *Journal of Statistical Software* 69(12): 1–43. An updated version of this paper is available on the [package website](#).

See the package website, <https://kingaa.github.io/pomp>, for more references.

## See Also

[pomp](#), [pomp low-level interface](#), [pfilter](#), [simulate](#), [mif](#), [nlf](#), [probe](#), [traj.match](#), [bsmc2](#), [pmcmc](#)

---

Approximate Bayesian computation

*Estimation by approximate Bayesian computation (ABC)*


---

## Description

The approximate Bayesian computation (ABC) algorithm for estimating the parameters of a partially-observed Markov process.

## Usage

```
## S4 method for signature 'pomp'
abc(object, Nabc = 1, start,
     proposal, probes, scale, epsilon,
     verbose = getOption("verbose"), ...)
## S4 method for signature 'probed.pomp'
abc(object, probes,
     verbose = getOption("verbose"), ...)
## S4 method for signature 'abc'
abc(object, Nabc, start, proposal,
     probes, scale, epsilon,
     verbose = getOption("verbose"), ...)
## S4 method for signature 'abc'
continue(object, Nabc = 1, ...)
## S4 method for signature 'abc'
conv.rec(object, pars, ...)
## S4 method for signature 'abcList'
conv.rec(object, ...)
## S4 method for signature 'abc'
plot(x, y, pars, scatter = FALSE, ...)
## S4 method for signature 'abcList'
plot(x, y, ...)
```

## Arguments

<code>object</code>	An object of class <code>pomp</code> .
<code>Nabc</code>	The number of ABC iterations to perform.
<code>start</code>	named numeric vector; the starting guess of the parameters.
<code>proposal</code>	optional function that draws from the proposal distribution. Currently, the proposal distribution must be symmetric for proper inference: it is the user's responsibility to ensure that it is. Several functions that construct appropriate proposal function are provided: see <a href="#">MCMC proposal functions</a> for more information.
<code>probes</code>	List of probes (AKA summary statistics). See <a href="#">probe</a> for details.
<code>scale</code>	named numeric vector of scales.
<code>epsilon</code>	ABC tolerance.

<code>verbose</code>	logical; if TRUE, print progress reports.
<code>pars</code>	Names of parameters.
<code>scatter</code>	optional logical; If TRUE, draw scatterplots. If FALSE, draw traceplots.
<code>x</code>	abc object.
<code>y</code>	Ignored.
<code>...</code>	Additional arguments. These are currently ignored.

### Running ABC

`abc` returns an object of class `abc`. One or more `abc` objects can be joined to form an `abcList` object.

### Re-running ABC iterations

To re-run a sequence of ABC iterations, one can use the `abc` method on a `abc` object. By default, the same parameters used for the original ABC run are re-used (except for `tol`, `max.fail`, and `verbose`, the defaults of which are shown above). If one does specify additional arguments, these will override the defaults.

### Continuing ABC iterations

One can continue a series of ABC iterations from where one left off using the `continue` method. A call to `abc` to perform  $N_{abc}=m$  iterations followed by a call to `continue` to perform  $N_{abc}=n$  iterations will produce precisely the same effect as a single call to `abc` to perform  $N_{abc}=m+n$  iterations. By default, all the algorithmic parameters are the same as used in the original call to `abc`. Additional arguments will override the defaults.

### Methods

Methods that can be used to manipulate, display, or extract information from an `abc` object:

`conv.rec(object, pars)` returns the columns of the convergence-record matrix corresponding to the names in `pars`. By default, all rows are returned.

`c` Concatenates `abc` objects into an `abcList`.

`plot` Diagnostic plots.

`covmat(object, start, thin, expand)` computes the empirical covariance matrix of the ABC samples beginning with iteration `start` and thinning by factor `thin`. It expands this by a factor  $\text{expand}^2/n$ , where  $n$  is the number of parameters estimated. The intention is that the resulting matrix is a suitable input to the proposal function `mvn.rw`.

### Author(s)

Edward L. Ionides, Aaron A. King

## References

- J.-M. Marin, P. Pudlo, C. P. Robert, and R. J. Ryder, Approximate Bayesian computational methods. *Statistics and Computing* 22:1167–1180, 2012.
- T. Toni and M. P. H. Stumpf, Simulation-based model selection for dynamical systems in systems and population biology, *Bioinformatics* 26:104–110, 2010.
- T. Toni, D. Welch, N. Strelkowa, A. Ipsen, and M. P. H. Stumpf, Approximate Bayesian computation scheme for parameter inference and model selection in dynamical systems *Journal of the Royal Society, Interface* 6:187–202, 2009.

## See Also

[pomp](#), [probe](#), [MCMC proposal distributions](#), and the tutorials on the [package website](#).

---

B-splines

*B-spline bases*

---

## Description

These functions generate B-spline basis functions. `bspline.basis` gives a basis of spline functions. `periodic.bspline.basis` gives a basis of periodic spline functions.

## Usage

```
bspline.basis(x, nbasis, degree = 3, deriv = 0, names = NULL)
periodic.bspline.basis(x, nbasis, degree = 3, period = 1, deriv = 0,
                        names = NULL)
```

## Arguments

<code>x</code>	Vector at which the spline functions are to be evaluated.
<code>nbasis</code>	The number of basis functions to return.
<code>degree</code>	Degree of requested B-splines.
<code>period</code>	The period of the requested periodic B-splines.
<code>deriv</code>	The order of the derivative required.
<code>names</code>	optional; the names to be given to the basis functions. These will be the column-names of the matrix returned. If the names are specified as a format string (e.g., "basis%d"), <a href="#">sprintf</a> will be used to generate the names from the column number. If a single non-format string is specified, the names will be generated by <a href="#">paste</a> -ing name to the column number. One can also specify each column name explicitly by giving a length-nbasis string vector. By default, no column-names are given.

**Value**

`bspline.basis` Returns a matrix with `length(x)` rows and `nbasis` columns. Each column contains the values one of the spline basis functions. If `deriv>0`, the derivatives of the corresponding spline basis functions are returned.

`periodic.bspline.basis` Returns a matrix with `length(x)` rows and `nbasis` columns. The basis functions returned are periodic with period `period`. If `deriv>0`, the derivatives of the corresponding spline basis functions are returned.

**C API**

Access to the underlying C routines is available: see the header file `'pomp.h'` for definition and documentation of the C API. At an R prompt, execute

```
file.show(system.file("include/pomp.h", package="pomp"))
```

to view this file.

**Author(s)**

Aaron A. King

**Examples**

```
x <- seq(0,2,by=0.01)
y <- bspline.basis(x,degree=3,nbasis=9,names="basis")
matplot(x,y,type='l',ylim=c(0,1.1))
lines(x,apply(y,1,sum),lwd=2)

x <- seq(-1,2,by=0.01)
y <- periodic.bspline.basis(x,nbasis=5,names="spline%d")
matplot(x,y,type='l')
```

---

Bayesian sequential Monte Carlo

*The Liu and West Bayesian particle filter*

---

**Description**

Modified versions of the Liu and West (2001) algorithm.



**Usage**

```
## S4 method for signature 'pomp'
bsmc2(object, params, Np, est, smooth = 0.1,
      tol = 1e-17, verbose = getOption("verbose"), max.fail = 0,
      transform = FALSE, ...)
## S4 method for signature 'pomp'
bsmc(object, params, Np, est, smooth = 0.1,
     ntries = 1, tol = 1e-17, lower = -Inf, upper = Inf,
     verbose = getOption("verbose"), max.fail = 0,
     transform = FALSE, ...)
```

**Arguments**

<code>object</code>	An object of class <code>pomp</code> or inheriting class <code>pomp</code> .
<code>params, Np</code>	Specifications for the prior distribution of particles. See details below.
<code>est</code>	Names of the rows of <code>params</code> that are to be estimated. No updates will be made to the other parameters. If <code>est</code> is not specified, all parameters for which there is variation in <code>params</code> will be estimated.
<code>smooth</code>	Kernel density smoothing parameters. The compensating shrinkage factor will be $\sqrt{1-\text{smooth}^2}$ . Thus, <code>smooth=0</code> means that no noise will be added to parameters. Generally, the value of <code>smooth</code> should be chosen close to 0 (i.e., $\text{shrink} \sim 0.1$ ).
<code>ntries</code>	Number of draws from <code>rprocess</code> per particle used to estimate the expected value of the state process at time $t+1$ given the state and parameters at time $t$ .
<code>tol</code>	Particles with log likelihood below <code>tol</code> are considered to be “lost”. A filtering failure occurs when, at some time point, all particles are lost. When all particles are lost, the conditional log likelihood at that time point is set to be $\log(\text{tol})$ .
<code>lower, upper</code>	optional; lower and upper bounds on the priors. This is useful in case there are box constraints satisfied by the priors. The posterior is guaranteed to lie within these bounds.
<code>verbose</code>	logical; if TRUE, print diagnostic messages.
<code>max.fail</code>	The maximum number of filtering failures allowed. If the number of filtering failures exceeds this number, execution will terminate with an error.
<code>transform</code>	logical; if TRUE, the algorithm operates on the transformed scale.
<code>...</code>	currently ignored.

**Details**

There are two ways to specify the prior distribution of particles. If `params` is unspecified or is a named vector, `Np` draws are made from the prior distribution, as specified by `rprior`. Alternatively, `params` can be specified as an `npars x Np` matrix (with rownames).

`bsmc` uses version of the original algorithm that includes a plug-and-play auxiliary particle filter. `bsmc2` discards this auxiliary particle filter and appears to give superior performance for the same amount of effort.

**Value**

An object of class “bsmcd.pomp”. The “params” slot of this object will hold the parameter posterior medians. The slots of this class include:

post	A matrix containing draws from the approximate posterior distribution.
prior	A matrix containing draws from the prior distribution (identical to params on call).
eff.sample.size	A vector containing the effective number of particles at each time point.
smooth	The smoothing parameter used (see above).
nfail	The number of filtering failures encountered.
cond.log.evidence	A vector containing the conditional log evidence scores at each time point.
log.evidence	The estimated log evidence.
weights	The resampling weights for each particle.

**Author(s)**

Michael Lavine (lavine at math dot umass dot edu), Matthew Ferrari (mferrari at psu dot edu), Aaron A. King (kingaa at umich dot edu), Edward L. Ionides (ionides at umich dot edu)

**References**

Liu, J. and M. West. Combining Parameter and State Estimation in Simulation-Based Filtering. In A. Doucet, N. de Freitas, and N. J. Gordon, editors, Sequential Monte Carlo Methods in Practice, pages 197-224. Springer, New York, 2001.

**See Also**

[pomp](#), [pfilter](#)

---

blowflies

*Model for Nicholson’s blowflies.*

---

**Description**

blowflies1 and blowflies2 are pomp objects encoding stochastic delay-difference models.

## Details

The data are from "population I", a control culture in one of A. J. Nicholson's experiments with the Australian sheep-blowfly *Lucilia cuprina*. The experiment is described on pp. 163–4 of Nicholson (1957). Unlimited quantities of larval food were provided; the adult food supply (ground liver) was constant at 0.4g per day. The data were taken from the table provided by Brillinger et al. (1980).

The models are discrete delay equations:

$$R(t+1) \sim \text{Poisson}(PN(t-\tau) \exp(-N(t-\tau)/N_0)e(t+1)\Delta t)$$

$$S(t+1) \sim \text{binomial}(N(t), \exp(-\delta\epsilon(t+1)\Delta t))$$

$$N(t) = R(t) + S(t)$$

where  $e(t)$  and  $\epsilon(t)$  are Gamma-distributed i.i.d. random variables with mean 1 and variances  $\sigma_p^2/\Delta t$ ,  $\sigma_d^2/\Delta t$ , respectively. `blowflies1` has a timestep ( $\Delta t$ ) of 1 day, and `blowflies2` has a timestep of 2 days. The process model in `blowflies1` thus corresponds exactly to that studied by Wood (2010). The measurement model in both cases is taken to be

$$y(t) \sim \text{negbin}(N(t), 1/\sigma_y^2)$$

, i.e., the observations are assumed to be negative-binomially distributed with mean  $N(t)$  and variance  $N(t) + (\sigma_y N(t))^2$ .

Do

```
pompExample(blowflies, show=TRUE)
```

to view the code that constructs these pomp objects.

## References

- A. J. Nicholson (1957) The self-adjustment of populations to change. *Cold Spring Harbor Symposia on Quantitative Biology*, **22**, 153–173.
- Y. Xia and H. Tong (2011) Feature Matching in Time Series Modeling. *Statistical Science* **26**, 21–46.
- E. L. Ionides (2011) Discussion of “Feature Matching in Time Series Modeling” by Y. Xia and H. Tong. *Statistical Science* **26**, 49–52.
- S. N. Wood (2010) Statistical inference for noisy nonlinear ecological dynamic systems. *Nature* **466**, 1102–1104.
- W. S. C. Gurney, S. P. Blythe, and R. M. Nisbet (1980) Nicholson's blowflies revisited. *Nature* **287**, 17–21.
- D. R. Brillinger, J. Guckenheimer, P. Guttorp and G. Oster (1980) Empirical modelling of population time series: The case of age and density dependent rates. in G. Oster (ed.), *Some Questions in Mathematical Biology*, vol. 13, pp. 65–90. American Mathematical Society, Providence.

## See Also

[pomp](#)

**Examples**

```
pompExample(blowflies)
plot(blowflies1)
plot(blowflies2)
```

---

Childhood disease incidence data

*Historical childhood disease incidence data*

---

**Description**

LondonYorke is a data frame containing the monthly number of reported cases of chickenpox, measles, and mumps from two American cities (Baltimore and New York) in the mid-20th century (1928–1972).

ewmeas and ewcitmeas are data frames containing weekly reported cases of measles in England and Wales. ewmeas records the total measles reports for the whole country, 1948–1966. One questionable data point has been replaced with an NA. ewcitmeas records the incidence in seven English cities 1948–1987. These data were kindly provided by Ben Bolker, who writes: “Most of these data have been manually entered from published records by various people, and are prone to errors at several levels. All data are provided as is; use at your own risk.”

**Usage**

```
LondonYorke
ewmeas
ewcitmeas
```

**References**

W. P. London and J. A. Yorke, Recurrent Outbreaks of Measles, Chickenpox and Mumps: I. Seasonal Variation in Contact Rates, *American Journal of Epidemiology*, 98:453–468, 1973.

**Examples**

```
plot(cases~time,data=LondonYorke,subset=disease=="measles",type='n',main="measles",bty='l')
lines(cases~time,data=LondonYorke,subset=disease=="measles"&town=="Baltimore",col="red")
lines(cases~time,data=LondonYorke,subset=disease=="measles"&town=="New York",col="blue")
legend("topright",legend=c("Baltimore","New York"),lty=1,col=c("red","blue"),bty='n')

plot(
  cases~time,
  data=LondonYorke,
  subset=disease=="chickenpox"&town=="New York",
  type='l',col="blue",main="chickenpox, New York",
  bty='l'
)

plot(
```

```

      cases~time,
      data=LondonYorke,
      subset=disease=="mumps"&town=="New York",
      type='l',col="blue",main="mumps, New York",
      bty='l'
    )

plot(reports~time,data=ewmeas,type='l')

plot(reports~date,data=ewcitmeas,subset=city=="Liverpool",type='l')

```

---

 dacca

---

*Model of cholera transmission for historic Bengal.*


---

## Description

dacca is a pomp object containing census and cholera mortality data from the Dacca district of the former British province of Bengal over the years 1891 to 1940 together with a stochastic differential equation transmission model. The model is that of King et al. (2008). The parameters are the MLE for the SIRS model with seasonal reservoir.

Data are provided courtesy of Dr. Menno J. Bouma, London School of Tropical Medicine and Hygiene.

## Details

dacca is a pomp object containing the model, data, and MLE parameters. Parameters that naturally range over the positive reals are log-transformed; parameters that range over the unit interval are logit-transformed; parameters that are naturally unbounded or take integer values are not transformed.

## References

A. A. King, E. L. Ionides, M. Pascual, and M. J. Bouma, Inapparent infections and cholera dynamics, *Nature*, 454:877-880, 2008

## See Also

[euler.sir](#), [pomp](#)

## Examples

```

pompExample(dacca)
plot(dacca)
#MLEs on the natural scale
coef(dacca)
#MLEs on the transformed scale
coef(dacca,transform=TRUE)
plot(simulate(dacca))

```

---

 design
 

---

*Design matrices for pomp calculations*


---

### Description

These functions are useful for generating designs for the exploration of parameter space. `sobolDesign` generate a Latin hypercube design using the Sobol' low-discrepancy sequence. `profileDesign` generates a data-frame where each row can be used as the starting point for a profile likelihood calculation. `sliceDesign` generates points along slices through a specified point.

### Usage

```
sobolDesign(lower, upper, nseq)
profileDesign(..., lower, upper, nprof,
              stringsAsFactors = default.stringsAsFactors())
sliceDesign(center, ...)
```

### Arguments

<code>lower, upper</code>	named numeric vectors giving the lower and upper bounds of the ranges, respectively.
<code>...</code>	In <code>profileDesign</code> , additional arguments specify the parameters over which to profile and the values of these parameters. In <code>sliceDesign</code> , additional numeric vector arguments specify the locations of points along the slices.
<code>nseq</code>	Total number of points requested.
<code>nprof</code>	The number of points per profile point.
<code>stringsAsFactors</code>	should character vectors be converted to factors?
<code>center</code>	<code>center</code> is a named numeric vector specifying the point through which the slice(s) is (are) to be taken.

### Details

The Sobol' sequence generation is performed using codes from the **NLopt** library by S. Johnson.

### Value

`sobolDesign`

`profileDesign` returns a data frame with `nprof` points per profile point. The other parameters in `vars` are sampled using `sobol`.

### Author(s)

Aaron A. King

## References

- W. H. Press, S. A. Teukolsky, W. T. Vetterling, and B. P. Flannery, Numerical Recipes in C, Cambridge University Press, 1992
- P. Bratley and B. L. Fox, Algorithm 659 Implementing Sobol's quasirandom sequence generator, ACM Trans. Math. Soft. 14, 88–100, 1988.
- S. Joe and F. Y. Kuo, Remark on algorithm 659: Implementing Sobol's quasirandom sequence generator ACM Trans. Math. Soft 29, 49–57, 2003.
- Steven G. Johnson, The **NLopt** nonlinear-optimization package, <http://ab-initio.mit.edu/nlopt>

## Examples

```
## Sobol' low-discrepancy design
plot(sobolDesign(lower=c(a=0,b=100),upper=c(b=200,a=1),100))

## A one-parameter profile design:
x <- profileDesign(p=1:10,lower=c(a=0,b=0),upper=c(a=1,b=5),nprof=20)
dim(x)
plot(x)

## A two-parameter profile design:
x <- profileDesign(p=1:10,q=3:5,lower=c(a=0,b=0),upper=c(b=5,a=1),nprof=20)
dim(x)
plot(x)

## A single 11-point slice through the point c(A=3,B=8,C=0) along the B direction.
x <- sliceDesign(center=c(A=3,B=8,C=0),B=seq(0,10,by=1))
dim(x)
plot(x)

## Two slices through the same point along the A and C directions.
x <- sliceDesign(c(A=3,B=8,C=0),A=seq(0,5,by=1),C=seq(0,5,length=11))
dim(x)
plot(x)
```

---

Ensemble Kalman filters

*Ensemble Kalman filters*

---

## Description

The ensemble Kalman filter and ensemble adjustment Kalman filter.

