# Package 'pomp'

June 23, 2020

Type Package

```
Title Statistical Inference for Partially Observed Markov Processes
Version 3.0.2.1
Date 2020-06-23
URL https://kingaa.github.io/pomp/
Description Tools for data analysis with partially observed Markov process (POMP) mod-
     els (also known as stochastic dynamical systems, hidden Markov models, and nonlinear, non-
     Gaussian, state-space models). The package provides facilities for implementing POMP mod-
     els, simulating them, and fitting them to time series data by a variety of frequen-
     tist and Bayesian methods. It is also a versatile platform for implementation of inference meth-
     ods for general POMP models.
Depends R(>= 4.0.0), methods
Imports stats, graphics, digest, mytnorm, deSolve, coda, reshape2, magrittr, plyr
Suggests ggplot2, knitr, tidyr, dplyr, subplex, nloptr
SystemRequirements For Windows users, Rtools (see https://cran.r-project.org/bin/windows/Rtools/).
License GPL-3
LazyData true
Contact kingaa at umich dot edu
BugReports https://github.com/kingaa/pomp/issues/
Encoding UTF-8
Collate 'pomp-package.R'
     'aaa.R'
     'pstop.R'
     'undefined.R'
     'csnippet.R'
     'pomp_fun.R'
     'parameter_trans.R'
     'covariate table.R'
     'skeleton_spec.R'
     'rprocess_spec.R'
     'safecall.R'
```

'pomp\_class.R'

'load.R'

'workhorses.R'

'continue.R'

'prior\_spec.R'

'dmeasure\_spec.R'

'dprocess\_spec.R'

'rmeasure\_spec.R'

'rinit\_spec.R'

'templates.R'

'builder.R'

'pomp.R'

'probe.R'

'abc.R'

'accumulators.R'

'kalman.R'

'pfilter.R'

'wpfilter.R'

'proposals.R'

'pmcmc.R'

'mif2.R'

'listie.R'

'simulate.R'

'spect.R'

'plot.R'

'bsmc2.R'

'as\_data\_frame.R'

'as\_pomp.R'

'authors.R'

'bake.R'

'basic\_probes.R'

'blowflies.R'

'bsflu.R'

'bsplines.R'

'coef.R'

'concat.R'

'cond\_logLik.R'

'covmat.R'

'dacca.R'

'design.R'

'distributions.R'

'ebola.R'

'eff\_sample\_size.R'

'extract.R'

'filter\_mean.R'

'filter\_traj.R'

'flow.R'

'forecast.R'

R topics documented:

'gompertz.R'
'probe_match.R'
'spect_match.R'
'summary.R'
'nlf.R'
'trajectory.R'
'traj_match.R'
'objfun.R'
'loglik.R'
'logmeanexp.R'
'lookup.R'
'measles.R'
'melt.R'
'obs.R'
'ou2.R'
'parmat.R'
'parus.R'
'pipe.R'
'pomp_examp.R'
'pred_mean.R'
'pred_var.R'
'show.R'
'print.R'
'profile_design.R'
'resample.R'
'ricker.R'
'runif_design.R'
'rw2.R'
'sannbox.R'
'sir.R'
'slice_design.R'
'sobol.R'
'spy.R'
'states.R'
'time.R'
'timezero.R'
'traces.R'
'transformations.R'
'userdata.R'
'verhulst.R'
'window.R'
RoxygenNote 7.1.0

# R topics documented:

pomp-package.	 																	5
abc	 																	7

accumulators	. 10
as.data.frame	. 12
bake	. 14
basic_probes	. 16
blowflies	. 18
bsflu	. 20
bsmc2	. 21
bsplines	
coef	
cond.logLik	
continue	
covariate table	. 27
covmat	. 28
Csnippet	. 29
dacca	
design	
distributions	
dmeasure	
dmeasure_spec	
dprior	
dprocess	
•	
dprocess_spec	
ebola	
eff.sample.size	
filter.mean	
filter.traj	
flow	
forecast	
gompertz	
hitch	
kalman	
logLik	
logmeanexp	
measles	
mif2	
nlf	
obs	. 65
ou2	. 65
parameter_trans	. 67
parmat	. 69
partrans	. 70
parus	. 70
pfilter	. 71
plot	. 74
pmcmc	. 76
pomp	. 79
pomp_examples	. 83
pred.mean	. 84

pomp-package 5

	pred.var	. 85
1	print	. 86
	prior_spec	. 86
	probe	. 87
	probe.match	. 90
	proposals	. 93
	ricker	. 95
	rinit	. 96
	rinit_spec	. 96
	rmeasure	. 98
	rmeasure_spec	. 99
	rprior	. 100
	rprocess	
	rprocess_spec	
	rw.sd	
	rw2	. 106
	sannbox	. 107
	simulate	. 108
	sir_models	. 111
	skeleton	. 113
	skeleton_spec	. 114
	spect	. 115
	spect.match	. 118
	spy	. 122
	states	. 122
	summary-probed_pomp	. 123
	time	
	timezero	. 124
	traces	. 125
i	traj.match	. 126
1	trajectory	. 129
i	transformations	. 130
1	userdata	. 131
	verhulst	
	window	. 136
	workhorses	. 136
	wpfilter	. 137
		140
		170

6 pomp-package

# **Description**

The **pomp** package provides facilities for inference on time series data using partially-observed Markov process (POMP) models. These models are also known as state-space models, hidden Markov models, or nonlinear stochastic dynamical systems. One can use **pomp** to fit nonlinear, non-Gaussian dynamic models to time-series data. The package is both a set of tools for data analysis and a platform upon which statistical inference methods for POMP models can be implemented.

# Data analysis using pomp

pomp provides algorithms for

- 1. simulation of stochastic dynamical systems; see simulate
- 2. particle filtering (AKA sequential Monte Carlo or sequential importance sampling); see pfilter
- 3. the iterated filtering methods of Ionides et al. (2006, 2011, 2015); see mif2
- 4. the nonlinear forecasting algorithm of Kendall et al. (2005); see nlf
- 5. the particle MCMC approach of Andrieu et al. (2010); see pmcmc
- 6. the probe-matching method of Kendall et al. (1999, 2005); see probe.match
- 7. a spectral probe-matching method (Reuman et al. 2006, 2008); see spect.match
- 8. synthetic likelihood a la Wood (2010); see probe
- 9. approximate Bayesian computation (Toni et al. 2009); see abc
- 10. the approximate Bayesian sequential Monte Carlo scheme of Liu & West (2001); see bsmc2
- 11. ensemble and ensemble adjusted Kalman filters; see kalman
- 12. simple trajectory matching; see traj.match.

The package also provides various tools for plotting and extracting information on models and data.

# Author(s)

Aaron A. King

#### References

A. A. King, D. Nguyen, and E. L. Ionides. Statistical Inference for Partially Observed Markov Processes via the Package **pomp**. *Journal of Statistical Software* **69**(12), 1–43, 2016. An updated version of this paper is available on the package website.

See the package website, https://kingaa.github.io/pomp/, for more references.

# See Also

Other information on model implementation: Csnippet, accumulators, covariate\_table(), distributions, dmeasure\_spec, dprocess\_spec, parameter\_trans(), prior\_spec, rinit\_spec, rmeasure\_spec, rprocess\_spec, skeleton\_spec, transformations, userdata

Other pomp parameter estimation methods: abc(), bsmc2(), kalman, mif2(), nlf, pmcmc(), probe.match, spect.match

Other elementary POMP methods: pfilter(), probe(), simulate(), spect(), wpfilter()

abc 7

abc

Approximate Bayesian computation

# **Description**

The approximate Bayesian computation (ABC) algorithm for estimating the parameters of a partially-observed Markov process.

# Usage

```
## S4 method for signature 'data.frame'
abc(
  data,
 Nabc = 1,
 proposal,
  scale,
  epsilon,
 probes,
  params,
  rinit,
  rprocess,
  rmeasure,
  dprior,
  verbose = getOption("verbose", FALSE)
)
## S4 method for signature 'pomp'
abc(
  data,
 Nabc = 1,
 proposal,
  scale,
  epsilon,
 probes,
  verbose = getOption("verbose", FALSE)
)
## S4 method for signature 'probed_pomp'
abc(data, probes, ..., verbose = getOption("verbose", FALSE))
## S4 method for signature 'abcd_pomp'
abc(
  data,
 Nabc,
 proposal,
```

8 abc

```
scale,
epsilon,
probes,
...,
verbose = getOption("verbose", FALSE)
```

## **Arguments**

data either a data frame holding the time series data, or an object of class 'pomp',

i.e., the output of another pomp calculation.

Nabc the number of ABC iterations to perform.

proposal optional function that draws from the proposal distribution. Currently, the pro-

posal distribution must be symmetric for proper inference: it is the user's responsibility to ensure that it is. Several functions that construct appropriate proposal

function are provided: see MCMC proposals for more information.

scale named numeric vector of scales.

epsilon ABC tolerance.

probes a single probe or a list of one or more probes. A probe is simply a scalar- or

vector-valued function of one argument that can be applied to the data array of a 'pomp'. A vector-valued probe must always return a vector of the same size. A number of useful probes are provided with the package: see basic probes.

params optional; named numeric vector of parameters. This will be coerced internally

to storage mode double.

rinit simulator of the initial-state distribution. This can be furnished either as a C

snippet, an R function, or the name of a pre-compiled native routine available in a dynamically loaded library. Setting rinit=NULL sets the initial-state simulator

to its default. For more information, see ?rinit\_spec.

rprocess simulator of the latent state process, specified using one of the rprocess plugins.

Setting rprocess=NULL removes the latent-state simulator. For more informa-

tion, see ?rprocess\_spec for the documentation on these plugins.

rmeasure simulator of the measurement model, specified either as a C snippet, an R func-

tion, or the name of a pre-compiled native routine available in a dynamically loaded library. Setting rmeasure=NULL removes the measurement model simu-

lator. For more information, see ?rmeasure\_spec.

dprior optional; prior distribution density evaluator, specified either as a C snippet, an R

function, or the name of a pre-compiled native routine available in a dynamically loaded library. For more information, see ?prior\_spec. Setting dprior=NULL resets the prior distribution to its default, which is a flat improper prior.

resets the prior distribution to its default, which is a flat improper prior.

.. additional arguments supply new or modify existing model characteristics or

components. See pomp for a full list of recognized arguments.

When named arguments not recognized by pomp are provided, these are made available to all basic components via the so-called *userdata* facility. This allows the user to pass information to the basic components outside of the usual routes of covariates (covar) and model parameters (params). See ?userdata for

information on how to use this facility.

verbose logical; if TRUE, diagnostic messages will be printed to the console.

abc 9

# **Running ABC**

abc returns an object of class 'abcd\_pomp'. One or more 'abcd\_pomp' objects can be joined to form an 'abcList' object.

## **Re-running ABC iterations**

To re-run a sequence of ABC iterations, one can use the abc method on a 'abcd\_pomp' object. By default, the same parameters used for the original ABC run are re-used (except for verbose, the default of which is shown above). If one does specify additional arguments, these will override the defaults.

# **Continuing ABC iterations**

One can continue a series of ABC iterations from where one left off using the continue method. A call to abc to perform Nabc=m iterations followed by a call to continue to perform Nabc=n iterations will produce precisely the same effect as a single call to abc to perform Nabc=m+n iterations. By default, all the algorithmic parameters are the same as used in the original call to abc. Additional arguments will override the defaults.

#### Methods

The following can be applied to the output of an abc operation:

plot produces a series of diagnostic plots

traces produces a mcmc object, to which the various coda convergence diagnostics can be applied

# Author(s)

Edward L. Ionides, Aaron A. King

## References

- J.-M. Marin, P. Pudlo, C. P. Robert, and R. J. Ryder. Approximate Bayesian computational methods. *Statistics and Computing* **22**, 1167–1180, 2012.
- T. Toni and M. P. H. Stumpf. Simulation-based model selection for dynamical systems in systems and population biology. *Bioinformatics* **26**, 104–110, 2010.
- T. Toni, D. Welch, N. Strelkowa, A. Ipsen, and M. P. H. Stumpf. Approximate Bayesian computation scheme for parameter inference and model selection in dynamical systems. *Journal of the Royal Society Interface* **6**, 187–202, 2009.

## See Also

# MCMC proposals

Other summary statistics methods: basic\_probes, probe.match, probe(), spect()

Other pomp parameter estimation methods: bsmc2(), kalman, mif2(), nlf, pmcmc(), pomp-package, probe.match, spect.match

10 accumulators

accumulators

accumulators

# Description

Accumulator variables

#### **Details**

In formulating models, one sometimes wishes to define a state variable that will accumulate some quantity over the interval between successive observations. **pomp** provides a facility to make such features more convenient. Specifically, variables named in the pomp's accumvars argument will be set to zero immediately following each observation. See sir and the tutorials on the package website for examples.

# See Also

sir

Other information on model implementation: Csnippet, covariate\_table(), distributions, dmeasure\_spec, dprocess\_spec, parameter\_trans(), pomp-package, prior\_spec, rinit\_spec, rmeasure\_spec, rprocess\_spec, skeleton\_spec, transformations, userdata

# **Examples**

```
## A simple SIR model.
ewmeas %>%
 subset(time < 1952) %>%
 pomp(
    times="time", t0=1948,
    rprocess=euler(
     Csnippet("
        int nrate = 6;
        double rate[nrate]; // transition rates
        double trans[nrate]; // transition numbers
        double dW;
        // gamma noise, mean=dt, variance=(sigma^2 dt)
        dW = rgammawn(sigma,dt);
        // compute the transition rates
        rate[0] = mu*pop; // birth into susceptible class
        rate[1] = (iota+Beta*I*dW/dt)/pop; // force of infection
        rate[2] = mu; // death from susceptible class
        rate[3] = gamma; // recovery
        rate[4] = mu; // death from infectious class
        rate[5] = mu; // death from recovered class
        // compute the transition numbers
```

accumulators 11

```
trans[0] = rpois(rate[0]*dt); // births are Poisson
        reulermultinom(2,S,&rate[1],dt,&trans[1]);
       reulermultinom(2,I,&rate[3],dt,&trans[3]);
       reulermultinom(1,R,&rate[5],dt,&trans[5]);
        // balance the equations
       S += trans[0]-trans[1]-trans[2];
       I += trans[1]-trans[3]-trans[4];
       R += trans[3]-trans[5];
      "),
     delta.t=1/52/20
   ),
    rinit=Csnippet("
     double m = pop/(S_0+I_0+R_0);
     S = nearbyint(m*S_0);
     I = nearbyint(m*I_0);
     R = nearbyint(m*R_0);
    "),
   paramnames=c("mu","pop","iota","gamma","Beta","sigma",
      "S_0","I_0","R_0"),
    statenames=c("S","I","R"),
   params=c(mu=1/50,iota=10,pop=50e6,gamma=26,Beta=400,sigma=0.1,
     S_0=0.07,I_0=0.001,R_0=0.93)
 ) -> ew1
ew1 %>%
 simulate() %>%
 plot(variables=c("S","I","R"))
## A simple SIR model that tracks cumulative incidence.
ew1 %>%
 pomp(
    rprocess=euler(
     Csnippet("
        int nrate = 6;
       double rate[nrate]; // transition rates
       double trans[nrate]; // transition numbers
       double dW;
        // gamma noise, mean=dt, variance=(sigma^2 dt)
       dW = rgammawn(sigma,dt);
       // compute the transition rates
       rate[0] = mu*pop; // birth into susceptible class
       rate[1] = (iota+Beta*I*dW/dt)/pop; // force of infection
       rate[2] = mu; // death from susceptible class
       rate[3] = gamma; // recovery
       rate[4] = mu; // death from infectious class
       rate[5] = mu; // death from recovered class
        // compute the transition numbers
        trans[0] = rpois(rate[0]*dt); // births are Poisson
```

12 as.data.frame

```
reulermultinom(2,S,&rate[1],dt,&trans[1]);
        reulermultinom(2,I,&rate[3],dt,&trans[3]);
        reulermultinom(1,R,&rate[5],dt,&trans[5]);
        // balance the equations
        S += trans[0]-trans[1]-trans[2];
        I += trans[1]-trans[3]-trans[4];
        R += trans[3]-trans[5];
        H += trans[3]; // cumulative incidence
      "),
      delta.t=1/52/20
    ),
    rmeasure=Csnippet("
      double mean = H*rho;
      double size = 1/tau;
      reports = rnbinom_mu(size,mean);
    "),
    rinit=Csnippet("
      double m = pop/(S_0+I_0+R_0);
      S = nearbyint(m*S_0);
     I = nearbyint(m*I_0);
     R = nearbyint(m*R_0);
     H = 0;
   "),
    paramnames=c("mu","pop","iota","gamma","Beta","sigma","tau","rho",
      "S_0","I_0","R_0"),
    statenames=c("S","I","R","H"),
   params=c(mu=1/50,iota=10,pop=50e6,gamma=26,
      Beta=400,sigma=0.1,tau=0.001,rho=0.6,
      S_0=0.07, I_0=0.001, R_0=0.93)
  ) -> ew2
ew2 %>%
  simulate() %>%
  plot()
## A simple SIR model that tracks weekly incidence.
ew2 %>%
  pomp(accumvars="H") -> ew3
ew3 %>%
  simulate() %>%
  plot()
```

as.data.frame

# **Description**

All **pomp** model objects can be recast as data frames. The contents of the resulting data frame depend on the nature of the object.

# Usage

```
## S3 method for class 'pomp'
as.data.frame(x, ...)
## S3 method for class 'pfilterd_pomp'
as.data.frame(x, ...)
## S3 method for class 'probed_pomp'
as.data.frame(x, ...)
## S3 method for class 'kalmand_pomp'
as.data.frame(x, ...)
## S3 method for class 'bsmcd_pomp'
as.data.frame(x, ...)
## S3 method for class 'pompList'
as.data.frame(x, ...)
## S3 method for class 'pfilterList'
as.data.frame(x, ...)
## S3 method for class 'abcList'
as.data.frame(x, ...)
## S3 method for class 'mif2List'
as.data.frame(x, ...)
## S3 method for class 'pmcmcList'
as.data.frame(x, ...)
## S3 method for class 'wpfilterd_pomp'
as.data.frame(x, ...)
```

#### **Arguments**

x any R object.

... additional arguments to be passed to or from methods.

# **Details**

When object is a simple 'pomp' object, as (object, "data.frame") or as.data.frame(object) results in a data frame with the times, observables, states (if known), and interpolated covariates (if

14 bake

any).

When object is a 'pfilterd\_pomp' object, coercion to a data frame results in a data frame with the same content as for a simple 'pomp', but with conditional log likelihood and effective sample size estimates included, as well as filtering means, prediction means, and prediction variances, if these have been computed.

When object is a 'probed\_pomp' object, coercion to a data frame results in a data frame with the values of the probes computed on the data and on simulations.

When object is a 'kalmand\_pomp' object, coercion to a data frame results in a data frame with prediction means, filter means and forecasts, in addition to the data.

When object is a 'bsmcd\_pomp' object, coercion to a data frame results in a data frame with samples from the prior and posterior distribution. The .id variable distinguishes them.

When object is a 'wpfilterd\_pomp' object, coercion to a data frame results in a data frame with the same content as for a simple 'pomp', but with conditional log likelihood and effective sample size estimates included.

bake

Bake, stew, and freeze

## **Description**

Tools for reproducible computations.

# Usage

```
bake(file, expr, seed = NULL, kind = NULL, normal.kind = NULL)
stew(file, expr, seed = NULL, kind = NULL, normal.kind = NULL)
freeze(expr, seed = NULL, kind = NULL, normal.kind = NULL)
```

#### **Arguments**

file

Name of the binary data file in which the result will be stored or retrieved, as appropriate. For bake, this will contain a single object and hence be an RDS file (extension 'rds'); for stew, this will contain one or more named objects and hence be an RDA file (extension 'rda').

expr

Expression to be evaluated.

seed, kind, normal.kind

optional. To set the state and of the RNG. See set.seed. The default, seed = NULL, will not change the RNG state. seed should be a single integer. See set.seed.

bake 15

#### **Details**

On cooking shows, recipes requiring lengthy baking or stewing are prepared beforehand. The bake and stew functions perform analogously: an computation is performed and stored in a named file. If the function is called again and the file is present, the computation is not executed. Instead, the results are loaded from the file in which they were previously stored. Moreover, via their optional seed argument, bake and stew can control the pseudorandom-number generator (RNG) for greater reproducibility. After the computation is finished, these functions restore the pre-existing RNG state to avoid side effects.

The freeze function doesn't save results, but does set the RNG state to the specified value and restore it after the computation is complete.

Both bake and stew first test to see whether file exists. If it does, bake reads it using readRDS and returns the resulting object. By contrast, stew loads the file using load and copies the objects it contains into the user's workspace (or the environment of the call to stew).

If file does not exist, then both bake and stew evaluate the expression expr; they differ in the results that they save. bake saves the value of the evaluated expression to file as a single object. The name of that object is not saved. By contrast, stew creates a local environment within which expr is evaluated; all objects in that environment are saved (by name) in file.

#### Value

bake returns the value of the evaluated expression expr. Other objects created in the evaluation of expr are discarded along with the temporary, local environment created for the evaluation.

The latter behavior differs from that of stew, which returns the names of the objects created during the evaluation of expr. After stew completes, these objects exist in the parent environment (that from which stew was called).

freeze returns the value of evaluated expression expr. However, freeze evaluates expr within the parent environment, so other objects created in the evaluation of expr will therefore exist after freeze completes.

bake and stew return information about the time used in evaluating the expression. This is recorded in the system. time attribute of the return value. In addition, if seed is specified, information about the seed (and the kind of random-number generator used) are stored as attributes of the return value.

## Author(s)

Aaron A. King

# **Examples**

```
## Not run:
    bake(file="example1.rds",{
        x <- runif(1000)
        mean(x)
})

stew(file="example2.rda",{
        x <- runif(10)
        y <- rnorm(n=10,mean=3*x+5,sd=2)</pre>
```

16 basic\_probes

```
})
plot(x,y)
freeze(runif(3), seed=5886730)
freeze(runif(3), seed=5886730)
## End(Not run)
```

basic\_probes

Useful probes for partially-observed Markov processes

# Description

Several simple and configurable probes are provided with in the package. These can be used directly and as templates for custom probes.

# Usage

```
probe.mean(var, trim = 0, transform = identity, na.rm = TRUE)
probe.median(var, na.rm = TRUE)
probe.var(var, transform = identity, na.rm = TRUE)
probe.sd(var, transform = identity, na.rm = TRUE)
probe.period(var, kernel.width, transform = identity)
probe.quantile(var, probs, ...)
probe.acf(
  var,
  lags,
  type = c("covariance", "correlation"),
  transform = identity
)
probe.ccf(
  vars,
  lags,
  type = c("covariance", "correlation"),
  transform = identity
)
probe.marginal(var, ref, order = 3, diff = 1, transform = identity)
probe.nlar(var, lags, powers, transform = identity)
```

basic\_probes 17

# **Arguments**

var, vars character; the name(s) of the observed variable(s).

trim the fraction of observations to be trimmed (see mean).

transform transformation to be applied to the data before the probe is computed.

na.rm if TRUE, remove all NA observations prior to computing the probe.

kernel.width width of modified Daniell smoothing kernel to be used in power-spectrum com-

putation: see kernel.

probs the quantile or quantiles to compute: see quantile.
... additional arguments passed to the underlying algorithms.

lags In probe.ccf, a vector of lags between time series. Positive lags correspond to

x advanced relative to y; negative lags, to the reverse.

In probe.nlar, a vector of lags present in the nonlinear autoregressive model that will be fit to the actual and simulated data. See Details, below, for a precise

description.

type Compute autocorrelation or autocovariance?

ref empirical reference distribution. Simulated data will be regressed against the

values of ref, sorted and, optionally, differenced. The resulting regression coefficients capture information about the shape of the marginal distribution. A

good choice for ref is the data itself.

order order of polynomial regression.
diff order of differencing to perform.

powers the powers of each term (corresponding to lags) in the the nonlinear autoregres-

sive model that will be fit to the actual and simulated data. See Details, below,

for a precise description.

# Value

A call to any one of these functions returns a probe function, suitable for use in probe or probe\_objfun. That is, the function returned by each of these takes a data array (such as comes from a call to obs) as input and returns a single numerical value.

# Author(s)

Daniel C. Reuman, Aaron A. King

#### References

B.E. Kendall, C.J. Briggs, W.W. Murdoch, P. Turchin, S.P. Ellner, E. McCauley, R.M. Nisbet, and S.N. Wood. Why do populations cycle? A synthesis of statistical and mechanistic modeling approaches. *Ecology* **80**, 1789–1805, 1999.

S. N. Wood Statistical inference for noisy nonlinear ecological dynamic systems. *Nature* **466**, 1102–1104, 2010.

#### See Also

Other summary statistics methods: abc(), probe.match, probe(), spect()

18 blowflies

blowflies

Nicholson's blowflies.

# **Description**

blowflies is a data frame containing the data from several of Nicholson's classic experiments with the Australian sheep blowfly, *Lucilia cuprina*.

# Usage

```
blowflies1(

P = 3.2838,

delta = 0.16073,

N0 = 679.94,

sigma.P = 1.3512,

sigma.d = 0.74677,

sigma.y = 0.026649

)

blowflies2(

P = 2.7319,

delta = 0.17377,

N0 = 800.31,

sigma.P = 1.442,

sigma.d = 0.76033,

sigma.y = 0.010846
```

# **Arguments**

Р	reproduction parameter
delta	death rate
NØ	population scale factor
sigma.P	intensity of $e$ noise
sigma.d	intensity of $eps$ noise
sigma.y	measurement error s.d.

#### **Details**

blowflies1() and blowflies2() construct 'pomp' objects encoding stochastic delay-difference equation models. The data for these come from "population I", a control culture. The experiment is described on pp. 163–4 of Nicholson (1957). Unlimited quantities of larval food were provided; the adult food supply (ground liver) was constant at 0.4g per day. The data were taken from the table provided by Brillinger et al. (1980).

blowflies 19

The models are discrete delay equations:

$$R(t+1) \sim \text{Poisson}(PN(t-\tau) \exp{(-N(t-\tau)/N_0)}e(t+1)\Delta t)$$
 
$$S(t+1) \sim \text{Binomial}(N(t), \exp{(-\delta\epsilon(t+1)\Delta t)})$$
 
$$N(t) = R(t) + S(t)$$

where e(t) and  $\epsilon(t)$  are Gamma-distributed i.i.d. random variables with mean 1 and variances  $\sigma_P^2/\Delta t$ ,  $\sigma_d^2/\Delta t$ , respectively. blowflies1 has a timestep ( $\Delta t$ ) of 1 day; blowflies2 has a timestep of 2 days. The process model in blowflies1 thus corresponds exactly to that studied by Wood (2010). The measurement model in both cases is taken to be

$$y(t) \sim \text{NegBin}(N(t), 1/\sigma_y^2)$$

i.e., the observations are assumed to be negative-binomially distributed with mean N(t) and variance  $N(t) + (\sigma_u N(t))^2$ .