## Usage

```
## S4 method for signature 'pomp'
enkf(object, params, Np, h, R,
```

```

        verbose = getOption("verbose"), ...)
## S4 method for signature 'pomp'
eakf(object, params, Np, C, R,
      verbose = getOption("verbose"), ...)
## S4 method for signature 'kalmand.pomp'
logLik(object, ...)
## S4 method for signature 'kalmand.pomp'
cond.logLik(object, ...)
## S4 method for signature 'kalmand.pomp'
pred.mean(object, pars, ...)
## S4 method for signature 'kalmand.pomp'
filter.mean(object, pars, ...)

```

### Arguments

<code>object</code>	An object of class <code>pomp</code> or inheriting class <code>pomp</code> .
<code>params</code>	optional named numeric vector containing the parameters at which the filtering should be performed. By default, <code>params = coef(object)</code> .
<code>Np</code>	the number of particles to use.
<code>verbose</code>	logical; if TRUE, progress information is reported.
<code>h</code>	function returning the expected value of the observation given the state.
<code>C</code>	matrix converting state vector into expected value of the observation.
<code>R</code>	matrix; variance of the measurement noise.
<code>pars</code>	Names of variables.
<code>...</code>	additional arguments (currently ignored).

### Value

An object of class `kalmand.pomp`. This class inherits from class `pomp`.

### Methods

**logLik** Extracts the estimated log likelihood.

**cond.logLik** Extracts the estimated conditional log likelihood

$$\ell_t(\theta) = \text{Prob}[y_t | y_1, \dots, y_{t-1}],$$

where  $y_t$  are the data, at time  $t$ .

**pred.mean** Extract the mean of the approximate prediction distribution. This prediction distribution is that of

$$X_t | y_1, \dots, y_{t-1},$$

where  $X_t, y_t$  are the state vector and data, respectively, at time  $t$ .

**filter.mean** Extract the mean of the filtering distribution, which is that of

$$X_t | y_1, \dots, y_t,$$

where  $X_t, y_t$  are the state vector and data, respectively, at time  $t$ .



**Author(s)**

Aaron A. King

**References**

Evensen, G. (1994) Sequential data assimilation with a nonlinear quasi-geostrophic model using Monte Carlo methods to forecast error statistics *Journal of Geophysical Research: Oceans* 99:10143–10162

Evensen, G. (2009) *Data assimilation: the ensemble Kalman filter* Springer-Verlag.

Anderson, J. L. (2001) An Ensemble Adjustment Kalman Filter for Data Assimilation *Monthly Weather Review* 129:2884–2903

**See Also**

[pomp](#), [pfilter](#), and the tutorials on the [package website](#).

---

eulermultinom	<i>The Euler-multinomial distributions and Gamma white-noise processes</i>
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---

**Description**

This page documents both the Euler-multinomial family of distributions and the package’s simulator of Gamma white-noise processes.

**Usage**

```
reulermultinom(n = 1, size, rate, dt)
deulermultinom(x, size, rate, dt, log = FALSE)
rgammawn(n = 1, sigma, dt)
```

**Arguments**

n	integer; number of random variates to generate.
size	scalar integer; number of individuals at risk.
rate	numeric vector of hazard rates.
sigma	numeric scalar; intensity of the Gamma white noise process.
dt	numeric scalar; duration of Euler step.
x	matrix or vector containing number of individuals that have succumbed to each death process.
log	logical; if TRUE, return logarithm(s) of probabilities.

### Details

If  $N$  individuals face constant hazards of death in  $k$  ways at rates  $r_1, r_2, \dots, r_k$ , then in an interval of duration  $\Delta t$ , the number of individuals remaining alive and dying in each way is multinomially distributed:

$$(N - \sum_{i=1}^k \Delta n_i, \Delta n_1, \dots, \Delta n_k) \sim \text{multinomial}(N; p_0, p_1, \dots, p_k),$$

where  $\Delta n_i$  is the number of individuals dying in way  $i$  over the interval, the probability of remaining alive is  $p_0 = \exp(-\sum_i r_i \Delta t)$ , and the probability of dying in way  $j$  is

$$p_j = \frac{r_j}{\sum_i r_i} (1 - \exp(-\sum_i r_i \Delta t)).$$

In this case, we say that

$$(\Delta n_1, \dots, \Delta n_k) \sim \text{eulermultinom}(N, r, \Delta t),$$

where  $r = (r_1, \dots, r_k)$ . Draw  $m$  random samples from this distribution by doing

```
dn <- reulermultinom(n=m, size=N, rate=r, dt=dt),
```

where  $r$  is the vector of rates. Evaluate the probability that  $x = (x_1, \dots, x_k)$  are the numbers of individuals who have died in each of the  $k$  ways over the interval  $\Delta t = dt$ , by doing

```
deulermultinom(x=x, size=N, rate=r, dt=dt).
```

Breto & Ionides (2011) discuss how an infinitesimally overdispersed death process can be constructed by compounding a binomial process with a Gamma white noise process. The Euler approximation of the resulting process can be obtained as follows. Let the increments of the equidispersed process be given by

```
reulermultinom(size=N, rate=r, dt=dt).
```

In this expression, replace the rate  $r$  with  $r \Delta W / \Delta t$ , where  $\Delta W \sim \text{Gamma}(\Delta t / \sigma^2, \sigma^2)$  is the increment of an integrated Gamma white noise process with intensity  $\sigma$ . That is,  $\Delta W$  has mean  $\Delta t$  and variance  $\sigma^2 \Delta t$ . The resulting process is overdispersed and converges (as  $\Delta t$  goes to zero) to a well-defined process. The following lines of R code accomplish this:

```
dW <- rgammawn(sigma=sigma, dt=dt)
```

```
dn <- reulermultinom(size=N, rate=r, dt=dW)
```

or

```
dn <- reulermultinom(size=N, rate=r*dW/dt, dt=dt).
```

He et al. use such overdispersed death processes in modeling measles.

For all of the functions described here, access to the underlying C routines is available: see below.

**Value**

<code>reulermultinom</code>	Returns a <code>length(rate)</code> by <code>n</code> matrix. Each column is a different random draw. Each row contains the numbers of individuals succumbed to the corresponding process.
<code>deulermultinom</code>	Returns a vector (of length equal to the number of columns of <code>x</code> ) containing the probabilities of observing each column of <code>x</code> given the specified parameters ( <code>size</code> , <code>rate</code> , <code>dt</code> ).
<code>rgammawn</code>	Returns a vector of length <code>n</code> containing random increments of the integrated Gamma white noise process with intensity <code>sigma</code> .

**C API**

An interface for C codes using these functions is provided by the package. At an R prompt, execute

```
file.show(system.file("include/pomp.h", package="pomp"))
```

to view the ‘`pomp.h`’ header file that defines and explains the API.

**Author(s)**

Aaron A. King

**References**

- C. Breto & E. L. Ionides, Compound Markov counting processes and their applications to modeling infinitesimally over-dispersed systems. *Stoch. Proc. Appl.*, 121:2571–2591, 2011.
- D. He, E. L. Ionides, & A. A. King, Plug-and-play inference for disease dynamics: measles in large and small populations as a case study. *J. R. Soc. Interface*, 7:271–283, 2010.

**Examples**

```
print(dn <- reulermultinom(5,size=100,rate=c(a=1,b=2,c=3),dt=0.1))
deulermultinom(x=dn,size=100,rate=c(1,2,3),dt=0.1)
## an Euler-multinomial with overdispersed transitions:
dt <- 0.1
dW <- rgammawn(sigma=0.1,dt=dt)
print(dn <- reulermultinom(5,size=100,rate=c(a=1,b=2,c=3),dt=dW))
```

---

Example pomp models      *Examples of the construction of POMP models*

---

**Description**

`pompExample` loads pre-built example pomp objects.

**Usage**

```
pompExample(example, ..., show = FALSE, envir = .GlobalEnv)
```

**Arguments**

<code>example</code>	example to load given as a name or literal character string. Evoked without an argument, <code>pompExample</code> lists all available examples.
<code>...</code>	additional arguments define symbols in the environment within which the example code is executed.
<code>show</code>	logical; if TRUE, display, but do not execute, the example R code.
<code>envir</code>	the environment into which the objects should be loaded. If <code>envir=NULL</code> , then the created objects are returned in a list.

**Details**

Directories listed in the global option `pomp.examples` (which can be changed using `options()`) are searched for file named '`<example>.R`'. If found, this file will be sourced in a temporary environment. Additional arguments to `pompExample` define variables within this environment and will therefore be available when the code in '`<example>.R`' is sourced.

The codes that construct these pomp objects can be found in the 'examples' directory in the installed package. Do `system.file("examples", package="pomp")` to find this directory.

**Value**

By default, `pompExample` has the side effect of creating one or more objects in the global workspace. If `envir=NULL`, there are no side effects; rather, the objects are returned as a list.

**Author(s)**

Aaron A. King

**See Also**

[blowflies](#), [dacca](#), [gompertz](#), [ou2](#), [ricker](#), [rw2](#), [euler.sir](#), [gillespie.sir](#), [bbs](#)

**Examples**

```
pompExample()
pompExample(euler.sir)
pompExample("gompertz")
pompExample(ricker,envir=NULL)
## Not run:
  pompExample(bbs,show=TRUE)

## End(Not run)
```

gompertz

*Gompertz model with log-normal observations.***Description**

gompertz is a pomp object encoding a stochastic Gompertz population model with log-normal measurement error.

**Details**

The state process is  $X_{t+1} = K^{1-S} X_t^S \epsilon_t$ , where  $S = e^{-r}$  and the  $\epsilon_t$  are i.i.d. lognormal random deviates with variance  $\sigma^2$ . The observed variables  $Y_t$  are distributed as  $\text{lognormal}(\log X_t, \tau)$ . Parameters include the per-capita growth rate  $r$ , the carrying capacity  $K$ , the process noise s.d.  $\sigma$ , the measurement error s.d.  $\tau$ , and the initial condition  $X_0$ . The pomp object includes parameter transformations that log-transform the parameters for estimation purposes.

**See Also**

pomp, ricker, and the tutorials at <https://kingaa.github.io/pomp>.

**Examples**

```
pompExample(gompertz)
plot(gompertz)
coef(gompertz)
coef(gompertz, transform=TRUE)
```

Iterated filtering

*Maximum likelihood by iterated filtering***Description**

Iterated filtering algorithms for estimating the parameters of a partially-observed Markov process. Running `mif` causes the iterated filtering algorithm to run for a specified number of iterations. At each iteration, the particle filter is performed on a perturbed version of the model. Specifically, parameters to be estimated are subjected to random perturbations at each observation. This extra variability effectively smooths the likelihood surface and combats particle depletion by introducing diversity into the population of particles. At the iterations progress, the magnitude of the perturbations is diminished according to a user-specified cooling schedule. For most purposes, `mif` has been superseded by `mif2`.

**Usage**

```
## S4 method for signature 'pomp'
mif(object, Nmif = 1, start, ivps = character(0),
    rw.sd, Np, ic.lag, var.factor = 1,
    cooling.type, cooling.fraction.50,
    method = c("mif", "unweighted", "fp", "mif2"),
    tol = 1e-17, max.fail = Inf,
    verbose = getOption("verbose"), transform = FALSE, ...)
## S4 method for signature 'pfilterd.pomp'
mif(object, Nmif = 1, Np, tol, ...)
## S4 method for signature 'mif'
mif(object, Nmif, start, ivps,
    rw.sd, Np, ic.lag, var.factor,
    cooling.type, cooling.fraction.50,
    method, tol, transform, ...)
## S4 method for signature 'mif'
continue(object, Nmif = 1, ...)
## S4 method for signature 'mif'
conv.rec(object, pars, transform = FALSE, ...)
## S4 method for signature 'mifList'
conv.rec(object, ...)
```

**Arguments**

<code>object</code>	An object of class <code>pomp</code> .
<code>Nmif</code>	The number of filtering iterations to perform.
<code>start</code>	named numerical vector; the starting guess of the parameters.
<code>ivps</code>	optional character vector naming the initial-value parameters (IVPs) to be estimated. Every parameter named in <code>ivps</code> must have a positive random-walk standard deviation specified in <code>rw.sd</code> . If there are no regular parameters with positive <code>rw.sd</code> , i.e., only IVPs are to be estimated, see below “Using <code>mif</code> to estimate initial-value parameters only”.
<code>rw.sd</code>	numeric vector with names; the intensity of the random walk to be applied to parameters. <code>names(rw.sd)</code> must be a subset of <code>names(start)</code> . The random walk is not dynamically added to the initial-value parameters (named in <code>ivps</code> ). The algorithm requires that the random walk be nontrivial, so that <code>rw.sd</code> be positive for at least one element.
<code>Np</code>	the number of particles to use in filtering. This may be specified as a single positive integer, in which case the same number of particles will be used at each timestep. Alternatively, if one wishes the number of particles to vary across timestep, one may specify <code>Np</code> either as a vector of positive integers (of length <code>length(time(object, t0=TRUE))</code> ) or as a function taking a positive integer argument. In the latter case, <code>Np(k)</code> must be a single positive integer, representing the number of particles to be used at the $k$ -th timestep: <code>Np(0)</code> is the number of particles to use going from <code>timezero(object)</code> to <code>time(object)[1]</code> , <code>Np(1)</code> , from <code>timezero(object)</code> to <code>time(object)[1]</code> , and so on, while when

	$T = \text{length}(\text{time}(\text{object}, t0 = \text{TRUE}))$ , $Np(T)$ is the number of particles to sample at the end of the time-series.
<code>ic.lag</code>	a positive integer; the timepoint for fixed-lag smoothing of initial-value parameters. The <code>mif</code> update for initial-value parameters consists of replacing them by their filtering mean at time <code>times[ic.lag]</code> , where <code>times=time(object)</code> . It makes no sense to set <code>ic.lag &gt; length(times)</code> ; if it is so set, <code>ic.lag</code> is set to <code>length(times)</code> with a warning.
<code>var.factor</code>	optional positive scalar; the scaling coefficient relating the width of the starting particle distribution to <code>rw.sd</code> . In particular, the width of the distribution of particles at the start of the first <code>mif</code> iteration will be <code>random.walk.sd*var.factor</code> . By default, <code>var.factor=1</code> .
<code>cooling.type</code> , <code>cooling.fraction.50</code>	specifications for the cooling schedule, i.e., the manner in which the intensity of the parameter perturbations is reduced with successive filtering iterations. <code>cooling.type</code> specifies the nature of the cooling schedule. When <code>cooling.type="geometric"</code> , on the $n$ -th <code>mif</code> iteration, the relative perturbation intensity is <code>cooling.fraction.50<sup>(n/50)</sup></code> . When <code>cooling.type="hyperbolic"</code> , on the $n$ -th <code>mif</code> iteration, the relative perturbation intensity is $(s+1)/(s+n)$ , where $(s+1)/(s+50) = \text{cooling.fraction.50}$ . <code>cooling.fraction.50</code> is the relative magnitude of the parameter perturbations after 50 <code>mif</code> iterations.
<code>method</code>	<code>method</code> sets the update rule used in the algorithm. <code>method="mif"</code> uses the iterated filtering update rule (Ionides 2006, 2011); <code>method="unweighted"</code> updates the parameter to the unweighted average of the filtering means of the parameters at each time; <code>method="fp"</code> updates the parameter to the filtering mean at the end of the time series.
<code>tol</code> , <code>max.fail</code>	See the description under <a href="#">pfilter</a> .
<code>verbose</code>	logical; if <code>TRUE</code> , print progress reports.
<code>transform</code>	logical; if <code>TRUE</code> , optimization is performed on the transformed scale, as defined by the user-supplied parameter transformations (see <a href="#">pomp</a> ).
<code>...</code>	additional arguments that override the defaults.
<code>pars</code>	names of parameters.

**Value**

Upon successful completion, `mif` returns an object of class `mif`. The latter inherits from the [pfilterd.pomp](#) and [pomp](#) classes.

**Regular parameters vs initial-value parameters**

Initial-value parameters (IVPs) differ from regular parameters in that the majority of the information about these parameters is restricted to the early part of the time series. That is, increasing the length of the time series provides progressively less additional information about IVPs than it does about regular parameters. In `mif`, while regular parameters are perturbed at the initial time and after every observation, IVPs are perturbed only at the initial time.

### Re-running `mif` Iterations

To re-run a sequence of `mif` iterations, one can use the `mif` method on a `mif` object. By default, the same parameters used for the original `mif` run are re-used (except for `tol`, `max.fail`, and `verbose`, the defaults of which are shown above). If one does specify additional arguments, these will override the defaults.

### Continuing `mif` Iterations

One can resume a series of `mif` iterations from where one left off using the `continue` method. A call to `mif` to perform  $N_{\text{mif}}=m$  iterations followed by a call to `continue` to perform  $N_{\text{mif}}=n$  iterations will produce precisely the same effect as a single call to `mif` to perform  $N_{\text{mif}}=m+n$  iterations. By default, all the algorithmic parameters are the same as used in the original call to `mif`. Additional arguments will override the defaults.

### Using `mif` to estimate initial-value parameters only

One can use `mif`'s fixed-lag smoothing to estimate only initial value parameters (IVPs). In this case, the IVPs to be estimated are named in `ivps` and no positive entries in `rw.sd` correspond to any parameters not named in `ivps`. If `theta` is the current parameter vector, then at each `mif` iteration,  $N_p$  particles are drawn from a normal distribution centered at `theta` and with width proportional to `var.factor*rw.sd`, a particle filtering operation is performed, and `theta` is replaced by the filtering mean at `time(object)[ic.lag]`. Note the implication that, when `mif` is used in this way on a time series any longer than `ic.lag`, unnecessary work is done. If the time series in `object` is longer than `ic.lag`, consider replacing `object` with `window(object, end=ic.lag)`.

### Methods

Methods that can be used to manipulate, display, or extract information from a `mif` object:

**conv.rec** `conv.rec(object, pars, transform = FALSE)` returns the columns of the convergence-record matrix corresponding to the names in `pars`. By default, all columns are returned. If `transform=TRUE`, the parameters are transformed from the estimation scale.

**logLik** Returns the value in the `loglik` slot. NB: this is *not* the same as the likelihood of the model at the MLE!

**c** Concatenates `mif` objects into a `mifList`.

**plot** Plots a series of diagnostic plots when applied to a `mif` or `mifList` object.

### Author(s)

Aaron A. King

### References

- E. L. Ionides, C. Breto, & A. A. King, Inference for nonlinear dynamical systems, *Proc. Natl. Acad. Sci. U.S.A.*, 103:18438–18443, 2006.
- E. L. Ionides, A. Bhadra, Y. Atchad'e, & A. A. King, Iterated filtering, *Annals of Statistics*, 39:1776–1802, 2011.



E. L. Ionides, D. Nguyen, Y. Atchad\`e, S. Stoev, and A. A. King. Inference for dynamic and latent variable models via iterated, perturbed Bayes maps. *Proc. Natl. Acad. Sci. U.S.A.*, 112:719–724, 2015.

A. A. King, E. L. Ionides, M. Pascual, and M. J. Bouma, Inapparent infections and cholera dynamics, *Nature*, 454:877–880, 2008.

## See Also

[pomp](#), [pfilter](#), [mif2](#)

---

Iterated filtering 2    *IF2: Maximum likelihood by iterated, perturbed Bayes maps*

---

## Description

An improved iterated filtering algorithm for estimating the parameters of a partially-observed Markov process. Running `mif2` causes the algorithm to perform a specified number of particle-filter iterations. At each iteration, the particle filter is performed on a perturbed version of the model, in which the parameters to be estimated are subjected to random perturbations at each observation. This extra variability effectively smooths the likelihood surface and combats particle depletion by introducing diversity into particle population. As the iterations progress, the magnitude of the perturbations is diminished according to a user-specified cooling schedule. The algorithm is presented and justified in Ionides et al. (2015).

## Usage

```
## S4 method for signature 'pomp'
mif2(object, Nmif = 1, start, Np, rw.sd, transform = FALSE,
      cooling.type = c("hyperbolic", "geometric"), cooling.fraction.50,
      tol = 1e-17, max.fail = Inf, verbose = getOption("verbose"), ...)
## S4 method for signature 'pfilterd.pomp'
mif2(object, Nmif = 1, Np, tol, ...)
## S4 method for signature 'mif2d.pomp'
mif2(object, Nmif, start, Np, rw.sd, transform,
      cooling.type, cooling.fraction.50, tol, ...)
## S4 method for signature 'mif2d.pomp'
continue(object, Nmif = 1, ...)
## S4 method for signature 'mif2d.pomp'
conv.rec(object, pars, transform = FALSE, ...)
## S4 method for signature 'mif2List'
conv.rec(object, ...)
rw.sd(...)
```

**Arguments**

<code>object</code>	An object of class <code>pomp</code> .
<code>Nmif</code>	The number of filtering iterations to perform.
<code>start</code>	named numerical vector; the starting guess of the parameters. By default, <code>start=coef(object)</code> .
<code>Np</code>	the number of particles to use in filtering. This may be specified as a single positive integer, in which case the same number of particles will be used at each timestep. Alternatively, if one wishes the number of particles to vary across timestep, one may specify <code>Np</code> either as a vector of positive integers (of length <code>length(time(object))</code> ) or as a function taking a positive integer argument. In the latter case, <code>Np(n)</code> must be a single positive integer, representing the number of particles to be used at the <i>n</i> -th timestep: <code>Np(1)</code> is the number of particles to use going from <code>timezero(object)</code> to <code>time(object)[1]</code> , <code>Np(2)</code> , from <code>time(object)[1]</code> to <code>time(object)[2]</code> , and so on. <b>Note that this behavior differs from that of <code>mif</code>!</b>
<code>rw.sd</code>	specification of the magnitude of the random-walk perturbations that will be applied to some or all model parameters. Parameters that are to be estimated should have positive perturbations specified here. The specification is given using the <code>rw.sd</code> function, which creates a list of unevaluated expressions. The latter are evaluated in a context where the model time variable is defined (as <code>time</code> ). The expression <code>ivp(s)</code> can be used in this context as shorthand for  <code>ifelse(time==time[1],s,0)</code> .  Likewise, <code>ivp(s,lag)</code> is equivalent to  <code>ifelse(time==time[lag],s,0)</code> .  See below for some examples. The perturbations that are applied are normally distributed with the specified s.d. If <code>transform = TRUE</code> , then they are applied on the estimation scale.
<code>transform</code>	logical; if <code>TRUE</code> , optimization is performed on the estimation scale, as defined by the user-supplied parameter transformations (see <a href="#">pomp</a> ). This can be used, for example, to enforce positivity or interval constraints on model parameters. See the tutorials on the <a href="#">package website</a> for examples.
<code>cooling.type</code> , <code>cooling.fraction.50</code>	specifications for the cooling schedule, i.e., the manner in which the intensity of the parameter perturbations is reduced with successive filtering iterations. <code>cooling.type</code> specifies the nature of the cooling schedule. See below (under “Specifying the perturbations”) for more detail.
<code>tol</code> , <code>max.fail</code>	passed to the particle filter. See the descriptions under <a href="#">pfilter</a> .
<code>verbose</code>	logical; if <code>TRUE</code> , print progress reports.
<code>...</code>	additional arguments that override the defaults.
<code>pars</code>	names of parameters.

**Value**

Upon successful completion, `mif2` returns an object of class `mif2d.pomp`. This class inherits from the `pfilterd.pomp` and `pomp` classes.

**Specifying the perturbations: the `rw.sd` function**

This function simply returns a list containing its arguments as unevaluated expressions. These are then evaluated in a context containing the model time variable. This allows for easy specification of the structure of the perturbations that are to be applied. For example,

```
rw.sd(a=0.05,
      b=ifelse(0.2,time==time[1],0),
      c=ivp(0.2),
      d=ifelse(time==time[13],0.2,0),
      e=ivp(0.2,lag=13),
      f=ifelse(time<23,0.02,0))
```

results in perturbations of parameter `a` with s.d. 0.05 at every time step, while parameters `b` and `c` both get perturbations of s.d. 0.2 only before the first observation. Parameters `d` and `e`, by contrast, get perturbations of s.d. 0.2 only before the thirteenth observation. Finally, parameter `f` gets a random perturbation of size 0.02 before every observation falling before  $t = 23$ .

On the  $m$ -th IF2 iteration, prior to time-point  $n$ , the  $d$ -th parameter is given a random increment normally distributed with mean 0 and standard deviation  $c_{m,n}\sigma_{d,n}$ , where  $c$  is the cooling schedule and  $\sigma$  is specified using `rw.sd`, as described above. Let  $N$  be the length of the time series and  $\alpha = \text{cooling.fraction} \cdot 50$ . Then, when `cooling.type="geometric"`, we have

$$c_{m,n} = \alpha^{\frac{n-1+(m-1)N}{50N}}.$$

When `cooling.type="hyperbolic"`, we have

$$c_{m,n} = \frac{s+1}{s+n+(m-1)N},$$

where  $s$  satisfies

$$\frac{s+1}{s+50N} = \alpha.$$

Thus, in either case, the perturbations at the end of 50 IF2 iterations are a fraction  $\alpha$  smaller than they are at first.

**Re-running `mif2` Iterations**

To re-run a sequence of `mif2` iterations, one can use the `mif2` method on a `mif2d.pomp` object. By default, the same parameters used for the original `mif2` run are re-used (except for `tol`, `max.fail`, and `verbose`, the defaults of which are shown above). If one does specify additional arguments, these will override the defaults.

### Continuing mif2 Iterations

One can resume a series of mif2 iterations from where one left off using the `continue` method. A call to `mif2` to perform  $N_{\text{mif}}=m$  iterations followed by a call to `continue` to perform  $N_{\text{mif}}=n$  iterations will produce precisely the same effect as a single call to `mif2` to perform  $N_{\text{mif}}=m+n$  iterations. By default, all the algorithmic parameters are the same as used in the original call to `mif2`. Additional arguments will override these defaults.

### Methods

Methods that can be used to manipulate, display, or extract information from a `mif2d.pomp` object:

**conv.rec** `conv.rec(object, pars, transform)` returns the columns of the convergence-record matrix corresponding to the names in `pars`. By default, all columns are returned. If `transform=TRUE`, the parameters are transformed from the estimation scale.

**logLik** Returns the value in the `loglik` slot. NB: this is *not* the same as the likelihood of the model at the MLE!

**c** Concatenates `mif2d.pomp` objects into a `mif2List`.

**plot** Plots a series of diagnostic plots when applied to a `mif2d.pomp` or `mif2List` object.

### Author(s)

Aaron A. King, Edward L. Ionides, and Dao Nguyen

### References

E. L. Ionides, D. Nguyen, Y. Atchad'e, S. Stoev, and A. A. King. Inference for dynamic and latent variable models via iterated, perturbed Bayes maps. *Proc. Natl. Acad. Sci. U.S.A.*, 112:719–724, 2015.

### See Also

[pomp](#), [pfilter](#), [mif](#), and the [IF2 tutorial](#) on the [package website](#).

### Examples

```
## Not run:
pompExample(ou2)

guess1 <- guess2 <- coef(ou2)
guess1[c('x1.0', 'x2.0', 'alpha.2', 'alpha.3')] <- 0.5*guess1[c('x1.0', 'x2.0', 'alpha.2', 'alpha.3')]
guess2[c('x1.0', 'x2.0', 'alpha.2', 'alpha.3')] <- 1.5*guess1[c('x1.0', 'x2.0', 'alpha.2', 'alpha.3')]

m1 <- mif2(ou2, Nmif=100, start=guess1, Np=1000,
          cooling.type="hyperbolic", cooling.fraction.50=0.05,
          rw.sd=rw.sd(x1.0=ivp(0.5), x2.0=ivp(0.5),
                     alpha.2=0.1, alpha.3=0.1))

m2 <- mif2(ou2, Nmif=100, start=guess2, Np=1000,
          cooling.type="hyperbolic", cooling.fraction.50=0.05,
          rw.sd=rw.sd(x1.0=ivp(0.5), x2.0=ivp(0.5),
```

```

alpha.2=0.1,alpha.3=0.1))

plot(c(m1,m2))

rbind(mle1=c(coef(m1),loglik=logLik(pfilter(m1,Np=1000))),
      mle2=c(coef(m2),loglik=logLik(pfilter(m1,Np=1000))),
      truth=c(coef(ou2),loglik=logLik(pfilter(m1,Np=1000))))

## End(Not run)

```

logmeanexp

*The log-mean-exp trick***Description**

logmeanexp computes

$$\log \frac{1}{N} \sum_{n=1}^N e_i^x,$$

avoiding over- and under-flow in doing so. It can optionally return an estimate of the standard error in this quantity.

**Usage**

```
logmeanexp(x, se = FALSE)
```

**Arguments**

x                    numeric  
se                    logical; give approximate standard error?

**Details**

When se = TRUE, logmeanexp uses a jackknife estimate of the variance in  $\log(x)$ .

**Value**

$\log(\text{mean}(\exp(x)))$  computed so as to avoid over- or underflow. If se = FALSE, the approximate standard error is returned as well.

**Author(s)**

Aaron A. King

## Examples

```
## generate a bifurcation diagram for the Ricker map
pompExample(ricker)
ll <- replicate(n=5, logLik(pfilter(ricker, Np=1000)))
## an estimate of the log likelihood:
logmeanexp(ll)
## with standard error:
logmeanexp(ll, se=TRUE)
```

---

Low-level-interface     *pomp low-level interface*

---

## Description

A **pomp** object implements a partially observed Markov process (POMP) model. Basic operations on this model (with shorthand terms) include:

1. simulation of the state process given parameters (`rprocess`)
2. evaluation of the likelihood of a given state trajectory given parameters (`dprocess`)
3. simulation of the observation process given the states and parameters (`rmeasure`)
4. evaluation of the likelihood of a set of observations given the states and parameters (`dmeasure`)
5. simulation from the prior probability distribution (`rprior`)
6. evaluation of the prior probability density (`dprior`)
7. simulation from the distribution of initial states, given parameters (`init.state`)
8. evaluation of the deterministic skeleton at a point in state space, given parameters (`skeleton`)
9. computation of a trajectory of the deterministic skeleton given parameters (`trajectory`)

**pomp** provides S4 methods that implement each of these basic operations. These operations can be combined to implement statistical inference methods that depend only on a model's POMP structure. For convenience, parameter transformations may also be enclosed in a **pomp** object.

This page documents these elements.

## Usage

```
## S4 method for signature 'pomp'
rprocess(object, xstart, times, params, offset = 0, ...)
## S4 method for signature 'pomp'
dprocess(object, x, times, params, log = FALSE, ...)
## S4 method for signature 'pomp'
rmeasure(object, x, times, params, ...)
## S4 method for signature 'pomp'
dmeasure(object, y, x, times, params, log = FALSE, ...)
## S4 method for signature 'pomp'
dprior(object, params, log = FALSE, ...)
## S4 method for signature 'pomp'
```

```

rprior(object, params, ...)
## S4 method for signature 'pomp'
init.state(object, params, t0, nsim, ...)
## S4 method for signature 'pomp'
skeleton(object, x, t, params, ...)
## S4 method for signature 'pomp'
trajectory(object, params, times, t0, as.data.frame = FALSE, ...)
## S4 method for signature 'pomp'
pompLoad(object, ...)
## S4 method for signature 'pomp'
pompUnload(object, ...)

```

### Arguments

<code>object</code>	an object of class <code>pomp</code> .
<code>xstart</code>	an <code>nvar x nrep</code> matrix containing the starting state of the system. Columns of <code>xstart</code> correspond to states; rows to components of the state vector. One independent simulation will be performed for each column. Note that in this case, <code>params</code> must also have <code>nrep</code> columns.
<code>x</code>	a rank-3 array containing states of the unobserved process. The dimensions of <code>x</code> are <code>nvars x nrep x ntimes</code> , where <code>nvars</code> is the number of state variables, <code>nrep</code> is the number of replicates, and <code>ntimes</code> is the length of times.
<code>y</code>	a matrix containing observations. The dimensions of <code>y</code> are <code>nobs x ntimes</code> , where <code>nobs</code> is the number of observables and <code>ntimes</code> is the length of times.
<code>times, t</code>	a numeric vector (length <code>ntimes</code> ) containing times. These must be in non-decreasing order.
<code>params</code>	a <code>npar x nrep</code> matrix of parameters. Each column is an independent parameter set and is paired with the corresponding column of <code>x</code> or <code>xstart</code> . In the case of <code>init.state</code> , <code>params</code> is a named vector of parameters.
<code>offset</code>	integer; the first <code>offset</code> times in <code>times</code> will not be returned.
<code>t0</code>	the initial time at which initial states are requested.
<code>nsim</code>	optional integer; the number of initial states to simulate. By default, this is equal to the number of columns of <code>params</code> .
<code>log</code>	if <code>TRUE</code> , log probabilities are returned.
<code>as.data.frame</code>	logical; if <code>TRUE</code> , return the result as a data-frame.
<code>...</code>	In <code>trajectory</code> , additional arguments are passed to the ODE integrator (if the skeleton is a vectorfield) and ignored if it is a map. See <a href="#">ode</a> for a description of the additional arguments accepted. In all other cases, additional arguments are ignored.

### rprocess

`rprocess` simulates the process-model portion of partially-observed Markov process.

When `rprocess` is called, the first entry of `times` is taken to be the initial time (i.e., that corresponding to `xstart`). Subsequent times are the additional times at which the state of the simulated processes are required.

`rprocess` returns a rank-3 array with rownames. Suppose `x` is the array returned. Then

`dim(x)=c(nvars,nrep,ntimes-offset),`

where `nvars` is the number of state variables (`=nrow(xstart)`), `nrep` is the number of independent realizations simulated (`=ncol(xstart)`), and `ntimes` is the length of the vector `times`. `x[,j,k]` is the value of the state process in the  $j$ -th realization at time `times[k+offset]`. The rownames of `x` must correspond to those of `xstart`.

### **dprocess**

`dprocess` evaluates the probability density of a sequence of consecutive state transitions.

`dprocess` returns a matrix of dimensions `nrep x ntimes-1`. If `d` is the returned matrix, `d[j,k]` is the likelihood of the transition from state `x[,j,k-1]` at time `times[k-1]` to state `x[,j,k]` at time `times[k]`.

### **rmeasure**

`rmeasure` simulate the measurement model given states and parameters.

`rmeasure` returns a rank-3 array of dimensions `nobs x nrep x ntimes`, where `nobs` is the number of observed variables.

### **dmeasure**

`dmeasure` evaluates the probability density of observations given states.

`dmeasure` returns a matrix of dimensions `nreps x ntimes`. If `d` is the returned matrix, `d[j,k]` is the likelihood of the observation `y[,k]` at time `times[k]` given the state `x[,j,k]`.

### **dprior, rprior**

`dprior` evaluates the prior probability density and `rprior` simulates from the prior.

### **init.state**

`init.state` returns an `nvar x nsim` matrix of state-process initial conditions when given an `npar x nsim` matrix of parameters, `params`, and an initial time `t0`. By default, `t0` is the initial time defined when the `pomp` object `ws` constructed. If `nsim` is not specified, then `nsim=ncol(params)`.

### **skeleton**

The method `skeleton` evaluates the deterministic skeleton at a point or points in state space, given parameters. In the case of a discrete-time system, the skeleton is a map. In the case of a continuous-time system, the skeleton is a vectorfield. NB: `skeleton` just evaluates the deterministic skeleton; it does not iterate or integrate.

`skeleton` returns an array of dimensions `nvar x nrep x ntimes`. If `f` is the returned matrix, `f[i,j,k]` is the  $i$ -th component of the deterministic skeleton at time `times[k]` given the state `x[,j,k]` and parameters `params[,j]`.



**trajectory**

`trajectory` computes a trajectory of the deterministic skeleton of a Markov process. In the case of a discrete-time system, the deterministic skeleton is a map and a trajectory is obtained by iterating the map. In the case of a continuous-time system, the deterministic skeleton is a vector-field; `trajectory` uses the numerical solvers in [deSolve](#) to integrate the vectorfield.

`trajectory` returns an array of dimensions `nvar x nrep x ntimes`. If `x` is the returned matrix, `x[i,j,k]` is the *i*-th component of the state vector at time `times[k]` given parameters `params[j]`.

When the skeleton is a vectorfield, `trajectory` integrates it using [ode](#). When the skeleton is a map, `trajectory` iterates it. By default, time is advanced 1 unit per iteration. The user can change this behavior by specifying the desired timestep using the argument `skelmap.delta.t` in the construction of the `pomp` object.