Default parameter values are the MLEs as estimated by Ionides (2011).

#### Value

blowflies1 and blowflies2 return 'pomp' objects containing the actual data and two variants of the model.

#### References

A.J. Nicholson. The self-adjustment of populations to change. *Cold Spring Harbor Symposia on Quantitative Biology* **22**, 153–173, 1957.

Y. Xia and H. Tong. Feature Matching in Time Series Modeling. *Statistical Science* **26**, 21–46, 2011.

E.L. Ionides. Discussion of "Feature Matching in Time Series Modeling" by Y. Xia and H. Tong. *Statistical Science* **26**, 49–52, 2011.

S. N. Wood Statistical inference for noisy nonlinear ecological dynamic systems. *Nature* **466**, 1102–1104, 2010.

W.S.C. Gurney, S.P. Blythe, and R.M. Nisbet. Nicholson's blowflies revisited. *Nature* **287**, 17–21, 1980.

D.R. Brillinger, J. Guckenheimer, P. Guttorp, and G. Oster. Empirical modelling of population time series: The case of age and density dependent rates. In: G. Oster (ed.), *Some Questions in Mathematical Biology* vol. 13, pp. 65–90, American Mathematical Society, Providence, 1980.

# See Also

Other pomp examples: bsflu, dacca(), ebola, gompertz(), measles, ou2(), parus, pomp\_examples, ricker(), rw2(), sir\_models, verhulst()

Other datasets: bsflu, dacca(), ebola, measles, parus

# **Examples**

```
plot(blowflies1())
plot(blowflies2())
```

20 bsflu

bsflu

Influenza outbreak in a boarding school

# **Description**

An outbreak of influenza in an all-boys boarding school.

#### **Details**

Data are recorded from a 1978 flu outbreak in a closed population. The variable 'B' refers to boys confined to bed on the corresponding day and 'C' to boys in convalescence, i.e., not yet allowed back to class. In total, 763 boys were at risk of infection and, over the course of the outbreak, 512 boys spent between 3 and 7 days away from class (either in bed or convalescent). The index case was a boy who arrived at school from holiday six days before the next case.

#### References

Anonymous. Influenza in a boarding school. British Medical Journal 1, 587, 1978.

#### See Also

```
sir_models
Other datasets: blowflies, dacca(), ebola, measles, parus
Other pomp examples: blowflies, dacca(), ebola, gompertz(), measles, ou2(), parus, pomp_examples, ricker(), rw2(), sir_models, verhulst()
```

# **Examples**

```
library(magrittr)
library(tidyr)
library(ggplot2)

bsflu %>%
   gather(variable,value,-date,-day) %>%
   ggplot(aes(x=date,y=value,color=variable))+
   geom_line()+
   labs(y="number of boys",title="boarding school flu outbreak")+
   theme_bw()
```

bsmc2 21

bsmc2

The Liu and West Bayesian particle filter

# Description

Modified version of the Liu and West (2001) algorithm.

# Usage

```
## S4 method for signature 'data.frame'
bsmc2(
  data.
  Nρ,
  smooth = 0.1,
  params,
  rprior,
  rinit,
  rprocess,
  dmeasure,
  partrans,
  . . . ,
  verbose = getOption("verbose", FALSE)
)
## S4 method for signature 'pomp'
bsmc2(data, Np, smooth = 0.1, ..., verbose = getOption("verbose", FALSE))
```

# **Arguments**

data

either a data frame holding the time series data, or an object of class 'pomp', i.e., the output of another **pomp** calculation.

Np

the number of particles to use. This may be specified as a single positive integer, in which case the same number of particles will be used at each timestep. Alternatively, if one wishes the number of particles to vary across timesteps, one may specify Np either as a vector of positive integers of length

```
length(time(object,t0=TRUE))
```

or as a function taking a positive integer argument. In the latter case, Np(k) must be a single positive integer, representing the number of particles to be used at the k-th timestep: Np(0) is the number of particles to use going from timezero(object) to time(object)[1], Np(1), from timezero(object) to time(object)[1], and so on, while when T=length(time(object)), Np(T) is the number of particles to sample at the end of the time-series.

smooth

Kernel density smoothing parameter. The compensating shrinkage factor will be  $sqrt(1-smooth^2)$ . Thus, smooth=0 means that no noise will be added to parameters. The general recommendation is that the value of smooth should be chosen close to 0 (e.g.,  $shrink \sim 0.1$ ).

22 bsmc2

optional; named numeric vector of parameters. This will be coerced internally

to storage mode double. optional; prior distribution sampler, specified either as a C snippet, an R funcrprior tion, or the name of a pre-compiled native routine available in a dynamically loaded library. For more information, see ?prior\_spec. Setting rprior=NULL removes the prior distribution sampler. rinit simulator of the initial-state distribution. This can be furnished either as a C snippet, an R function, or the name of a pre-compiled native routine available in a dynamically loaded library. Setting rinit=NULL sets the initial-state simulator to its default. For more information, see ?rinit\_spec. rprocess simulator of the latent state process, specified using one of the rprocess plugins. Setting rprocess=NULL removes the latent-state simulator. For more information, see ?rprocess\_spec for the documentation on these plugins. evaluator of the measurement model density, specified either as a C snippet, an dmeasure R function, or the name of a pre-compiled native routine available in a dynamically loaded library. Setting dmeasure=NULL removes the measurement density evaluator. For more information, see ?dmeasure\_spec. optional parameter transformations, constructed using parameter\_trans. partrans Many algorithms for parameter estimation search an unconstrained space of parameters. When working with such an algorithm and a model for which the parameters are constrained, it can be useful to transform parameters. One should supply the partrans argument via a call to parameter\_trans. For more information, see ?parameter trans. Setting partrans=NULL removes the parameter transformations, i.e., sets them to the identity transformation.

additional arguments supply new or modify existing model characteristics or components. See pomp for a full list of recognized arguments.

When named arguments not recognized by pomp are provided, these are made available to all basic components via the so-called userdata facility. This allows the user to pass information to the basic components outside of the usual routes of covariates (covar) and model parameters (params). See ?userdata for information on how to use this facility.

verbose logical; if TRUE, diagnostic messages will be printed to the console.

## **Details**

params

bsmc2 uses a version of the original algorithm (Liu \& West 2001), but discards the auxiliary particle filter. The modification appears to give superior performance for the same amount of effort.

Samples from the prior distribution are drawn using the rprior component. This is allowed to depend on elements of params, i.e., some of the elements of params can be treated as "hyperparameters". Np draws are made from the prior distribution.

## Value

An object of class 'bsmcd\_pomp'. The following methods are avaiable:

plot produces diagnostic plots

as.data.frame puts the prior and posterior samples into a data frame

bsplines 23

# Author(s)

Michael Lavine, Matthew Ferrari, Aaron A. King, Edward L. Ionides

# References

Liu, J. and M. West. Combining Parameter and State Estimation in Simulation-Based Filtering. In A. Doucet, N. de Freitas, and N. J. Gordon, editors, Sequential Monte Carlo Methods in Practice, pages 197-224. Springer, New York, 2001.

# See Also

```
Other particle filter methods: cond.logLik(), eff.sample.size(), filter.mean(), filter.traj(), mif2(), pfilter(), pmcmc(), pred.mean(), pred.var(), wpfilter()

Other pomp parameter estimation methods: abc(), kalman, mif2(), nlf, pmcmc(), pomp-package, probe.match, spect.match
```

bsplines

B-spline bases

# **Description**

These functions generate B-spline basis functions. bspline.basis gives a basis of spline functions. periodic.bspline.basis gives a basis of periodic spline functions.

# Usage

```
bspline.basis(x, nbasis, degree = 3, deriv = 0, names = NULL)

periodic.bspline.basis(
    x,
    nbasis,
    degree = 3,
    period = 1,
    deriv = 0,
    names = NULL
)
```

#### **Arguments**

Vector at which the spline functions are to be evaluated.
 The number of basis functions to return.
 Degree of requested B-splines.
 The order of the derivative required.

24 coef

names optional; the names to be given to the basis functions. These will be the column-

names of the matrix returned. If the names are specified as a format string (e.g., "basis%d"), sprintf will be used to generate the names from the column number. If a single non-format string is specified, the names will be generated by paste-ing name to the column number. One can also specify each column name explicitly by giving a length-nbasis string vector. By default, no column-

names are given.

period The period of the requested periodic B-splines.

#### Value

bspline.basis Returns a matrix with length(x) rows and nbasis columns. Each column

contains the values one of the spline basis functions.

periodic.bspline.basis

Returns a matrix with length(x) rows and nbasis columns. The basis functions returned are periodic with period period.

If deriv>0, the derivative of that order of each of the corresponding spline basis functions are returned.

#### C API

Access to the underlying C routines is available: see the **pomp** C API document. for definition and documentation of the C API.

# Author(s)

Aaron A. King

# **Examples**

```
x <- seq(0,2,by=0.01)
y <- bspline.basis(x,degree=3,nbasis=9,names="basis")
matplot(x,y,type='l',ylim=c(0,1.1))
lines(x,apply(y,1,sum),lwd=2)

x <- seq(-1,2,by=0.01)
y <- periodic.bspline.basis(x,nbasis=5,names="spline%d")
matplot(x,y,type='l')</pre>
```

coef

Extract, set, or alter coefficients

# Description

Extract, set, or modify the estimated parameters from a fitted model.

cond.logLik 25

# Usage

```
## S4 method for signature 'listie'
coef(object, ...)
## S4 method for signature 'pomp'
coef(object, pars, transform = FALSE, ...)
## S4 replacement method for signature 'pomp'
coef(object, pars, transform = FALSE, ...) <- value
## S4 method for signature 'objfun'
coef(object, ...)</pre>
```

# **Arguments**

object an object of class 'pomp', or of a class extending 'pomp'

... ignored

pars optional character; names of parameters to be retrieved or set.

transform logical; perform parameter transformation?

value numeric vector or list; values to be assigned. If value = NULL, the parameters

are unset.

#### **Details**

coef allows one to extract the parameters from a fitted model.

coef(object,transform=TRUE) returns the parameters transformed onto the estimation scale.

coef(object) <-value sets or alters the coefficients of a 'pomp' object.</pre>

coef(object,transform=TRUE) <-value assumes that value is on the estimation scale, and applies the "from estimation scale" parameter transformation from object before altering the coefficients.

cond.logLik

Conditional log likelihood

# **Description**

The estimated conditional log likelihood from a fitted model.

# Usage

```
## S4 method for signature 'kalmand_pomp'
cond.logLik(object, ...)
## S4 method for signature 'pfilterd_pomp'
cond.logLik(object, ...)
```

26 continue

```
## S4 method for signature 'wpfilterd_pomp'
cond.logLik(object, ...)
## S4 method for signature 'bsmcd_pomp'
cond.logLik(object, ...)
```

# **Arguments**

object result of a filtering computation

... ignored

#### **Details**

The conditional likelihood is defined to be the value of the density of

$$Y(t_k)|Y(t_1),...,Y(t_{k-1})$$

evaluated at  $Y(t_k) = y_k^*$ . Here,  $Y(t_k)$  is the observable process, and  $y_k^*$  the data, at time  $t_k$ .

Thus the conditional log likelihood at time  $t_k$  is

$$\ell_k(\theta) = \log f[Y(t_k) = y_k^* | Y(t_1) = y_1^*, \dots, Y(t_{k-1}) = y_{k-1}^*],$$

where f is the probability density above.

# Value

The numerical value of the conditional log likelihood. Note that some methods compute not the log likelihood itself but instead a related quantity. To keep the code simple, the cond.logLik function is nevertheless used to extract this quantity.

When object is of class 'bsmcd\_pomp' (i.e., the result of a bsmc2 computation), cond.logLik returns the conditional log "evidence" (see bsmc2).

# See Also

```
Other particle filter methods: bsmc2(), eff.sample.size(), filter.mean(), filter.traj(), mif2(), pfilter(), pmcmc(), pred.mean(), pred.var(), wpfilter()
```

continue

Continue an iterative calculation

# Description

Continue an iterative computation where it left off.

covariate\_table 27

# Usage

```
continue(object, ...)
## S4 method for signature 'abcd_pomp'
continue(object, Nabc = 1, ...)
## S4 method for signature 'pmcmcd_pomp'
continue(object, Nmcmc = 1, ...)
## S4 method for signature 'mif2d_pomp'
continue(object, Nmif = 1, ...)
```

# Arguments

the result of an iterative pomp computation
 additional arguments will be passed to the underlying method. This allows one to modify parameters used in the original computations.
 positive integer; number of additional ABC iterations to perform
 positive integer; number of additional PMCMC iterations to perform
 positive integer; number of additional filtering iterations to perform

#### See Also

mif2 pmcmc abc

# Description

Constructing lookup tables for time-varying covariates.

# Usage

```
## S4 method for signature 'numeric'
covariate_table(..., order = c("linear", "constant"), times)
## S4 method for signature 'character'
covariate_table(..., order = c("linear", "constant"), times)
```

28 covmat

## **Arguments**

... numeric vectors or data frames containing time-varying covariates. It must be

possible to bind these into a data frame.

order the order of interpolation to be used. Options are "linear" (the default) and

"constant". Setting order="linear" treats the covariates as piecewise linear functions of time; order="constant" treats them as right-continuous piecewise

constant functions.

times the times corresponding to the covariates. This may be given as a vector of (non-

decreasing, finite) numerical values. Alternatively, one can specify by name

which of the given variables is the time variable.

#### **Details**

If the 'pomp' object contains covariates (specified via the covar argument), then interpolated values of the covariates will be available to each of the model components whenever it is called. In particular, variables with names as they appear in the covar covariate table will be available to any C snippet. When a basic component is defined using an R function, that function will be called with an extra argument, covars, which will be a named numeric vector containing the interpolated values from the covariate table.

An exception to this rule is the prior (rprior and dprior): covariate-dependent priors are not allowed. Nor are parameter transformations permitted to depend upon covariates.

# See Also

lookup

Other information on model implementation: Csnippet, accumulators, distributions, dmeasure\_spec, dprocess\_spec, parameter\_trans(), pomp-package, prior\_spec, rinit\_spec, rmeasure\_spec, rprocess\_spec, skeleton\_spec, transformations, userdata

covmat

Estimate a covariance matrix from algorithm traces

# **Description**

A helper function to extract a covariance matrix.

# Usage

```
## S4 method for signature 'pmcmcd_pomp'
covmat(object, start = 1, thin = 1, expand = 2.38, ...)
## S4 method for signature 'pmcmcList'
covmat(object, start = 1, thin = 1, expand = 2.38, ...)
## S4 method for signature 'abcd_pomp'
covmat(object, start = 1, thin = 1, expand = 2.38, ...)
```

Csnippet 29

```
## S4 method for signature 'abcList'
covmat(object, start = 1, thin = 1, expand = 2.38, ...)
## S4 method for signature 'probed_pomp'
covmat(object, ...)
```

# **Arguments**

object an object extending 'pomp'

start the first iteration number to be used in estimating the covariance matrix. Setting

thin > 1 allows for a burn-in period.

thin factor by which the chains are to be thinned

expand the expansion factor

... ignored

#### Value

When object is the result of a pmcmc or abc computation, covmat(object) gives the covariance matrix of the chains. This can be useful, for example, in tuning the proposal distribution.

When object is a 'probed\_pomp' object (i.e., the result of a probe computation), covmat(object) returns the covariance matrix of the probes, as applied to simulated data.

# See Also

MCMC proposals.

Csnippet Csnippets

# **Description**

Accelerating computations through inline snippets of C code

# Usage

```
Csnippet(text)
```

# **Arguments**

text character; text written in the C language

#### **Details**

**pomp** provides a facility whereby users can define their model's components using inline C code. C snippets are written to a C file, by default located in the R session's temporary directory, which is then compiled (via R CMD SHLIB) into a dynamically loadable shared object file. This is then loaded as needed.

30 Csnippet

#### Note to Windows and Mac users

By default, your R installation may not support R CMD SHLIB. The package website contains installation instructions that explain how to enable this powerful feature of R.

## General rules for writing C snippets

In writing a C snippet one must bear in mind both the *goal* of the snippet, i.e., what computation it is intended to perform, and the *context* in which it will be executed. These are explained here in the form of general rules. Additional specific rules apply according to the function of the particular C snippet. Illustrative examples are given in the tutorials on the package website.

- C snippets must be valid C. They will embedded verbatim in a template file which will then be compiled by a call to R CMD SHLIB. If the resulting file does not compile, an error message will be generated. Compiler messages will be displayed, but no attempt will be made by **pomp** to interpret them. Typically, compilation errors are due to either invalid C syntax or undeclared variables.
- 2. State variables, parameters, observables, and covariates must be left undeclared within the snippet. State variables and parameters are declared via the statenames or paramnames arguments to pomp, respectively. Compiler errors that complain about undeclared state variables or parameters are usually due to failure to declare these in statenames or paramnames, as appropriate.
- 3. A C snippet can declare local variables. Be careful not to use names that match those of state variables, observables, or parameters. One must never declare state variables, observables, covariates, or parameters within a C snippet.
- 4. Names of observables must match the names given given in the data. They must be referred to in measurement model C snippets (rmeasure and dmeasure) by those names.
- 5. If the 'pomp' object contains a table of covariates (see above), then the variables in the covariate table will be available, by their names, in the context within which the C snippet is executed.
- 6. Because the dot '.' has syntactic meaning in C, R variables with names containing dots ('.') are replaced in the C codes by variable names in which all dots have been replaced by underscores ('\_').
- 7. The headers 'R.h' and 'Rmath.h', provided with R, will be included in the generated C file, making all of the R C API available for use in the C snippet. This makes a great many useful functions available, including all of R's statistical distribution functions.
- 8. The header 'pomp.h', provided with **pomp**, will also be included, making all of the **pomp** C API available for use in every C snippet.
- 9. Snippets of C code passed to the globals argument of pomp will be included at the head of the generated C file. This can be used to declare global variables, define useful functions, and include arbitrary header files.
- 10. INCLUDE INFORMATION ABOUT LINKING TO PRECOMPILED LIBRARIES!

# See Also

Other information on model implementation: accumulators, covariate\_table(), distributions, dmeasure\_spec, dprocess\_spec, parameter\_trans(), pomp-package, prior\_spec, rinit\_spec, rmeasure\_spec, rprocess\_spec, skeleton\_spec, transformations, userdata

dacca 31

dacca

Model of cholera transmission for historic Bengal.

# Description

dacca constructs a 'pomp' object containing census and cholera mortality data from the Dacca district of the former British province of Bengal over the years 1891 to 1940 together with a stochastic differential equation transmission model. The model is that of King et al. (2008). The parameters are the MLE for the SIRS model with seasonal reservoir.

# Usage

```
dacca(
  gamma = 20.8,
  eps = 19.1,
  rho = 0,
  delta = 0.02,
  deltaI = 0.06,
  clin = 1,
  alpha = 1,
  beta_trend = -0.00498,
  logbeta = c(0.747, 6.38, -3.44, 4.23, 3.33, 4.55),
  logomega = log(c(0.184, 0.0786, 0.0584, 0.00917, 0.000208, 0.0124)),
  sd_beta = 3.13,
  tau = 0.23,
  S_0 = 0.621
  I_0 = 0.378,
  Y_0 = 0,
 R1_0 = 0.000843,
 R2_0 = 0.000972,
 R3_0 = 1.16e-07
```

# **Arguments**

gamma	recovery rate
eps	rate of waning of immunity for severe infections
rho	rate of waning of immunity for inapparent infections
delta	baseline mortality rate
deltaI	cholera mortality rate
clin	fraction of infections that lead to severe infection
alpha	transmission function exponent
beta_trend	slope of secular trend in transmission
logbeta	seasonal transmission rates

32 dacca

logomega	seasonal environmental reservoir parameters
sd_beta	environmental noise intensity
tau	measurement error s.d.
S_0	initial susceptible fraction
I_0	initial fraction of population infected
Y_0	initial fraction of the population in the Y class
R1_0, R2_0, R3_0	)
	initial fractions in the respective R classes

# **Details**

Data are provided courtesy of Dr. Menno J. Bouma, London School of Tropical Medicine and Hygiene.

# Value

dacca returns a 'pomp' object containing the model, data, and MLE parameters, as estimated by King et al. (2008).

# References

A.A. King, E.L. Ionides, M. Pascual, and M.J. Bouma. Inapparent infections and cholera dynamics. *Nature* **454**, 877-880, 2008

# See Also

```
Other pomp examples: blowflies, bsflu, ebola, gompertz(), measles, ou2(), parus, pomp_examples, ricker(), rw2(), sir_models, verhulst()

Other datasets: blowflies, bsflu, ebola, measles, parus
```

# **Examples**

```
po <- dacca()
plot(po)
## MLE:
coef(po)
plot(simulate(po))</pre>
```

design 33

design

Design matrices for pomp calculations

# **Description**

These functions are useful for generating designs for the exploration of parameter space.

profileDesign generates a data-frame where each row can be used as the starting point for a profile likelihood calculation.

runifDesign generates a design based on random samples from a multivariate uniform distribution. sliceDesign generates points along slices through a specified point.

sobolDesign generates a Latin hypercube design based on the Sobol' low-discrepancy sequence.

# Usage

```
profileDesign(
    ...,
    lower,
    upper,
    nprof,
    type = c("sobol", "runif"),
    stringsAsFactors = getOption("stringsAsFactors", FALSE)
)

runifDesign(lower = numeric(0), upper = numeric(0), nseq)
sliceDesign(center, ...)
sobolDesign(lower = numeric(0), upper = numeric(0), nseq)
```

# Arguments

... In profileDesign, additional arguments specify the parameters over which to

profile and the values of these parameters. In sliceDesign, additional numeric

vector arguments specify the locations of points along the slices.

lower, upper named numeric vectors giving the lower and upper bounds of the ranges, respec-

tively.

nprof The number of points per profile point.

type the type of design to use. type="sobol" uses sobolDesign; type="runif"

uses runifDesign.

stringsAsFactors

should character vectors be converted to factors?

nseq Total number of points requested.

center center is a named numeric vector specifying the point through which the slice(s)

is (are) to be taken.

34 design

#### **Details**

The Sobol' sequence generation is performed using codes from the **NLopt** library by S. Johnson.

#### Value

profileDesign returns a data frame with nprof points per profile point.

runifDesign returns a data frame with nseq rows and one column for each variable named in lower and upper.

sliceDesign returns a data frame with one row per point. The 'slice' variable indicates which slice the point belongs to.

sobolDesign returns a data frame with nseq rows and one column for each variable named in lower and upper.

# Author(s)

Aaron A. King

#### References

- P. Bratley and B.L. Fox. Algorithm 659 Implementing Sobol's quasirandom sequence generator. *ACM Transactions on Mathematical Software* **14**, 88–100, 1988.
- S. Joe and F.Y. Kuo. Remark on algorithm 659: Implementing Sobol' quasirandom sequence generator. *ACM Transactions on Mathematical Software* **29**, 49–57, 2003.
- S.G. Johnson. The **NLopt** nonlinear-optimization package. http://ab-initio.mit.edu/nlopt.

# **Examples**

```
## Sobol' low-discrepancy design
plot(sobolDesign(lower=c(a=0,b=100),upper=c(b=200,a=1),nseq=100))
## Uniform random design
plot(runifDesign(lower=c(a=0,b=100),upper=c(b=200,a=1),100))
## A one-parameter profile design:
x \leftarrow profileDesign(p=1:10,lower=c(a=0,b=0),upper=c(a=1,b=5),nprof=20)
dim(x)
plot(x)
## A two-parameter profile design:
x \leftarrow profileDesign(p=1:10,q=3:5,lower=c(a=0,b=0),upper=c(b=5,a=1),nprof=200)
dim(x)
plot(x)
## A two-parameter profile design with random points:
x < -profileDesign(p=1:10,q=3:5,lower=c(a=0,b=0),upper=c(b=5,a=1),nprof=200,type="runif")
dim(x)
plot(x)
## A single 11-point slice through the point c(A=3,B=8,C=0) along the B direction.
```

distributions 35

```
x <- sliceDesign(center=c(A=3,B=8,C=0),B=seq(0,10,by=1))  
    dim(x)  
    plot(x)  

## Two slices through the same point along the A and C directions.  
    x <- sliceDesign(c(A=3,B=8,C=0),A=seq(0,5,by=1),C=seq(0,5,length=11))  
    dim(x)  
    plot(x)
```

distributions

Probability distributions

# **Description**

**pomp** provides a number of probability distributions that have proved useful in modeling partially observed Markov processes. These include the Euler-multinomial family of distributions and the the Gamma white-noise processes.

# Usage

```
reulermultinom(n = 1, size, rate, dt)
deulermultinom(x, size, rate, dt, log = FALSE)
rgammawn(n = 1, sigma, dt)
```

# Arguments

n	integer; number of random variates to generate.
size	scalar integer; number of individuals at risk.
rate	numeric vector of hazard rates.
dt	numeric scalar; duration of Euler step.
X	matrix or vector containing number of individuals that have succumbed to each death process.
log	logical; if TRUE, return logarithm(s) of probabilities.
sigma	numeric scalar; intensity of the Gamma white noise process.