**Parameter transformations**

User-defined parameter transformations enclosed in the `pomp` object can be accessed via [partrans](#).

**pompLoad, pompUnload**

`pompLoad` and `pompUnload` cause compiled codes associated with object to be dynamically linked or unlinked, respectively. When C snippets are used in the construction of a `pomp` object, the resulting shared-object library is dynamically loaded (linked) before each use, and unloaded afterward. These functions are provided because in some instances, greater control may be desired. These functions have no effect on shared-object libraries linked by the user.

**Author(s)**

Aaron A. King

**See Also**

[pomp](#), [pomp methods](#)

**Examples**

```
pompExample(ricker)

p <- parmat(c(r=42,c=1,phi=10,sigma=0.3,N.0=7,e.0=0),10)
t <- c(1:10,20,30)
t0 <- 0
x0 <- init.state(ricker,params=p,t0=t0)
x <- rprocess(ricker,xstart=x0,times=c(t0,t),params=p,offset=1)
y <- rmeasure(ricker,params=p,x=x,times=t)
ll <- dmeasure(ricker,y=y[,3,,drop=FALSE],x=x,times=t,params=p,log=TRUE)
apply(ll,1,sum)
f <- skeleton(ricker,x=x,t=t,params=p)
z <- trajectory(ricker,params=p,times=t,t0=t0)

## short arguments are recycled:
p <- c(r=42,phi=10,c=1,sigma=0.3,N.0=7,e.0=0)
t <- c(1:10,20,30)
```

```

t0 <- 0
x0 <- init.state(ricker, params=p, t0=t0)
x <- rprocess(ricker, xstart=x0, times=c(t0, t), params=p, offset=1)
y <- rmeasure(ricker, params=p, x=x, times=t)
ll <- dmeasure(ricker, y=y, x=x, times=t, params=p, log=TRUE)
f <- skeleton(ricker, x=x, t=t, params=p)
z <- trajectory(ricker, params=p, times=t, t0=t0)

```

---

MCMC proposal distributions

*MCMC proposal distributions*

---

## Description

Functions to construct proposal distributions for use with MCMC methods.

## Usage

```

mvn.rw(rw.var)
mvn.diag.rw(rw.sd)
mvn.rw.adaptive(rw.sd, rw.var, scale.start = NA, scale.cooling = 0.999,
               shape.start = NA, target = 0.234, max.scaling = 50)

```

## Arguments

<code>rw.var</code>	square numeric matrix with row- and column-names. Specifies the variance-covariance matrix for a multivariate normal random-walk proposal distribution.
<code>rw.sd</code>	named numeric vector; random-walk SDs for a multivariate normal random-walk proposal with diagonal variance-covariance matrix.
<code>scale.start</code> , <code>scale.cooling</code> , <code>shape.start</code> , <code>target</code> , <code>max.scaling</code>	parameters to control the proposal adaptation algorithm. Beginning with MCMC iteration <code>scale.start</code> , the scale of the proposal covariance matrix will be adjusted in an effort to match the <code>target</code> acceptance ratio. This initial scale adjustment is “cooled”, i.e., the adjustment diminishes as the chain moves along. The parameter <code>scale.cooling</code> specifies the cooling schedule: at $n$ iterations after <code>scale.start</code> , the current scaling factor is multiplied with $\text{scale.cooling}^n$ . The maximum scaling factor allowed at any one iteration is <code>max.scaling</code> . After <code>shape.start</code> accepted proposals have accumulated, a scaled empirical covariance matrix will be used for the proposals, following Roberts and Rosenthal (2009).

## Value

Each of these calls constructs a function suitable for use as the proposal argument of `pmcmc` or `abc`. Given a parameter vector, each such function returns a single draw from the corresponding proposal distribution.

**Author(s)**

Aaron A. King, Sebastian Funk

**References**

Gareth O. Roberts and Jeffrey S. Rosenthal. Examples of Adaptive MCMC. *J. Comput. Graph. Stat.*, 18:349–367, 2009.

**See Also**

[pmcmc](#), [abc](#)

---

Nonlinear forecasting    *Parameter estimation my maximum simulated quasi-likelihood (non-linear forecasting)*

---

**Description**

`nlf` calls an optimizer to maximize the nonlinear forecasting (NLF) goodness of fit. The latter is computed by simulating data from a model, fitting a nonlinear autoregressive model to the simulated time series, and quantifying the ability of the resulting fitted model to predict the data time series. NLF is an ‘indirect inference’ method using a quasi-likelihood as the objective function.

**Usage**

```
## S4 method for signature 'pomp'
nlf(object, start, est, lags, period = NA, tensor = FALSE,
     nconverge=1000, nasymp=1000, seed = 1066,
     transform.data, nrbf = 4,
     method = c("subplex", "Nelder-Mead", "BFGS", "CG", "L-BFGS-B", "SANN", "Brent"),
     skip.se = FALSE, verbose = getOption("verbose"), bootsamp = NULL,
     lql.frac = 0.1, se.par.frac = 0.1, eval.only = FALSE,
     transform = FALSE, ...)
## S4 method for signature 'nlfd.pomp'
nlf(object, start, est, lags, period, tensor,
     nconverge, nasymp, seed, transform.data, nrbf, method,
     lql.frac, se.par.frac, transform, ...)
```

**Arguments**

<code>object</code>	A <code>pomp</code> object, with the data and model to fit to it.
<code>start</code>	Named numeric vector with guessed parameters.
<code>est</code>	Vector containing the names or indices of parameters to be estimated.
<code>lags</code>	A vector specifying the lags to use when constructing the nonlinear autoregressive prediction model. The first lag is the prediction interval.

period	numeric; period=NA means the model is nonseasonal. period>0 is the period of seasonal forcing in 'real time'.
tensor	logical; if FALSE, the fitted model is a generalized additive model with time mod period as one of the predictors, i.e., a gam with time-varying intercept. If TRUE, the fitted model is a gam with lagged state variables as predictors and time-periodic coefficients, constructed using tensor products of basis functions of state variables with basis functions of time.
nconverge	number of convergence timesteps to be discarded from the model simulation.
nasymp	number of asymptotic timesteps to be recorded from the model simulation.
seed	integer specifying the random number seed to use. When fitting, it is usually best to always run the simulations with the same sequence of random numbers, which is accomplished by setting seed to an integer. If you want a truly random simulation, set seed=NULL.
transform	logical; if TRUE, parameters are optimized on the transformed scale.
transform.data	optional function. If specified, forecasting is performed using data and model simulations transformed by this function. By default, transform.data is the identity function, i.e., no transformation is performed. The main purpose of transform.data is to achieve approximately multivariate normal forecasting errors. If data are univariate, transform.data should take a scalar and return a scalar. If data are multivariate, transform.data should assume a vector input and return a vector of the same length.
nrbf	integer scalar; the number of radial basis functions to be used at each lag.
method	Optimization method. Choices are <a href="#">subplex</a> and any of the methods used by <a href="#">optim</a> .
skip.se	logical; if TRUE, skip the computation of standard errors.
verbose	logical; if TRUE, the negative log quasiliikelihood and parameter values are printed at each iteration of the optimizer.
bootsamp	vector of integers; used to have the quasi-loglikelihood evaluated using a bootstrap re-sampling of the data set.
lql.frac	target fractional change in log quasi-likelihood for quadratic standard error estimate
se.par.frac	initial parameter-change fraction for quadratic standard error estimate
eval.only	logical; if TRUE, no optimization is attempted and the quasi-loglikelihood value is evaluated at the start parameters.
...	Arguments that will be passed to optim or subplex in the control list.

### Details

This runs an optimizer to maximize `nlf.objfun`.

### Value

An object of class `nlf.d.pomp`. `logLik` applied to such an object returns the log quasi likelihood. The `$` method allows extraction of arbitrary slots from the `nlf.d.pomp` object.

**Author(s)**

Stephen P. Ellner, Bruce E. Kendall, Aaron A. King

**References**

The following papers describe and motivate the NLF approach to model fitting:

Ellner, S. P., Bailey, B. A., Bobashev, G. V., Gallant, A. R., Grenfell, B. T. and Nychka D. W. (1998) Noise and nonlinearity in measles epidemics: combining mechanistic and statistical approaches to population modeling. *American Naturalist* **151**, 425–440.

Kendall, B. E., Briggs, C. J., Murdoch, W. W., Turchin, P., Ellner, S. P., McCauley, E., Nisbet, R. M. and Wood S. N. (1999) Why do populations cycle? A synthesis of statistical and mechanistic modeling approaches. *Ecology* **80**, 1789–1805.

Kendall, B. E., Ellner, S. P., McCauley, E., Wood, S. N., Briggs, C. J., Murdoch, W. W. and Turchin, P. (2005) Population cycles in the pine looper moth (*Bupalus piniarius*): dynamical tests of mechanistic hypotheses. *Ecological Monographs* **75**, 259–276.

---

ou2

---

Two-dimensional discrete-time Ornstein-Uhlenbeck process

---

**Description**

ou2 is a pomp object encoding a bivariate discrete-time Ornstein-Uhlenbeck process.

**Details**

If the state process is  $X(t) = (x_1(t), x_2(t))$ , then

$$X(t+1) = \alpha X(t) + \sigma \epsilon(t),$$

where  $\alpha$  and  $\sigma$  are 2x2 matrices,  $\sigma$  is lower-triangular, and  $\epsilon(t)$  is standard bivariate normal. The observation process is  $Y(t) = (y_1(t), y_2(t))$ , where  $y_i(t) \sim \text{normal}(x_i(t), \tau)$ . The functions `rprocess`, `dprocess`, `rmeasure`, `dmeasure`, and `skeleton` are implemented using compiled C code for computational speed: see the source code for details.

**See Also**

[pomp](#)

**Examples**

```
pompExample(ou2)
plot(ou2)
coef(ou2)
x <- simulate(ou2)
plot(x)
pf <- pfilter(ou2, Np=1000)
logLik(pf)
```

---

parmat	<i>Create a matrix of parameters</i>
--------	--------------------------------------

---

### Description

parmat is a utility that makes a vector of parameters suitable for use in **pomp** functions.

### Usage

```
parmat(params, nrep = 1)
```

### Arguments

params	named numeric vector or matrix of parameters.
nrep	number of replicates (columns) desired.

### Value

parmat returns a matrix consisting of nrep copies of params.

### Author(s)

Aaron A. King

### Examples

```
## generate a bifurcation diagram for the Ricker map
pompExample(ricker)
p <- parmat(coef(ricker), nrep=500)
p["r",] <- exp(seq(from=1.5, to=4, length=500))
x <- trajectory(ricker, times=seq(from=1000, to=2000, by=1), params=p)
matplot(p["r",], x["N",,], pch='.', col='black', xlab="log(r)", ylab="N", log='x')
```

---

Particle filter	<i>Particle filter</i>
-----------------	------------------------

---

### Description

A plain vanilla sequential Monte Carlo (particle filter) algorithm. Resampling is performed at each observation.

**Usage**

```
## S4 method for signature 'pomp'
pfilter(object, params, Np, tol = 1e-17,
        max.fail = Inf, pred.mean = FALSE, pred.var = FALSE,
        filter.mean = FALSE, filter.traj = FALSE, save.states = FALSE,
        save.params = FALSE, verbose = getOption("verbose"), ...)
## S4 method for signature 'pfilterd.pomp'
pfilter(object, params, Np, tol, ...)
## S4 method for signature 'pfilterd.pomp'
logLik(object, ...)
## S4 method for signature 'pfilterd.pomp'
cond.logLik(object, ...)
## S4 method for signature 'pfilterd.pomp'
eff.sample.size(object, ...)
## S4 method for signature 'pfilterd.pomp'
pred.mean(object, pars, ...)
## S4 method for signature 'pfilterd.pomp'
pred.var(object, pars, ...)
## S4 method for signature 'pfilterd.pomp'
filter.mean(object, pars, ...)
## S4 method for signature 'pfilterd.pomp'
filter.traj(object, vars, ...)
```

**Arguments**

object	An object of class <code>pomp</code> or inheriting class <code>pomp</code> .
params	optional named numeric vector containing the parameters at which the filtering should be performed. By default, <code>params = coef(object)</code> .
Np	<p>the number of particles to use. This may be specified as a single positive integer, in which case the same number of particles will be used at each timestep. Alternatively, if one wishes the number of particles to vary across timesteps, one may specify <code>Np</code> either as a vector of positive integers of length</p> <pre>length(time(object, t0=TRUE))</pre> <p>or as a function taking a positive integer argument. In the latter case, <code>Np(k)</code> must be a single positive integer, representing the number of particles to be used at the <i>k</i>-th timestep: <code>Np(0)</code> is the number of particles to use going from <code>timezero(object)</code> to <code>time(object)[1]</code>, <code>Np(1)</code>, from <code>timezero(object)</code> to <code>time(object)[1]</code>, and so on, while when <code>T=length(time(object, t0=TRUE))</code>, <code>Np(T)</code> is the number of particles to sample at the end of the time-series. When object is of class <code>mif</code>, this is by default the same number of particles used in the <code>mif</code> iterations.</p> <p>One should omit <code>Np</code> if <code>params</code> is a matrix of parameters, with one column for each particle. In this case, obviously, the number of particles is <code>ncol(params)</code>.</p>
tol	positive numeric scalar; particles with likelihood less than <code>tol</code> are considered to be incompatible with the data. See the section on <i>Filtering Failures</i> below for more information.

<code>max.fail</code>	integer; the maximum number of filtering failures allowed (see below). If the number of filtering failures exceeds this number, execution will terminate with an error. By default, <code>max.fail</code> is set to infinity, so no error can be triggered.
<code>pred.mean</code>	logical; if TRUE, the prediction means are calculated for the state variables and parameters.
<code>pred.var</code>	logical; if TRUE, the prediction variances are calculated for the state variables and parameters.
<code>filter.mean</code>	logical; if TRUE, the filtering means are calculated for the state variables and parameters.
<code>filter.traj</code>	logical; if TRUE, a filtered trajectory is returned for the state variables and parameters.
<code>save.states, save.params</code>	logical. If <code>save.states=TRUE</code> , the state-vector for each particle at each time is saved in the <code>saved.states</code> slot of the returned <code>pfilterd.pomp</code> object. If <code>save.params=TRUE</code> , the parameter-vector for each particle at each time is saved in the <code>saved.params</code> slot of the returned <code>pfilterd.pomp</code> object.
<code>verbose</code>	logical; if TRUE, progress information is reported as <code>pfilter</code> works.
<code>pars</code>	Names of parameters.
<code>vars</code>	Names of state variables.
<code>...</code>	additional arguments that override the defaults.

### Value

An object of class `pfilterd.pomp`. This class inherits from class `pomp`. The following additional slots can be accessed via the `$` operator:

**saved.states** If `pfilter` was called with `save.states=TRUE`, this is the list of state-vectors at each time point, for each particle. It is a length-`ntimes` list of `nvars`-by-`Np` arrays. In particular, `saved.states[[t]][,i]` can be considered a sample from  $f[X_t|y_{1:t}]$ .

**saved.params** If `pfilter` was called with `save.params=TRUE`, this is the list of parameter-vectors at each time point, for each particle. It is a length-`ntimes` list of `npars`-by-`Np` arrays. In particular, `saved.params[[t]][,i]` is the parameter portion of the  $i$ -th particle at time  $t$ .

**Np, tol, nfail** the number of particles used, failure tolerance, and number of filtering failures (see below), respectively.

### Methods

**logLik** Extracts the estimated log likelihood.

**cond.logLik** Extracts the estimated conditional log likelihood

$$\ell_t(\theta) = \text{Prob}[y_t|y_1, \dots, y_{t-1}],$$

where  $y_t$  are the data, at time  $t$ .

**eff.sample.size** Extracts the (time-dependent) estimated effective sample size, computed as

$$\left( \sum_i w_{it}^2 \right)^{-1},$$

where  $w_{it}$  is the normalized weight of particle  $i$  at time  $t$ .



**pred.mean, pred.var** Extract the mean and variance of the approximate prediction distribution. This prediction distribution is that of

$$X_t|y_1, \dots, y_{t-1},$$

where  $X_t, y_t$  are the state vector and data, respectively, at time  $t$ .

**filter.mean** Extract the mean of the filtering distribution, which is that of

$$X_t|y_1, \dots, y_t,$$

where  $X_t, y_t$  are the state vector and data, respectively, at time  $t$ .

### Filtering failures

If the degree of disagreement between model and data becomes sufficiently large, a “filtering failure” results. A filtering failure occurs when, at some time point, none of the  $N_p$  particles is compatible with the data. In particular, if the conditional likelihood of a particle at any time is below the tolerance value `tol`, then that particle is considered to be uninformative and its likelihood is taken to be zero. A filtering failure occurs when this is the case for all particles. A warning is generated when this occurs unless the cumulative number of failures exceeds `max.fail`, in which case an error is generated.

### Author(s)

Aaron A. King

### References

M. S. Arulampalam, S. Maskell, N. Gordon, & T. Clapp. A Tutorial on Particle Filters for Online Nonlinear, Non-Gaussian Bayesian Tracking. *IEEE Trans. Sig. Proc.* 50:174–188, 2002.

### See Also

[pomp](#), [mif](#), [pmcmc](#), [bsmc2](#), and the tutorials on the [package website](#).

### Examples

```
pompExample(gompertz)
pf <- pfilter(gompertz, Np=1000) ## use 1000 particles
plot(pf)
logLik(pf)
cond.logLik(pf) ## conditional log-likelihoods
eff.sample.size(pf) ## effective sample size
logLik(pfilter(pf)) ## run it again with 1000 particles
## run it again with 2000 particles
pf <- pfilter(pf, Np=2000, filter.mean=TRUE)
fm <- filter.mean(pf) ## extract the filtering means
```

---

Particle Markov Chain Monte Carlo

*The particle Markov chain Metropolis-Hastings algorithm*


---

**Description**

The Particle MCMC algorithm for estimating the parameters of a partially-observed Markov process. Running `pmcmc` causes a particle random-walk Metropolis-Hastings Markov chain algorithm to run for the specified number of proposals.

**Usage**

```
## S4 method for signature 'pomp'
pmcmc(object, Nmcmc = 1, start, proposal, Np,
      tol = 1e-17, max.fail = Inf, verbose = getOption("verbose"), ...)
## S4 method for signature 'pfilterd.pomp'
pmcmc(object, Nmcmc = 1, Np, tol, ...)
## S4 method for signature 'pmcmc'
pmcmc(object, Nmcmc, start, proposal, Np, tol,
      max.fail = Inf, verbose = getOption("verbose"), ...)
## S4 method for signature 'pmcmc'
continue(object, Nmcmc = 1, ...)
```

**Arguments**

<code>object</code>	An object of class <code>pomp</code> .
<code>Nmcmc</code>	The number of PMCMC iterations to perform.
<code>start</code>	named numeric vector; the starting guess of the parameters.
<code>proposal</code>	optional function that draws from the proposal distribution. Currently, the proposal distribution must be symmetric for proper inference: it is the user's responsibility to ensure that it is. Several functions that construct appropriate proposal function are provided: see <a href="#">MCMC proposal functions</a> for more information.
<code>Np</code>	a positive integer; the number of particles to use in each filtering operation.
<code>tol</code>	numeric scalar; particles with log likelihood below <code>tol</code> are considered to be "lost". A filtering failure occurs when, at some time point, all particles are lost.
<code>max.fail</code>	integer; maximum number of filtering failures permitted. If the number of failures exceeds this number, execution will terminate with an error.
<code>verbose</code>	logical; if TRUE, print progress reports.
<code>...</code>	additional arguments that override the defaults.

**Value**

An object of class `pmcmc`.

### Re-running PMCMC Iterations

To re-run a sequence of PMCMC iterations, one can use the `pmcmc` method on a `pmcmc` object. By default, the same parameters used for the original PMCMC run are re-used (except for `tol`, `max.fail`, and `verbose`, the defaults of which are shown above). If one does specify additional arguments, these will override the defaults.

### Continuing PMCMC Iterations

One can continue a series of PMCMC iterations from where one left off using the `continue` method. A call to `pmcmc` to perform `Nmcmc=m` iterations followed by a call to `continue` to perform `Nmcmc=n` iterations will produce precisely the same effect as a single call to `pmcmc` to perform `Nmcmc=m+n` iterations. By default, all the algorithmic parameters are the same as used in the original call to `pmcmc`. Additional arguments will override the defaults.

### Details

`pmcmc` implements an MCMC algorithm in which the true likelihood of the data is replaced by an unbiased estimate computed by a particle filter. This gives an asymptotically correct Bayesian procedure for parameter estimation (Andrieu and Roberts, 2009).

**Note** that `pmcmc` does not make use of any parameter transformations supplied by the user.

### Methods

- c** Concatenates `pmcmc` objects into a `pmcmcList`.
- conv.rec(object, pars)** returns the columns of the convergence-record matrix corresponding to the names in `pars` as an object of class `mcsmc` or `mcsmc.list`.
- filter.traj(object, vars)** returns filter trajectories from a `pmcmc` or `pmcmcList` object.
- plot** Diagnostic plots.
- logLik** Returns the value in the `loglik` slot.
- coef** Returns the last state of the MCMC chain. As such, it's not very useful for inference.
- covmat(object, start, thin, expand)** computes the empirical covariance matrix of the MCMC samples beginning with iteration `start` and thinning by factor `thin`. It expands this by a factor  $\text{expand}^2/n$ , where `n` is the number of parameters estimated. By default, `expand=2.38`. The intention is that the resulting matrix is a suitable input to the proposal function `mvn.rw`.

### Author(s)

Edward L. Ionides, Aaron A. King, Sebastian Funk

### References

- C. Andrieu, A. Doucet and R. Holenstein, Particle Markov chain Monte Carlo methods, J. R. Stat. Soc. B, to appear, 2010.
- C. Andrieu and G.O. Roberts, The pseudo-marginal approach for efficient computation, Ann. Stat. 37:697-725, 2009.

**See Also**

[pomp](#), [pfilter](#), [MCMC proposal distributions](#), and the tutorials on the [package website](#).

**Examples**

```
## Not run:
library(pomp)

pompExample(ou2)

pmcmc(
  pomp(ou2, dprior=Csnippet("
    lik = dnorm(alpha_2,-0.5,1,1) + dnorm(alpha_3,0.3,1,1);
    lik = (give_log) ? lik : exp(lik);"),
    paramnames=c("alpha.2","alpha.3")),
  Nmcmc=2000, Np=500, verbose=TRUE,
  proposal=mvn.rw.adaptive(rw.sd=c(alpha.2=0.01, alpha.3=0.01),
    scale.start=200, shape.start=100)) -> chain
  continue(chain, Nmcmc=2000, proposal=mvn.rw(covmat(chain))) -> chain
  plot(chain)
  chain <- pmcmc(chain)
  plot(chain)

  library(coda)
  trace <- window(conv.rec(chain, c("alpha.2", "alpha.3")), start=2000)
  rejectionRate(trace)
  effectiveSize(trace)
  autocorr.diag(trace)

  summary(trace)
  plot(trace)

  heidel.diag(trace)
  geweke.diag(trace)

## End(Not run)
```

---

pomp constructor

*Constructor of the basic pomp object*

---

**Description**

This function constructs a `pomp` object, encoding a partially-observed Markov process model together with a uni- or multi-variate time series. As such, it is central to all the package's functionality. One implements the model by specifying some or all of its *basic components*. These include:

**rprocess**, the simulator of the unobserved Markov state process;

**dprocess**, the evaluator of the probability density function for transitions of the unobserved Markov state process;

**rmeasure**, the simulator of the observed process, conditional on the unobserved state;  
**dmeasure**, the evaluator of the measurement model probability density function;  
**initializer**, which samples from the distribution of the state process at the zero-time;  
**rprior**, which samples from a prior probability distribution on the parameters;  
**dprior** which evaluates the prior probability density function;  
**skeleton** which computes the deterministic skeleton of the unobserved state process.

The basic structure and its rationale are described in the *Journal of Statistical Software* paper, an updated version of which is to be found on the [package website](#).

## Usage

```
pomp(data, times, t0, ..., rprocess, dprocess, rmeasure, dmeasure,
      measurement.model, skeleton, initializer, rprior, dprior,
      params, covar, tcovar, obsnames, statenames, paramnames,
      covarnames, zeronames, PACKAGE,
      fromEstimationScale, toEstimationScale, globals,
      cdir, cfile, shlib.args)
```

## Arguments

data, times	required; the time series data and times at which observations are made. data should be given as a data-frame and times must indicate the column of observation times by name or index. times must be numeric and strictly increasing. Internally, data will be internally coerced to an array with storage-mode double.  In addition, a pomp object can be supplied in the data argument. In this case, the call to pomp will add element to, or replace elements of, the supplied pomp object.
t0	The zero-time, at which the stochastic dynamical system is to be initialized. This must be no later than the time of the first observation, i.e., $t0 \leq \text{times}[1]$ . This argument is required whenever data is a data-frame.
rprocess, dprocess	optional; specification of the simulator and probability density evaluation function of the unobserved state process. See below under “The Unobserved Markov State-Process Model” for details.  <b>Note:</b> it is not typically necessary (or even feasible) to define dprocess. In fact, no current <b>pomp</b> inference algorithm makes use of dprocess. This functionality is provided only to support future algorithm development.
rmeasure, dmeasure, measurement.model	optional; specifications of the measurement model. See below under “The Measurement Model” for details.
skeleton	optional; the deterministic skeleton of the unobserved state process. See below under “The Deterministic Skeleton” for details.

<code>initializer</code>	optional; draws from the distribution of initial values of the unobserved Markov state process. Specifically, given a vector of parameters, <code>params</code> and an initial time, <code>t0</code> , the initializer determines the state vector at time <code>t0</code> . See below under “The State-Process Initializer” for details.
<code>rprior</code> , <code>dprior</code>	optional; specification of the prior distribution on parameters. See below under “Specifying a Prior” for details.
<code>params</code>	optional; named numeric vector of parameters. This will be coerced internally to storage mode <code>double</code> .
<code>covar</code> , <code>tcovar</code>	optional data frame of covariates: <code>covar</code> is the table of covariates (one column per variable); <code>tcovar</code> the name or the index of the time variable. If a covariate table is supplied, then the value of each of the covariates is interpolated as needed. The resulting interpolated values are made available to the appropriate basic components. Note that <code>covar</code> will be coerced internally to storage mode <code>double</code> . See below under “Covariates” for more details.
<code>obsnames</code> , <code>statenames</code> , <code>paramnames</code> , <code>covarnames</code>	optional character vectors specifying the names of observables, state variables, parameters, and covariates, respectively. These are used only in the event that one or more of the basic components are defined using C snippets or native routines. It is usually unnecessary to specify <code>obsnames</code> or <code>covarnames</code> , as these will by default be read from data and covars, respectively.
<code>zeronames</code>	optional character vector specifying the names of accumulator variables (see below under “Accumulator Variables”).
<code>PACKAGE</code>	optional string giving the name of the dynamically loaded library in which any native routines are to be found. This is only useful if one or more of the model components has been specified using a precompiled dynamically loaded library; it is not useful if the components are specified using C snippets.
<code>fromEstimationScale</code> , <code>toEstimationScale</code>	optional parameter transformations. Many algorithms for parameter estimation search an unconstrained space of parameters. When working with such an algorithm and a model for which the parameters are constrained, it can be useful to transform parameters. <code>toEstimationScale</code> and <code>fromEstimationScale</code> are transformations from the model scale to the estimation scale, and vice versa, respectively. See below under “Parameter Transformations” for more details.
<code>globals</code>	optional character; C code that will be included in the source for (and therefore hard-coded into) the shared-object library created when the call to <code>pomp</code> uses C snippets. If no C snippets are used, <code>globals</code> has no effect.
<code>cdir</code> , <code>cfile</code> , <code>shlib.args</code>	optional character variables. <code>cdir</code> specifies the name of the directory within which C snippet code will be compiled. By default, this is in a temporary directory specific to the running instance of R. <code>cfile</code> gives the name of the file (in directory <code>cdir</code> ) into which C snippet codes will be written. By default, a random filename is used. The <code>shlib.args</code> can be used to pass command-line arguments to the R CMD SHLIB call that will compile the C snippets.
<code>...</code>	Any additional arguments given to <code>pomp</code> will be made available to each of the basic components. To prevent errors due to misspellings, a warning is issued if any such arguments are detected.

## Value

The `pomp` constructor function returns an object, call it `P`, of class `pomp`. `P` contains, in addition to the data, any elements of the model that have been specified as arguments to the `pomp` constructor function. One can add or modify elements of `P` by means of further calls to `pomp`, using `P` as the first argument in such calls.

## Important note

**It is not typically necessary (or even feasible) to define all of the basic components for any given purpose. Each `pomp` algorithm makes use of only a subset of these components. Any algorithm requiring a component that is not present will generate an error letting you know that you have not provided a needed component.**

## Using C snippets to accelerate computations

**pomp** provides a facility whereby users can define their model's components using inline C code. Furnishing one or more C snippets as arguments to the `pomp` constructor causes them to be written to a C file stored in the R session's temporary directory, which is then compiled (via `R CMD SHLIB`) into a dynamically loadable shared object file. This is then loaded as needed.

**Note to Windows and Mac users:** By default, your R installation may not support `R CMD SHLIB`. The [package website contains installation instructions](#) that explain how to enable this powerful feature of R.

## General rules for writing C snippets

In writing a C snippet one must bear in mind both the *goal* of the snippet, i.e., what computation it is intended to perform, and the *context* in which it will be executed. These are explained here in the form of general rules. Additional specific rules apply according to the function of the particular C snippet. Illustrative examples are given in the tutorials on the [package website](#).

1. C snippets must be valid C. They will be embedded verbatim in a template file which will then be compiled by a call to `R CMD SHLIB`. If the resulting file does not compile, an error message will be generated. No attempt is made by **pomp** to interpret this message. Typically, compilation errors are due to either invalid C syntax or undeclared variables.
2. State variables, parameters, observables, and covariates must be left undeclared within the snippet. State variables and parameters are declared via the `statenames` or `paramnames` arguments to `pomp`, respectively. Compiler errors that complain about undeclared state variables or parameters are usually due to failure to declare these in `statenames` or `paramnames`, as appropriate.
3. A C snippet can declare local variables. Be careful not to use names that match those of state variables, observables, or parameters. The latter must never be declared within a C snippet.
4. Names of observables are determined by their names in the data. They must be referred to in measurement model C snippets (`rmeasure` and `dmeasure`) by those names.
5. If the `pomp` object contains a table of covariates (see above), then the variables in the covariate table will be available, by their names, in the context within which the C snippet is executed.
6. Because the dot `'.'` has syntactic meaning in C, R variables with names containing dots (`'.'`) are replaced in the C codes by variable names in which all dots have been replaced by underscores (`'_'`).

7. The header 'R.h', provided with R, will be included in the generated C file, making all of the **R C API** available for use in the C snippet. This makes a great many useful functions available, including all of R's **statistical distribution functions**.
8. The header 'pomp.h', provided with **pomp**, will also be included, making all of the **pomp C API** available for use in every C snippet. Do

```
file.show(system.file("include/pomp.h", package="pomp"))
```

to view this header file.

9. Snippets of C code passed to the `globals` argument of `pomp` will be included at the head of the generated C file. This can be used to declare global variables, define useful functions, and include arbitrary header files.

### The Unobserved Markov State-Process Model

Specification of process-model codes `rprocess` and/or `dprocess` is facilitated by **pomp**'s so-called plug-ins, which allow one to easily specify the most common kinds of process model.

**Discrete-time processes:** If the state process evolves in discrete time, specify `rprocess` using the `discrete.time.sim` plug-in. Specifically, provide

```
rprocess = discrete.time.sim(step.fun = f, delta.t)
```

to `pomp`, where `f` is a C snippet or R function that takes and simulates one step of the state process. The former is the preferred option, due to its much greater computational efficiency. The goal of such a C snippet is to replace the state variables with their new random values at the end of the time interval. Accordingly, each state variable should be over-written with its new value. In addition to the states, parameters, covariates (if any), and observables, the variables `t` and `dt`, containing respectively the time at the beginning of the step and the step's duration, will be defined in the context in which the C snippet is executed. See above under "General rules for C snippet writing" for more details. Examples are to be found in the tutorials on the [package website](#).

If `f` is given as an R function, it should have prototype

```
f(x, t, params, delta.t, ...)
```

When `f` is called, `x` will be a named numeric vector containing the value of the state process at time `t`, `params` will be a named numeric vector containing parameters, and `delta.t` will be the time-step. It should return a named vector of the same length, and with the same set of names, as `x`, representing a draw from the distribution of the state process at time `t+delta.t`, conditional on its having value `x` at time `t`.

**Continuous-time processes:** If the state process evolves in continuous time, but you can use an Euler approximation, specify `rprocess` using the `euler.sim` plug-in. Furnish

```
rprocess = euler.sim(step.fun = f, delta.t)
```

to `pomp` in this case. As before, `f` can be provided either as a C snippet or as an R function, the former resulting in much quicker computations. The form of `f` will be the same as above (in the discrete-time case).

If you have a procedure that allows you, given the value of the state process at any time, to simulate it at an arbitrary time in the future, use the `onestep.sim` plug-in. To do so, furnish

```
rprocess = onestep.sim(step.fun = f)
```



to `pomp`. Again, `f` can be provided either as a C snippet or as an R function, the former resulting in much quicker computations. The form of `f` should be as above (in the discrete-time or Euler cases).

If you desire exact simulation of certain continuous-time Markov chains, an implementation of Gillespie's algorithm (Gillespie 1977) is available, via the `gillespie.sim` and `gillespie.hl.sim` plug-ins. The former allows for the rate function to be provided as an R function or a single C snippet, while the latter provides a means of specifying the elementary events via a list of C snippets.

A high-level interface to the simulator is provided by `gillespie.hl.sim`. To use it, supply

```
rprocess = gillespie.hl.sim(..., .pre = "", .post = "", hmax = Inf)
```

to `pomp`. Each argument in `...` corresponds to a single elementary event and should be a list containing two elements. The first should be a string or C snippet; the second should be a named integer vector. The string contains C code that assigns to the variable `rate` the corresponding elementary event rate. The variable `rate` will exist in the context of the code, as will the covariates (as named in `covar`) and the time `t`. The state variables and parameters will also be available provided that the `statenames` and `paramnames` arguments are provided to `pomp`. The named integer vector contains the changes to the state variables corresponding to the elementary event. There should be named value for each of the state variables returned by the initializer. Typically, these changes will be integers but floating point values are permissible. The arguments `.pre` and `.post` can be used to provide C code that will run either before or after the code in the event arguments. These hooks could be useful for avoiding duplication of code that performs calculations needed to obtain several of the different event rates. Here's how a simple birth-death model might be specified:

```
gillespie.hl.sim(
  birth=list("rate = b*N;",c(N=1)),
  death=list("rate = m*N;",c(N=-1)))
```

In the above, the state variable `N` represents the population size and parameters `b`, `m` are the birth and death rates, respectively.

To use the lower-level `gillespie.sim` interface, furnish

```
rprocess = gillespie.sim(rate.fun = f, v, hmax = Inf)
```

to `pomp`, where `f` gives the rates of the elementary events. Here, `f` may be an R function of the form

```
f(j, x, t, params,...)
```

When `f` is called, the integer `j` will be the number of the elementary event (corresponding to the column the matrix `v`, see below), `x` will be a named numeric vector containing the value of the state process at time `t` and `params` is a named numeric vector containing parameters. `f` should return a single numerical value, representing the rate of that elementary event at that point in state space and time.

Matrix `v` specifies the continuous-time Markov process in terms of its elementary events. It should have dimensions `nvar` x `nevent`, where `nvar` is the number of state variables and `nevent` is the number of elementary events. `v` describes the changes that occur in each elementary event: it will usually comprise the values 1, -1, and 0 according to whether a state variable is incremented, decremented, or unchanged in an elementary event. The rows of `v` may be unnamed or named. If the rows are unnamed, they are assumed to be in the same order as the vector of state variables

returned by the initializer. If the rows are named, the names of the state variables returned by the initializer will be matched to the rows of `v` to ensure a correct mapping. If any of the row names of `v` cannot be found among the state variables or if any row names of `v` are duplicated, an error will occur.

It is also possible to provide a C snippet via the `rate.fn` argument to `gillespie.sim`. Such a snippet should assign the correct value to a rate variable depending on the value of `j`. The same variables will be available as for the C code provided to `gillespie.hl.sim`. This lower-level interface may be preferable if it is easier to write code that calculates the correct rate based on `j` rather than to write a snippet for each possible value of `j`. For example, if the number of possible values of `j` is large and the rates vary according to a few simple rules, the lower-level interface may provide the easier way of specifying the model.

When the process is non-autonomous (i.e., the event rates depend explicitly on time), it can be useful to set `hmax` to the maximum step that will be taken. By default, the elementary event rates will be recomputed at least once per observation interval.