## **Details**

If N individuals face constant hazards of death in k ways at rates  $r_1, r_2, \ldots, r_k$ , then in an interval of duration  $\Delta t$ , the number of individuals remaining alive and dying in each way is multinomially distributed:

$$(N - \sum_{i=1}^{k} \Delta n_i, \Delta n_1, \dots, \Delta n_k) \sim \text{Multinomial}(N; p_0, p_1, \dots, p_k),$$

36 distributions

where  $\Delta n_i$  is the number of individuals dying in way i over the interval, the probability of remaining alive is  $p_0 = \exp(-\sum_i r_i \Delta t)$ , and the probability of dying in way j is

$$p_j = \frac{r_j}{\sum_i r_i} (1 - \exp(-\sum_i r_i \Delta t)).$$

In this case, we say that

$$(\Delta n_1, \ldots, \Delta n_k) \sim \text{Eulermultinom}(N, r, \Delta t),$$

where  $r = (r_1, \ldots, r_k)$ . Draw m random samples from this distribution by doing

where r is the vector of rates. Evaluate the probability that  $x = (x_1, \dots, x_k)$  are the numbers of individuals who have died in each of the k ways over the interval  $\Delta t = dt$ , by doing

```
deulermultinom(x=x,size=N,rate=r,dt=dt).
```

Breto & Ionides (2011) discuss how an infinitesimally overdispersed death process can be constructed by compounding a multinomial process with a Gamma white noise process. The Euler approximation of the resulting process can be obtained as follows. Let the increments of the equidispersed process be given by

```
reulermultinom(size=N,rate=r,dt=dt).
```

In this expression, replace the rate r with  $r\Delta W/\Delta t$ , where  $\Delta W \sim \mathrm{Gamma}(\Delta t/\sigma^2, \sigma^2)$  is the increment of an integrated Gamma white noise process with intensity  $\sigma$ . That is,  $\Delta W$  has mean  $\Delta t$  and variance  $\sigma^2 \Delta t$ . The resulting process is overdispersed and converges (as  $\Delta t$  goes to zero) to a well-defined process. The following lines of code accomplish this:

```
dW <- rgammawn(sigma=sigma,dt=dt)</pre>
```

dn <- reulermultinom(size=N,rate=r,dt=dW)</pre>

or

```
dn <- reulermultinom(size=N,rate=r*dW/dt,dt=dt).</pre>
```

He et al. (2010) use such overdispersed death processes in modeling measles.

For all of the functions described here, access to the underlying C routines is available: see below.

# Value

reulermultinom Returns a length(rate) by n matrix. Each column is a different random draw.

Each row contains the numbers of individuals that have succumbed to the corre-

sponding process.

deulermultinom Returns a vector (of length equal to the number of columns of x) containing

the probabilities of observing each column of x given the specified parameters

(size, rate, dt).

rgammawn Returns a vector of length n containing random increments of the integrated

Gamma white noise process with intensity sigma.

dmeasure 37

## C API

An interface for C codes using these functions is provided by the package. Visit the package homepage to view the **pomp C** API document.

#### Author(s)

Aaron A. King

### References

C. Bretó and E. L. Ionides. Compound Markov counting processe and their applications to modeling infinitesimally over-dispersed systems. *Stochastic Processes and their Applications* **121**, 2571–2591, 2011.

D. He, E.L. Ionides, & A.A. King. Plug-and-play inference for disease dynamics: measles in large and small populations as a case study. *Journal of the Royal Society Interface* 7, 271–283, 2010.

#### See Also

Other information on model implementation: Csnippet, accumulators, covariate\_table(), dmeasure\_spec, dprocess\_spec, parameter\_trans(), pomp-package, prior\_spec, rinit\_spec, rmeasure\_spec, rprocess\_spec, skeleton\_spec, transformations, userdata

# **Examples**

```
print(dn <- reulermultinom(5,size=100,rate=c(a=1,b=2,c=3),dt=0.1))
deulermultinom(x=dn,size=100,rate=c(1,2,3),dt=0.1)
## an Euler-multinomial with overdispersed transitions:
dt <- 0.1
dW <- rgammawn(sigma=0.1,dt=dt)
print(dn <- reulermultinom(5,size=100,rate=c(a=1,b=2,c=3),dt=dW))</pre>
```

dmeasure

dmeasure

## **Description**

dmeasure evaluates the probability density of observations given states.

# Usage

```
## S4 method for signature 'pomp'
dmeasure(object, y, x, times, params, ..., log = FALSE)
```

38 dmeasure\_spec

## **Arguments**

object	an object of class 'pomp', or of a class that extends 'pomp'. This will typically be the output of pomp, simulate, or one of the <b>pomp</b> inference algorithms.
У	a matrix containing observations. The dimensions of $y$ are nobs $x$ ntimes, where nobs is the number of observables and ntimes is the length of times.
х	an array containing states of the unobserved process. The dimensions of x are nvars x nrep x ntimes, where nvars is the number of state variables, nrep is the number of replicates, and ntimes is the length of times. One can also pass x as a named numeric vector, which is equivalent to the nrep=1, ntimes=1 case.
times	a numeric vector (length ntimes) containing times. These must be in non-decreasing order.
params	a npar x nrep matrix of parameters. Each column is treated as an independent parameter set, in correspondence with the corresponding column of x.
	additional arguments are ignored.
log	if TRUE, log probabilities are returned.

#### Value

dmeasure returns a matrix of dimensions nreps x ntimes. If d is the returned matrix, d[j,k] is the likelihood (or log likelihood if log = TRUE) of the observation y[,k] at time times[k] given the state x[,j,k].

## See Also

Specification of the measurement density evaluator: dmeasure\_spec

Other pomp workhorses: dprior(), dprocess(), flow(), partrans(), rinit(), rmeasure(), rprior(), rprocess(), skeleton(), workhorses

dmeasure\_spec

The measurement model density

## Description

Specification of dmeasure.

## **Details**

The measurement model is the link between the data and the unobserved state process. It can be specified either by using one or both of the rmeasure and dmeasure arguments.

Suppose you have a procedure to compute the probability density of an observation given the value of the latent state variables. Then you can furnish

dmeasure = f

dprior 39

to **pomp** algorithms, where f is a C snippet or R function that implements your procedure.

Using a C snippet is much preferred, due to its much greater computational efficiency. See Csnippet for general rules on writing C snippets. The goal of a *dmeasure* C snippet is to fill the variable lik with the either the probability density or the log probability density, depending on the value of the variable give\_log.

In writing a dmeasure C snippet, observe that:

- In addition to the states, parameters, covariates (if any), and observables, the variable t, containing the time of the observation will be defined in the context in which the snippet is executed.
- 2. Moreover, the Boolean variable give\_log will be defined.
- 3. The goal of a dmeasure C snippet is to set the value of the lik variable to the likelihood of the data given the state, if give\_log == 0. If give\_log == 1, lik should be set to the log likelihood.

If dmeasure is to be provided instead as an R function, this is accomplished by supplying

```
dmeasure = f
```

to pomp, where f is a function. The arguments of f should be chosen from among the observables, state variables, parameters, covariates, and time. It must also have the arguments ..., and log. It can take additional arguments via the facility. f must return a single numeric value, the probability density (or log probability density if log = TRUE) of y given x at time t.

### Important note

It is a common error to fail to account for both log = TRUE and log = FALSE when writing the dmeasure C snippet or function.

#### **Default behavior**

If dmeasure is left unspecified, calls to dmeasure will return missing values (NA).

#### See Also

Other information on model implementation: Csnippet, accumulators, covariate\_table(), distributions, dprocess\_spec, parameter\_trans(), pomp-package, prior\_spec, rinit\_spec, rmeasure\_spec, rprocess\_spec, skeleton\_spec, transformations, userdata

## **Description**

Evaluates the prior probability density.

40 dprocess

## Usage

```
## S4 method for signature 'pomp'
dprior(object, params, ..., log = FALSE)
```

## Arguments

object an object of class 'pomp', or of a class that extends 'pomp'. This will typically be the output of pomp, simulate, or one of the **pomp** inference algorithms.

params a npar x nrep matrix of parameters. Each column is treated as an independent parameter set, in correspondence with the corresponding column of x.

additional arguments are ignored.

log if TRUE, log probabilities are returned.

#### Value

The required density (or log density), as a numeric vector.

### See Also

```
Specification of the prior density evaluator: prior_spec

Other pomp workhorses: dmeasure(), dprocess(), flow(), partrans(), rinit(), rmeasure(), rprior(), rprocess(), skeleton(), workhorses
```

dprocess dprocess

## **Description**

Evaluates the probability density of a sequence of consecutive state transitions.

# Usage

```
## S4 method for signature 'pomp'
dprocess(object, x, times, params, ..., log = FALSE)
```

## **Arguments**

object	an object of class 'pomp', or of a class that extends 'pomp'. This will typically be the output of pomp, simulate, or one of the <b>pomp</b> inference algorithms.
Х	an array containing states of the unobserved process. The dimensions of x are nvars x nrep x ntimes, where nvars is the number of state variables, nrep is the number of replicates, and ntimes is the length of times. One can also pass x as a named numeric vector, which is equivalent to the nrep=1, ntimes=1 case.
times	a numeric vector (length ntimes) containing times. These must be in non-decreasing order.

dprocess\_spec 41

params	a npar x nrep matrix of parameters. Each column is treated as an independent parameter set, in correspondence with the corresponding column of x.
	additional arguments are ignored.
log	if TRUE, log probabilities are returned.

#### Value

dprocess returns a matrix of dimensions nrep x ntimes-1. If d is the returned matrix, d[j,k] is the likelihood (or the log likelihood if log=TRUE) of the transition from state x[,j,k-1] at time times[k-1] to state x[,j,k] at time times[k].

### See Also

Specification of the process-model density evaluator: dprocess\_spec

Other pomp workhorses: dmeasure(), dprior(), flow(), partrans(), rinit(), rmeasure(), rprior(), rprocess(), skeleton(), workhorses

dprocess\_spec The la

The latent state process density

### **Description**

Specification of dprocess.

## **Details**

Suppose you have a procedure that allows you to compute the probability density of an arbitrary transition from state  $x_1$  at time  $t_1$  to state  $x_2$  at time  $t_2 > t_1$  under the assumption that the state remains unchanged between  $t_1$  and  $t_2$ . Then you can furnish

```
dprocess = f
```

to pomp, where f is a C snippet or R function that implements your procedure. Specifically, f should compute the *log* probability density.

Using a C snippet is much preferred, due to its much greater computational efficiency. See Csnippet for general rules on writing C snippets. The goal of a *dprocess* C snippet is to fill the variable loglik with the log probability density. In the context of such a C snippet, the parameters, and covariates will be defined, as will the times t\_1 and t\_2. The state variables at time t\_1 will have their usual name (see statenames) with a "\_1" appended. Likewise, the state variables at time t\_2 will have a "\_2" appended.

If f is given as an R function, it should take as arguments any or all of the state variables, parameter, covariates, and time. The state-variable and time arguments will have suffices "\_1" and "\_2" appended. Thus for example, if var is a state variable, when f is called, var\_1 will value of state variable var at time t\_1, var\_2 will have the value of var at time t\_2. f should return the *log* likelihood of a transition from x1 at time t1 to x2 at time t2, assuming that no intervening transitions have occurred.

To see examples, consult the demos and the tutorials on the package website.

42 ebola

## Note

It is not typically necessary (or even feasible) to define dprocess. In fact, no current **pomp** inference algorithm makes use of dprocess. This functionality is provided only to support future algorithm development.

#### **Default behavior**

By default, dprocess returns missing values (NA).

#### See Also

Other information on model implementation: Csnippet, accumulators, covariate\_table(), distributions, dmeasure\_spec, parameter\_trans(), pomp-package, prior\_spec, rinit\_spec, rmeasure\_spec, rprocess\_spec, skeleton\_spec, transformations, userdata

ebola

Ebola outbreak, West Africa, 2014-2016

## **Description**

Data and models for the 2014–2016 outbreak of Ebola virus disease in West Africa.

## Usage

```
ebolaModel(
    country = c("GIN", "LBR", "SLE"),
    data = NULL,
    timestep = 1/8,
    nstageE = 3L,
    R0 = 1.4,
    rho = 0.2,
    cfr = 0.7,
    k = 0,
    index_case = 10,
    incubation_period = 11.4,
    infectious_period = 7
)
```

## **Arguments**

country	ISO symbol for the country (GIN=Guinea, LBR=Liberia, SLE=Sierra Leone).
data	if NULL, the situation report data (see ebolaWHO) for the appropriate country or region will be used. Providing a dataset here will override this behavior.
timestep	duration (in days) of Euler time-step for the simulations.
nstageE	integer; number of incubation stages.
R0	basic reproduction ratio

ebola 43

rho case reporting efficiency

cfr case fatality rate

k dispersion parameter (negative binomial size parameter)

index\_case number of cases on day 0 (2014-04-01)

incubation\_period, infectious\_period

mean duration (in days) of the incubation and infectious periods.

#### **Details**

The data include monthly case counts and death reports derived from WHO situation reports, as reported by the U.S. CDC. The models are described in King et al. (2015).

The data-cleaning script is included in the R source code file 'ebola.R'.

#### Model structure

The default incubation period is supposed to be Gamma distributed with shape parameter nstageE and mean 11.4 days and the case-fatality ratio ('cfr') is taken to be 0.7 (cf. WHO Ebola Response Team 2014). The discrete-time formula is used to calculate the corresponding alpha (cf. He et al. 2010).

The observation model is a hierarchical model for cases and deaths:

$$p(R_t, D_t|C_t) = p(R_t|C_t)p(D_t|C_t, R_t).$$

Here,  $p(R_t|C_t)$  is negative binomial with mean  $\rho C_t$  and dispersion parameter 1/k;  $p(D_t|C_t,R_t)$  is binomial with size  $R_t$  and probability equal to the case fatality rate cfr.

#### References

A.A. King, M. Domenech de Cellès, F.M.G. Magpantay, and P. Rohani. Avoidable errors in the modelling of outbreaks of emerging pathogens, with special reference to Ebola. *Proceedings of the Royal Society of London, Series B* **282**, 20150347, 2015.

WHO Ebola Response Team. Ebola virus disease in West Africa—the first 9 months of the epidemic and forward projections. *New England Journal of Medicine* **371**, 1481–1495, 2014.

D. He, E.L. Ionides, & A.A. King. Plug-and-play inference for disease dynamics: measles in large and small populations as a case study. *Journal of the Royal Society Interface* 7, 271–283, 2010.

#### See Also

Other datasets: blowflies, bsflu, dacca(), measles, parus

Other pomp examples: blowflies, bsflu, dacca(), gompertz(), measles, ou2(), parus, pomp\_examples, ricker(), rw2(), sir\_models, verhulst()

eff.sample.size

### **Examples**

```
data(ebolaWA2014)
library(ggplot2)
library(tidyr)
ebolaWA2014 %>%
  gather(variable,count,cases,deaths) %>%
  ggplot(aes(x=date,y=count,group=country,color=country))+
  geom_line()+
  facet_grid(variable~.,scales="free_y")+
  theme_bw()+
  theme(axis.text=element_text(angle=-90))
ebolaWA2014 %>%
  gather(variable,count,cases,deaths) %>%
  ggplot(aes(x=date,y=count,group=variable,color=variable))+
  geom_line()+
  facet_grid(country~.,scales="free_y")+
  theme_bw()+
  theme(axis.text=element_text(angle=-90))
plot(ebolaModel(country="SLE"))
plot(ebolaModel(country="LBR"))
plot(ebolaModel(country="GIN"))
```

eff.sample.size

Effective sample size

## Description

Estimate the effective sample size of a Monte Carlo computation.

# Usage

```
## S4 method for signature 'bsmcd_pomp'
eff.sample.size(object, ...)
## S4 method for signature 'pfilterd_pomp'
eff.sample.size(object, ...)
## S4 method for signature 'wpfilterd_pomp'
eff.sample.size(object, ...)
```

# Arguments

object result of a filtering computation ... ignored

filter.mean 45

### **Details**

Effective sample size is computed as

$$\left(\sum_{i} w_{it}^{2}\right)^{-1}$$

where  $w_{it}$  is the normalized weight of particle i at time t.

### See Also

```
Other particle filter methods: bsmc2(), cond.logLik(), filter.mean(), filter.traj(), mif2(), pfilter(), pmcmc(), pred.mean(), pred.var(), wpfilter()
```

filter.mean

Filtering mean

# Description

The mean of the filtering distribution

## Usage

```
## S4 method for signature 'kalmand_pomp'
filter.mean(object, vars, ...)
## S4 method for signature 'pfilterd_pomp'
filter.mean(object, vars, ...)
```

## Arguments

object result of a filtering computation
vars optional character; names of variables
... ignored

### **Details**

The filtering distribution is that of

$$X(t_k)|Y(t_1) = y_1^*, \dots, Y(t_k) = y_k^*,$$

where  $X(t_k)$ ,  $Y(t_k)$  are the latent state and observable processes, respectively, and  $y_t^*$  is the data, at time  $t_k$ .

The filtering mean is therefore the expectation of this distribution

$$E[X(t_k)|Y(t_1) = y_1^*, \dots, Y(t_k) = y_k^*].$$

```
Other particle filter methods: bsmc2(), cond.logLik(), eff.sample.size(), filter.traj(), mif2(), pfilter(), pmcmc(), pred.mean(), pred.var(), wpfilter()
```

46 filter.traj

filter.traj

Filtering trajectories

#### Description

Drawing from the smoothing distribution

## Usage

```
## S4 method for signature 'pfilterd_pomp'
filter.traj(object, vars, ...)
## S4 method for signature 'pfilterList'
filter.traj(object, vars, ...)
## S4 method for signature 'pmcmcd_pomp'
filter.traj(object, vars, ...)
## S4 method for signature 'pmcmcList'
filter.traj(object, vars, ...)
```

## **Arguments**

object result of a filtering computation
vars optional character; names of variables
... ignored

#### **Details**

The smoothing distribution is the distribution of

$$X(t_k)|Y(t_1) = y_1^*, \dots, Y(t_n) = y_n^*,$$

where  $X(t_k)$  is the latent state process and  $Y(t_k)$  is the observable process at time  $t_k$ , and n is the number of observations.

To draw samples from this distribution, one can run a number of independent particle filter (pfilter) operations, sampling the full trajectory of *one* randomly-drawn particle from each one. One should view these as *weighted* samples from the smoothing distribution, where the weights are the *likelihoods* returned by each of the pfilter computations.

One accomplishes this by setting filter.traj = TRUE in each pfilter computation and extracting the trajectory using the filter.traj command.

In particle MCMC (pmcmc), the tracking of an individual trajectory is performed automatically.

```
Other particle filter methods: bsmc2(), cond.logLik(), eff.sample.size(), filter.mean(), mif2(), pfilter(), pmcmc(), pred.mean(), pred.var(), wpfilter()
```

flow 47

flow	Flow of a deterministic model	

## Description

Compute the flow induced by a deterministic vectorfield or map.

## Usage

```
## S4 method for signature 'pomp'
flow(object, x0, t0, times, params, ..., verbose = getOption("verbose", FALSE))
```

## Arguments

object	an object of class 'pomp', or of a class that extends 'pomp'. This will typically be the output of pomp, simulate, or one of the <b>pomp</b> inference algorithms.
x0	an array with dimensions nvar x nrep giving the initial conditions of the trajectories to be computed.
t0	the time at which the initial conditions are assumed to hold.
times	a numeric vector (length ntimes) containing times at which the itineraries are desired. These must be in non-decreasing order with times[1]>t0.
params	a npar $x$ nrep matrix of parameters. Each column is treated as an independent parameter set, in correspondence with the corresponding column of $x$ .
	Additional arguments are passed to the ODE integrator (if the skeleton is a vectorfield) and are ignored if it is a map. See ode for a description of the additional arguments accepted by the ODE integrator.
verbose	logical; if TRUE, diagnostic messages will be printed to the console.

## **Details**

In the case of a discrete-time system (map), flow iterates the map to yield trajectories of the system. In the case of a continuous-time system (vectorfield), flow uses the numerical solvers in **deSolve** to integrate the vectorfield starting from given initial conditions.

# Value

flow returns an array of dimensions nvar x nrep x ntimes. If x is the returned matrix, x[i,j,k] is the i-th component of the state vector at time times[k] given parameters params[,j].

```
skeleton, trajectory, rprocess
Other pomp workhorses: dmeasure(), dprior(), dprocess(), partrans(), rinit(), rmeasure(),
rprior(), rprocess(), skeleton(), workhorses
```

48 gompertz

forecast

Forecast mean

## **Description**

Mean of the one-step-ahead forecasting distribution.

# Usage

```
forecast(object, ...)
## S4 method for signature 'kalmand_pomp'
forecast(object, vars, ...)
```

# Arguments

object result of a filtering computation
... ignored
vars optional character; names of variables

gompertz

Gompertz model with log-normal observations.

## **Description**

gompertz() constructs a 'pomp' object encoding a stochastic Gompertz population model with log-normal measurement error.

# Usage

```
gompertz(
  K = 1,
  r = 0.1,
  sigma = 0.1,
  tau = 0.1,
  X_0 = 1,
  times = 1:100,
  t0 = 0
)
```

hitch 49

## Arguments

K	carrying capacity
r	growth rate
sigma	process noise intensity
tau	measurement error s.d.
X_0	value of the latent state variable X at the zero time
times	observation times
t0	zero time

#### **Details**

The state process is  $X_{t+1} = K^{1-S} X_t^S \epsilon_t$ , where  $S = e^{-r}$  and the  $\epsilon_t$  are i.i.d. lognormal random deviates with variance  $\sigma^2$ . The observed variables  $Y_t$  are distributed as  $\log (X_t, \tau)$ . Parameters include the per-capita growth rate r, the carrying capacity K, the process noise s.d.  $\sigma$ , the measurement error s.d.  $\tau$ , and the initial condition  $X_0$ . The 'pomp' object includes parameter transformations that  $\log T$  transform the parameters for estimation purposes.

### Value

A 'pomp' object with simulated data.

#### See Also

```
Other pomp examples: blowflies, bsflu, dacca(), ebola, measles, ou2(), parus, pomp_examples, ricker(), rw2(), sir_models, verhulst()
```

### **Examples**

```
plot(gompertz())
plot(gompertz(K=2,r=0.01))
```

hitch

Hitching C snippets and R functions to pomp\_fun objects

## Description

The algorithms in **pomp** are formulated in terms of elementary functions that access the basic model components (rprocess, dprocess, rmeasure, dmeasure, etc.). For short, we refer to these elementary functions as "workhorses". In implementing a model, the user specifies basic model components using functions, procedures in dynamically-linked libraries, or C snippets. Each component is then packaged into a 'pomp\_fun' objects, which gives a uniform interface. The construction of 'pomp\_fun' objects is handled by the hitch function, which conceptually "hitches" the workhorses to the user-defined procedures.

50 hitch

## Usage

```
hitch(
    ...,
    templates,
    obsnames,
    statenames,
    paramnames,
    covarnames,
    PACKAGE,
    globals,
    cfile,
    cdir = getOption("pomp_cdir", NULL),
    shlib.args,
    compile = TRUE,
    verbose = getOption("verbose", FALSE)
)
```

#### **Arguments**

. . .

named arguments representing the user procedures to be hitched. These can be functions, character strings naming routines in external, dynamically-linked libraries, C snippets, or NULL. The first three are converted by hitch to 'pomp\_fun' objects which perform the indicated computations. NULL arguments are translated to default 'pomp\_fun' objects. If any of these procedures are already 'pomp\_fun' objects, they are returned unchanged.

templates

named list of templates. Each workhorse must have a corresponding template. See pomp:::workhorse\_templates for a list.

obsnames, statenames, paramnames, covarnames

character vectors specifying the names of observable variables, latent state variables, parameters, and covariates, respectively. These are only needed if one or more of the horses are furnished as C snippets.

PACKAGE

optional character; the name (without extension) of the external, dynamically loaded library in which any native routines are to be found. This is only useful if one or more of the model components has been specified using a precompiled dynamically loaded library; it is not used for any component specified using C snippets. PACKAGE can name at most one library.

globals

optional character; arbitrary C code that will be hard-coded into the shared-object library created when C snippets are provided. If no C snippets are used, globals has no effect.

cfile

optional character variable. cfile gives the name of the file (in directory cdir) into which C snippet codes will be written. By default, a random filename is used. If the chosen filename would result in over-writing an existing file, an error is generated.

cdir

optional character variable. cdir specifies the name of the directory within which C snippet code will be compiled. By default, this is in a temporary directory specific to the R session. One can also set this directory using the pomp\_cdir option.

kalman 51

shlib.args	optional character variables. Command-line arguments to the R CMD SHLIB call that compiles the C snippets.
compile	logical; if FALSE, compilation of the C snippets will be postponed until they are needed.
verbose	logical. Setting verbose=TRUE will cause additional information to be displayed.

### Value

hitch returns a named list of length two. The element named "funs" is itself a named list of 'pomp\_fun' objects, each of which corresponds to one of the horses passed in. The element named "lib" contains information on the shared-object library created using the C snippets (if any were passed to hitch). If no C snippets were passed to hitch, lib is NULL. Otherwise, it is a length-3 named list with the following elements:

**name** The name of the library created.

**dir** The directory in which the library was created. If this is NULL, the library was created in the session's temporary directory.

**src** A character string with the full contents of the C snippet file.

### Author(s)

Aaron A. King

### See Also

```
pomp, spy
```

kalman

Ensemble Kalman filters

# Description

The ensemble Kalman filter and ensemble adjustment Kalman filter.

## Usage

```
## $4 method for signature 'data.frame'
enkf(
   data,
   Np,
   h,
   R,
   params,
   rinit,
   rprocess,
   ...,
```

52 kalman

```
verbose = getOption("verbose", FALSE)
)
## S4 method for signature 'pomp'
enkf(data, Np, h, R, ..., verbose = getOption("verbose", FALSE))
## S4 method for signature 'data.frame'
eakf(
  data.
 Np,
  С,
 R,
  params,
  rinit,
  rprocess,
  verbose = getOption("verbose", FALSE)
)
## S4 method for signature 'pomp'
eakf(data, Np, C, R, ..., verbose = getOption("verbose", FALSE))
```

#### **Arguments**

data either a data frame holding the time series data, or an object of class 'pomp',

i.e., the output of another **pomp** calculation.

Np the number of particles to use.

h function returning the expected value of the observation given the state.

R matrix; variance of the measurement noise.

params optional; named numeric vector of parameters. This will be coerced internally

to storage mode double.

rinit simulator of the initial-state distribution. This can be furnished either as a C

snippet, an R function, or the name of a pre-compiled native routine available in a dynamically loaded library. Setting rinit=NULL sets the initial-state simulator

to its default. For more information, see ?rinit\_spec.

rprocess simulator of the latent state process, specified using one of the rprocess plugins.

Setting rprocess=NULL removes the latent-state simulator. For more informa-

tion, see ?rprocess\_spec for the documentation on these plugins.

.. additional arguments supply new or modify existing model characteristics or

components. See pomp for a full list of recognized arguments.

When named arguments not recognized by pomp are provided, these are made available to all basic components via the so-called *userdata* facility. This allows the user to pass information to the basic components outside of the usual routes of covariates (covar) and model parameters (params). See ?userdata for

information on how to use this facility.

verbose logical; if TRUE, diagnostic messages will be printed to the console.

C matrix converting state vector into expected value of the observation.

logLik 53

### Value

An object of class 'kalmand\_pomp'.