**Size of time step:** The simulator plug-ins `discrete.time.sim`, `euler.sim`, and `onestep.sim` all work by taking discrete time steps. They differ as to how this is done. Specifically,

1. `onestep.sim` takes a single step to go from any given time  $t_1$  to any later time  $t_2$  ( $t_1 < t_2$ ). Thus, this plug-in is designed for use in situations where a closed-form solution to the process exists.
2. To go from  $t_1$  to  $t_2$ , `euler.sim` takes  $n$  steps of equal size, where  

$$n = \text{ceiling}((t_2 - t_1) / \text{delta.t}).$$
3. `discrete.time.sim` assumes that the process evolves in discrete time, where the interval between successive times is `delta.t`. Thus, to go from  $t_1$  to  $t_2$ , `discrete.time.sim` takes  $n$  steps of size exactly `delta.t`, where  

$$n = \text{floor}((t_2 - t_1) / \text{delta.t}).$$

**Specifying dprocess:** If you have a procedure that allows you to compute the probability density of an arbitrary transition from state  $x_1$  at time  $t_1$  to state  $x_2$  at time  $t_2 > t_1$ , assuming that the state remains unchanged between  $t_1$  and  $t_2$ , then you can use the `onestep.dens` plug-in. This is accomplished by furnishing

```
dprocess = onestep.dens(dens.fun = f)
```

to `pomp`, where `f` is an R function with prototype

```
f(x1, x2, t1, t2, params, ...)
```

When `f` is called, `x1` and `x2` will be named numeric vectors containing the values of the state process at times  $t_1$  and  $t_2$ , respectively, and `params` will be a named numeric vector containing parameters. `f` should return the *log* likelihood of a transition from `x1` at time  $t_1$  to `x2` at time  $t_2$ , assuming that no intervening transitions have occurred.

To see examples, consult the tutorials on the [package website](#).

## The Measurement Model

The measurement model is the link between the data and the unobserved state process. It can be specified either by using one or both of the `rprocess` and `dprocess` arguments, or via the `measurement.model` argument. If `measurement.model` is given it overrides any specification via the `rmeasure` or `dmeasure` arguments, with a warning.

The best way to specify the measurement model is by giving C snippets for `rmeasure` and `dmeasure`. In writing an `rmeasure` C snippet, bear in mind that:

1. The goal of such a snippet is to fill the observables with random values drawn from the measurement model distribution. Accordingly, each observable should be assigned a new value.
2. In addition to the states, parameters, covariates (if any), and observables, the variable `t`, containing the time of the observation, will be defined in the context in which the snippet is executed.

General rules for writing C snippets are provided above. The tutorials on the [package website](#) give examples as well.

It is also possible, though far less efficient, to specify `rmeasure` using an R function. In this case, specify the measurement model simulator by furnishing

```
rmeasure = f
```

to `pomp`, where `f` is an R function with prototype

```
f(x, t, params, ...)
```

It can also take any additional arguments if these are passed along with it in the call to `pomp`. When `f` is called,

- `x` will be a named numeric vector of length `nvar`, the number of state variables.
- `t` will be a scalar quantity, the time at which the measurement is made.
- `params` will be a named numeric vector of length `npar`, the number of parameters.

`f` must return a named numeric vector of length `nobs`, the number of observable variables.

In writing a `dmeasure` C snippet, observe that:

1. In addition to the states, parameters, covariates (if any), and observables, the variable `t`, containing the time of the observation, and the Boolean variable `give_log` will be defined in the context in which the snippet is executed.
2. The goal of such a snippet is to set the value of the `lik` variable to the likelihood of the data given the state. Alternatively, if `give_log == 1`, `lik` should be set to the log likelihood.

If `dmeasure` is to be provided instead as an R function, this is accomplished by supplying

```
dmeasure = f
```

to `pomp`, where `f` has prototype

```
f(y, x, t, params, log, ...)
```

Again, it can take additional arguments that are passed with it in the call to `pomp`. When `f` is called,

- `y` will be a named numeric vector of length `nobs` containing values of the observed variables;
- `x` will be a named numeric vector of length `nvar` containing state variables;
- `params` will be a named numeric vector of length `npar` containing parameters;

- $t$  will be a scalar, the corresponding observation time.

$f$  must return a single numeric value, the probability density of  $y$  given  $x$  at time  $t$ . If `log == TRUE`, then  $f$  should return instead the log of the probability density. **Note: it is a common error to fail to account for both `log = TRUE` and `log = FALSE` when writing the dmeasure C snippet or function.**

One can also specify both the `rmeasure` and `dmeasure` components at once via the `measurement.model` argument. It should be a formula or list of `nobs` formulae. These are parsed internally to generate `rmeasure` and `dmeasure` functions. **Note:** this is a convenience function, primarily designed to facilitate model exploration; it will typically be possible (and as a practical matter necessary) to accelerate measurement model computations by writing `dmeasure` and/or `rmeasure` using C snippets.

### The Deterministic Skeleton

The skeleton is a dynamical system that expresses the central tendency of the unobserved Markov state process. As such, it is not uniquely defined, but can be both interesting in itself and useful in practice. In **pomp**, the skeleton is used by `trajectory` and `traj.match`.

If the state process is a discrete-time stochastic process, then the skeleton is a discrete-time map. To specify it, provide

```
skeleton = map(f, delta.t)
```

to `pomp`, where  $f$  implements the map and `delta.t` is the size of the timestep covered at one map iteration.

If the state process is a continuous-time stochastic process, then the skeleton is a vectorfield (i.e., a system of ordinary differential equations). To specify it, supply

```
skeleton = vectorfield(f)
```

to `pomp`, where  $f$  implements the vectorfield, i.e., the right-hand-side of the differential equations.

In either case,  $f$  can be furnished either as a C snippet (the preferred choice), or an R function. In writing a skeleton C snippet, be aware that:

1. For each state variable, there is a corresponding component of the deterministic skeleton. The goal of such a snippet is to compute all the components.
2. When the skeleton is a map, the component corresponding to state variable  $x$  is named  $Dx$  and is the new value of  $x$  after one iteration of the map.
3. When the skeleton is a vectorfield, the component corresponding to state variable  $x$  is named  $Dx$  and is the value of  $dx/dt$ .
4. As with the other C snippets, all states, parameters and covariates, as well as the current time,  $t$ , will be defined in the context within which the snippet is executed.

The tutorials on the [package website](#) give some examples.

If  $f$  is an R function, it must be of prototype

```
f(x, t, params, ...)
```

where, as usual,

- $x$  is a numeric vector (length  $nvar$ ) containing the coordinates of a point in state space at which evaluation of the skeleton is desired.
- $t$  is a scalar value giving the time at which evaluation of the skeleton is desired.
- $params$  is a numeric vector (length  $npar$ ) holding the parameters.

As with the other basic components,  $f$  may take additional arguments, provided these are passed along with it in the call to `pomp`. The function  $f$  must return a numeric vector of the same length as  $x$ , which contains the value of the map or vectorfield at the required point and time.

### The State-Process Initializer

To fully specify the unobserved Markov state process, one must give its distribution at the zero-time ( $t_0$ ). By default, `pomp` assumes that this initial distribution is concentrated on a single point. In particular, any parameters in  $params$ , the names of which end in “.0”, are assumed to be initial values of states. When the state process is initialized, these are simply copied over as initial conditions. The names of the resulting state variables are obtained by dropping the “.0” suffix.

One can override this default behavior by furnishing a value for the `initializer` argument of `pomp`. As usual, this can be provided either as a C snippet or as an R function. In the former case, bear in mind that:

1. The goal of this snippet is the construction of a state vector, i.e., the setting of the dynamical states at time  $t_0$ .
2. In addition to the parameters and covariates (if any), the variable  $t$ , containing the zero-time, will be defined in the context in which the snippet is executed.
3. **NB:** The `statenames` argument plays a particularly important role when the initializer is specified using a C snippet. In particular, every state variable must be named in `statenames`. **Failure to follow this rule will result in undefined behavior.**

If an R function is to be used, pass

```
initializer = f
```

to `pomp`, where  $f$  is a function with prototype

```
f(params, t0, ...)
```

When  $f$  is called,

- $params$  will be a named numeric vector of parameters.
- $t_0$  will be the time at which initial conditions are desired.

As usual,  $f$  may take additional arguments, provided these are passed along with it in the call to `pomp`.  $f$  must return a named numeric vector of initial states. It is of course important that the names of the states match the expectations of the other basic components.

Note that the state-process initializer can be either deterministic (the default) or stochastic. In the latter case, it samples from the distribution of the state process at the zero-time,  $t_0$ .

## Specifying a Prior

A prior distribution on parameters is specified by means of the `rprior` and/or `dprior` arguments to `pomp`. As with the other basic model components, it is preferable to specify these using C snippets. In writing a C snippet for the prior sampler (`rprior`), keep in mind that:

1. Within the context in which the snippet will be evaluated, only the parameters will be defined.
2. The goal of such a snippet is the replacement of parameters with values drawn from the prior distribution.
3. Hyperparameters can be included in the ordinary parameter list. Obviously, hyperparameters should not be replaced with random draws.

In writing a C snippet for the prior density function (`dprior`), observe that:

1. Within the context in which the snippet will be evaluated, only the parameters and `give_log` will be defined.
2. The goal of such a snippet is computation of the prior probability density, or the log of same, at a given point in parameter space. This scalar value should be returned in the variable `lik`. When `give_log == 1`, `lik` should contain the log of the prior probability density.
3. Hyperparameters can be included in the ordinary parameter list.

Alternatively, one can furnish R functions for one or both of these arguments. In this case, `rprior` must be a function of prototype

```
f(params, ...)
```

that makes a draw from the prior distribution given `params` and returns a named vector of the same length and with the same set of names, as `params`. The `dprior` function must be of prototype

```
f(params, log = FALSE, ...).
```

Its role is to evaluate the prior probability density (or log density if `log == TRUE`) and return that single scalar value.

## Covariates

If the `pomp` object contains covariates (specified via the `covar` argument; see above), then interpolated values of the covariates will be available to each of the model components whenever it is called. In particular, variables with names as they appear in the `covar` data frame will be available to any C snippet. When a basic component is defined using an R function, that function will be called with an extra argument, `covars`, which will be a named numeric vector containing the interpolated values from the covariate table.

An exception to this rule is the prior (`rprior` and `dprior`): covariate-dependent priors are not allowed. Nor are parameter transformations permitted to depend upon covariates.

## Parameter Transformations

When parameter transformations are desired, they can be integrated into the `pomp` object via the `toEstimationScale` and `fromEstimationScale` arguments. As with the basic model components, these should ordinarily be specified using C snippets. When doing so, note that:

1. The parameter transformation mapping a parameter vector from the scale used by the model codes to another scale is specified using the `toEstimationScale` argument whilst the transformation mapping a parameter vector from the alternative scale to that on which the model is defined is specified with the `fromEstimationScale` argument.
2. The goal of these snippets is the computation of the values of the transformed parameters. The value of transformed parameter `p` should be assigned to variable `TP`.
3. Time-, state-, and covariate-dependent transformations are not allowed. Therefore, neither the time, nor any state variables, nor any of the covariates will be available in the context within which a parameter transformation snippet is executed.

These transformations can also be specified using R functions with arguments `params` and `...`. In this case, `toEstimationScale` should transform parameters from the scale that the basic components use internally to the scale used in estimation. `fromEstimationScale` should be the inverse of `toEstimationScale`.

Note that it is the user's responsibility to make sure that the transformations are mutually inverse. If `obj` is the constructed `pomp` object, and `coef(obj)` is non-empty, a simple check of this property is

```
x <- coef(obj, transform = TRUE)
obj1 <- obj
coef(obj1, transform = TRUE) <- x
identical(coef(obj), coef(obj1))
identical(coef(obj1, transform=TRUE), x)
```

By default, both functions are the identity transformation.

## Accumulator Variables

In formulating models, one sometimes wishes to define a state variable that will accumulate some quantity over the interval between successive observations. **pomp** provides a facility to make such features more convenient. Specifically, variables named in the `pomp`'s `zernames` argument will be set to zero immediately following each observation. See [euler.sir](#) and the tutorials on the [package website](#) for examples.

## Viewing generated C code

It can be useful to view the C code generated by calling `pomp` with one or more C snippet arguments. You can set `cdir` and `cfile` to control where this code is written. Alternatively, set `options(verbose=TRUE)` before calling `pomp`. This will cause a message giving the name of the generated C file (in the session temporary directory) to be printed.

**Warning**

Some error checking is done by `pomp`, but complete error checking for arbitrary models is impossible. If the user-specified functions do not conform to the above specifications, then the results may be invalid. In particular, if both `rmeasure` and `dmeasure` are specified, the user should verify that these two functions correspond to the same probability distribution. If `skeleton` is specified, the user is responsible for verifying that it corresponds to a deterministic skeleton of the model.

**Author(s)**

Aaron A. King

**References**

A. A. King, D. Nguyen, and E. L. Ionides (2016) Statistical Inference for Partially Observed Markov Processes via the R Package **pomp**. *Journal of Statistical Software* 69(12): 1–43.

D. T. Gillespie (1977) Exact stochastic simulation of coupled chemical reactions. *Journal of Physical Chemistry* 81:2340–2361.

**See Also**

[pomp methods](#), [pomp low-level interface](#)

**Examples**

```
## pomp encoding a stochastic Ricker model with a covariate:

pomp(data = data.frame(t = 1:100, y = NA),
      times = "t", t0 = 0,
      covar = data.frame(t=0:100,K=seq(from=50,to=200,length=101)),
      tcovar = "t",
      rprocess = discrete.time.sim(Csnippet("double e = rnorm(0,sigma);
                                           n = r*n*exp(1-n/K+e);"), delta.t = 1),
      skeleton = map(Csnippet("Dn = r*n*exp(1-n/K);"), delta.t = 1),
      rmeasure = Csnippet("y = rpois(n);"),
      dmeasure = Csnippet("lik = dpois(y,n,give_log);"),
      rprior = Csnippet("r = rgamma(1,1); sigma = rgamma(1,1);"),
      dprior = Csnippet("lik = dgamma(r,1,1,1) + dgamma(sigma,1,1,1);
                        if (!give_log) lik = exp(lik);"),
      initializer = Csnippet("n = n_0;"),
      toEstimationScale = Csnippet("Tr = log(r); Tsigma = log(sigma);"),
      fromEstimationScale = Csnippet("Tr = exp(r); Tsigma = exp(sigma);"),
      paramnames = c("n_0", "r", "sigma"),
      statenames = "n") -> rick

## fill it with simulated data:

rick <- simulate(rick, params = c(r=17, sigma = 0.1, n_0 = 50))
plot(rick)

## Not run:
```



```
pompExample()
demos(package="pomp")

## End(Not run)
```

---

pomp methods

*Functions for manipulating, displaying, and extracting information  
from objects of the pomp class*


---

## Description

This page documents the various methods that allow one to extract information from, display, plot, and modify pomp objects.

## Usage

```
## S4 method for signature 'pomp'
coef(object, pars, transform = FALSE, ...)
## S4 replacement method for signature 'pomp'
coef(object, pars, transform = FALSE, ...) <- value
## S4 method for signature 'pomp'
obs(object, vars, ...)
## S4 method for signature 'pomp'
partrans(object, params, dir = c("fromEstimationScale",
  "toEstimationScale", "forward", "inverse"), ...)
## S4 method for signature 'pomp'
plot(x, y, variables, panel = lines,
  nc = NULL, yax.flip = FALSE,
  mar = c(0, 5.1, 0, if (yax.flip) 5.1 else 2.1),
  oma = c(6, 0, 5, 0), axes = TRUE, ...)
## S4 method for signature 'pomp'
print(x, ...)
## S4 method for signature 'pomp'
show(object)
## S4 method for signature 'pomp'
states(object, vars, ...)
## S4 method for signature 'pomp'
time(x, t0 = FALSE, ...)
## S4 replacement method for signature 'pomp'
time(object, t0 = FALSE, ...) <- value
## S4 method for signature 'pomp'
timezero(object, ...)
## S4 replacement method for signature 'pomp'
timezero(object, ...) <- value
## S4 method for signature 'pomp'
window(x, start, end, ...)
## S4 method for signature 'pomp'
as(object, class)
```

**Arguments**

<code>object, x</code>	The pomp object.
<code>pars</code>	optional character; names of parameters to be retrieved or set.
<code>vars</code>	optional character; names of observed variables to be retrieved.
<code>transform</code>	optional logical; should the parameter transformations be applied?
<code>value</code>	numeric; values to be assigned.
<code>params</code>	a vector or matrix of parameters to be transformed.
<code>dir</code>	direction of the transformation. <code>dir="forward"</code> applies the transformation from the “natural” scale to the “internal” scale. This is the transformation specified by the <code>parameter.transform</code> argument to <code>pomp</code> ; it is stored in the ‘ <code>par.trans</code> ’ slot of <code>object</code> . <code>dir="inverse"</code> applies the inverse transformation (stored in the ‘ <code>par.untrans</code> ’ slot).
<code>t0</code>	logical; if TRUE on a call to <code>time</code> , the zero time is prepended to the time vector; if TRUE on a call to <code>time&lt;-</code> , the first element in <code>value</code> is taken to be the initial time.
<code>start, end</code>	start and end times of the window.
<code>class</code>	character; name of the class to which object should be coerced.
<code>y</code>	ignored.
<code>variables</code>	optional character; names of variables to plot.
<code>panel</code>	a function of prototype <code>panel(x, col, bg, pch, type, ...)</code> which gives the action to be carried out in each panel of the display.
<code>nc</code>	the number of columns to use. Defaults to 1 for up to 4 series, otherwise to 2.
<code>yax.flip</code>	logical; if TRUE, the y-axis (ticks and numbering) should flip from side 2 (left) to 4 (right) from series to series.
<code>mar, oma</code>	the ‘ <code>par</code> ’ settings for ‘ <code>mar</code> ’ and ‘ <code>oma</code> ’ to use. Modify with care!
<code>axes</code>	logical; indicates if x- and y- axes should be drawn.
<code>...</code>	Further arguments (either ignored or passed to underlying functions).

**Details**

**coef** `coef(object)` returns the contents of the `params` slot of `object`. `coef(object,pars)` returns only those parameters named in `pars`.

`coef(object,transform=TRUE)`

returns

`parameter.inv.transform(coef(object)),`

where `parameter.inv.transform` is the user parameter inverse transformation function specified when `object` was created. Likewise,

`coef(object,pars,transform=TRUE)`

returns

`parameter.inv.transform(coef(object))[pars].`

- coef**`<-` Assigns values to the `params` slot of the `pomp` object. `coef(object) <- value` has the effect of replacing the parameters of `object` with `value`. If `coef(object)` exists, then `coef(object,pars) <- value` replaces those parameters of `object` named in `pars` with the elements of `value`; the names of `value` are ignored. If some of the names in `pars` do not already name parameters in `coef(object)`, then they are concatenated. If `coef(object)` does not exist, then `coef(object,pars) <- value` assigns `value` to the parameters of `object`; in this case, the names of `object` will be `pars` and the names of `value` will be ignored. `coef(object,transform=TRUE) <- value` assigns `parameter.transform(value)` to the `params` slot of `object`. Here, `parameter.transform` is the parameter transformation function specified when `object` was created. `coef(object,pars,transform=TRUE) <- value` first, discards any names the `value` may have, sets `names(value) <- pars`, and then replaces the elements of `object`'s `params` slot with `parameter.transform(value)`. In this case, if some of the names in `pars` do not already name parameters in `coef(object,transform=TRUE)`, then they are concatenated.
- obs** `obs(object)` returns the array of observations. `obs(object,vars)` gives just the observations of variables named in `vars`. `vars` may specify the variables by position or by name.
- states** `states(object)` returns the array of states. `states(object,vars)` gives just the state variables named in `vars`. `vars` may specify the variables by position or by name.
- time** `time(object)` returns the vector of observation times. `time(object,t0=TRUE)` returns the vector of observation times with the zero-time `t0` prepended.
- time**`<-` `time(object) <- value` replaces the observation times slot (`times`) of `object` with `value`. `time(object,t0=TRUE) <- value` has the same effect, but the first element in `value` is taken to be the initial time. The second and subsequent elements of `value` are taken to be the observation times. Those data and states (if they exist) corresponding to the new times are retained.
- timezero, timezero**`<-` `timezero(object)` returns the zero-time `t0`. `timezero(object) <- value` sets the zero-time to `value`.
- window** `window(x,start=t1,end=t2)` returns a new `pomp` object, identical to `x` but with only the data in the window between times `t1` and `t2` (inclusive). By default, `start` is the time of the first observation and `end` is the time of the last.
- show** Displays the `pomp` object.
- print** Print method.
- plot** Plots the data and state trajectories (if the latter exist). Additional arguments are passed to the low-level plotting routine.
- as** A `pomp` object can be coerced to a data frame via  
`as(object,"data.frame")`.  
 The data frame contains the times, the data, and the state trajectories, if they exist.

**Author(s)**

Aaron A. King

**See Also**

[pomp](#), [pomp low-level interface](#), [simulate](#), [pfilter](#), [probe](#).

**Description**

`simulate` generates simulations of the state and measurement processes.

**Usage**

```
## S4 method for signature 'pomp'
simulate(object, nsim = 1, seed = NULL, params,
         states = FALSE, obs = FALSE, times, t0,
         as.data.frame = FALSE, include.data = FALSE, ...)
```

**Arguments**

<code>object</code>	An object of class <code>pomp</code> .
<code>nsim</code>	The number of simulations to perform. Note that the number of replicates will be <code>nsim</code> times <code>ncol(params)</code> .
<code>seed</code>	optional; if set, the pseudorandom number generator (RNG) will be initialized with <code>seed</code> . the random seed to use. The RNG will be restored to its original state afterward.
<code>params</code>	either a named numeric vector or a numeric matrix with rownames. The parameters to use in simulating the model. If <code>params</code> is not given, then the contents of the <code>params</code> slot of <code>object</code> will be used, if they exist.
<code>states</code>	Do we want the state trajectories?
<code>obs</code>	Do we want data-frames of the simulated observations?
<code>times, t0</code>	<code>times</code> specifies the times at which simulated observations will be made. <code>t0</code> specifies the start time (the time at which the initial conditions hold). The default for <code>times</code> is <code>times=time(object,t0=FALSE)</code> and <code>t0=timezero(object)</code> , respectively.
<code>as.data.frame, include.data</code>	logical; if <code>as.data.frame=TRUE</code> , the results are returned as a data-frame. A factor variable, <code>'sim'</code> , distinguishes one simulation from another. If, in addition, <code>include.data=TRUE</code> , the original data are included as an additional <code>'simulation'</code> . If <code>as.data.frame=FALSE</code> , <code>include.data</code> is ignored.
<code>...</code>	further arguments that are currently ignored.

**Details**

Simulation of the state process and of the measurement process are each accomplished by a single call to the user-supplied `rprocess` and `rmeasure` functions, respectively. This makes it possible for the user to write highly optimized code for these potentially expensive computations.

**Value**

If `states=FALSE` and `obs=FALSE` (the default), a list of `nsim` `pomp` objects is returned. Each has a simulated data set, together with the parameters used (in `slot params`) and the state trajectories also (in `slot states`). If `times` is specified, then the simulated observations will be at times `times`.

If `nsim=1`, then a single `pomp` object is returned (and not a singleton list).

If `states=TRUE` and `obs=FALSE`, simulated state trajectories are returned as a rank-3 array with dimensions `nvar` x `(ncol(params)*nsim)` x `ntimes`. Here, `nvar` is the number of state variables and `ntimes` the length of the argument `times`. The measurement process is not simulated in this case.

If `states=FALSE` and `obs=TRUE`, simulated observations are returned as a rank-3 array with dimensions `nobs` x `(ncol(params)*nsim)` x `ntimes`. Here, `nobs` is the number of observables.

If both `states=TRUE` and `obs=TRUE`, then a named list is returned. It contains the state trajectories and simulated observations as above.

**Author(s)**

Aaron A. King

**See Also**

[pomp](#)

**Examples**

```
pompExample(ou2)
x <- simulate(ou2, seed=3495485, nsim=10)
x <- simulate(ou2, seed=3495485, nsim=10, states=TRUE, obs=TRUE)
x <- simulate(ou2, seed=3495485, nsim=10, obs=TRUE,
              as.data.frame=TRUE, include.data=TRUE)
```

---

Power spectrum computation and matching

*Power spectrum computation and spectrum-matching for partially-  
observed Markov processes*

---

**Description**

`spect` estimates the power spectrum of time series data and model simulations and compares the results. It can be used to diagnose goodness of fit and/or as the basis for frequency-domain parameter estimation (`spect.match`).

`spect.match` tries to match the power spectrum of the model to that of the data. It calls an optimizer to adjust model parameters to minimize the discrepancy between simulated and actual data.

**Usage**

```
## S4 method for signature 'pomp'
spect(object, params, vars, kernel.width, nsim, seed = NULL,
      transform.data, detrend = c("none", "mean", "linear", "quadratic"),
      ...)
## S4 method for signature 'spect.pomp'
spect(object, params, vars, kernel.width, nsim, seed = NULL,
      transform.data, detrend, ...)
## S4 method for signature 'pomp'
spect.match(object, start, est = character(0), vars, nsim,
            seed = NULL, kernel.width, transform.data,
            detrend = c("none", "mean", "linear", "quadratic"), weights = 1,
            method = c("subplex", "Nelder-Mead", "SANN"), verbose = getOption("verbose"),
            fail.value = NA, ...)
## S4 method for signature 'spect.pomp'
spect.match(object, start, est = character(0), vars, nsim,
            seed = NULL, kernel.width, transform.data, detrend, weights = 1,
            method = c("subplex", "Nelder-Mead", "SANN"), verbose = getOption("verbose"),
            fail.value = NA, ...)
## S4 method for signature 'pomp'
spect.match(object, start, est, vars, nsim,
            seed = NULL, kernel.width, transform.data, detrend,
            weights, method, verbose = getOption("verbose"),
            fail.value, ...)
```

**Arguments**

<code>object</code>	An object of class <code>pomp</code> .
<code>params</code>	optional named numeric vector of model parameters. By default, <code>params=coef(object)</code> .
<code>vars</code>	optional; names of observed variables for which the power spectrum will be computed. This must be a subset of <code>rownames(obs(object))</code> . By default, the spectrum will be computed for all observables.
<code>kernel.width</code>	width parameter for the smoothing kernel used for calculating the estimate of the spectrum.
<code>nsim</code>	number of model simulations to be computed.
<code>seed</code>	optional; if non-NULL, the random number generator will be initialized with this seed for simulations. See <a href="#">simulate</a> .
<code>transform.data</code>	function; this transformation will be applied to the observables prior to estimation of the spectrum, and prior to any detrending.
<code>detrend</code>	de-trending operation to perform. Options include no detrending, and subtraction of constant, linear, and quadratic trends from the data. Detrending is applied to each data series and to each model simulation independently.
<code>weights</code>	optional. The mismatch between model and data is measured by a weighted average of mismatch at each frequency. By default, all frequencies are weighted equally. <code>weights</code> can be specified either as a vector (which must have length

	equal to the number of frequencies) or as a function of frequency. If the latter, <code>weights(freq)</code> must return a nonnegative weight for each frequency.
<code>start</code>	named numeric vector; the initial guess of parameters.
<code>est</code>	character vector; the names of parameters to be estimated.
<code>method</code>	Optimization method. Choices are <code>subplex</code> , <code>sannbox</code> , and any of the methods used by <code>optim</code> .
<code>verbose</code>	logical; print diagnostic messages?
<code>fail.value</code>	optional scalar; if non-NA, this value is substituted for non-finite values of the objective function.
<code>...</code>	Additional arguments. In the case of <code>spect</code> , these are currently ignored. In the case of <code>spect.match</code> , these are passed to <code>optim</code> or <code>subplex</code> in the control list.

### Details

A call to `spect` results in the estimation of the power spectrum for the (transformed, detrended) data and `nsim` model simulations. The results of these computations are stored in an object of class `spect.pomp`.

A call to `spect.match` results in an attempt to optimize the agreement between model and data spectrum over the parameters named in `est`. The results, including coefficients of the fitted model and power spectra of fitted model and data, are stored in an object of class `spect.matched.pomp`.

### Value

`spect` returns an object of class `spect.pomp`, which is derived from class `pomp` and therefore has all the slots of that class. In addition, `spect.pomp` objects have the following slots:

**kernel.width** width parameter of the smoothing kernel used.

**transform** transformation function used.

**freq** numeric vector of the frequencies at which the power spectrum is estimated.

**datSPEC, simSPEC** estimated power spectra for data and simulations, respectively.

**pvals** one-sided p-values: fraction of the simulated spectra that differ more from the mean simulated spectrum than does the data. The metric used is  $L^2$  distance.

**detrend** detrending option used.

`spect.match` returns an object of class `spect.matched.pomp`, which is derived from class `spect.pomp` and therefore has all the slots of that class. In addition, `spect.matched.pomp` objects have the following slots:

**est, weights, fail.value** values of the corresponding arguments in the call to `spect.match`.

**evals** number of function and gradient evaluations by the optimizer. See `optim`.

**value** Value of the objective function.

**convergence, msg** Convergence code and message from the optimizer. See `optim`.

### Author(s)

Daniel C. Reuman, Cai GoGwilt, Aaron A. King

## References

D.C. Reuman, R.A. Desharnais, R.F. Costantino, O. Ahmad, J.E. Cohen (2006) Power spectra reveal the influence of stochasticity on nonlinear population dynamics. *Proceedings of the National Academy of Sciences* **103**, 18860-18865.

D.C. Reuman, R.F. Costantino, R.A. Desharnais, J.E. Cohen (2008) Color of environmental noise affects the nonlinear dynamics of cycling, stage-structured populations. *Ecology Letters*, **11**, 820-830.

## See Also

[pomp](#), [probe](#)

## Examples

```
pompExample(ou2)
good <- spect(
  ou2,
  vars=c("y1", "y2"),
  kernel.width=3,
  detrend="mean",
  nsim=500
)
summary(good)
plot(good)

ou2.bad <- ou2
coef(ou2.bad, c("x1.0", "x2.0", "alpha.1", "alpha.4")) <- c(0, 0, 0.1, 0.2)
bad <- spect(
  ou2.bad,
  vars=c("y1", "y2"),
  kernel.width=3,
  detrend="mean",
  nsim=500
)
summary(bad)
plot(bad)
```

---

Probe functions

*Some useful probes for partially-observed Markov processes*

---

## Description

Several simple and configurable probes are provided with in the package. These can be used directly and as templates for custom probes.



**Usage**

```

probe.mean(var, trim = 0, transform = identity, na.rm = TRUE)
probe.median(var, na.rm = TRUE)
probe.var(var, transform = identity, na.rm = TRUE)
probe.sd(var, transform = identity, na.rm = TRUE)
probe.marginal(var, ref, order = 3, diff = 1, transform = identity)
probe.nlar(var, lags, powers, transform = identity)
probe.acf(var, lags, type = c("covariance", "correlation"),
          transform = identity)
probe.ccf(vars, lags, type = c("covariance", "correlation"),
          transform = identity)
probe.period(var, kernel.width, transform = identity)
probe.quantile(var, prob, transform = identity)

```

**Arguments**

<code>var, vars</code>	character; the name(s) of the observed variable(s).
<code>trim</code>	the fraction of observations to be trimmed (see <a href="#">mean</a> ).
<code>transform</code>	transformation to be applied to the data before the probe is computed.
<code>na.rm</code>	if TRUE, remove all NA observations prior to computing the probe.
<code>kernel.width</code>	width of modified Daniell smoothing kernel to be used in power-spectrum computation: see <a href="#">kernel</a> .
<code>prob</code>	a single probability; the quantile to compute: see <a href="#">quantile</a> .
<code>lags</code>	In <code>probe.ccf</code> , a vector of lags between time series. Positive lags correspond to <i>x</i> advanced relative to <i>y</i> ; negative lags, to the reverse.  In <code>probe.nlar</code> , a vector of lags present in the nonlinear autoregressive model that will be fit to the actual and simulated data. See Details, below, for a precise description.
<code>powers</code>	the powers of each term (corresponding to lags) in the the nonlinear autoregressive model that will be fit to the actual and simulated data. See Details, below, for a precise description.
<code>type</code>	Compute autocorrelation or autocovariance?
<code>ref</code>	empirical reference distribution. Simulated data will be regressed against the values of <code>ref</code> , sorted and, optionally, differenced. The resulting regression coefficients capture information about the shape of the marginal distribution. A good choice for <code>ref</code> is the data itself.
<code>order</code>	order of polynomial regression.
<code>diff</code>	order of differencing to perform.

**Details**

Each of these functions is relatively simple. See the source code for a complete understanding of what each does.

`probe.mean`, `probe.median`, `probe.var`, `probe.sd` return functions that compute the mean, median, variance, and standard deviation of variable `var`, respectively.

- `probe.period` returns a function that estimates the period of the Fourier component of the var series with largest power.
- `probe.marginal` returns a function that regresses the marginal distribution of variable `var` against the reference distribution `ref`. If `diff>0`, the data and the reference distribution are first differenced `diff` times and centered. Polynomial regression of order `order` is used. This probe returns order regression coefficients (the intercept is zero).
- `probe.nlar` returns a function that fit a nonlinear (polynomial) autoregressive model to the univariate series (variable `var`). Specifically, a model of the form  $y_t = \sum \beta_k y_{t-\tau_k}^{p_k} + \epsilon_t$  will be fit, where  $\tau_k$  are the lags and  $p_k$  are the powers. The data are first centered. This function returns the regression coefficients,  $\beta_k$ .
- `probe.acf` returns a function that, if `type=="covariance"`, computes the autocovariance of variable `var` at lags `lags`; if `type=="correlation"`, computes the autocorrelation of variable `var` at lags `lags`.
- `probe.ccf` returns a function that, if `type=="covariance"`, computes the cross covariance of the two variables named in `vars` at lags `lags`; if `type=="correlation"`, computes the cross correlation.
- `probe.quantile` returns a function that estimates the `prob`-th quantile of variable `var`.

### Value

A call to any one of these functions returns a probe function, suitable for use in [probe](#) or [probe.match](#). That is, the function returned by each of these takes a data array (such as comes from a call to [obs](#)) as input and returns a single numerical value.

### Author(s)

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Aaron A. King (kingaa at umich dot edu)

### References

B. E. Kendall, C. J. Briggs, W. M. Murdoch, P. Turchin, S. P. Ellner, E. McCauley, R. M. Nisbet, S. N. Wood Why do populations cycle? A synthesis of statistical and mechanistic modeling approaches, *Ecology*, 80:1789–1805, 1999.

S. N. Wood Statistical inference for noisy nonlinear ecological dynamic systems, *Nature*, 466: 1102–1104, 2010.

### See Also

[pomp](#)

---

Probes and synthetic likelihood

*Probe a partially-observed Markov process by computing summary statistics and the synthetic likelihood.*

---

**Description**

probe applies one or more “probes” to time series data and model simulations and compares the results. It can be used to diagnose goodness of fit and/or as the basis for “probe-matching”, a generalized method-of-moments approach to parameter estimation. `probe.match` calls an optimizer to adjust model parameters to do probe-matching, i.e., to minimize the discrepancy between simulated and actual data. This discrepancy is measured using the “synthetic likelihood” as defined by Wood (2010). `probe.match.objfun` constructs an objective function for probe-matching suitable for use in optim-like optimizers.

**Usage**

```
## S4 method for signature 'pomp'
probe(object, probes, params, nsim, seed = NULL, ...)
## S4 method for signature 'probed.pomp'
probe(object, probes, params, nsim, seed, ...)
## S4 method for signature 'pomp'
probe.match.objfun(object, params, est, probes, nsim,
  seed = NULL, fail.value = NA, transform = FALSE, ...)
## S4 method for signature 'probed.pomp'
probe.match.objfun(object, probes, nsim, seed, ...)
## S4 method for signature 'pomp'
probe.match(object, start, est = character(0),
  probes, nsim, seed = NULL,
  method = c("subplex", "Nelder-Mead", "SANN", "BFGS",
    "sannbox", "nloptr"),
  verbose = getOption("verbose"),
  fail.value = NA, transform = FALSE, ...)
## S4 method for signature 'probed.pomp'
probe.match(object, probes, nsim, seed,
  ..., verbose = getOption("verbose"))
## S4 method for signature 'probe.matched.pomp'
probe.match(object, est, probes,
  nsim, seed, transform, fail.value, ...,
  verbose = getOption("verbose"))
## S4 method for signature 'probed.pomp'
logLik(object, ...)
## S4 method for signature 'probed.pomp'
values(object, ...)
```

**Arguments**

<code>object</code>	An object of class <code>pomp</code> .
<code>probes</code>	A single probe or a list of one or more probes. A probe is simply a scalar- or vector-valued function of one argument that can be applied to the data array of a <code>pomp</code> . A vector-valued probe must always return a vector of the same size. A number of useful examples are provided with the package: see <a href="#">probe functions</a> ).
<code>params</code>	optional named numeric vector of model parameters. By default, <code>params=coef(object)</code> .
<code>nsim</code>	The number of model simulations to be computed.
<code>seed</code>	optional; if non-NULL, the random number generator will be initialized with this seed for simulations. See <a href="#">simulate-pomp</a> .
<code>start</code>	named numeric vector; the initial guess of parameters.
<code>est</code>	character vector; the names of parameters to be estimated.
<code>method</code>	Optimization method. Choices refer to algorithms used in <a href="#">optim</a> , <a href="#">subplex</a> , and <a href="#">nloptr</a> .
<code>verbose</code>	logical; print diagnostic messages?
<code>fail.value</code>	optional numeric scalar; if non-NA, this value is substituted for non-finite values of the objective function. It should be a large number (i.e., bigger than any legitimate values the objective function is likely to take).
<code>transform</code>	logical; if TRUE, optimization is performed on the transformed scale.
<code>...</code>	Additional arguments. In the case of <code>probe</code> , these are currently ignored. In the case of <code>probe.match</code> , these are passed to the optimizer (one of <a href="#">optim</a> , <a href="#">subplex</a> , <a href="#">nloptr</a> , or <a href="#">sannbox</a> ). These are passed via the optimizer's control list (in the case of <code>optim</code> , <code>subplex</code> , and <code>sannbox</code> ) or the <code>opts</code> list (in the case of <code>nloptr</code> ).