#### Author(s)

Aaron A. King

#### References

- G. Evensen. Sequential data assimilation with a nonlinear quasi-geostrophic model using Monte Carlo methods to forecast error statistics. *Journal of Geophysical Research: Oceans* **99**, 10143–10162, 1994.
- J.L. Anderson. An Ensemble Adjustment Kalman Filter for Data Assimilation. *Monthly Weather Review* **129**, 2884–2903, 2001.
- G. Evensen. Data assimilation: the ensemble Kalman filter. Springer-Verlag, 2009.

#### See Also

Other pomp parameter estimation methods: abc(), bsmc2(), mif2(), nlf, pmcmc(), pomp-package, probe.match, spect.match

logLik

Log likelihood

## **Description**

Extract the estimated log likelihood (or related quantity) from a fitted model.

## Usage

```
logLik(object, ...)
## S4 method for signature 'listie'
logLik(object, ...)
## S4 method for signature 'pfilterd_pomp'
logLik(object)
## S4 method for signature 'wpfilterd_pomp'
logLik(object)
## S4 method for signature 'probed_pomp'
logLik(object)
## S4 method for signature 'kalmand_pomp'
logLik(object)
```

54 logmeanexp

```
## S4 method for signature 'pmcmcd_pomp'
logLik(object)

## S4 method for signature 'bsmcd_pomp'
logLik(object)

## S4 method for signature 'objfun'
logLik(object)

## S4 method for signature 'spect_match_objfun'
logLik(object)

## S4 method for signature 'nlf_objfun'
logLik(object, ...)
```

## **Arguments**

object fitted model object

... ignored

#### Value

numerical value of the log likelihood. Note that some methods compute not the log likelihood itself but instead a related quantity. To keep the code simple, the logLik function is nevertheless used to extract this quantity.

When object is of 'probed\_pomp' class (i.e., the result of a probe computation), logLik retrieves the "synthetic likelihood" (see probe).

When object is of 'bsmcd\_pomp' class (i.e., the result of a bsmc2 computation), logLik retrieves the "log evidence" (see bsmc2).

When object is an NLF objective function, i.e., the result of a call to nlf\_objfun, logLik retrieves the "quasi log likelihood" (see nlf).

logmeanexp

The log-mean-exp trick

### Description

logmeanexp computes

$$\log \frac{1}{N} \sum_{n=1}^{N} e_i^x,$$

avoiding over- and under-flow in doing so. It can optionally return an estimate of the standard error in this quantity.

measles 55

### Usage

```
logmeanexp(x, se = FALSE)
```

## **Arguments**

```
x numeric
```

se logical; give approximate standard error?

### **Details**

When se = TRUE, logmeanexp uses a jackknife estimate of the variance in log(x).

### Value

log(mean(exp(x))) computed so as to avoid over- or underflow. If se = FALSE, the approximate standard error is returned as well.

#### Author(s)

Aaron A. King

### **Examples**

```
## an estimate of the log likelihood:
po <- ricker()
ll <- replicate(n=5,logLik(pfilter(po,Np=1000)))
logmeanexp(ll)
## with standard error:
logmeanexp(ll,se=TRUE)</pre>
```

measles

Historical childhood disease incidence data

### **Description**

LondonYorke is a data frame containing the monthly number of reported cases of chickenpox, measles, and mumps from two American cities (Baltimore and New York) in the mid-20th century (1928–1972).

ewmeas and ewcitmeas are data frames containing weekly reported cases of measles in England and Wales. ewmeas records the total measles reports for the whole country, 1948–1966. One questionable data point has been replaced with an NA. ewcitmeas records the incidence in seven English cities 1948–1987. These data were kindly provided by Ben Bolker, who writes: "Most of these data have been manually entered from published records by various people, and are prone to errors at several levels. All data are provided as is; use at your own risk."

56 mif2

### References

W. P. London and J. A. Yorke, Recurrent Outbreaks of Measles, Chickenpox and Mumps: I. Seasonal Variation in Contact Rates, *American Journal of Epidemiology* **98**, 453–468, 1973.

#### See Also

```
Other datasets: blowflies, bsflu, dacca(), ebola, parus

Other pomp examples: blowflies, bsflu, dacca(), ebola, gompertz(), ou2(), parus, pomp_examples, ricker(), rw2(), sir_models, verhulst()
```

## **Examples**

```
plot(cases~time,data=LondonYorke,subset=disease=="measles",type='n',main="measles",bty='l')
lines(cases~time,data=LondonYorke,subset=disease=="measles"&town=="Baltimore",col="red")
lines(cases~time,data=LondonYorke,subset=disease=="measles"&town=="New York",col="blue")
legend("topright",legend=c("Baltimore","New York"),lty=1,col=c("red","blue"),bty='n')
plot(
     cases~time,
     data=LondonYorke,
     subset=disease=="chickenpox"&town=="New York",
     type='l',col="blue",main="chickenpox, New York",
     bty='1'
    )
plot(
     cases~time,
     data=LondonYorke.
     subset=disease=="mumps"&town=="New York",
     type='l',col="blue",main="mumps, New York",
    bty='1'
    )
plot(reports~time,data=ewmeas,type='l')
plot(reports~date, data=ewcitmeas, subset=city=="Liverpool", type='l')
```

mif2

Iterated filtering: maximum likelihood by iterated, perturbed Bayes maps

### **Description**

An iterated filtering algorithm for estimating the parameters of a partially-observed Markov process. Running mif2 causes the algorithm to perform a specified number of particle-filter iterations. At each iteration, the particle filter is performed on a perturbed version of the model, in which the parameters to be estimated are subjected to random perturbations at each observation. This extra

mif2 57

variability effectively smooths the likelihood surface and combats particle depletion by introducing diversity into particle population. As the iterations progress, the magnitude of the perturbations is diminished according to a user-specified cooling schedule. The algorithm is presented and justified in Ionides et al. (2015).

## Usage

```
## S4 method for signature 'data.frame'
mif2(
  data,
 Nmif = 1,
  rw.sd,
  cooling.type = c("geometric", "hyperbolic"),
  cooling.fraction.50,
 Nρ,
 params,
  rinit,
  rprocess,
  dmeasure,
 partrans,
  . . . ,
  verbose = getOption("verbose", FALSE)
)
## S4 method for signature 'pomp'
mif2(
  data,
 Nmif = 1,
  rw.sd,
  cooling.type = c("geometric", "hyperbolic"),
  cooling.fraction.50,
 Nρ,
  verbose = getOption("verbose", FALSE)
)
## S4 method for signature 'pfilterd_pomp'
mif2(data, Nmif = 1, Np, ..., verbose = getOption("verbose", FALSE))
## S4 method for signature 'mif2d_pomp'
mif2(
  data,
 Nmif,
  rw.sd,
  cooling.type,
  cooling.fraction.50,
  verbose = getOption("verbose", FALSE)
)
```

58 mif2

#### **Arguments**

data

either a data frame holding the time series data, or an object of class 'pomp', i.e., the output of another **pomp** calculation.

Nmif

The number of filtering iterations to perform.

rw.sd

specification of the magnitude of the random-walk perturbations that will be applied to some or all model parameters. Parameters that are to be estimated should have positive perturbations specified here. The specification is given using the rw. sd function, which creates a list of unevaluated expressions. The latter are evaluated in a context where the model time variable is defined (as time). The expression ivp(s) can be used in this context as shorthand for

ifelse(time==time[1],s,0).

Likewise, ivp(s,lag) is equivalent to

ifelse(time==time[lag],s,0).

See below for some examples.

The perturbations that are applied are normally distributed with the specified s.d. If parameter transformations have been supplied, then the perturbations are applied on the transformed (estimation) scale.

cooling.type, cooling.fraction.50

specifications for the cooling schedule, i.e., the manner and rate with which the intensity of the parameter perturbations is reduced with successive filtering iterations. cooling.type specifies the nature of the cooling schedule. See below (under "Specifying the perturbations") for more detail.

Np

the number of particles to use. This may be specified as a single positive integer, in which case the same number of particles will be used at each timestep. Alternatively, if one wishes the number of particles to vary across timesteps, one may specify Np either as a vector of positive integers of length

length(time(object,t0=TRUE))

or as a function taking a positive integer argument. In the latter case, Np(k) must be a single positive integer, representing the number of particles to be used at the k-th timestep: Np(0) is the number of particles to use going from timezero(object) to time(object)[1], Np(1), from timezero(object) to time(object)[1], and so on, while when T=length(time(object)), Np(T) is the number of particles to sample at the end of the time-series.

params

optional; named numeric vector of parameters. This will be coerced internally to storage mode double.

rinit

simulator of the initial-state distribution. This can be furnished either as a C snippet, an R function, or the name of a pre-compiled native routine available in a dynamically loaded library. Setting rinit=NULL sets the initial-state simulator to its default. For more information, see ?rinit\_spec.

rprocess

simulator of the latent state process, specified using one of the rprocess plugins. Setting rprocess=NULL removes the latent-state simulator. For more information, see ?rprocess\_spec for the documentation on these plugins.

dmeasure evaluator of the measurement model density, specified either as a C snippet, an

R function, or the name of a pre-compiled native routine available in a dynamically loaded library. Setting dmeasure=NULL removes the measurement density

evaluator. For more information, see ?dmeasure\_spec.

partrans optional parameter transformations, constructed using parameter\_trans.

Many algorithms for parameter estimation search an unconstrained space of parameters. When working with such an algorithm and a model for which the parameters are constrained, it can be useful to transform parameters. One should supply the partrans argument via a call to parameter\_trans. For more information, see ?parameter\_trans. Setting partrans=NULL removes the parameter

transformations, i.e., sets them to the identity transformation.

.. additional arguments supply new or modify existing model characteristics or

components. See pomp for a full list of recognized arguments.

When named arguments not recognized by pomp are provided, these are made available to all basic components via the so-called *userdata* facility. This allows the user to pass information to the basic components outside of the usual routes of covariates (covar) and model parameters (params). See ?userdata for

information on how to use this facility.

verbose logical; if TRUE, diagnostic messages will be printed to the console.

#### Value

Upon successful completion, mif2 returns an object of class 'mif2d pomp'.

### Number of particles

If Np is anything other than a constant, the user must take care that the number of particles requested at the end of the time series matches that requested at the beginning. In particular, if T=length(time(object)), then one should have Np[1]==Np[T+1] when Np is furnished as an integer vector and Np(0)==Np(T) when Np is furnished as a function.

#### Methods

The following methods are available for such an object:

continue picks up where mif2 leaves off and performs more filtering iterations.

logLik returns the so-called *mif log likelihood* which is the log likelihood of the perturbed model, not of the focal model itself. To obtain the latter, it is advisable to run several pfilter operations on the result of a mif2 computation.

coef extracts the point estimate

eff. sample. size extracts the effective sample size of the final filtering iteration

Various other methods can be applied, including all the methods applicable to a pfilterd\_pomp object and all other **pomp** estimation algorithms and diagnostic methods.

60 mif2

### Specifying the perturbations

The rw. sd function simply returns a list containing its arguments as unevaluated expressions. These are then evaluated in a context containing the model time variable. This allows for easy specification of the structure of the perturbations that are to be applied. For example,

results in perturbations of parameter a with s.d. 0.05 at every time step, while parameters b and c both get perturbations of s.d. 0.2 only before the first observation. Parameters d and e, by contrast, get perturbations of s.d. 0.2 only before the thirteenth observation. Finally, parameter f gets a random perturbation of size 0.02 before every observation falling before t=23.

On the m-th IF2 iteration, prior to time-point n, the d-th parameter is given a random increment normally distributed with mean 0 and standard deviation  $c_{m,n}\sigma_{d,n}$ , where c is the cooling schedule and  $\sigma$  is specified using rw.sd, as described above. Let N be the length of the time series and  $\alpha$  =cooling.fraction.50. Then, when cooling.type="geometric", we have

$$c_{m,n} = \alpha^{\frac{n-1+(m-1)N}{50N}}.$$

When cooling.type="hyperbolic", we have

$$c_{m,n} = \frac{s+1}{s+n+(m-1)N},$$

where s satisfies

$$\frac{s+1}{s+50N} = \alpha.$$

Thus, in either case, the perturbations at the end of 50 IF2 iterations are a fraction  $\alpha$  smaller than they are at first.

#### **Re-running IF2 iterations**

To re-run a sequence of IF2 iterations, one can use the mif2 method on a 'mif2d\_pomp' object. By default, the same parameters used for the original IF2 run are re-used (except for verbose, the default of which is shown above). If one does specify additional arguments, these will override the defaults.

## Author(s)

Aaron A. King, Edward L. Ionides, Dao Nguyen

## References

E.L. Ionides, D. Nguyen, Y. Atchadé, S. Stoev, and A.A. King. Inference for dynamic and latent variable models via iterated, perturbed Bayes maps. *Proceedings of the National Academy of Sciences* **112**, 719–724, 2015.

nlf 61

## See Also

```
Other particle filter methods: bsmc2(), cond.logLik(), eff.sample.size(), filter.mean(), filter.traj(), pfilter(), pmcmc(), pred.mean(), pred.var(), wpfilter()

Other pomp parameter estimation methods: abc(), bsmc2(), kalman, nlf, pmcmc(), pomp-package, probe.match, spect.match
```

nlf

Nonlinear forecasting

## **Description**

Parameter estimation by maximum simulated quasi-likelihood.

## Usage

```
## S4 method for signature 'data.frame'
nlf_objfun(
  data,
  est = character(0),
  lags,
  nrbf = 4,
  ti,
  tf,
  seed = NULL,
  transform.data = identity,
  period = NA,
  tensor = TRUE,
  fail.value = NA_real_,
  params,
  rinit,
  rprocess,
  rmeasure,
  verbose = getOption("verbose")
)
## S4 method for signature 'pomp'
nlf_objfun(
  data,
  est = character(0),
  lags,
  nrbf = 4,
  ti,
  tf,
  seed = NULL,
  transform.data = identity,
```

62 nlf

```
period = NA,
  tensor = TRUE,
  fail.value = NA,
  verbose = getOption("verbose")
)
## S4 method for signature 'nlf_objfun'
nlf_objfun(
  data,
  est,
  lags,
  nrbf.
  ti,
  tf,
  seed = NULL,
  period,
  tensor,
  transform.data,
  fail.value,
  verbose = getOption("verbose", FALSE)
)
```

## **Arguments**

either a data frame holding the time series data, or an object of class 'pomp', data

i.e., the output of another **pomp** calculation.

est character vector; the names of parameters to be estimated.

A vector specifying the lags to use when constructing the nonlinear autoregreslags

sive prediction model. The first lag is the prediction interval.

nrbf integer scalar; the number of radial basis functions to be used at each lag.

required numeric values. NLF works by generating simulating long time series from the model. The simulated time series will be from ti to tf, with the same sampling frequency as the data. ti should be chosen large enough so that transient dynamics have died away. tf should be chosen large enough so that sufficiently many data points are available to estimate the nonlinear forecasting model well. An error will be generated unless the data-to-parameter ratio

exceeds 10 and a warning will be given if the ratio is smaller than 30.

integer. When fitting, it is often best to fix the seed of the random-number generator (RNG). This is accomplished by setting seed to an integer. By default,

seed = NULL, which does not alter the RNG state.

transform.data optional function. If specified, forecasting is performed using data and model simulations transformed by this function. By default, transform.data is the identity function, i.e., no transformation is performed. The main purpose of transform.data is to achieve approximately multivariate normal forecasting errors. If the data are univariate, transform.data should take a scalar and

seed

ti, tf

period

tensor

fail.value

params

rinit

vector input and return a vector of the same length. numeric; period=NA means the model is nonseasonal. period > 0 is the period of seasonal forcing. period <= 0 is equivalent to period = NA. logical; if FALSE, the fitted model is a generalized additive model with time mod period as one of the predictors, i.e., a gam with time-varying intercept. If TRUE, the fitted model is a gam with lagged state variables as predictors and time-periodic coefficients, constructed using tensor products of basis functions of state variables with basis functions of time. optional numeric scalar; if non-NA, this value is substituted for non-finite values of the objective function. It should be a large number (i.e., bigger than any legitimate values the objective function is likely to take). optional; named numeric vector of parameters. This will be coerced internally to storage mode double. simulator of the initial-state distribution. This can be furnished either as a C snippet, an R function, or the name of a pre-compiled native routine available in a dynamically loaded library. Setting rinit=NULL sets the initial-state simulator to its default. For more information, see ?rinit\_spec.

return a scalar. If the data are multivariate, transform.data should assume a

rmeasure

rprocess

simulator of the measurement model, specified either as a C snippet, an R function, or the name of a pre-compiled native routine available in a dynamically loaded library. Setting rmeasure=NULL removes the measurement model simulator. For more information, see ?rmeasure\_spec.

simulator of the latent state process, specified using one of the rprocess plugins.

Setting rprocess=NULL removes the latent-state simulator. For more informa-

tion, see ?rprocess spec for the documentation on these plugins.

additional arguments supply new or modify existing model characteristics or components. See pomp for a full list of recognized arguments.

When named arguments not recognized by pomp are provided, these are made available to all basic components via the so-called userdata facility. This allows the user to pass information to the basic components outside of the usual routes of covariates (covar) and model parameters (params). See ?userdata for

information on how to use this facility.

verbose

logical; if TRUE, diagnostic messages will be printed to the console.

#### **Details**

Nonlinear forecasting (NLF) is an 'indirect inference' method. The NLF approximation to the log likelihood of the data series is computed by simulating data from a model, fitting a nonlinear autoregressive model to the simulated time series, and quantifying the ability of the resulting fitted model to predict the data time series. The nonlinear autoregressive model is implemented as a generalized additive model (GAM), conditional on lagged values, for each observation variable. The errors are assumed multivariate normal.

The NLF objective function constructed by nlf\_objfun simulates long time series (nasymp is the number of observations in the simulated times series), perhaps after allowing for a transient period (ntransient steps). It then fits the GAM for the chosen lags to the simulated time series. Finally, it computes the quasi-likelihood of the data under the fitted GAM.

64 nlf

NLF assumes that the observation frequency (equivalently the time between successive observations) is uniform.

#### Value

nlf\_objfun constructs a stateful objective function for NLF estimation. Specfically, nlf\_objfun returns an object of class 'nlf\_objfun', which is a function suitable for use in an optim-like optimizer. In particular, this function takes a single numeric-vector argument that is assumed to contain the parameters named in est, in that order. When called, it will return the negative log quasilikelihood. It is a stateful function: Each time it is called, it will remember the values of the parameters and its estimate of the log quasilikelihood.

### Periodically-forced systems (seasonality)

Unlike other **pomp** estimation methods, NLF cannot accommodate general time-dependence in the model via explicit time-dependence or dependence on time-varying covariates. However, NLF can accommodate periodic forcing. It does this by including forcing phase as a predictor in the nonlinear autoregressive model. To accomplish this, one sets period to the period of the forcing (a positive numerical value). In this case, if tensor = FALSE, the effect is to add a periodic intercept in the autoregressive model. If tensor = TRUE, by contrast, the fitted model includes time-periodic coefficients, constructed using tensor products of basis functions of observables with basis functions of time.

## **Important Note**

Since **pomp** cannot guarantee that the *final* call an optimizer makes to the function is a call *at* the optimum, it cannot guarantee that the parameters stored in the function are the optimal ones. Therefore, it is a good idea to evaluate the function on the parameters returned by the optimization routine, which will ensure that these parameters are stored.

### Author(s)

Stephen P. Ellner, Bruce E. Kendall, Aaron A. King

## References

S.P. Ellner, B.A. Bailey, G.V. Bobashev, A.R. Gallant, B.T. Grenfell, and D.W. Nychka. Noise and nonlinearity in measles epidemics: combining mechanistic and statistical approaches to population modeling. *American Naturalist* **151**, 425–440, 1998.

B.E. Kendall, C.J. Briggs, W.W. Murdoch, P. Turchin, S.P. Ellner, E. McCauley, R.M. Nisbet, and S.N. Wood. Why do populations cycle? A synthesis of statistical and mechanistic modeling approaches. *Ecology* **80**, 1789–1805, 1999.

B.E. Kendall, S.P. Ellner, E. McCauley, S.N. Wood, C.J. Briggs, W.W. Murdoch, and P. Turchin. Population cycles in the pine looper moth (*Bupalus piniarius*): dynamical tests of mechanistic hypotheses. *Ecological Monographs* **75** 259–276, 2005.

#### See Also

Other pomp parameter estimation methods: abc(), bsmc2(), kalman, mif2(), pmcmc(), pomp-package, probe.match, spect.match

obs 65

## **Examples**

```
library(magrittr)

ricker() %>%
  nlf_objfun(est=c("r","sigma","N_0"),lags=c(4,6),
    partrans=parameter_trans(log=c("r","sigma","N_0")),
    paramnames=c("r","sigma","N_0"),
    ti=100,tf=2000,seed=426094906L) -> m1

library(subplex)
subplex(par=log(c(20,0.5,5)),fn=m1,control=list(reltol=1e-4)) -> out

m1(out$par)
coef(m1)
plot(simulate(m1))
```

obs

obs

## **Description**

Extract the data array from a 'pomp' object.

## Usage

```
## S4 method for signature 'pomp'
obs(object, vars, ...)
```

### **Arguments**

object an object of class 'pomp', or of a class extending 'pomp' vars names of variables to retrieve
... ignored

ou2

Two-dimensional discrete-time Ornstein-Uhlenbeck process

# Description

ou2() constructs a 'pomp' object encoding a bivariate discrete-time Ornstein-Uhlenbeck process with noisy observations.

66 ou2

### Usage

```
ou2(
   alpha_1 = 0.8,
   alpha_2 = -0.5,
   alpha_3 = 0.3,
   alpha_4 = 0.9,
   sigma_1 = 3,
   sigma_2 = -0.5,
   sigma_3 = 2,
   tau = 1,
   x1_0 = -3,
   x2_0 = 4,
   times = 1:100,
   t0 = 0
)
```

# Arguments

alpha\_1, alpha\_2, alpha\_3, alpha\_4

entries of the alpha matrix, in column-major order. That is, alpha\_2 is in the lower-left position.

sigma\_1, sigma\_2, sigma\_3

entries of the lower-triangular sigma matrix.  $sigma_2$  is the entry in the lower-left position.

tau measurement error s.d.

x1\_0, x2\_0 latent variable values at time t0

times vector of observation times

to the zero time

## **Details**

If the state process is  $X(t) = (x_1(t), x_2(t))$ , then

$$X(t+1) = \alpha X(t) + \sigma \epsilon(t),$$

where  $\alpha$  and  $\sigma$  are 2x2 matrices,  $\sigma$  is lower-triangular, and  $\epsilon(t)$  is standard bivariate normal. The observation process is  $Y(t) = (y_1(t), y_2(t))$ , where  $y_i(t) \sim \operatorname{normal}(x_i(t), \tau)$ .

## Value

A 'pomp' object with simulated data.

```
Other pomp examples: blowflies, bsflu, dacca(), ebola, gompertz(), measles, parus, pomp_examples, ricker(), rw2(), sir_models, verhulst()
```

parameter\_trans 67

### **Examples**

```
po <- ou2()
plot(po)
coef(po)
x <- simulate(po)
plot(x)
pf <- pfilter(po,Np=1000)
logLik(pf)</pre>
```

parameter\_trans

Parameter transformations

## **Description**

Equipping models with parameter transformations.

## Usage

```
## S4 method for signature 'Csnippet,Csnippet'
parameter_trans(toEst, fromEst, ..., log, logit, barycentric)
## S4 method for signature 'missing,missing'
parameter_trans(..., log, logit, barycentric)
## S4 method for signature 'character,character'
parameter_trans(toEst, fromEst, ...)
## S4 method for signature '`function`,`function`'
parameter_trans(toEst, fromEst, ...)
```

### **Arguments**

toEst, fromEst procedures that perform transformation of model parameters to and from the

estimation scale, respectively. These can be furnished using C snippets, R func-

tions, or via procedures in an external, dynamically loaded library.

... ignored.

log names of parameters to be log transformed.

logit names of parameters to be logit transformed.

barycentric names of parameters to be collectively transformed according to the log barycen-

tric transformation. Important note: variables to be log-barycentrically trans-

formed must be adjacent in the parameter vector.

68 parameter\_trans

#### **Details**

When parameter transformations are desired, they can be integrated into the 'pomp' object via the partrans arguments using the parameter\_trans function. As with the basic model components, these should ordinarily be specified using C snippets. When doing so, note that:

1. The parameter transformation mapping a parameter vector from the scale used by the model codes to another scale, and the inverse transformation, are specified via a call to

```
\verb|parameter_trans|(to Est, from Est)|
```

.

- 2. The goal of these snippets is the transformation of the parameters from the natural scale to the estimation scale, and vice-versa. If p is the name of a variable on the natural scale, its value on the estimation scale is T\_p. Thus the toEst snippet computes T\_p given p whilst the fromEst snippet computes p given T\_p.
- 3. Time-, state-, and covariate-dependent transformations are not allowed. Therefore, neither the time, nor any state variables, nor any of the covariates will be available in the context within which a parameter transformation snippet is executed.

These transformations can also be specified using R functions with arguments chosen from among the parameters. Such an R function must also have the argument '...'. In this case, toEst should transform parameters from the scale that the basic components use internally to the scale used in estimation. fromEst should be the inverse of toEst.

Note that it is the user's responsibility to make sure that the transformations are mutually inverse. If obj is the constructed 'pomp' object, and coef(obj) is non-empty, a simple check of this property is

```
x <- coef(obj, transform = TRUE)
obj1 <- obj
coef(obj1, transform = TRUE) <- x
identical(coef(obj), coef(obj1))
identical(coef(obj1, transform=TRUE), x)</pre>
```

One can use the log and logit arguments of parameter\_trans to name variables that should be log-transformed or logit-transformed, respectively. The barycentric argument can name sets of parameters that should be log-barycentric transformed.

Note that using the log, logit, or barycentric arguments causes C snippets to be generated. Therefore, you must make sure that variables named in any of these arguments are also mentioned in paramnames at the same time.

The logit transform is defined by

$$logit(\theta) = log \frac{\theta}{1 - \theta}.$$

The log barycentric transformation of variables  $\theta_1, \dots, \theta_n$  is given by

logbarycentric
$$(\theta_1, \dots, \theta_n) = \left(\log \frac{\theta_1}{\sum_i \theta_i}, \dots, \log \frac{\theta_n}{\sum_i \theta_i}\right)$$
.

parmat 69

### See Also

Other information on model implementation: Csnippet, accumulators, covariate\_table(), distributions, dmeasure\_spec, dprocess\_spec, pomp-package, prior\_spec, rinit\_spec, rmeasure\_spec, rprocess\_spec, skeleton\_spec, transformations, userdata

parmat

Create a matrix of parameters

### **Description**

parmat is a utility that makes a vector of parameters suitable for use in pomp functions.

## Usage

```
parmat(params, nrep = 1)
```

## **Arguments**

params named numeric vector or matrix of parameters.

nrep number of replicates (columns) desired.

#### Value

parmat returns a matrix consisting of nrep copies of params.

## Author(s)

Aaron A. King

# **Examples**

```
## generate a bifurcation diagram for the Ricker map p \leftarrow proper proper p \leftarrow proper p \leftarrow
```

70 parus

### **Description**

Performs parameter transformations.

### Usage

```
## S4 method for signature 'pomp'
partrans(object, params, dir = c("fromEst", "toEst"), ...)
```

# **Arguments**

object	an object of class 'pomp', or of a class that extends 'pomp'. This will typically be the output of pomp, simulate, or one of the <b>pomp</b> inference algorithms.
params	a npar x nrep matrix of parameters. Each column is treated as an independent parameter set, in correspondence with the corresponding column of x.
dir	the direction of the transformation to perform.
	additional arguments are ignored.

#### Value

If dir=fromEst, the parameters in params are assumed to be on the estimation scale and are transformed onto the natural scale. If dir=toEst, they are transformed onto the estimation scale. In both cases, the parameters are returned as a named numeric vector or an array with rownames, as appropriate.

# See Also

```
Specification of parameter transformations: parameter_trans
Other pomp workhorses: dmeasure(), dprior(), dprocess(), flow(), rinit(), rmeasure(),
rprior(), rprocess(), skeleton(), workhorses
```

parus

Parus major population dynamics

# **Description**

Size of a population of great tits (Parus major) from Wytham Wood, near Oxford.

## **Details**

Provenance: Global Population Dynamics Database dataset #10163. (NERC Centre for Population Biology, Imperial College (2010) The Global Population Dynamics Database Version 2. https://www.imperial.ac.uk/cpb/gpdd2/). Original source: McCleer and Perrins (1991).

pfilter 71

### References

R. McCleery and C. Perrins. Effects of predation on the numbers of Great Tits, *Parus major*. In: C.M. Perrins, J.-D. Lebreton, and G.J.M. Hirons (eds.), *Bird Population Studies*, pp. 129–147, Oxford. Univ. Press, 1991.

### See Also

```
Other datasets: blowflies, bsflu, dacca(), ebola, measles

Other pomp examples: blowflies, bsflu, dacca(), ebola, gompertz(), measles, ou2(), pomp_examples, ricker(), rw2(), sir_models, verhulst()
```

## **Examples**

```
parus %>%
  pfilter(Np=1000, times="year", t0=1960,
  params=c(K=190,r=2.7,sigma=0.2,theta=0.05,N.0=148),
  rprocess=discrete_time(
     function (r, K, sigma, N, ...) {
       e <- rnorm(n=1,mean=0,sd=sigma)
       c(N = exp(log(N)+r*(1-N/K)+e))
     },
     delta.t=1
  ),
  rmeasure=function (N, theta, ...) {
     c(pop=rnbinom(n=1, size=1/theta, mu=N+1e-10))
  },
  dmeasure=function (pop, N, theta, ..., log) {
     dnbinom(x=pop,mu=N+1e-10,size=1/theta,log=log)
  },
  partrans=parameter_trans(log=c("sigma","theta","N_0","r","K")),
  paramnames=c("sigma","theta","N_0","r","K")
) -> pf
pf %>% logLik()
pf %>% simulate() %>% plot()
```

pfilter

Particle filter

### **Description**

A plain vanilla sequential Monte Carlo (particle filter) algorithm. Resampling is performed at each observation.

72 pfilter

## Usage

```
## S4 method for signature 'data.frame'
pfilter(
  data,
  Nρ,
  params,
  rinit,
  rprocess,
  dmeasure,
  pred.mean = FALSE,
  pred.var = FALSE,
  filter.mean = FALSE,
  filter.traj = FALSE,
  save.states = FALSE,
  verbose = getOption("verbose", FALSE)
)
## S4 method for signature 'pomp'
pfilter(
  data,
  Nρ,
  pred.mean = FALSE,
  pred.var = FALSE,
  filter.mean = FALSE,
  filter.traj = FALSE,
  save.states = FALSE,
  verbose = getOption("verbose", FALSE)
## S4 method for signature 'pfilterd_pomp'
pfilter(data, Np, ..., verbose = getOption("verbose", FALSE))
## S4 method for signature 'objfun'
pfilter(data, ...)
```

### Arguments

data

either a data frame holding the time series data, or an object of class 'pomp', i.e., the output of another **pomp** calculation.

Np

the number of particles to use. This may be specified as a single positive integer, in which case the same number of particles will be used at each timestep. Alternatively, if one wishes the number of particles to vary across timesteps, one may specify Np either as a vector of positive integers of length

```
length(time(object,t0=TRUE))
```

or as a function taking a positive integer argument. In the latter case, Np(k)

pfilter 73

	must be a single positive integer, representing the number of particles to be used at the k-th timestep: $Np(0)$ is the number of particles to use going from timezero(object) to time(object)[1], $Np(1)$ , from timezero(object) to time(object)[1], and so on, while when $T=length(time(object))$ , $Np(T)$ is the number of particles to sample at the end of the time-series.
params	optional; named numeric vector of parameters. This will be coerced internally to storage mode double.
rinit	simulator of the initial-state distribution. This can be furnished either as a C snippet, an R function, or the name of a pre-compiled native routine available in a dynamically loaded library. Setting rinit=NULL sets the initial-state simulator to its default. For more information, see ?rinit_spec.
rprocess	simulator of the latent state process, specified using one of the rprocess plugins. Setting rprocess=NULL removes the latent-state simulator. For more information, see ?rprocess_spec for the documentation on these plugins.
dmeasure	evaluator of the measurement model density, specified either as a C snippet, an R function, or the name of a pre-compiled native routine available in a dynamically loaded library. Setting dmeasure=NULL removes the measurement density evaluator. For more information, see ?dmeasure_spec.
pred.mean	logical; if TRUE, the prediction means are calculated for the state variables and parameters.
pred.var	logical; if TRUE, the prediction variances are calculated for the state variables and parameters.
filter.mean	logical; if TRUE, the filtering means are calculated for the state variables and parameters.
filter.traj	logical; if TRUE, a filtered trajectory is returned for the state variables and parameters. See filter.traj for more information.
save.states	logical. If save.states=TRUE, the state-vector for each particle at each time is saved.

additional arguments supply new or modify existing model characteristics or components. See pomp for a full list of recognized arguments.

When named arguments not recognized by pomp are provided, these are made available to all basic components via the so-called userdata facility. This allows the user to pass information to the basic components outside of the usual routes of covariates (covar) and model parameters (params). See ?userdata for information on how to use this facility.

logical; if TRUE, diagnostic messages will be printed to the console. verbose

# Value

An object of class 'pfilterd\_pomp', which extends class 'pomp'. Information can be extracted from this object using the methods documented below.

# Methods

logLik the estimated log likelihood

74 plot

```
cond.logLik the estimated conditional log likelihood

eff.sample.size the (time-dependent) estimated effective sample size

pred.mean, pred.var the mean and variance of the approximate prediction distribution

filter.mean the mean of the filtering distribution

filter.traj retrieve one particle trajectory. Useful for building up the smoothing distribution.

as.data.frame coerce to a data frame

plot diagnostic plots
```

# Author(s)

Aaron A. King

#### References

M.S. Arulampalam, S. Maskell, N. Gordon, & T. Clapp. A Tutorial on Particle Filters for Online Nonlinear, Non-Gaussian Bayesian Tracking. *IEEE Transactions on Signal Processing* **50**, 174–188, 2002.

#### See Also

```
Other elementary POMP methods: pomp-package, probe(), simulate(), spect(), wpfilter()
Other particle filter methods: bsmc2(), cond.logLik(), eff.sample.size(), filter.mean(),
filter.traj(), mif2(), pmcmc(), pred.mean(), pred.var(), wpfilter()
```

## **Examples**

```
pf <- pfilter(gompertz(),Np=1000) ## use 1000 particles

plot(pf)
logLik(pf)
cond.logLik(pf) ## conditional log-likelihoods
eff.sample.size(pf) ## effective sample size
logLik(pfilter(pf)) ## run it again with 1000 particles

## run it again with 2000 particles
pf <- pfilter(pf,Np=2000,filter.mean=TRUE,filter.traj=TRUE)
fm <- filter.mean(pf) ## extract the filtering means
ft <- filter.traj(pf) ## one draw from the smoothing distribution</pre>
```

plot

**Plotting** 

# **Description**

Diagnostic plots.

plot 75

# Usage

```
## S4 method for signature 'pomp_plottable'
plot(
  х,
  variables,
  panel = lines,
  nc = NULL,
 yax.flip = FALSE,
 mar = c(0, 5.1, 0, if (yax.flip) 5.1 else 2.1),
 oma = c(6, 0, 5, 0),
  axes = TRUE,
)
## S4 method for signature 'Pmcmc'
plot(x, ..., pars)
## S4 method for signature 'Abc'
plot(x, ..., pars, scatter = FALSE)
## S4 method for signature 'Mif2'
plot(x, y, ...)
## S4 method for signature 'probed_pomp'
plot(x, y, ...)
## S4 method for signature 'spectd_pomp'
plot(
 х,
  . . . ,
 max.plots.per.page = 4,
 plot.data = TRUE,
  quantiles = c(0.025, 0.25, 0.5, 0.75, 0.975),
  quantile.styles = list(lwd = 1, lty = 1, col = "gray70"),
  data.styles = list(lwd = 2, lty = 2, col = "black")
)
## S4 method for signature 'bsmcd_pomp'
plot(x, pars, thin, ...)
## S4 method for signature 'probe_match_objfun'
plot(x, y, ...)
## S4 method for signature 'spect_match_objfun'
plot(x, y, ...)
```

76 pmcmc

# **Arguments**

X	the object to plot	
variables	optional character; names of variables to be displayed	
panel	function of prototype panel( $x$ ,col,bg,pch,type,) which gives the action to be carried out in each panel of the display.	
nc	the number of columns to use. Defaults to 1 for up to 4 series, otherwise to 2.	
yax.flip	logical; if TRUE, the y-axis (ticks and numbering) should flip from side 2 (left) to 4 (right) from series to series.	
mar, oma	the par mar and oma settings. Modify with care!	
axes	logical; indicates if x- and y- axes should be drawn	
	ignored or passed to low-level plotting functions	
pars	names of parameters.	
scatter	logical; if FALSE, traces of the parameters named in pars will be plotted against ABC iteration number. If TRUE, the traces will be displayed or as a scatterplot.	
у	ignored	
max.plots.per.p	page	
	positive integer; maximum number of plots on a page	
plot.data	logical; should the data spectrum be included?	
quantiles	numeric; quantiles to display	
quantile.styles		
	list; plot styles to use for quantiles	
data.styles	list; plot styles to use for data	
thin	integer; when the number of samples is very large, it can be helpful to plot a random subsample: thin specifies the size of this subsample.	

pmcmc

The particle Markov chain Metropolis-Hastings algorithm

# Description

The Particle MCMC algorithm for estimating the parameters of a partially-observed Markov process. Running pmcmc causes a particle random-walk Metropolis-Hastings Markov chain algorithm to run for the specified number of proposals.

# Usage

```
## $4 method for signature 'data.frame'
pmcmc(
   data,
   Nmcmc = 1,
   proposal,
   Np,
```

pmcmc 77

```
params,
  rinit,
  rprocess,
  dmeasure,
  dprior,
  verbose = getOption("verbose", FALSE)
)
## S4 method for signature 'pomp'
pmcmc(
  data,
 Nmcmc = 1,
  proposal,
 Nρ,
  verbose = getOption("verbose", FALSE)
## S4 method for signature 'pfilterd_pomp'
pmcmc(
  data,
 Nmcmc = 1,
  proposal,
 Nρ,
  verbose = getOption("verbose", FALSE)
)
## S4 method for signature 'pmcmcd_pomp'
pmcmc(data, Nmcmc, proposal, ..., verbose = getOption("verbose", FALSE))
```

# Arguments

data

either a data frame holding the time series data, or an object of class 'pomp', i.e., the output of another **pomp** calculation.

Nmcmc

The number of PMCMC iterations to perform.

proposal

optional function that draws from the proposal distribution. Currently, the proposal distribution must be symmetric for proper inference: it is the user's responsibility to ensure that it is. Several functions that construct appropriate proposal function are provided: see MCMC proposals for more information.

Np

the number of particles to use. This may be specified as a single positive integer, in which case the same number of particles will be used at each timestep. Alternatively, if one wishes the number of particles to vary across timesteps, one may specify Np either as a vector of positive integers of length

```
length(time(object,t0=TRUE))
```

78 pmcmc

or as a function taking a positive integer argument. In the latter case, Np(k) must be a single positive integer, representing the number of particles to be used at the k-th timestep: Np(0) is the number of particles to use going from timezero(object) to time(object)[1], Np(1), from timezero(object) to time(object)[1], and so on, while when T=length(time(object)), Np(T) is the number of particles to sample at the end of the time-series.

params optional; named numeric vector of parameters. This will be coerced internally

to storage mode double.

rinit simulator of the initial-state distribution. This can be furnished either as a C snippet, an R function, or the name of a pre-compiled native routine available in

a dynamically loaded library. Setting rinit=NULL sets the initial-state simulator

to its default. For more information, see ?rinit\_spec.

rprocess simulator of the latent state process, specified using one of the rprocess plugins.

Setting rprocess=NULL removes the latent-state simulator. For more informa-

tion, see ?rprocess\_spec for the documentation on these plugins.

dmeasure evaluator of the measurement model density, specified either as a C snippet, an

R function, or the name of a pre-compiled native routine available in a dynamically loaded library. Setting dmeasure=NULL removes the measurement density

evaluator. For more information, see ?dmeasure\_spec.

dprior optional; prior distribution density evaluator, specified either as a C snippet, an R

function, or the name of a pre-compiled native routine available in a dynamically loaded library. For more information, see ?prior\_spec. Setting dprior=NULL

resets the prior distribution to its default, which is a flat improper prior.

.. additional arguments supply new or modify existing model characteristics or

components. See pomp for a full list of recognized arguments.

When named arguments not recognized by pomp are provided, these are made available to all basic components via the so-called *userdata* facility. This allows the user to pass information to the basic components outside of the usual routes of covariates (covar) and model parameters (params). See ?userdata for

information on how to use this facility.

verbose logical; if TRUE, diagnostic messages will be printed to the console.

#### Value

An object of class 'pmcmcd\_pomp'.

# **Re-running PMCMC Iterations**

To re-run a sequence of PMCMC iterations, one can use the pmcmc method on a 'pmcmc' object. By default, the same parameters used for the original PMCMC run are re-used (except for verbose, the default of which is shown above). If one does specify additional arguments, these will override the defaults.

# Author(s)

Edward L. Ionides, Aaron A. King, Sebastian Funk

#### References

C. Andrieu, A. Doucet, and R. Holenstein. Particle Markov chain Monte Carlo methods. *Journal of the Royal Statistical Society, Series B* **72**, 269–342, 2010.

## See Also

```
MCMC proposals
```

```
Other particle filter methods: bsmc2(), cond.logLik(), eff.sample.size(), filter.mean(), filter.traj(), mif2(), pfilter(), pred.mean(), pred.var(), wpfilter()
```

Other pomp parameter estimation methods: abc(), bsmc2(), kalman, mif2(), nlf, pomp-package, probe.match, spect.match

pomp

Constructor of the basic pomp object

# **Description**

This function constructs a 'pomp' object, encoding a partially-observed Markov process (POMP) model together with a uni- or multi-variate time series. As such, it is central to all the package's functionality. One implements the POMP model by specifying some or all of its *basic components*. These comprise:

rinit, which samples from the distribution of the state process at the zero-time;

rprocess, the simulator of the unobserved Markov state process;

**dprocess**, the evaluator of the probability density function for transitions of the unobserved Markov state process;

**rmeasure**, the simulator of the observed process, conditional on the unobserved state;

**dmeasure**, the evaluator of the measurement model probability density function;

**rprior,** which samples from a prior probability distribution on the parameters;

**dprior**, which evaluates the prior probability density function;

**skeleton**, which computes the deterministic skeleton of the unobserved state process;

partrans, which performs parameter transformations.

The basic structure and its rationale are described in the *Journal of Statistical Software* paper, an updated version of which is to be found on the package website.

# Usage

```
pomp(
  data,
  times,
  t0,
   ...,
  rinit,
```

```
rprocess,
dprocess,
rmeasure,
dmeasure,
skeleton,
rprior,
dprior,
partrans,
covar,
params,
accumvars,
obsnames,
statenames,
paramnames,
covarnames,
PACKAGE,
globals,
cdir = getOption("pomp_cdir", NULL),
cfile,
shlib.args,
compile = TRUE,
verbose = getOption("verbose", FALSE)
```

### **Arguments**

)

data either a data frame holding the time series data, or an object of class 'pomp',

i.e., the output of another **pomp** calculation.

the times at which observations are made. times must indicate the column of

observation times by name or index. The time vector must be numeric and nondecreasing. Internally, data will be internally coerced to an array with storage-

mode double.

The zero-time, i.e., the time of the initial state. This must be no later than the

time of the first observation, i.e.,  $t0 \le times[1]$ .

additional arguments supply new or modify existing model characteristics or components. See pomp for a full list of recognized arguments.

When named arguments not recognized by pomp are provided, these are made available to all basic components via the so-called userdata facility. This allows the user to pass information to the basic components outside of the usual routes of covariates (covar) and model parameters (params). See ?userdata for

information on how to use this facility.

rinit simulator of the initial-state distribution. This can be furnished either as a C snippet, an R function, or the name of a pre-compiled native routine available in

a dynamically loaded library. Setting rinit=NULL sets the initial-state simulator

to its default. For more information, see ?rinit\_spec.

simulator of the latent state process, specified using one of the rprocess plugins.

Setting rprocess=NULL removes the latent-state simulator. For more informa-

tion, see ?rprocess\_spec for the documentation on these plugins.

times

t0

rprocess

optional; specification of the probability density evaluation function of the unobserved state process. Setting dprocess=NULL removes the latent-state density

evaluator. For more information, see ?dprocess\_spec.

rmeasure simulator of the measurement model, specified either as a C snippet, an R func-

tion, or the name of a pre-compiled native routine available in a dynamically loaded library. Setting rmeasure=NULL removes the measurement model simu-

lator. For more information, see ?rmeasure\_spec.

dmeasure evaluator of the measurement model density, specified either as a C snippet, an

R function, or the name of a pre-compiled native routine available in a dynamically loaded library. Setting dmeasure=NULL removes the measurement density

evaluator. For more information, see ?dmeasure\_spec.

skeleton optional; the deterministic skeleton of the unobserved state process. Depending

on whether the model operates in continuous or discrete time, this is either a vectorfield or a map. Accordingly, this is supplied using either the vectorfield or map fnctions. For more information, see ?skeleton\_spec. Setting skeleton=NULL

removes the deterministic skeleton.

rprior optional; prior distribution sampler, specified either as a C snippet, an R func-

tion, or the name of a pre-compiled native routine available in a dynamically loaded library. For more information, see ?prior\_spec. Setting rprior=NULL

removes the prior distribution sampler.

dprior optional; prior distribution density evaluator, specified either as a C snippet, an R

function, or the name of a pre-compiled native routine available in a dynamically loaded library. For more information, see ?prior\_spec. Setting dprior=NULL

resets the prior distribution to its default, which is a flat improper prior.

partrans optional parameter transformations, constructed using parameter\_trans.

Many algorithms for parameter estimation search an unconstrained space of parameters. When working with such an algorithm and a model for which the parameters are constrained, it can be useful to transform parameters. One should supply the partrans argument via a call to parameter\_trans. For more information, see ?parameter\_trans. Setting partrans=NULL removes the parameter

transformations, i.e., sets them to the identity transformation.

covar optional covariate table, constructed using covariate\_table.

If a covariate table is supplied, then the value of each of the covariates is interpolated as needed. The resulting interpolated values are made available to the appropriate basic components. See the documentation for covariate\_table

for details.

params optional; named numeric vector of parameters. This will be coerced internally

to storage mode double.

accumvars optional character vector; contains the names of accumulator variables. See

?accumulators for a definition and discussion of accumulator variables.

obsnames optional character vector; names of the observables. It is not usually necessary

to specify obsnames since, by default, these are read from the names of the data

variables.

statenames optional character vector; names of the latent state variables. It is typically only

necessary to supply statenames when C snippets are in use.

optional character vector; names of model parameters. It is typically only necparamnames essary to supply paramnames when C snippets are in use. optional character vector; names of the covariates. It is not usually necessary covarnames to specify covarnames since, by default, these are read from the names of the covariates. **PACKAGE** optional character; the name (without extension) of the external, dynamically loaded library in which any native routines are to be found. This is only useful if one or more of the model components has been specified using a precompiled dynamically loaded library; it is not used for any component specified using C snippets. PACKAGE can name at most one library. globals optional character; arbitrary C code that will be hard-coded into the sharedobject library created when C snippets are provided. If no C snippets are used, globals has no effect. optional character variable. cdir specifies the name of the directory within cdir which C snippet code will be compiled. By default, this is in a temporary directory specific to the R session. One can also set this directory using the pomp\_cdir option. cfile optional character variable. cfile gives the name of the file (in directory cdir) into which C snippet codes will be written. By default, a random filename is used. If the chosen filename would result in over-writing an existing file, an error is generated. optional character variables. Command-line arguments to the R CMD SHLIB call shlib.args that compiles the C snippets. compile logical; if FALSE, compilation of the C snippets will be postponed until they are needed. logical; if TRUE, diagnostic messages will be printed to the console. verbose

# Details

Each basic component is supplied via an argument of the same name. These can be given in the call to pomp, or to many of the package's other functions. In any case, the effect is the same: to add, remove, or modify the basic component.

Each basic component can be furnished using C snippets, R functions, or pre-compiled native routine available in user-provided dynamically loaded libraries.

#### Value

The pomp constructor function returns an object, call it P, of class 'pomp'. P contains, in addition to the data, any elements of the model that have been specified as arguments to the pomp constructor function. One can add or modify elements of P by means of further calls to pomp, using P as the first argument in such calls. One can pass P to most of the **pomp** package methods via their data argument.

#### Note

It is not typically necessary (or indeed often feasible) to define all of the basic components for any given purpose. Each pomp algorithm makes use of only a subset of these components.

pomp\_examples 83

Any algorithm requiring a component that is not present will generate an error letting you know that you have not provided a needed component. FIXME

## Author(s)

Aaron A. King

#### References

A. A. King, D. Nguyen, and E. L. Ionides. Statistical Inference for Partially Observed Markov Processes via the Package **pomp**. *Journal of Statistical Software* **69**(12), 1–43, 2016. An updated version of this paper is available on the package website.

pomp\_examples

pomp examples

### **Description**

Pre-built POMP examples

#### **Details**

**pomp** includes a number of pre-built examples of pomp objects and data that can be analyzed using **pomp** methods. These include:

blowflies Data from Nicholson's experiments with sheep blowfly populations

blowflies1() A pomp object with some of the blowfly data together with a discrete delay equation model.

blowflies2() A variant of blowflies1.

bsflu Data from an outbreak of influenza in a boarding school.

dacca() Fifty years of census and cholera mortality data, together with a stochastic differential equation transmission model (King et al. 2008).

ebolaModel() Data from the 2014 West Africa outbreak of Ebola virus disease, together with simple transmission models (King et al. 2015).

gompertz() The Gompertz population dynamics model, with simulated data.

LondonYorke Data on incidence of several childhood diseases (London and Yorke 1973)

ewmeas Measles incidence data from England and Wales

ewcitmeas Measles incidence data from 7 English cities

ou2() A 2-D Ornstein-Uhlenbeck process with simulated data

parus Population censuses of a Parus major population in Wytham Wood, England.

ricker The Ricker population dynamics model, with simulated data

rw2 A 2-D Brownian motion model, with simulated data.

sir() A simple continuous-time Markov chain SIR model, coded using Euler-multinomial steps, with simulated data. 84 pred.mean

sir2() A simple continuous-time Markov chain SIR model, coded using Gillespie's algorithm, with simulated data.

verhulst() The Verhulst-Pearl (logistic) model, a continuous-time model of population dynamics, with simulated data

See also the tutorials on the package website for more examples.

#### References

Anonymous. Influenza in a boarding school. British Medical Journal 1, 587, 1978.

A.A. King, E.L. Ionides, M. Pascual, and M.J. Bouma. Inapparent infections and cholera dynamics. *Nature* **454**, 877-880, 2008

A.A. King, M. Domenech de Cellès, F.M.G. Magpantay, and P. Rohani. Avoidable errors in the modelling of outbreaks of emerging pathogens, with special reference to Ebola. *Proceedings of the Royal Society of London, Series B* **282**, 20150347, 2015.

W. P. London and J. A. Yorke, Recurrent Outbreaks of Measles, Chickenpox and Mumps: I. Seasonal Variation in Contact Rates, *American Journal of Epidemiology* **98**, 453–468, 1973.

A.J. Nicholson. The self-adjustment of populations to change. *Cold Spring Harbor Symposia on Quantitative Biology* **22**, 153–173, 1957.

#### See Also

```
Other pomp examples: blowflies, bsflu, dacca(), ebola, gompertz(), measles, ou2(), parus, ricker(), rw2(), sir_models, verhulst()
```

pred.mean

Prediction mean

### **Description**

The mean of the prediction distribution

### Usage

```
## S4 method for signature 'kalmand_pomp'
pred.mean(object, vars, ...)
## S4 method for signature 'pfilterd_pomp'
pred.mean(object, vars, ...)
```

# **Arguments**

object result of a filtering computation
vars optional character; names of variables
... ignored

pred.var 85

## **Details**

The prediction distribution is that of

$$X(t_k)|Y(t_1) = y_1^*, \dots, Y(t_{k-1}) = y_{k-1}^*,$$

where  $X(t_k)$ ,  $Y(t_k)$  are the latent state and observable processes, respectively, and  $y_k^*$  is the data, at time  $t_k$ .

The prediction mean is therefore the expectation of this distribution

$$E[X(t_k)|Y(t_1) = y_1^*, \dots, Y(t_{k-1}) = y_{k-1}^*].$$

## See Also

Other particle filter methods: bsmc2(), cond.logLik(), eff.sample.size(), filter.mean(), filter.traj(), mif2(), pfilter(), pmcmc(), pred.var(), wpfilter()

pred.var

Prediction variance

### **Description**

The variance of the prediction distribution

### Usage

```
## S4 method for signature 'pfilterd_pomp'
pred.var(object, vars, ...)
```

# **Arguments**

object result of a filtering computation
vars optional character; names of variables
... ignored

## **Details**

The prediction distribution is that of

$$X(t_k)|Y(t_1) = y_1^*, \dots, Y(t_{k-1}) = y_{k-1}^*,$$

where  $X(t_k)$ ,  $Y(t_k)$  are the latent state and observable processes, respectively, and  $y_k^*$  is the data, at time  $t_k$ .