**Details**

A call to `probe` results in the evaluation of the probe(s) in `probes` on the data. Additionally, `nsim` simulated data sets are generated (via a call to [simulate](#)) and the probe(s) are applied to each of these. The results of the probe computations on real and simulated data are stored in an object of class `probed.pomp`.

A call to `probe.match` results in an attempt to optimize the agreement between model and data, as measured by the specified probes, over the parameters named in `est`. The results, including coefficients of the fitted model and values of the probes for data and fitted-model simulations, are stored in an object of class [probe.matched.pomp](#).

The objective function minimized by `probe.match` — in a form suitable for use with `optim`-like optimizers — is created by a call to `probe.match.objfun`. Specifically, `probe.match.objfun` will return a function that takes a single numeric-vector argument that is assumed to contain the parameters named in `est`, in that order. This function will return the negative synthetic log likelihood for the probes specified.

**Value**

`probe` returns an object of class `probed.pomp`. `probed.pomp` is derived from the [pomp](#) class and therefore have all the slots of `pomp`. In addition, a `probed.pomp` class has the following slots:

**probes** list of the probes applied.

**datvals, simvals** values of each of the probes applied to the real and simulated data, respectively.

**quantiles** fraction of simulations with probe values less than the value of the probe of the data.

**pvals** two-sided p-values: fraction of the `simvals` that deviate more extremely from the mean of the `simvals` than does `datvals`.

**synth.loglik** the log synthetic likelihood (Wood 2010). This is the likelihood assuming that the probes are multivariate-normally distributed.

`probe.match` returns an object of class `probe.matched.pomp`, which is derived from class `probed.pomp`. `probe.matched.pomp` objects therefore have all the slots above plus the following:

**est, transform, fail.value** values of the corresponding arguments in the call to `probe.match`.

**value** value of the objective function at the optimum.

**evals** number of function and gradient evaluations by the optimizer. See [optim](#).

**convergence, msg** Convergence code and message from the optimizer. See [optim](#) and [nloptr](#).

`probe.match.objfun` returns a function suitable for use as an objective function in an [optim](#)-like optimizer.

## Methods

**plot** displays diagnostic plots.

**summary** displays summary information.

**values** extracts the realized values of the probes on the data and on the simulations as a data frame in long format. The variable `.id` indicates whether the probes are from the data or simulations.

**logLik** returns the synthetic likelihood for the probes. NB: in general, this is not the same as the likelihood.

**as, as.data.frame** when a ‘`probed.pomp`’ is coerced to a ‘`data.frame`’, the first row gives the probes applied to the data; the rest of the rows give the probes evaluated on simulated data. The rownames of the result can be used to distinguish these.

In addition, slots of this object can be accessed via the `$` operator.

## Author(s)

Daniel C. Reuman, Aaron A. King

## References

B. E. Kendall, C. J. Briggs, W. M. Murdoch, P. Turchin, S. P. Ellner, E. McCauley, R. M. Nisbet, S. N. Wood Why do populations cycle? A synthesis of statistical and mechanistic modeling approaches, *Ecology*, 80:1789–1805, 1999.

S. N. Wood Statistical inference for noisy nonlinear ecological dynamic systems, *Nature*, 466: 1102–1104, 2010.

## See Also

[pomp](#), [probe functions](#), [spect](#), and the tutorials on the [package website](#).

## Examples

```
pompExample(ou2)
good <- probe(
  ou2,
  probes=list(
    y1.mean=probe.mean(var="y1"),
    y2.mean=probe.mean(var="y2"),
    y1.sd=probe.sd(var="y1"),
    y2.sd=probe.sd(var="y2"),
    extra=function(x)max(x["y1",])
  ),
  nsim=300
)
summary(good)
plot(good)

bad <- probe(
  ou2,
  params=c(alpha.1=0.1,alpha.4=0.2,x1.0=0,x2.0=0,
    alpha.2=-0.5,alpha.3=0.3,
    sigma.1=3,sigma.2=-0.5,sigma.3=2,
    tau=1),
  probes=list(
    y1.mean=probe.mean(var="y1"),
    y2.mean=probe.mean(var="y2"),
    y1.sd=probe.sd(var="y1"),
    y2.sd=probe.sd(var="y2"),
    extra=function(x)range(x["y1",])
  ),
  nsim=300
)
summary(bad)
plot(bad)
```

---

ricker

*Ricker model with Poisson observations.*


---

## Description

ricker is a pomp object encoding a stochastic Ricker model with Poisson measurement error.

## Details

The state process is  $N_{t+1} = rN_t \exp(-cN_t + e_t)$ , where the  $e_t$  are i.i.d. normal random deviates with zero mean and variance  $\sigma^2$ . The observed variables  $y_t$  are distributed as  $\text{Poisson}(\phi N_t)$ .

## See Also

[pomp](#), [gompertz](#), and the tutorials on the [package website](#).

**Examples**

```
pompExample(ricker)
plot(ricker)
coef(ricker)
```

rw2

*Two-dimensional random-walk process***Description**

rw2 is a pomp object encoding a 2-D normal random walk.

**Details**

The random-walk process is fully but noisily observed.

**See Also**

[pomp](#), [ou2](#)

**Examples**

```
pompExample(rw2)
plot(rw2)
x <- simulate(rw2, nsim=10, seed=20348585L, params=c(x1.0=0, x2.0=0, s1=1, s2=3, tau=1))
plot(x[[1]])
```

Simulated annealing

*Simulated annealing with box constraints.***Description**

sannbox is a straightforward implementation of simulated annealing with box constraints.

**Usage**

```
sannbox(par, fn, control = list(), ...)
```

**Arguments**

par	Initial values for the parameters to be optimized over.
fn	A function to be minimized, with first argument the vector of parameters over which minimization is to take place. It should return a scalar result.
control	A named list of control parameters. See ‘Details’.
...	ignored.

### Details

The control argument is a list that can supply any of the following components:

- trace** Non-negative integer. If positive, tracing information on the progress of the optimization is produced. Higher values may produce more tracing information.
- fnscale** An overall scaling to be applied to the value of `fn` during optimization. If negative, turns the problem into a maximization problem. Optimization is performed on `fn(par)/fnscale`.
- parscale** A vector of scaling values for the parameters. Optimization is performed on `par/parscale` and these should be comparable in the sense that a unit change in any element produces about a unit change in the scaled value.
- maxit** The total number of function evaluations: there is no other stopping criterion. Defaults to 10000.
- temp** starting temperature for the cooling schedule. Defaults to 1.
- tmax** number of function evaluations at each temperature. Defaults to 10.
- candidate.dist** function to randomly select a new candidate parameter vector. This should be a function with three arguments, the first being the current parameter vector, the second the temperature, and the third the parameter scaling. By default, `candidate.dist` is
 

```
function(par, temp, scale) rnorm(n=length(par), mean=par, sd=scale*temp).
```
- sched** cooling schedule. A function of a three arguments giving the temperature as a function of iteration number and the control parameters `temp` and `tmax`. By default, `sched` is
 

```
function(k, temp, tmax) temp/log(((k-1)/tmax)*tmax+exp(1)).
```

 Alternatively, one can supply a numeric vector of temperatures. This must be of length at least `maxit`.
- lower, upper** optional numeric vectors. These describe the lower and upper box constraints, respectively. Each can be specified either as a single scalar (common to all parameters) or as a vector of the same length as `par`. By default, `lower=-Inf` and `upper=Inf`, i.e., there are no constraints.

### Value

`sannbox` returns a list with components:

- counts** two-element integer vector. The first number gives the number of calls made to `fn`. The second number is provided for compatibility with `optim` and will always be NA.
- convergence** provided for compatibility with `optim`; will always be 0.
- final.params** last tried value of `par`.
- final.value** value of `fn` corresponding to `final.params`.
- par** best tried value of `par`.
- value** value of `fn` corresponding to `par`.

### Author(s)

Daniel Reuman, Aaron A. King



**See Also**

[traj.match](#), [probe.match](#).

---

sir

*Compartmental epidemiological models*

---

**Description**

`euler.sir` is a `pomp` object encoding a simple seasonal SIR model. Simulation is performed using an Euler multinomial approximation. `gillespie.sir` has the same model implemented using Gillespie's algorithm. `bbs` is a nonseasonal SIR model together with data from a 1978 outbreak of influenza in a British boarding school.

**Details**

This and similar examples are discussed and constructed in tutorials available on the [package website](#).

The boarding school influenza outbreak is described in Anonymous (1978).

**References**

Anonymous (1978). Influenza in a boarding school. *British Medical Journal* 1:587

**See Also**

[pomp](#) and the tutorials on the [package website](#).

**Examples**

```
pompExample(euler.sir)
plot(euler.sir)
plot(simulate(euler.sir, seed=20348585))
coef(euler.sir)

pompExample(gillespie.sir)
plot(gillespie.sir)
plot(simulate(window(gillespie.sir, end=3), seed=20348585))
coef(gillespie.sir)

pompExample(bbs)
plot(bbs)
coef(bbs)
```

---

Trajectory matching	<i>Parameter estimation by fitting the trajectory of a model's deterministic skeleton to data</i>
---------------------	---

---

## Description

This function attempts to match trajectories of a model's deterministic skeleton to data. Trajectory matching is equivalent to maximum likelihood estimation under the assumption that process noise is entirely absent, i.e., that all stochasticity is measurement error. Accordingly, this method uses only the skeleton and dmeasure components of a POMP model.

## Usage

```
## S4 method for signature 'pomp'
traj.match(object, start, est = character(0),
           method = c("Nelder-Mead", "subplex", "SANN", "BFGS",
                     "sannbox", "nloptr"),
           transform = FALSE, ...)
## S4 method for signature 'traj.matched.pomp'
traj.match(object, est, transform, ...)
## S4 method for signature 'pomp'
traj.match.objfun(object, params, est, transform = FALSE, ...)
```

## Arguments

object	A <a href="#">pomp</a> object. If object has no skeleton slot, an error will be generated.
start	named numeric vector containing an initial guess for parameters. By default start=coef(object) if the latter exists.
params	optional named numeric vector of parameters. This should contain all parameters needed by the skeleton and dmeasure slots of object. In particular, any parameters that are to be treated as fixed should be present here. Parameter values given in params for parameters named in est will be ignored. By default, params=coef(object) if the latter exists.
est	character vector containing the names of parameters to be estimated. In the case of traj.match.objfun, the objective function that is constructed will assume that its argument contains the parameters in this order.
method	Optimization method. Choices are <a href="#">subplex</a> , "sannbox", any of the methods used by <a href="#">optim</a> , and <a href="#">nloptr</a> . The latter makes available all the optimization algorithms of the <a href="#">nloptr</a> package ( <a href="https://cran.r-project.org/package=nloptr">https://cran.r-project.org/package=nloptr</a> ).
transform	logical; if TRUE, optimization is performed on the transformed scale.
...	Extra arguments that will be passed either to the optimizer ( <a href="#">optim</a> , <a href="#">subplex</a> , <a href="#">nloptr</a> , or <a href="#">sannbox</a> , via their control (optim, subplex, sannbox) or opts (nloptr) lists) or to the ODE integrator. In traj.match, extra arguments will be passed to the optimizer. In traj.match.objfun, extra arguments are passed to

[trajectory](#). If extra arguments are needed by both optimizer and [trajectory](#), construct an objective function first using `traj.match.objfun`, then give this objective function to the optimizer.

## Details

In **pomp**, trajectory matching is the term used for maximizing the likelihood of the data under the assumption that there is no process noise. Specifically, `traj.match` calls an optimizer ([optim](#), [subplex](#), and [sannbox](#) are the currently supported options) to minimize an objective function. For any value of the model parameters, this objective function is calculated by

1. computing the deterministic trajectory of the model given the parameters. This is the trajectory returned by [trajectory](#), which relies on the model's deterministic skeleton as specified in the construction of the `pomp` object.
2. evaluating the negative log likelihood of the data under the measurement model given the deterministic trajectory and the model parameters. This is accomplished via the model's `dmeasure` slot. The negative log likelihood is the objective function's value.

The objective function itself — in a form suitable for use with [optim](#)-like optimizers — is created by a call to `traj.match.objfun`. Specifically, `traj.match.objfun` will return a function that takes a single numeric-vector argument that is assumed to contain the parameters named in `est`, in that order.

## Value

`traj.match` returns an object of class `traj.matched.pomp`. This class inherits from class [pomp](#) and contains the following additional slots:

**transform, est** the values of these arguments on the call to `traj.match`.

**evals** number of function and gradient evaluations by the optimizer. See [optim](#).

**value** value of the objective function. Larger values indicate better fit (i.e., `traj.match` attempts to maximize this quantity).

**convergence, msg** convergence code and message from the optimizer. See [optim](#).

Available methods for objects of this type include `summary` and `logLik`. The other slots of this object can be accessed via the `$` operator.

`traj.match.objfun` returns a function suitable for use as an objective function in an [optim](#)-like optimizer.

## See Also

[trajectory](#), [pomp](#), [optim](#), [subplex](#)

## Examples

```
pompExample(ou2)
true.p <- c(
  alpha.1=0.9,alpha.2=0,alpha.3=-0.4,alpha.4=0.99,
  sigma.1=2,sigma.2=0.1,sigma.3=2,
  tau=1,
```

```

      x1.0=50,x2.0=-50
    )
simdata <- simulate(ou2,nsim=1,params=true.p,seed=43553)
guess.p <- true.p
res <- traj.match(
  simdata,
  start=guess.p,
  est=c('alpha.1','alpha.3','alpha.4','x1.0','x2.0','tau'),
  maxit=2000,
  method="Nelder-Mead",
  reltol=1e-8
)

summary(res)

plot(range(time(res)),range(c(obs(res),states(res))),type='n',xlab="time",ylab="x,y")
points(y1~time,data=as(res,"data.frame"),col='blue')
points(y2~time,data=as(res,"data.frame"),col='red')
lines(x1~time,data=as(res,"data.frame"),col='blue')
lines(x2~time,data=as(res,"data.frame"),col='red')

## Not run:
res1 <- traj.match(
  simdata,
  start=guess.p,
  est=c('alpha.1','alpha.3','alpha.4','x1.0','x2.0','tau'),
  maxit=2000,
  method="nloptr",
  algorithm="NLOPT_LN_SBPLX",
  xtol_rel=1e-5, maxeval=1e5
)

summary(res1)

## End(Not run)

pompExample(ricker)
ofun <- traj.match.objfun(ricker,est=c("r","phi"),transform=TRUE)
optim(fn=ofun,par=c(2,0),method="BFGS")

pompExample(bbs)
## some options are passed to the ODE integrator
ofun <- traj.match.objfun(bbs,est=c("beta","gamma"),transform=TRUE,hmax=0.001,rtol=1e-6)
optim(fn=ofun,par=c(0,-1),method="Nelder-Mead",control=list(reltol=1e-10))

```

## Description

On cooking shows, recipes requiring lengthy baking or stewing are prepared beforehand. The `bake` and `stew` functions perform analogously: an R computation is performed and stored in a named file. If the function is called again and the file is present, the computation is not executed; rather, the results are loaded from the file in which they were previously stored. Moreover, via their optional `seed` argument, `bake` and `stew` can control the pseudorandom-number generator (RNG) for greater reproducibility. After the computation is finished, these functions restore the pre-existing RNG state to avoid side effects.

The `freeze` function doesn't save results, but does set the RNG state to the specified value and restore it after the computation is complete.

## Usage

```
bake(file, expr, seed, kind = NULL, normal.kind = NULL)
stew(file, expr, seed, kind = NULL, normal.kind = NULL)
freeze(expr, seed, kind = NULL, normal.kind = NULL)
```

## Arguments

<code>file</code>	Name of the binary data file in which the result will be stored or retrieved, as appropriate. For <code>bake</code> , this will contain a single R object and hence be an RDS file (extension 'rds'); for <code>stew</code> , this will contain one or more named R objects and hence be an RDA file (extension 'rda').
<code>expr</code>	Expression to be evaluated.
<code>seed, kind, normal.kind</code>	Optional. To set the state and, optionally, kind of RNG used. See <a href="#">set.seed</a> .

## Details

Both `bake` and `stew` first test to see whether file exists. If it does, `bake` reads it using [readRDS](#) and returns the resulting object. By contrast, `stew` loads the file using [load](#) and copies the objects it contains into the user's workspace (or the environment of the call to `stew`).

If file does not exist, then both `bake` and `stew` evaluate the expression `expr`; they differ in the results that they save. `bake` saves the value of the evaluated expression to `file` as a single R object. The name of that object is not saved. By contrast, `stew` creates a local environment within which `expr` is evaluated; all objects in that environment are saved (by name) in `file`.

## Value

`bake` returns the value of the evaluated expression `expr`. Other objects created in the evaluation of `expr` are discarded along with the temporary, local environment created for the evaluation.

The latter behavior differs from that of `stew`, which returns the names of the objects created during the evaluation of `expr`. After `stew` completes, these objects exist in the parent environment (that from which `stew` was called).

`freeze` returns the value of evaluated expression `expr`. However, `freeze` evaluates `expr` within the parent environment, so other objects created in the evaluation of `expr` will therefore exist after `freeze` completes.

All these functions return information about the time used in evaluating the expression. This is recorded in the `system.time` attribute of the return value. In addition, if seed is specified, information about the seed (and the kind of random-number generator used) are stored as attributes of the return value.

**Author(s)**

Aaron A. King

**Examples**

```
## Not run:
bake(file="example1.rds",{
  x <- runif(1000)
  mean(x)
})

stew(file="example2.rda",{
  x <- runif(10)
  y <- rnorm(n=10,mean=3*x+5,sd=2)
})

plot(x,y)

## End(Not run)

freeze(runif(3),seed=5886730)
freeze(runif(3),seed=5886730)
```

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