The prediction variance is therefore the variance of this distribution

$$Var[X(t_k)|Y(t_1) = y_1^*, \dots, Y(t_{k-1}) = y_{k-1}^*].$$

## See Also

```
Other particle filter methods: bsmc2(), cond.logLik(), eff.sample.size(), filter.mean(), filter.traj(), mif2(), pfilter(), pmcmc(), pred.mean(), wpfilter()
```

86 prior\_spec

print	Print methods	
-------	---------------	--

### **Description**

These methods print their argument and return it \*invisibly\*.

prior\_spec prior specification

# **Description**

Specify the prior distribution

#### **Details**

A prior distribution on parameters is specified by means of the rprior and/or dprior arguments to pomp. As with the other basic model components, it is preferable to specify these using C snippets. In writing a C snippet for the prior sampler (rprior), keep in mind that:

- 1. Within the context in which the snippet will be evaluated, only the parameters will be defined.
- 2. The goal of such a snippet is the replacement of parameters with values drawn from the prior distribution.
- 3. Hyperparameters can be included in the ordinary parameter list. Obviously, hyperparameters should not be replaced with random draws.

In writing a C snippet for the prior density function (dprior), observe that:

- Within the context in which the snippet will be evaluated, only the parameters and give\_log will be defined.
- 2. The goal of such a snippet is computation of the prior probability density, or the log of same, at a given point in parameter space. This scalar value should be returned in the variable lik. When give\_log == 1, lik should contain the log of the prior probability density.
- 3. Hyperparameters can be included in the ordinary parameter list.

# General rules for writing C snippets can be found here.

Alternatively, one can furnish R functions for one or both of these arguments. In this case, rprior must be a function of prototype

```
f(params, ...)
```

that makes a draw from the prior distribution given params and returns a named vector of the same length and with the same set of names, as params. The dprior function must be of prototype

```
f(params, log = FALSE, ...).
```

Its role is to evaluate the prior probability density (or log density if log == TRUE) and return that single scalar value.

probe 87

## **Default behavior**

By default, the prior is assumed flat and improper. In particular, dprior returns 1 (0 if log = TRUE) for every parameter set. Since it is impossible to simulate from a flat improper prior, rprocess returns missing values (NAs).

#### See Also

Other information on model implementation: Csnippet, accumulators, covariate\_table(), distributions, dmeasure\_spec, dprocess\_spec, parameter\_trans(), pomp-package, rinit\_spec, rmeasure\_spec, rprocess\_spec, skeleton\_spec, transformations, userdata

probe

Probes (AKA summary statistics)

# Description

Probe a partially-observed Markov process by computing summary statistics and the synthetic likelihood.

# Usage

```
## S4 method for signature 'data.frame'
probe(
  data,
  probes,
  nsim,
  seed = NULL,
  params,
  rinit,
  rprocess,
  rmeasure,
  verbose = getOption("verbose", FALSE)
## S4 method for signature 'pomp'
probe(
  data,
  probes,
  nsim,
  seed = NULL,
  verbose = getOption("verbose", FALSE)
)
## S4 method for signature 'probed_pomp'
probe(
```

88 probe

```
data,
  probes,
  nsim,
  seed = NULL,
    ...,
  verbose = getOption("verbose", FALSE)
)

## S4 method for signature 'probe_match_objfun'
  probe(data, seed, ..., verbose = getOption("verbose", FALSE))

## S4 method for signature 'objfun'
  probe(data, seed = NULL, ...)
```

## **Arguments**

data either a data frame holding the time series data, or an object of class 'pomp',

i.e., the output of another **pomp** calculation.

probes a single probe or a list of one or more probes. A probe is simply a scalar- or

vector-valued function of one argument that can be applied to the data array of a 'pomp'. A vector-valued probe must always return a vector of the same size.

A number of useful probes are provided with the package: see basic probes.

nsim the number of model simulations to be computed.

seed optional integer; if non-NULL, the random number generator will be initialized

with this seed for simulations. See simulate.

params optional; named numeric vector of parameters. This will be coerced internally

to storage mode double.

rinit simulator of the initial-state distribution. This can be furnished either as a C

snippet, an R function, or the name of a pre-compiled native routine available in a dynamically loaded library. Setting rinit=NULL sets the initial-state simulator

to its default. For more information, see ?rinit spec.

rprocess simulator of the latent state process, specified using one of the rprocess plugins.

Setting rprocess=NULL removes the latent-state simulator. For more informa-

tion, see ?rprocess\_spec for the documentation on these plugins.

rmeasure simulator of the measurement model, specified either as a C snippet, an R func-

tion, or the name of a pre-compiled native routine available in a dynamically loaded library. Setting rmeasure=NULL removes the measurement model simu-

lator. For more information, see ?rmeasure\_spec.

.. additional arguments supply new or modify existing model characteristics or

components. See pomp for a full list of recognized arguments.

When named arguments not recognized by pomp are provided, these are made available to all basic components via the so-called *userdata* facility. This allows the user to pass information to the basic components outside of the usual routes of covariates (covar) and model parameters (params). See ?userdata for

information on how to use this facility.

verbose logical; if TRUE, diagnostic messages will be printed to the console.

probe 89

#### **Details**

probe applies one or more "probes" to time series data and model simulations and compares the results. It can be used to diagnose goodness of fit and/or as the basis for "probe-matching", a generalized method-of-moments approach to parameter estimation.

A call to probe results in the evaluation of the probe(s) in probes on the data. Additionally, nsim simulated data sets are generated (via a call to simulate) and the probe(s) are applied to each of these. The results of the probe computations on real and simulated data are stored in an object of class 'probed\_pomp'.

When probe operates on a probe-matching objective function (a 'probe\_match\_objfun' object), by default, the random-number generator seed is fixed at the value given when the objective function was constructed. Specifying NULL or an integer for seed overrides this behavior.

#### Value

probe returns an object of class 'probed\_pomp', which contains the data and the model, together with the results of the probe calculation.

#### Methods

The following methods are available.

plot displays diagnostic plots.

summary displays summary information. The summary includes quantiles (fractions of simulations with probe values less than those realized on the data) and the corresponding two-sided p-values. In addition, the "synthetic likelihood" (Wood 2010) is computed, under the assumption that the probe values are multivariate-normally distributed.

**logLik** returns the synthetic likelihood for the probes. NB: in general, this is not the same as the likelihood.

**as.data.frame** coerces a 'probed\_pomp' to a 'data.frame'. The latter contains the realized values of the probes on the data and on the simulations. The variable .id indicates whether the probes are from the data or simulations.

### Author(s)

Daniel C. Reuman, Aaron A. King

# References

B.E. Kendall, C.J. Briggs, W.W. Murdoch, P. Turchin, S.P. Ellner, E. McCauley, R.M. Nisbet, and S.N. Wood. Why do populations cycle? A synthesis of statistical and mechanistic modeling approaches. *Ecology* **80**, 1789–1805, 1999.

S. N. Wood Statistical inference for noisy nonlinear ecological dynamic systems. *Nature* **466**, 1102–1104, 2010.

#### See Also

Other elementary POMP methods: pfilter(), pomp-package, simulate(), spect(), wpfilter() Other summary statistics methods: abc(), basic\_probes, probe.match, spect()

90 probe.match

probe.match

Probe matching

## **Description**

Estimation of parameters by maximum synthetic likelihood

# Usage

```
## S4 method for signature 'data.frame'
probe_objfun(
  data,
  est = character(0),
 fail.value = NA,
 probes,
  nsim,
  seed = NULL,
 params,
  rinit,
  rprocess,
  rmeasure,
 partrans,
  verbose = getOption("verbose", FALSE)
)
## S4 method for signature 'pomp'
probe_objfun(
 data,
  est = character(0),
  fail.value = NA,
 probes,
 nsim,
  seed = NULL,
  verbose = getOption("verbose", FALSE)
)
## S4 method for signature 'probed_pomp'
probe_objfun(
  data,
  est = character(0),
  fail.value = NA,
  probes,
 nsim,
  seed = NULL,
  . . . ,
```

probe.match 91

```
verbose = getOption("verbose", FALSE)
)

## S4 method for signature 'probe_match_objfun'
probe_objfun(
   data,
   est,
   fail.value,
   seed = NULL,
   ...,
   verbose = getOption("verbose", FALSE)
)
```

### **Arguments**

data either a data frame holding the time series data, or an object of class 'pomp',

i.e., the output of another **pomp** calculation.

est character vector; the names of parameters to be estimated.

fail.value optional numeric scalar; if non-NA, this value is substituted for non-finite values

of the objective function. It should be a large number (i.e., bigger than any

legitimate values the objective function is likely to take).

probes a single probe or a list of one or more probes. A probe is simply a scalar- or

vector-valued function of one argument that can be applied to the data array of a 'pomp'. A vector-valued probe must always return a vector of the same size. A number of useful probes are provided with the package: see basic probes.

nsim the number of model simulations to be computed.

seed integer. When fitting, it is often best to fix the seed of the random-number

generator (RNG). This is accomplished by setting seed to an integer. By default,

seed = NULL, which does not alter the RNG state.

params optional; named numeric vector of parameters. This will be coerced internally

to storage mode double.

rinit simulator of the initial-state distribution. This can be furnished either as a C

snippet, an R function, or the name of a pre-compiled native routine available in a dynamically loaded library. Setting rinit=NULL sets the initial-state simulator

to its default. For more information, see ?rinit\_spec.

rprocess simulator of the latent state process, specified using one of the rprocess plugins.

Setting rprocess=NULL removes the latent-state simulator. For more informa-

tion, see ?rprocess\_spec for the documentation on these plugins.

rmeasure simulator of the measurement model, specified either as a C snippet, an R func-

tion, or the name of a pre-compiled native routine available in a dynamically loaded library. Setting rmeasure=NULL removes the measurement model simulation.

lator. For more information, see ?rmeasure\_spec.

partrans optional parameter transformations, constructed using parameter\_trans.

Many algorithms for parameter estimation search an unconstrained space of parameters. When working with such an algorithm and a model for which the parameters are constrained, it can be useful to transform parameters. One should

92 probe.match

supply the partrans argument via a call to parameter\_trans. For more information, see ?parameter\_trans. Setting partrans=NULL removes the parameter transformations, i.e., sets them to the identity transformation.

additional arguments supply new or modify existing model characteristics or components. See pomp for a full list of recognized arguments.

When named arguments not recognized by pomp are provided, these are made available to all basic components via the so-called *userdata* facility. This allows the user to pass information to the basic components outside of the usual routes of covariates (covar) and model parameters (params). See ?userdata for information on how to use this facility.

verbose logical; if TRUE, diagnostic messages will be printed to the console.

#### **Details**

In probe-matching, one attempts to minimize the discrepancy between simulated and actual data, as measured by a set of summary statistics called *probes*. In **pomp**, this discrepancy is measured using the "synthetic likelihood" as defined by Wood (2010).

#### Value

probe\_objfun constructs a stateful objective function for probe matching. Specifically, probe\_objfun returns an object of class 'probe\_match\_objfun', which is a function suitable for use in an optim-like optimizer. In particular, this function takes a single numeric-vector argument that is assumed to contain the parameters named in est, in that order. When called, it will return the negative synthetic log likelihood for the probes specified. It is a stateful function: Each time it is called, it will remember the values of the parameters and its estimate of the synthetic likelihood.

#### **Important Note**

Since **pomp** cannot guarantee that the *final* call an optimizer makes to the function is a call *at* the optimum, it cannot guarantee that the parameters stored in the function are the optimal ones. Therefore, it is a good idea to evaluate the function on the parameters returned by the optimization routine, which will ensure that these parameters are stored.

#### Author(s)

Aaron A. King

#### See Also

```
optim subplex nloptr
```

Other summary statistics methods: abc(), basic\_probes, probe(), spect()

Other pomp parameter estimation methods: abc(), bsmc2(), kalman, mif2(), nlf, pmcmc(), pomp-package, spect.match

proposals 93

# **Examples**

```
library(magrittr)
gompertz() -> po
## A list of probes:
plist <- list(</pre>
 mean=probe.mean("Y",trim=0.1,transform=sqrt),
  sd=probe.sd("Y",transform=sqrt),
 probe.marginal("Y",ref=obs(po)),
 probe.acf("Y",lags=c(1,3,5),type="correlation",transform=sqrt),
 probe.quantile("Y",prob=c(0.25,0.75),na.rm=TRUE)
)
## Construct the probe-matching objective function.
## Here, we just want to estimate 'K'.
 probe_objfun(probes=plist,nsim=100,seed=5069977,
    est="K") -> f
## Any numerical optimizer can be used to minimize 'f'.
library(subplex)
subplex(fn=f,par=0.4,control=list(reltol=1e-5)) -> out
## Call the objective one last time on the optimal parameters:
f(out$par)
## There are 'plot' and 'summary' methods:
f %>% as("probed_pomp") %>% plot()
f %>% summary()
f %>% probe() %>% plot()
## One can modify the objective function with another call
## to 'probe_objfun':
f %>% probe_objfun(est=c("r","K")) -> f1
```

proposals

MCMC proposal distributions

# **Description**

Functions to construct proposal distributions for use with MCMC methods.

94 proposals

## Usage

```
mvn.diag.rw(rw.sd)
mvn.rw(rw.var)

mvn.rw.adaptive(
   rw.sd,
   rw.var,
   scale.start = NA,
   scale.cooling = 0.999,
   shape.start = NA,
   target = 0.234,
   max.scaling = 50
)
```

## **Arguments**

rw.sd

named numeric vector; random-walk SDs for a multivariate normal random-walk proposal with diagonal variance-covariance matrix.

rw.var

square numeric matrix with row- and column-names. Specifies the variance-covariance matrix for a multivariate normal random-walk proposal distribution.

scale.start, scale.cooling, shape.start, target, max.scaling

parameters to control the proposal adaptation algorithm. Beginning with MCMC iteration scale.start, the scale of the proposal covariance matrix will be adjusted in an effort to match the target acceptance ratio. This initial scale adjustment is "cooled", i.e., the adjustment diminishes as the chain moves along. The parameter scale.cooling specifies the cooling schedule: at n iterations after scale.start, the current scaling factor is multiplied with scale.cooling^n. The maximum scaling factor allowed at any one iteration is max.scaling. After shape.start accepted proposals have accumulated, a scaled empirical covariance matrix will be used for the proposals, following Roberts and Rosenthal (2009).

### Value

Each of these calls constructs a function suitable for use as the proposal argument of pmcmc or abc. Given a parameter vector, each such function returns a single draw from the corresponding proposal distribution.

### Author(s)

Aaron A. King, Sebastian Funk

### References

G.O. Roberts and J.S. Rosenthal. Examples of Adaptive MCMC. *Journal of Computational and Graphical Statistics* **18**, 349–367, 2009.

ricker 95

## See Also

```
pmcmc, abc
```

ricker

Ricker model with Poisson observations.

# **Description**

ricker is a 'pomp' object encoding a stochastic Ricker model with Poisson measurement error.

## Usage

```
ricker(r = \exp(3.8), sigma = 0.3, phi = 10, c = 1, N_0 = 7)
```

# **Arguments**

r	intrinsic growth rate
sigma	environmental process noise s.d.
phi	sampling rate
С	density dependence parameter
N 0	initial condition

# **Details**

The state process is  $N_{t+1} = rN_t \exp(-cN_t + e_t)$ , where the  $e_t$  are i.i.d. normal random deviates with zero mean and variance  $\sigma^2$ . The observed variables  $y_t$  are distributed as  $Poisson(\phi N_t)$ .

# Value

A 'pomp' object containing the Ricker model and simulated data.

# See Also

```
Other pomp examples: blowflies, bsflu, dacca(), ebola, gompertz(), measles, ou2(), parus, pomp_examples, rw2(), sir_models, verhulst()
```

# **Examples**

```
po <- ricker()
plot(po)
coef(po)
simulate(po) %>% plot()
```

96 rinit\_spec

# **Description**

Samples from the initial-state distribution.

# Usage

```
## S4 method for signature 'pomp'
rinit(object, params, t0, nsim = 1, ...)
```

# **Arguments**

object	an object of class 'pomp', or of a class that extends 'pomp'. This will typically be the output of pomp, simulate, or one of the <b>pomp</b> inference algorithms.
params	a npar $x$ nrep matrix of parameters. Each column is treated as an independent parameter set, in correspondence with the corresponding column of $x$ .
t0	the initial time, i.e., the time corresponding to the initial-state distribution.
nsim	optional integer; the number of initial states to simulate per column of params.
	additional arguments are ignored.

## Value

rinit returns an nvar x nsim\*ncol(params) matrix of state-process initial conditions when given an npar x nsim matrix of parameters, params, and an initial time t0. By default, t0 is the initial time defined when the 'pomp' object ws constructed.

## See Also

```
Specification of the initial-state distribution: rinit_spec

Other pomp workhorses: dmeasure(), dprior(), dprocess(), flow(), partrans(), rmeasure(), rprior(), rprocess(), skeleton(), workhorses
```

rinit_spec	The initial-state distribution

# **Description**

Specification of rinit

rinit\_spec 97

#### **Details**

To fully specify the unobserved Markov state process, one must give its distribution at the zero-time (t0). One does this by furnishing a value for the rinit argument. As usual, this can be provided either as a C snippet or as an R function. In the former case, bear in mind that:

- 1. The goal of a this snippet is the construction of a state vector, i.e., the setting of the dynamical states at time  $t_0$ .
- 2. In addition to the parameters and covariates (if any), the variable t, containing the zero-time, will be defined in the context in which the snippet is executed.
- 3. **NB:** The statenames argument plays a particularly important role when the rinit is specified using a C snippet. In particular, every state variable must be named in statenames. **Failure to follow this rule will result in undefined behavior.**

General rules for writing C snippets can be found here.

If an R function is to be used, pass

```
rinit = f
```

to pomp, where f is a function with arguments that can include the initial time t0, any of the model parameters, and any covariates. As usual, f may take additional arguments, provided these are passed along with it in the call to pomp. f must return a named numeric vector of initial states. It is of course important that the names of the states match the expectations of the other basic components.

Note that the state-process rinit can be either deterministic (as in the default) or stochastic. In the latter case, it samples from the distribution of the state process at the zero-time, t0.

# **Default behavior**

By default, pomp assumes that the initial distribution is concentrated on a single point. In particular, any parameters in params, the names of which end in "\_0" or ".0", are assumed to be initial values of states. When the state process is initialized, these are simply copied over as initial conditions. The names of the resulting state variables are obtained by dropping the suffix.

# See Also

Other information on model implementation: Csnippet, accumulators, covariate\_table(), distributions, dmeasure\_spec, dprocess\_spec, parameter\_trans(), pomp-package, prior\_spec, rmeasure\_spec, rprocess\_spec, skeleton\_spec, transformations, userdata

### **Examples**

```
## We set up a trivial process model:
trivial <- function (X, Y, ...) {
  c(X = X+1, Y = Y-1)
}
## We specify \code{rinit} with a function that
## sets state variables X and Y to the values in</pre>
```

98 rmeasure

```
## parameters X0, Y0:

f <- function (X0, Y0, ...) {
   c(X = X0, Y = Y0)
}

plot(simulate(times=1:5,t0=0,params=c(X0=3,Y0=-7),
        rinit=f,rprocess=onestep(trivial)))

## A function that depends on covariate P and
## time t0, as well as parameter X0:

g <- function (t0, X0, P, ...) {
   c(X = X0, Y = P + sin(2*pi*t0))
}

plot(simulate(times=1:5,t0=0,params=c(X0=3,Y0=-7),
   covar=covariate_table(t=0:10,P=3:13,times="t"),
   rinit=g,rprocess=onestep(trivial)))</pre>
```

rmeasure

rmeasure

# **Description**

Sample from the measurement model distribution, given values of the latent states and the parameters.

## Usage

```
## S4 method for signature 'pomp'
rmeasure(object, x, times, params, ...)
```

# **Arguments**

object	an object of class 'pomp', or of a class that extends 'pomp'. This will typically be the output of pomp, simulate, or one of the <b>pomp</b> inference algorithms.
X	an array containing states of the unobserved process. The dimensions of x are nvars x nrep x ntimes, where nvars is the number of state variables, nrep is the number of replicates, and ntimes is the length of times. One can also pass x as a named numeric vector, which is equivalent to the nrep=1, ntimes=1 case.
times	a numeric vector (length ntimes) containing times. These must be in non-decreasing order.
params	a npar $x$ nrep matrix of parameters. Each column is treated as an independent parameter set, in correspondence with the corresponding column of $x$ .
• • •	additional arguments are ignored.

rmeasure\_spec 99

#### Value

rmeasure returns a rank-3 array of dimensions nobs x nrep x ntimes, where nobs is the number of observed variables.

#### See Also

Specification of the measurement-model simulator: rmeasure\_spec

Other pomp workhorses: dmeasure(), dprior(), dprocess(), flow(), partrans(), rinit(), rprior(), rprocess(), skeleton(), workhorses

rmeasure\_spec

The measurement-model simulator

### **Description**

Specification of rmeasure

#### **Details**

The measurement model is the link between the data and the unobserved state process. It can be specified either by using one or both of the rmeasure and dmeasure arguments.

Suppose you have a procedure to simulate observations given the value of the latent state variables. Then you can furnish

```
rmeasure = f
```

to **pomp** algorithms, where f is a C snippet or R function that implements your procedure.

Using a C snippet is much preferred, due to its much greater computational efficiency. See Csnippet for general rules on writing C snippets.

In writing an rmeasure C snippet, bear in mind that:

- 1. The goal of such a snippet is to fill the observables with random values drawn from the measurement model distribution. Accordingly, each observable should be assigned a new value.
- 2. In addition to the states, parameters, covariates (if any), and observables, the variable t, containing the time of the observation, will be defined in the context in which the snippet is executed.

The demos and the tutorials on the package website give examples as well.

It is also possible, though far less efficient, to specify rmeasure using an R function. In this case, specify the measurement model simulator by furnishing

```
rmeasure = f
```

to pomp, where f is an R function. The arguments of f should be chosen from among the state variables, parameters, covariates, and time. It must also have the argument . . . . f must return a named numeric vector of length equal to the number of observable variables.

100 rprior

## **Default behavior**

The default rmeasure is undefined. It will yield missing values (NA).

# See Also

Other information on model implementation: Csnippet, accumulators, covariate\_table(), distributions, dmeasure\_spec, dprocess\_spec, parameter\_trans(), pomp-package, prior\_spec, rinit\_spec, rprocess\_spec, skeleton\_spec, transformations, userdata

rprior rprior

## **Description**

Sample from the prior probability distribution.

# Usage

```
## S4 method for signature 'pomp'
rprior(object, params, ...)
```

# **Arguments**

object	an object of class 'pomp', or of a class that extends 'pomp'. This will typically be the output of pomp, simulate, or one of the <b>pomp</b> inference algorithms.
params	a npar $x$ nrep matrix of parameters. Each column is treated as an independent parameter set, in correspondence with the corresponding column of $x$ .
	additional arguments are ignored.

# Value

A numeric matrix containing the required samples.

### See Also

```
Specification of the prior distribution simulator: prior_spec

Other pomp workhorses: dmeasure(), dprior(), dprocess(), flow(), partrans(), rinit(), rmeasure(), rprocess(), skeleton(), workhorses
```

rprocess 101

# **Description**

rprocess simulates the process-model portion of partially-observed Markov process.

# Usage

```
## S4 method for signature 'pomp'
rprocess(object, x0, t0, times, params, ...)
```

# Arguments

object	an object of class 'pomp', or of a class that extends 'pomp'. This will typically be the output of pomp, simulate, or one of the <b>pomp</b> inference algorithms.
x0	an nvar x nrep matrix containing the starting state of the system. Columns of x0 correspond to states; rows to components of the state vector. One independent simulation will be performed for each column. Note that in this case, params must also have nrep columns.
t0	the initial time, i.e., the time corresponding to the state in $x0$ .
times	a numeric vector (length ntimes) containing times. These must be in non-decreasing order.
params	a npar x nrep matrix of parameters. Each column is treated as an independent parameter set, in correspondence with the corresponding column of $x0$ .
	additional arguments are ignored.

#### **Details**

When rprocess is called, t0 is taken to be the initial time (i.e., that corresponding to x0). The values in times are the times at which the state of the simulated processes are required.

#### Value

```
rprocess returns a rank-3 array with rownames. Suppose x is the array returned. Then dim(x)=c(nvars,nrep,ntimes),
```

where nvars is the number of state variables (=nrow(x0)), nrep is the number of independent realizations simulated (=ncol(x0)), and ntimes is the length of the vector times. x[,j,k] is the value of the state process in the j-th realization at time times[k]. The rownames of x will correspond to those of x0.

# See Also

```
Specification of the process-model simulator: rprocess_spec
Other pomp workhorses: dmeasure(), dprior(), dprocess(), flow(), partrans(), rinit(),
rmeasure(), rprior(), skeleton(), workhorses
```

102 rprocess\_spec

rprocess\_spec

The latent state process simulator

# **Description**

Specification of rprocess using "plugins".

# Usage

```
onestep(step.fun)
discrete_time(step.fun, delta.t = 1)
euler(step.fun, delta.t)
gillespie(rate.fun, v, hmax = Inf)
gillespie_hl(..., .pre = "", .post = "", hmax = Inf)
```

#### **Arguments**

step.fun a C snippet, an R function, or the name of a native routine in a shared-object

library. This gives a procedure by which one simulates a single step of the latent

state process.

delta.t positive numerical value; for euler and discrete\_time, the size of the step to

take

rate. fun a C snippet, an R function, or the name of a native routine in a shared-object

library. This gives a procedure by which one computes the event-rate of the

elementary events in the continuous-time latent Markov chain.

v integer matrix; giving the stoichiometry of the continuous-time latent Markov process. It should have dimensions nvar x nevent, where nvar is the number

of state variables and nevent is the number of elementary events. v describes the changes that occur in each elementary event: it will usually comprise the values 1, -1, and 0 according to whether a state variable is incremented, decremented, or unchanged in an elementary event. The rows of v may be unnamed or named. If the rows are unnamed, they are assumed to be in the same order as the vector of state variables returned by rinit. If the rows are named, the names of the state variables returned by rinit will be matched to the rows of v to ensure a correct mapping. If any of the row names of v cannot be found among the state

variables or if any row names of v are duplicated, an error will occur.

hmax maximum time step allowed (see below)

... individual C snippets corresponding to elementary events

.pre, .post C snippets (see Details)

rprocess\_spec 103

### **Discrete-time processes**

If the state process evolves in discrete time, specify rprocess using the discrete\_time plug-in. Specifically, provide

```
rprocess = discrete_time(step.fun = f, delta.t),
```

where f is a C snippet or R function that simulates one step of the state process. The former is the preferred option, due to its much greater computational efficiency. The goal of such a C snippet is to replace the state variables with their new random values at the end of the time interval. Accordingly, each state variable should be over-written with its new value. In addition to the states, parameters, covariates (if any), and observables, the variables t and dt, containing respectively the time at the beginning of the step and the step's duration, will be defined in the context in which the C snippet is executed. See Csnippet for general rules on writing C snippets. Examples are to be found in the tutorials on the package website.

If f is given as an R function, its arguments should come from the state variables, parameters, covariates, and time. It may also take the argument 'delta.t'; when called, the latter will be the time-step. It must also have the argument '...'. It should return a named vector of length equal to the number of state variables, representing a draw from the distribution of the state process at time t+delta.t conditional on its value at time t.

### **Continuous-time processes**

If the state process evolves in continuous time, but you can use an Euler approximation, implement rprocess using the euler plug-in. Specify

```
rprocess = euler(step.fun = f, delta.t)
```

in this case. As before, f can be provided either as a C snippet or as an R function, the former resulting in much quicker computations. The form of f will be the same as above (in the discrete-time case).

If you have a procedure that allows you, given the value of the state process at any time, to simulate it at an arbitrary time in the future, use the onestep plug-in. To do so, specify

```
rprocess = onestep(step.fun = f).
```

Again, f can be provided either as a C snippet or as an R function, the former resulting in much quicker computations. The form of f should be as above (in the discrete-time or Euler cases).

# Size of time step

The simulator plug-ins discrete\_time, euler, and onestep all work by taking discrete time steps. They differ as to how this is done. Specifically,

- 1. onestep takes a single step to go from any given time t1 to any later time t2 (t1 < t2). Thus, this plug-in is designed for use in situations where a closed-form solution to the process exists.
- 2. To go from t1 to t2, euler takes n steps of equal size, where

```
n = ceiling((t2-t1)/delta.t).
```

104 rprocess\_spec

 discrete\_time assumes that the process evolves in discrete time, where the interval between successive times is delta.t. Thus, to go from t1 to t2, discrete\_time takes n steps of size exactly delta.t, where

```
n = floor((t2-t1)/delta.t).
```

#### **Exact (event-driven) simulations**

If you desire exact simulation of certain continuous-time Markov chains, an implementation of Gillespie's algorithm (Gillespie 1977) is available, via the gillespie and gillespie\_hl plug-ins. The former allows for the rate function to be provided as an R function or a single C snippet, while the latter provides a means of specifying the elementary events via a list of C snippets.

A high-level interface to the simulator is provided by gillespie\_hl. To use it, supply

```
rprocess = gillespie_hl(..., .pre = "", .post = "", hmax = Inf)
```

to pomp. Each argument in ... corresponds to a single elementary event and should be a list containing two elements. The first should be a string or C snippet; the second should be a named integer vector. The variable rate will exist in the context of the C snippet, as will the parameter, state variables, covariates, and the time t. The C snippet should assign to the variable rate the corresponding elementary event rate.

The named integer vector specifies the changes to the state variables corresponding to the elementary event. There should be named value for each of the state variables returned by rinit. The arguments .pre and .post can be used to provide C code that will run respectively before and after the elementary-event snippets. These hooks can be useful for avoiding duplication of code that performs calculations needed to obtain several of the different event rates.

Here's how a simple birth-death model might be specified:

```
gillespie_hl(
    birth=list("rate = b*N;",c(N=1)),
    death=list("rate = m*N;",c(N=-1))
)
```

In the above, the state variable N represents the population size and parameters b, m are the birth and death rates, respectively.

To use the lower-level gillespie interface, furnish

```
rprocess = gillespie(rate.fun = f, v, hmax = Inf)
```

to pomp, where f gives the rates of the elementary events. Here, f may be an R function with prototype

```
f(j, x, t, params, ...)
```

When f is called, the integer j will be the number of the elementary event (corresponding to the column the matrix v, see below), x will be a named numeric vector containing the value of the state process at time t and params is a named numeric vector containing parameters. f should return a single numerical value, representing the rate of that elementary event at that point in state space and time.

rw.sd

Here, the stoichiometric matrix v specifies the continuous-time Markov process in terms of its elementary events. It should have dimensions nvar x nevent, where nvar is the number of state variables and nevent is the number of elementary events. v describes the changes that occur in each elementary event: it will usually comprise the values 1, -1, and 0 according to whether a state variable is incremented, decremented, or unchanged in an elementary event. The rows of v should have names corresponding to the state variables. If any of the row names of v cannot be found among the state variables or if any row names of v are duplicated, an error will occur.

It is also possible to provide a C snippet via the rate. fun argument to gillespie. Such a snippet should assign the correct value to a rate variable depending on the value of j. The same variables will be available as for the C code provided to gillespie\_hl. This lower-level interface may be preferable if it is easier to write code that calculates the correct rate based on j rather than to write a snippet for each possible value of j. For example, if the number of possible values of j is large and the rates vary according to a few simple rules, the lower-level interface may provide the easier way of specifying the model.

When the process is non-autonomous (i.e., the event rates depend explicitly on time), it can be useful to set hmax to the maximum step that will be taken. By default, the elementary event rates will be recomputed at least once per observation interval.

#### **Default behavior**

The default rprocess is undefined. It will yield missing values (NA) for all state variables.

#### See Also

Other information on model implementation: Csnippet, accumulators, covariate\_table(), distributions, dmeasure\_spec, dprocess\_spec, parameter\_trans(), pomp-package, prior\_spec, rinit\_spec, rmeasure\_spec, skeleton\_spec, transformations, userdata

rw.sd rw.sd

## **Description**

Specifying random-walk intensities.

#### Usage

```
rw.sd(...)
```

# **Arguments**

... Specification of the random-walk intensities (as standard deviations).

### Details

See mif2 for details.

106 rw2

## See Also

mif2

rw2

Two-dimensional random-walk process

# **Description**

rw2 constructs a 'pomp' object encoding a 2-D Gaussian random walk.

# Usage

```
rw2(x1_0 = 0, x2_0 = 0, s1 = 1, s2 = 3, tau = 1, times = 1:100, t0 = 0)
```

# **Arguments**

```
    x1_0, x2_0 initial conditions (i.e., latent state variable values at the zero time t0)
    s1, s2 random walk intensities
    tau observation error s.d.
    times observation times
    zero time
```

## **Details**

The random-walk process is fully but noisily observed.

## Value

A 'pomp' object containing simulated data.

# See Also

```
Other pomp examples: blowflies, bsflu, dacca(), ebola, gompertz(), measles, ou2(), parus, pomp_examples, ricker(), sir_models, verhulst()
```

## **Examples**

```
library(ggplot2)
rw2() %>% plot()
rw2(s1=1,s2=1,tau=0.1) %>%
    simulate(nsim=10,format="d") %>%
    ggplot(aes(x=y1,y=y2,group=.id,color=.id))+
    geom_path()+
    guides(color=FALSE)+
    theme_bw()
```

sannbox 107

## **Description**

A straightforward implementation of simulated annealing with box constraints.

## Usage

```
sannbox(par, fn, control = list(), ...)
```

# **Arguments**

par	Initial values for the parameters to be optimized over.
fn	A function to be minimized, with first argument the vector of parameters over which minimization is to take place. It should return a scalar result.
control	A named list of control parameters. See 'Details'.
	ignored.

### **Details**

The control argument is a list that can supply any of the following components:

**trace** Non-negative integer. If positive, tracing information on the progress of the optimization is produced. Higher values may produce more tracing information.

**fnscale** An overall scaling to be applied to the value of fn during optimization. If negative, turns the problem into a maximization problem. Optimization is performed on fn(par)/fnscale.

parscale A vector of scaling values for the parameters. Optimization is performed on par/parscale and these should be comparable in the sense that a unit change in any element produces about a unit change in the scaled value.

**maxit** The total number of function evaluations: there is no other stopping criterion. Defaults to 10000.

**temp** starting temperature for the cooling schedule. Defaults to 1.

tmax number of function evaluations at each temperature. Defaults to 10.

**candidate.dist** function to randomly select a new candidate parameter vector. This should be a function with three arguments, the first being the current parameter vector, the second the temperature, and the third the parameter scaling. By default, candidate.dist is

**sched** cooling schedule. A function of a three arguments giving the temperature as a function of iteration number and the control parameters temp and tmax. By default, sched is

```
function(k, temp, tmax) temp/log(((k-1)\%/\%tmax)*tmax+exp(1)).
```

108 simulate

Alternatively, one can supply a numeric vector of temperatures. This must be of length at least maxit.

**lower,upper** optional numeric vectors. These describe the lower and upper box constraints, respectively. Each can be specified either as a single scalar (common to all parameters) or as a vector of the same length as par. By default, lower=-Inf and upper=Inf, i.e., there are no constraints.

#### Value

sannbox returns a list with components:

**counts** two-element integer vector. The first number gives the number of calls made to fn. The second number is provided for compatibility with optim and will always be NA.

**convergence** provided for compatibility with optim; will always be 0.

final.params last tried value of par.

final.value value of fn corresponding to final.params.

par best tried value of par.

value value of fn corresponding to par.

## Author(s)

Daniel Reuman, Aaron A. King

### See Also

```
traj.match, probe.match.
```

simulate

Simulations of a partially-observed Markov process

# Description

simulate generates simulations of the state and measurement processes.

## Usage

```
## S4 method for signature 'missing'
simulate(
   nsim = 1,
   seed = NULL,
   times,
   t0,
   params,
   rinit,
   rprocess,
   rmeasure,
```

simulate 109

```
format = c("pomps", "arrays", "data.frame"),
  include.data = FALSE,
  verbose = getOption("verbose", FALSE)
)
## S4 method for signature 'data.frame'
simulate(
 object.
 nsim = 1,
  seed = NULL,
  times,
  t0,
  params,
  rinit,
  rprocess,
  rmeasure,
  format = c("pomps", "arrays", "data.frame"),
  include.data = FALSE,
  verbose = getOption("verbose", FALSE)
)
## S4 method for signature 'pomp'
simulate(
 object,
 nsim = 1,
  seed = NULL,
  format = c("pomps", "arrays", "data.frame"),
  include.data = FALSE,
  verbose = getOption("verbose", FALSE)
)
## S4 method for signature 'objfun'
simulate(object, nsim = 1, seed = NULL, ...)
```

# **Arguments**

nsim The number of simulations to perform. Note that the number of replicates will

be nsim times ncol(params).

seed optional; if set, the pseudorandom number generator (RNG) will be initialized

with seed. the random seed to use. The RNG will be restored to its original

state afterward.

times the times at which observations are made. times must indicate the column of

observation times by name or index. The time vector must be numeric and non-decreasing. Internally, data will be internally coerced to an array with storage-

mode double.

110 simulate

The zero-time, i.e., the time of the initial state. This must be no later than the t0 time of the first observation, i.e.,  $t0 \le times[1]$ .

a named numeric vector or a matrix with rownames containing the parameters

at which the simulations are to be performed.

simulator of the initial-state distribution. This can be furnished either as a C rinit

snippet, an R function, or the name of a pre-compiled native routine available in a dynamically loaded library. Setting rinit=NULL sets the initial-state simulator

to its default. For more information, see ?rinit\_spec.

rprocess simulator of the latent state process, specified using one of the rprocess plugins.

Setting rprocess=NULL removes the latent-state simulator. For more informa-

tion, see ?rprocess spec for the documentation on these plugins.

rmeasure simulator of the measurement model, specified either as a C snippet, an R function, or the name of a pre-compiled native routine available in a dynamically

loaded library. Setting rmeasure=NULL removes the measurement model simu-

lator. For more information, see ?rmeasure\_spec.

format the format in which to return the results.

> format = "pomps" causes the results to be returned as a single "pomp" object, identical to object except for the latent states and observations, which have been replaced by the simulated values.

> format = "arrays" causes the results to be returned as a list of two arrays. The "states" element will contain the simulated state trajectories in a rank-3 array with dimensions nvar x (ncol(params)\*nsim) x ntimes. Here, nvar is the number of state variables and ntimes the length of the argument times. The "obs" element will contain the simulated data, returned as a rank-3 array with dimensions nobs x (ncol(params)\*nsim) x ntimes. Here, nobs is the number of observables.

> format = "data. frame" causes the results to be returned as a single data frame containing the time, states, and observations. An ordered factor variable, '.id', distinguishes one simulation from another.

if TRUE, the original data are included (with .id = "rep"). This option is ignored include.data

unless format = "data.frame".

additional arguments supply new or modify existing model characteristics or components. See pomp for a full list of recognized arguments.

When named arguments not recognized by pomp are provided, these are made available to all basic components via the so-called userdata facility. This allows the user to pass information to the basic components outside of the usual routes of covariates (covar) and model parameters (params). See ?userdata for

information on how to use this facility.

verbose logical; if TRUE, diagnostic messages will be printed to the console.

optional; if present, it should be the output of one of pomp's methods object

#### Value

A single "pomp" object, a "pompList" object, a named list of two arrays, or a data frame, according to the format option.

params

. . .

sir\_models 111

If params is a matrix, each column is treated as a distinct parameter set. In this case, if nsim=1, then simulate will return one simulation for each parameter set. If nsim>1, then simulate will yield nsim simulations for each parameter set. These will be ordered such that the first ncol(params) simulations represent one simulation from each of the distinct parameter sets, the second ncol(params) simulations represent a second simulation from each, and so on.

Adding column names to params can be helpful.

## Author(s)

Aaron A. King

#### See Also

Other elementary POMP methods: pfilter(), pomp-package, probe(), spect(), wpfilter()

sir\_models

Compartmental epidemiological models

## **Description**

Simple SIR-type models implemented in various ways.

## Usage

```
sir(
  gamma = 26,
 mu = 0.02,
 iota = 0.01,
 beta1 = 400,
 beta2 = 480,
 beta3 = 320,
 beta_sd = 0.001,
  rho = 0.6,
  pop = 2100000,
  S_0 = 26/400,
  I_0 = 0.001,
 R_0 = 1 - S_0 - I_0
  t0 = 0,
  times = seq(from = t0 + 1/52, to = t0 + 4, by = 1/52),
  seed = 329343545,
  delta.t = 1/52/20
sir2(
 gamma = 24,
 mu = 1/70,
 iota = 0.1,
```

112 sir\_models

```
beta1 = 330,
beta2 = 410,
beta3 = 490,
rho = 0.1,
pop = 1e+06,
S_0 = 0.05,
I_0 = 1e-04,
R_0 = 1 - S_0 - I_0,
t0 = 0,
times = seq(from = t0 + 1/12, to = t0 + 10, by = 1/12),
seed = 1772464524
)
```

## **Arguments**

gamma recovery rate death rate (assumed equal to the birth rate) mu infection import rate iota beta1, beta2, beta3 seasonal contact rates environmental noise intensity beta\_sd reporting efficiency rho pop overall host population size S\_0, I\_0, R\_0 the fractions of the host population that are susceptible, infectious, and recovered, respectively, at time zero. t0 zero time times observation times seed seed of the random number generator delta.t Euler step size

# Details

sir() produces a 'pomp' object encoding a simple seasonal SIR model with simulated data. Simulation is performed using an Euler multinomial approximation.

sir2() has the same model implemented using Gillespie's algorithm.

This and similar examples are discussed and constructed in tutorials available on the package website.

#### Value

These functions return 'pomp' objects containing simulated data.

## See Also

```
Other pomp examples: blowflies, bsflu, dacca(), ebola, gompertz(), measles, ou2(), parus, pomp_examples, ricker(), rw2(), verhulst()
```

skeleton 113

## **Examples**

```
po <- sir()
plot(po)
coef(po)

po <- sir2()
plot(po)
plot(simulate(window(po,end=3)))
coef(po)</pre>
```

skeleton

skeleton

# **Description**

Evaluates the deterministic skeleton at a point or points in state space, given parameters. In the case of a discrete-time system, the skeleton is a map. In the case of a continuous-time system, the skeleton is a vectorfield. NB: skeleton just evaluates the deterministic skeleton; it does not iterate or integrate (see trajectory for this).

# Usage

```
## S4 method for signature 'pomp'
skeleton(object, x, times, params, ...)
```

# Arguments

object	an object of class 'pomp', or of a class that extends 'pomp'. This will typically be the output of pomp, simulate, or one of the <b>pomp</b> inference algorithms.
X	an array containing states of the unobserved process. The dimensions of x are nvars x nrep x ntimes, where nvars is the number of state variables, nrep is the number of replicates, and ntimes is the length of times. One can also pass x as a named numeric vector, which is equivalent to the nrep=1, ntimes=1 case.
times	a numeric vector (length ntimes) containing times. These must be in non-decreasing order.
params	a npar $x$ nrep matrix of parameters. Each column is treated as an independent parameter set, in correspondence with the corresponding column of $x$ .
	additional arguments are ignored.

# Value

skeleton returns an array of dimensions nvar x nrep x ntimes. If f is the returned matrix, f[i,j,k] is the i-th component of the deterministic skeleton at time times[k] given the state x[j,k] and parameters params[,j].

114 skeleton\_spec

## See Also

Specification of the deterministic skeleton: skeleton\_spec

Other pomp workhorses: dmeasure(), dprior(), dprocess(), flow(), partrans(), rinit(), rmeasure(), rprior(), rprocess(), workhorses

skeleton\_spec

The deterministic skeleton of a model

## **Description**

Specification of skeleton.

## Usage

```
vectorfield(f)
map(f, delta.t = 1)
```

## **Arguments**

f procedure for evaluating the deterministic skeleton This can be a C snippet, an R function, or the name of a native routine in a dynamically linked library.

delta.t positive numerical value; the size of the discrete time step corresponding to an application of the map

# **Details**

The skeleton is a dynamical system that expresses the central tendency of the unobserved Markov state process. As such, it is not uniquely defined, but can be both interesting in itself and useful in practice. In **pomp**, the skeleton is used by trajectory and traj.match.

If the state process is a discrete-time stochastic process, then the skeleton is a discrete-time map. To specify it, provide

```
skeleton = map(f, delta.t)
```

to pomp, where f implements the map and delta.t is the size of the timestep covered at one map iteration.

If the state process is a continuous-time stochastic process, then the skeleton is a vectorfield (i.e., a system of ordinary differential equations). To specify it, supply

```
skeleton = vectorfield(f)
```

to pomp, where f implements the vectorfield, i.e., the right-hand-size of the differential equations.

In either case, f can be furnished either as a C snippet (the preferred choice), or an R function. General rules for writing C snippets can be found here. In writing a skeleton C snippet, be aware that:

spect 115

1. For each state variable, there is a corresponding component of the deterministic skeleton. The goal of such a snippet is to compute all the components.

- 2. When the skeleton is a map, the component corresponding to state variable x is named Dx and is the new value of x after one iteration of the map.
- 3. When the skeleton is a vectorfield, the component corresponding to state variable x is named Dx and is the value of dx/dt.
- 4. As with the other C snippets, all states, parameters and covariates, as well as the current time, t, will be defined in the context within which the snippet is executed.

The tutorials on the package website give some examples.

If f is an R function, its arguments should be taken from among the state variables, parameters, covariates, and time. It must also take the argument '...'. As with the other basic components, f may take additional arguments, provided these are passed along with it in the call to pomp. The function f must return a numeric vector of the same length as the number of state variables, which contains the value of the map or vectorfield at the required point and time.

## **Default behavior**

The default skeleton is undefined. It will yield missing values (NA) for all state variables.

#### See Also

Other information on model implementation: Csnippet, accumulators, covariate\_table(), distributions, dmeasure\_spec, dprocess\_spec, parameter\_trans(), pomp-package, prior\_spec, rinit\_spec, rmeasure\_spec, rprocess\_spec, transformations, userdata

spect

Power spectrum

## **Description**

Power spectrum computation and spectrum-matching for partially-observed Markov processes.

## Usage

```
## $4 method for signature 'data.frame'
spect(
   data,
   vars,
   kernel.width,
   nsim,
   seed = NULL,
   transform.data = identity,
   detrend = c("none", "mean", "linear", "quadratic"),
   params,
   rinit,
```

spect spect

```
rprocess,
  rmeasure,
  verbose = getOption("verbose", FALSE)
)
## S4 method for signature 'pomp'
spect(
 data,
  vars,
  kernel.width,
 nsim,
  seed = NULL,
  transform.data = identity,
 detrend = c("none", "mean", "linear", "quadratic"),
  verbose = getOption("verbose", FALSE)
)
## S4 method for signature 'spectd_pomp'
spect(
 data,
  vars,
 kernel.width,
 nsim,
  seed = NULL,
  transform.data,
 detrend,
 verbose = getOption("verbose", FALSE)
)
## S4 method for signature 'spect_match_objfun'
spect(data, seed, ..., verbose = getOption("verbose", FALSE))
## S4 method for signature 'objfun'
spect(data, seed = NULL, ...)
```

## **Arguments**

data	either a data frame holding the time series data, or an object of class 'pomp', i.e., the output of another <b>pomp</b> calculation.
vars	optional; names of observed variables for which the power spectrum will be computed. By default, the spectrum will be computed for all observables.
kernel.width	width parameter for the smoothing kernel used for calculating the estimate of the spectrum.
nsim	number of model simulations to be computed.

spect 117

seed optional; if non-NULL, the random number generator will be initialized with this seed for simulations. See simulate.

transform.data function; this transformation will be applied to the observables prior to estima-

tion of the spectrum, and prior to any detrending.

detrend de-trending operation to perform. Options include no detrending, and subtrac-

tion of constant, linear, and quadratic trends from the data. Detrending is applied

to each data series and to each model simulation independently.

params optional; named numeric vector of parameters. This will be coerced internally

to storage mode double.

rinit simulator of the initial-state distribution. This can be furnished either as a C

snippet, an R function, or the name of a pre-compiled native routine available in a dynamically loaded library. Setting rinit=NULL sets the initial-state simulator

to its default. For more information, see ?rinit\_spec.

rprocess simulator of the latent state process, specified using one of the rprocess plugins.

Setting rprocess=NULL removes the latent-state simulator. For more informa-

tion, see ?rprocess\_spec for the documentation on these plugins.

rmeasure simulator of the measurement model, specified either as a C snippet, an R func-

tion, or the name of a pre-compiled native routine available in a dynamically loaded library. Setting rmeasure=NULL removes the measurement model simu-

lator. For more information, see ?rmeasure\_spec.

.. additional arguments supply new or modify existing model characteristics or

components. See pomp for a full list of recognized arguments.

When named arguments not recognized by pomp are provided, these are made available to all basic components via the so-called *userdata* facility. This allows the user to pass information to the basic components outside of the usual routes of covariates (covar) and model parameters (params). See ?userdata for

information on how to use this facility.

verbose logical; if TRUE, diagnostic messages will be printed to the console.

## Details

spect estimates the power spectrum of time series data and model simulations and compares the results. It can be used to diagnose goodness of fit and/or as the basis for frequency-domain parameter estimation (spect.match).

A call to spect results in the estimation of the power spectrum for the (transformed, detrended) data and nsim model simulations. The results of these computations are stored in an object of class 'spectd\_pomp'.

When spect operates on a spectrum-matching objective function (a 'spect\_match\_objfun' object), by default, the random-number generator seed is fixed at the value given when the objective function was constructed. Specifying NULL or an integer for seed overrides this behavior.

## Value

An object of class 'spectd\_pomp', which contains the model, the data, and the results of the spect computation. The following methods are available:

```
plot produces some diagnostic plotssummary displays a summarylogLik gives a measure of the agreement of the power spectra
```

# Author(s)

Daniel C. Reuman, Cai GoGwilt, Aaron A. King

## References

D.C. Reuman, R.A. Desharnais, R.F. Costantino, O. Ahmad, J.E. Cohen. Power spectra reveal the influence of stochasticity on nonlinear population dynamics. *Proceedings of the National Academy of Sciences* **103**, 18860-18865, 2006

D.C. Reuman, R.F. Costantino, R.A. Desharnais, J.E. Cohen. Color of environmental noise affects the nonlinear dynamics of cycling, stage-structured populations. *Ecology Letters* **11**, 820-830, 2008.

# See Also

```
Other summary statistics methods: abc(), basic_probes, probe.match, probe()
Other elementary POMP methods: pfilter(), pomp-package, probe(), simulate(), wpfilter()
```

spect.match

Spectrum matching

## **Description**

Estimation of parameters by matching power spectra

# Usage

```
## S4 method for signature 'data.frame'
spect_objfun(
 data,
 est = character(0),
 weights = 1,
  fail.value = NA,
  vars,
  kernel.width,
  nsim,
  seed = NULL,
  transform.data = identity,
  detrend = c("none", "mean", "linear", "quadratic"),
  params,
  rinit,
  rprocess,
  rmeasure,
```

```
partrans,
 verbose = getOption("verbose", FALSE)
)
## S4 method for signature 'pomp'
spect_objfun(
 data,
 est = character(0),
 weights = 1,
 fail.value = NA,
  vars,
  kernel.width,
 nsim,
  seed = NULL,
  transform.data = identity,
 detrend = c("none", "mean", "linear", "quadratic"),
  verbose = getOption("verbose", FALSE)
## S4 method for signature 'spectd_pomp'
spect_objfun(
 data,
 est = character(0),
 weights = 1,
 fail.value = NA,
 vars,
 kernel.width,
 nsim,
  seed = NULL,
  transform.data = identity,
 detrend,
  verbose = getOption("verbose", FALSE)
)
## S4 method for signature 'spect_match_objfun'
spect_objfun(
 data,
 est,
 weights,
 fail.value,
 seed = NULL,
 verbose = getOption("verbose", FALSE)
)
```

## Arguments

data either a data frame holding the time series data, or an object of class 'pomp',

i.e., the output of another **pomp** calculation.

est character vector; the names of parameters to be estimated.

weights optional numeric or function. The mismatch between model and data is mea-

sured by a weighted average of mismatch at each frequency. By default, all frequencies are weighted equally. weights can be specified either as a vector (which must have length equal to the number of frequencies) or as a function of frequency. If the latter, weights(freq) must return a nonnegative weight for

each frequency.

fail.value optional numeric scalar; if non-NA, this value is substituted for non-finite values

of the objective function. It should be a large number (i.e., bigger than any

legitimate values the objective function is likely to take).

vars optional; names of observed variables for which the power spectrum will be

computed. By default, the spectrum will be computed for all observables.

kernel.width width parameter for the smoothing kernel used for calculating the estimate of

the spectrum.

nsim the number of model simulations to be computed.

seed integer. When fitting, it is often best to fix the seed of the random-number

generator (RNG). This is accomplished by setting seed to an integer. By default,

seed = NULL, which does not alter the RNG state.

transform.data function; this transformation will be applied to the observables prior to estima-

tion of the spectrum, and prior to any detrending.

detrend de-trending operation to perform. Options include no detrending, and subtrac-

tion of constant, linear, and quadratic trends from the data. Detrending is applied

to each data series and to each model simulation independently.

params optional; named numeric vector of parameters. This will be coerced internally

to storage mode double.

rinit simulator of the initial-state distribution. This can be furnished either as a C

snippet, an R function, or the name of a pre-compiled native routine available in a dynamically loaded library. Setting rinit=NULL sets the initial-state simulator

to its default. For more information, see ?rinit\_spec.

rprocess simulator of the latent state process, specified using one of the rprocess plugins.

Setting rprocess=NULL removes the latent-state simulator. For more informa-

tion, see ?rprocess\_spec for the documentation on these plugins.

rmeasure simulator of the measurement model, specified either as a C snippet, an R func-

tion, or the name of a pre-compiled native routine available in a dynamically loaded library. Setting rmeasure=NULL removes the measurement model simu-

lator. For more information, see ?rmeasure\_spec.

partrans optional parameter transformations, constructed using parameter\_trans.

Many algorithms for parameter estimation search an unconstrained space of parameters. When working with such an algorithm and a model for which the parameters are constrained, it can be useful to transform parameters. One should

supply the partrans argument via a call to parameter\_trans. For more information, see ?parameter\_trans. Setting partrans=NULL removes the parameter transformations, i.e., sets them to the identity transformation.

additional arguments supply new or modify existing model characteristics or components. See pomp for a full list of recognized arguments.

When named arguments not recognized by pomp are provided, these are made available to all basic components via the so-called *userdata* facility. This allows the user to pass information to the basic components outside of the usual routes of covariates (covar) and model parameters (params). See ?userdata for information on how to use this facility.

verbose logical; if TRUE, diagnostic messages will be printed to the console.

#### **Details**

In spectrum matching, one attempts to minimize the discrepancy between a POMP model's predictions and data, as measured in the frequency domain by the power spectrum.

spect\_objfun constructs an objective function that measures the discrepancy. It can be passed to any one of a variety of numerical optimization routines, which will adjust model parameters to minimize the discrepancies between the power spectrum of model simulations and that of the data.

#### Value

spect\_objfun constructs a stateful objective function for spectrum matching. Specifically, spect\_objfun returns an object of class 'spect\_match\_objfun', which is a function suitable for use in an optim-like optimizer. This function takes a single numeric-vector argument that is assumed to contain the parameters named in est, in that order. When called, it will return the (optionally weighted)  $L^2$  distance between the data spectrum and simulated spectra. It is a stateful function: Each time it is called, it will remember the values of the parameters and the discrepancy measure.

## **Important Note**

Since **pomp** cannot guarantee that the *final* call an optimizer makes to the function is a call *at* the optimum, it cannot guarantee that the parameters stored in the function are the optimal ones. Therefore, it is a good idea to evaluate the function on the parameters returned by the optimization routine, which will ensure that these parameters are stored.

## See Also

```
spect optim subplex nloptr
Other pomp parameter estimation methods: abc(), bsmc2(), kalman, mif2(), nlf, pmcmc(),
pomp-package, probe.match
```

## **Examples**

```
library(magrittr)
ricker() %>%
  spect_objfun(
```

states states

```
est=c("r","sigma","N_0"),
    partrans=parameter_trans(log=c("r","sigma","N_0")),
    paramnames=c("r","sigma","N_0"),
    kernel.width=3,
    nsim=100,
    seed=5069977
) -> f

f(log(c(20,0.3,10)))
f %>% spect() %>% plot()

library(subplex)
subplex(fn=f,par=log(c(20,0.3,10)),control=list(reltol=1e-5)) -> out
f(out$par)
f %>% summary()

f %>% spect() %>% plot()
```

spy

Spy

# **Description**

Peek into the inside of one of **pomp**'s objects.

## Usage

```
## S4 method for signature 'pomp'
spy(object)
```

# Arguments

object

the object whose structure we wish to examine

states

Latent states

# **Description**

Extract the latent states from a 'pomp' object.

## Usage

```
## S4 method for signature 'pomp'
states(object, vars, ...)
```

summary-probed\_pomp 123

# **Arguments**

```
object an object of class 'pomp', or of a class extending 'pomp' vars names of variables to retrieve
... ignored
```

summary-probed\_pomp Summary methods

# **Description**

Display a summary of a fitted model object.

## Usage

```
## S4 method for signature 'probed_pomp'
summary(object, ...)
## S4 method for signature 'spectd_pomp'
summary(object, ...)
## S4 method for signature 'objfun'
summary(object, ...)
```

# Arguments

object a fitted model object ... ignored

time

Methods to manipulate the obseration times

## **Description**

Get and set the vector of observation times.

# Usage

```
## S4 method for signature 'pomp'
time(x, t0 = FALSE, ...)
## S4 replacement method for signature 'pomp'
time(object, t0 = FALSE, ...) <- value</pre>
```

124 timezero

## **Arguments**

X	a 'pomp' object
t0	logical; should the zero time be included?
	ignored
object	a 'pomp' object
value	numeric vector; the new vector of times

#### **Details**

time(object) returns the vector of observation times. time(object,t0=TRUE) returns the vector of observation times with the zero-time t0 prepended.

time(object) <-value replaces the observation times slot (times) of object with value. time(object, t0=TRUE) <-value has the same effect, but the first element in value is taken to be the initial time. The second and subsequent elements of value are taken to be the observation times. Those data and states (if they exist) corresponding to the new times are retained.

timezero The zero time

# Description

Get and set the zero-time.

# Usage

```
## S4 method for signature 'pomp'
timezero(object, ...)
## S4 replacement method for signature 'pomp'
timezero(object, ...) <- value</pre>
```

# **Arguments**

```
object an object of class 'pomp', or of a class that extends 'pomp'
... ignored
value numeric; the new zero-time value
```

## Value

the value of the zero time

traces 125

|--|

## Description

Retrieve the history of an iterative calculation.

# Usage

```
## S4 method for signature 'mif2d_pomp'
traces(object, pars, transform = FALSE, ...)
## S4 method for signature 'mif2List'
traces(object, pars, ...)
## S4 method for signature 'abcd_pomp'
traces(object, pars, ...)
## S4 method for signature 'abcList'
traces(object, pars, ...)
## S4 method for signature 'pmcmcd_pomp'
traces(object, pars, ...)
## S4 method for signature 'pmcmcd_traces(object, pars, ...)
```

## Arguments

object	an object of class extending 'pomp', the result of the application of a parameter estimation algorithm
pars	names of parameters
transform	logical; should the traces be transformed back onto the natural scale?
	ignored or (in the case of the listie, passed to the more primitive function)

#### **Details**

Note that pmcmc does not currently support parameter transformations.

## Value

When object is the result of a mif2 calculation, traces(object,pars,transform = FALSE) returns the traces of the parameters named in pars. By default, the traces of all parameters are returned. Note that, if the computation was performed with transformed parameters, the traces are on the estimation scale. If transform=TRUE, the parameters are transformed from the estimation scale onto the natural scale.

126 traj.match

When object is a 'abcd\_pomp', traces(object) extracts the traces as a coda::mcmc.

When object is a 'abcList', traces(object) extracts the traces as a coda::mcmc.list.

When object is a 'pmcmcd\_pomp', traces(object) extracts the traces as a coda::mcmc.

When object is a 'pmcmcList', traces(object) extracts the traces as a coda::mcmc.list.

traj.match

Trajectory matching

# Description

Estimation of parameters for deterministic POMP models

## Usage

```
## S4 method for signature 'data.frame'
traj_objfun(
 data,
 est = character(0),
  fail.value = NA,
 ode_control = list(),
 params,
  rinit,
  skeleton,
 dmeasure,
 partrans,
 verbose = getOption("verbose", FALSE)
)
## S4 method for signature 'pomp'
traj_objfun(
 data,
 est = character(0),
 fail.value = NA,
 ode_control = list(),
  verbose = getOption("verbose", FALSE)
)
## S4 method for signature 'traj_match_objfun'
traj_objfun(
 data,
  est,
 fail.value,
 ode_control,
  . . . ,
```

traj.match 127

```
verbose = getOption("verbose", FALSE)
)
```

## **Arguments**

data either a data frame holding the time series data, or an object of class 'pomp',

i.e., the output of another **pomp** calculation.

est character vector; the names of parameters to be estimated.

fail.value optional numeric scalar; if non-NA, this value is substituted for non-finite values

of the objective function. It should be a large number (i.e., bigger than any

legitimate values the objective function is likely to take).

ode\_control optional list; the elements of this list will be passed to ode.

params optional; named numeric vector of parameters. This will be coerced internally

to storage mode double.

rinit simulator of the initial-state distribution. This can be furnished either as a C

snippet, an R function, or the name of a pre-compiled native routine available in a dynamically loaded library. Setting rinit=NULL sets the initial-state simulator

to its default. For more information, see ?rinit\_spec.

skeleton optional; the deterministic skeleton of the unobserved state process. Depending

on whether the model operates in continuous or discrete time, this is either a vectorfield or a map. Accordingly, this is supplied using either the vectorfield or map fnctions. For more information, see ?skeleton\_spec. Setting skeleton=NULL

removes the deterministic skeleton.

dmeasure evaluator of the measurement model density, specified either as a C snippet, an

R function, or the name of a pre-compiled native routine available in a dynamically loaded library. Setting dmeasure=NULL removes the measurement density

evaluator. For more information, see ?dmeasure\_spec.

partrans optional parameter transformations, constructed using parameter\_trans.

Many algorithms for parameter estimation search an unconstrained space of parameters. When working with such an algorithm and a model for which the parameters are constrained, it can be useful to transform parameters. One should supply the partrans argument via a call to parameter\_trans. For more information, see ?parameter\_trans. Setting partrans=NULL removes the parameter

transformations, i.e., sets them to the identity transformation.

. . . additional arguments will modify the model structure

verbose logical; if TRUE, diagnostic messages will be printed to the console.

### **Details**

In trajectory matching, one attempts to minimize the discrepancy between a POMP model's predictions and data under the assumption that the latent state process is deterministic and all discrepancies between model and data are due to measurement error. The measurement model likelihood (dmeasure), or rather its negative, is the natural measure of the discrepancy.

Trajectory matching is a generalization of the traditional nonlinear least squares approach. In particular, if, on some scale, measurement errors are normal with constant variance, then trajectory matching is equivalent to least squares on that particular scale.

128 traj.match

traj\_objfun constructs an objective function that evaluates the likelihood function. It can be passed to any one of a variety of numerical optimization routines, which will adjust model parameters to minimize the discrepancies between the power spectrum of model simulations and that of the data.

#### Value

traj\_objfun constructs a stateful objective function for spectrum matching. Specifically, traj\_objfun returns an object of class 'traj\_match\_objfun', which is a function suitable for use in an optim-like optimizer. In particular, this function takes a single numeric-vector argument that is assumed to contain the parameters named in est, in that order. When called, it will return the negative log likelihood. It is a stateful function: Each time it is called, it will remember the values of the parameters and its estimate of the log likelihood.

## **Important Note**

Since **pomp** cannot guarantee that the *final* call an optimizer makes to the function is a call *at* the optimum, it cannot guarantee that the parameters stored in the function are the optimal ones. Therefore, it is a good idea to evaluate the function on the parameters returned by the optimization routine, which will ensure that these parameters are stored.

#### See Also

```
trajectory, optim, subplex, nloptr
```

## **Examples**

```
library(magrittr)

ricker() %>%
    traj_objfun(
        est=c("r","sigma","N_0"),
        partrans=parameter_trans(log=c("r","sigma","N_0")),
        paramnames=c("r","sigma","N_0"),
    ) -> f

f(log(c(20,0.3,10)))

library(subplex)
subplex(fn=f,par=log(c(20,0.3,10)),control=list(reltol=1e-5)) -> out
f(out$par)

library(ggplot2)

f %>%
    trajectory(format="data.frame") %>%
    ggplot(aes(x=time,y=N))+geom_line()+theme_bw()
```

trajectory 129

trajectory

Trajectory of a deterministic model

# Description

Compute trajectories of the deterministic skeleton of a Markov process.

# Usage

```
## S4 method for signature 'pomp'
trajectory(
  object,
  params,
  times,
  t0,
  format = c("array", "data.frame"),
    ...,
  verbose = getOption("verbose", FALSE)
)

## S4 method for signature 'traj_match_objfun'
trajectory(object, ..., verbose = getOption("verbose", FALSE))
```

# Arguments

verbose

object	an object of class 'pomp', or of a class that extends 'pomp'. This will typically be the output of pomp, simulate, or one of the <b>pomp</b> inference algorithms.
params	a npar $x$ nrep matrix of parameters. Each column is treated as an independent parameter set, in correspondence with the corresponding column of $x$ .
times	a numeric vector (length ntimes) containing times at which the itineraries are desired. These must be in non-decreasing order with times[1]>t0.
t0	the time at which the initial conditions are assumed to hold.
format	the format in which to return the results.
	format = "array" causes the trajectories to be returned in a rank-3 array with dimensions nvar x ncol(params) x ntimes. Here, nvar is the number of state variables and ntimes the length of the argument times.
	format = "data.frame" causes the results to be returned as a single data frame containing the time and states. An ordered factor variable, '.id', distinguishes the trajectories from one another.
	Additional arguments are passed to the ODE integrator (if the skeleton is a vectorfield) and are ignored if it is a map. See ode for a description of the additional arguments accepted by the ODE integrator.

logical; if TRUE, diagnostic messages will be printed to the console.

transformations

# **Details**

In the case of a discrete-time system, the deterministic skeleton is a map and a trajectory is obtained by iterating the map. In the case of a continuous-time system, the deterministic skeleton is a vector-field; trajectory uses the numerical solvers in **deSolve** to integrate the vectorfield.

Note that the handling of . . . in trajectory differs from that of most other functions in **pomp**. In particular, it is not possible to modify the model structure in a call to trajectory.

## Value

trajectory returns an array of dimensions nvar x nrep x ntimes. If x is the returned matrix, x[i,j,k] is the i-th component of the state vector at time times[k] given parameters params[,j].

## See Also

```
skeleton, flow
```

transformations

Transformations

# **Description**

Some useful parameter transformations.

# Usage

```
logit(p)
expit(x)
log_barycentric(X)
inv_log_barycentric(Y)
```

## **Arguments**

р	numeric; a quantity in [0,1].
X	numeric; the log odds ratio.
X	numeric; a vector containing the quantities to be transformed according to the log-barycentric transformation.
Υ	numeric; a vector containing the log fractions.

userdata 131

#### **Details**

Parameter transformations can be used in many cases to recast constrained optimization problems as unconstrained problems. Although there are no limits to the transformations one can implement using the parameter\_trans facilty, **pomp** provides a few ready-built functions to implement some very commonly useful ones.

The logit transformation takes a probability p to its log odds,  $\log \frac{p}{1-p}$ . It maps the unit interval [0,1] into the extended real line  $[-\infty,\infty]$ .

The inverse of the logit transformation is the expit transformation.

The log-barycentric transformation takes a vector  $X_i$ , i = 1, ..., n, to a vector  $Y_i$ , where

$$Y_i = \log \frac{X_i}{\sum_j X_j}.$$

If X is an n-vector, it takes every simplex defined by  $\sum_i X_i = c$ , c constant, to n-dimensional Euclidean space  $\mathbb{R}^n$ .

The inverse of the log-barycentric transformation is implemented as inv\_log\_barycentric. Note that it is not a true inverse, in the sense that it takes  $R^n$  to the *unit* simplex,  $\sum_i X_i = 1$ . Thus,

```
log_barycentric(inv_log_barycentric(Y)) == Y,
```

but

```
inv_log_barycentric(log_barycentric(X)) == X
only if sum(X) == 1.
```

## See Also

Other information on model implementation: Csnippet, accumulators, covariate\_table(), distributions, dmeasure\_spec, dprocess\_spec, parameter\_trans(), pomp-package, prior\_spec, rinit\_spec, rmeasure\_spec, rprocess\_spec, skeleton\_spec, userdata

userdata

Facilities for making additional information to basic components

## **Description**

When POMP basic components need information they can't get from parameters or covariates.

132 userdata

#### **Details**

It can happen that one desires to pass information to one of the POMP model *basic components* (see here for a definition of this term) outside of the standard routes (i.e., via model parameters or covariates). **pomp** provides facilities for this purpose. We refer to the objects one wishes to pass in this way as *user data*.

The following will apply to every basic model component. For the sake of definiteness, however, we'll use the rmeasure component as an example. To be even more specific, the measurement model we wish to implement is

```
y1 ~ Poisson(x1+theta), y2 ~ Poisson(x2+theta),
```

where theta is a parameter. Although it would be very easy (and indeed far preferable) to include theta among the ordinary parameters (by including it in params), we will assume here that we have some reason for not wanting to do so.

Now, we have the choice of providing rmeasure in one of three ways:

- 1. as an R function,
- 2. as a C snippet, or
- 3. as a procedure in an external, dynamically loaded library.

We'll deal with these three cases in turn.

## When the basic component is specified as an R function

We can implement a simulator for the aforementioned measurement model so:

```
f <- function (t, x, params, theta, ...) {
   y <- rpois(n=2,x[c("x1","x2")]+theta)
   setNames(y,c("y1","y2"))
}</pre>
```

So far, so good, but how do we get theta to this function? We simply provide an additional argument to whichever **pomp** algorithm we are employing (e.g., simulate, pfilter, mif2, abc, etc.). For example:

```
simulate(..., rmeasure = f, theta = 42, ...)
```

where the ... represent the other simulate arguments we might want to supply. When we do so, a message will be generated, informing us that theta is available for use by the POMP basic components. This warning helps forestall accidental triggering of this facility due to typographical error.

## When the basic component is specified via a C snippet

A C snippet implementation of the aforementioned measurement model is:

```
f <- Csnippet("
  double theta = *(get_userdata_double(\"theta\"));
  y1 = rpois(x1+theta); y2 = rpois(x2+theta);
")</pre>
```

userdata 133

Here, the call to get\_userdata\_double retrieves a *pointer* to the stored value of theta. Note the need to escape the quotes in the C snippet text.

It is possible to store and retrieve integer objects also, using get\_userdata\_int.

One must take care that one stores the user data with the appropriate storage type. For example, it is wise to wrap floating point scalars and vectors with as .double and integers with as .integer. In the present example, our call to simulate might look like

```
simulate(..., rmeasure = f, theta = as.double(42), ...)
```

Since the two functions get\_userdata\_double and get\_userdata\_int return pointers, it is trivial to pass vectors of double-precision and integers.

A simpler and more elegant approach is afforded by the globals argument (see below).

# When the basic component is specified via an external library

The rules are essentially the same as for C snippets. typedef declarations for the get\_userdata\_double and get\_userdata\_int are given in the 'pomp.h' header file and these two routines are registered so that they can be retrieved via a call to R\_GetCCallable. See the Writing R extensions manual for more information.

## Setting globals

The use of the userdata facilities incurs a run-time cost. It is faster and more elegant, when using C snippets, to put the needed objects directly into the C snippet library. The globals argument does this. See the example below.

#### See Also

Other information on model implementation: Csnippet, accumulators, covariate\_table(), distributions, dmeasure\_spec, dprocess\_spec, parameter\_trans(), pomp-package, prior\_spec, rinit\_spec, rmeasure\_spec, rprocess\_spec, skeleton\_spec, transformations

## **Examples**

```
## The familiar Ricker example
## For some bizarre reason, we wish to pass 'phi' via the userdata facility.

## C snippet approach:

simulate(times=1:100,t0=0,
    phi=as.double(100),
    params=c(r=3.8,sigma=0.3,N.0=7),
    rprocess=discrete_time(
        step.fun=Csnippet("
            double e = (sigma > 0.0) ? rnorm(0,sigma) : 0.0;
        N = r*N*exp(-N+e);"
        ),
        delta.t=1
      ),
      rmeasure=Csnippet("
```

verhulst verhulst

```
double phi = *(get_userdata_double(\"phi\"));
       y = rpois(phi*N);"
 ),
 paramnames=c("r","sigma"),
 statenames="N",
 obsnames="y"
) -> rick1
## The same problem solved using 'globals':
simulate(times=1:100,t0=0,
 globals=Csnippet("static double phi = 100;"),
 params=c(r=3.8, sigma=0.3, N.0=7),
 rprocess=discrete_time(
   step.fun=Csnippet("
      double e = (sigma > 0.0) ? rnorm(0, sigma) : 0.0;
      N = r*N*exp(-N+e);
   ),
   delta.t=1
 ),
 rmeasure=Csnippet("
       y = rpois(phi*N);"
 paramnames=c("r","sigma"),
 statenames="N",
 obsnames="y"
) -> rick2
## Finally, the R function approach:
simulate(times=1:100,t0=0,
 phi=100,
 params=c(r=3.8, sigma=0.3, N_0=7),
 rprocess=discrete_time(
   step.fun=function (r, N, sigma, ...) {
      e <- rnorm(n=1,mean=0,sd=sigma)
       c(N=r*N*exp(-N+e))
   },
   delta.t=1
 rmeasure=function(phi, N, ...) {
      c(y=rpois(n=1,lambda=phi*N))
) -> rick3
```

verhulst

Verhulst-Pearl model

# **Description**

The Verhulst-Pearl (logistic) model of population growth.

verhulst 135

# Usage

```
verhulst(n_0 = 10000, K = 10000, r = 0.9, sigma = 0.4, tau = 0.1, dt = 0.01)
```

## **Arguments**

n_0	initial condition
K	carrying capacity
r	intrinsic growth rate
sigma	environmental process noise s.d.
tau	measurement error s.d.
dt	Euler time-step

#### **Details**

A stochastic version of the Verhulst-Pearl logistic model. This evolves in continuous time, according to the stochastic differential equation

$$dn = r n \left(1 - \frac{n}{K}\right) dt + \sigma n dW.$$

Numerically, we simulate the stochastic dynamics using an Euler approximation.

The measurements are assumed to be log-normally distributed.

#### Value

A 'pomp' object containing the model and simulated data. The following basic components are included in the 'pomp' object: 'rinit', 'rprocess', 'rmeasure', 'dmeasure', and 'skeleton'.

## See Also

```
Other pomp examples: blowflies, bsflu, dacca(), ebola, gompertz(), measles, ou2(), parus, pomp_examples, ricker(), rw2(), sir_models
```

## **Examples**

```
verhulst() -> po
plot(po)
plot(simulate(po))
pfilter(po,Np=1000) -> pf
logLik(pf)
spy(po)
```

136 workhorses

window Window

# **Description**

Restrict to a portion of a time series.

# Usage

```
## S4 method for signature 'pomp'
window(x, start, end, ...)
```

## Arguments

```
x a 'pomp' object or object of class extending 'pomp' start, end the left and right ends of the window, in units of time ignored
```

workhorses

Workhorse functions for the pomp algorithms.

## Description

These functions mediate the interface between the user's model and the package algorithms. They are low-level functions that do the work needed by the package's inference methods.

## **Details**

```
They include
```

```
dmeasure which evaluates the measurement model density,
rmeasure which samples from the measurement model distribution,
dprocess which evaluates the process model density,
rprocess which samples from the process model distribution,
dprior which evaluates the prior probability density,
rprior which samples from the prior distribution,
skeleton which evaluates the model's deterministic skeleton,
flow which iterates or integrates the deterministic skeleton to yield trajectories,
partrans which performs parameter transformations associated with the model.
```

# Author(s)

Aaron A. King

wpfilter 137

## See Also

```
simulate, trajectory, pfilter, probe
Other pomp workhorses: dmeasure(), dprior(), dprocess(), flow(), partrans(), rinit(),
rmeasure(), rprior(), rprocess(), skeleton()
```

wpfilter

Weighted particle filter

# **Description**

A sequential importance sampling (particle filter) algorithm. Unlike in pfilter, resampling is performed only when triggered by deficiency in the effective sample size.

# Usage

```
## S4 method for signature 'data.frame'
wpfilter(
  data,
  Nρ,
  params,
  rinit,
  rprocess,
  dmeasure,
  trigger = 1,
  target = 0.5,
  verbose = getOption("verbose", FALSE)
)
## S4 method for signature 'pomp'
wpfilter(
  data,
 Nρ,
  trigger = 1,
  target = 0.5,
  verbose = getOption("verbose", FALSE)
)
## S4 method for signature 'wpfilterd_pomp'
wpfilter(data, Np, trigger, target, ..., verbose = getOption("verbose", FALSE))
```

## **Arguments**

data

either a data frame holding the time series data, or an object of class 'pomp', i.e., the output of another **pomp** calculation.

138 wpfilter

Np

the number of particles to use. This may be specified as a single positive integer, in which case the same number of particles will be used at each timestep. Alternatively, if one wishes the number of particles to vary across timesteps, one may specify Np either as a vector of positive integers of length

length(time(object,t0=TRUE))

or as a function taking a positive integer argument. In the latter case, Np(k) must be a single positive integer, representing the number of particles to be used at the k-th timestep: Np(0) is the number of particles to use going from timezero(object) to time(object)[1], Np(1), from timezero(object) to time(object)[1], and so on, while when T=length(time(object)), Np(T) is the number of particles to sample at the end of the time-series.

params

optional; named numeric vector of parameters. This will be coerced internally to storage mode double.

rinit

simulator of the initial-state distribution. This can be furnished either as a C snippet, an R function, or the name of a pre-compiled native routine available in a dynamically loaded library. Setting rinit=NULL sets the initial-state simulator to its default. For more information, see ?rinit\_spec.

rprocess

simulator of the latent state process, specified using one of the rprocess plugins. Setting rprocess=NULL removes the latent-state simulator. For more information, see ?rprocess\_spec for the documentation on these plugins.

dmeasure

evaluator of the measurement model density, specified either as a C snippet, an R function, or the name of a pre-compiled native routine available in a dynamically loaded library. Setting dmeasure=NULL removes the measurement density evaluator. For more information, see ?dmeasure\_spec.

trigger

numeric; if the effective sample size becomes smaller than trigger \* Np, resampling is triggered.

target

numeric; target power.

. . .

additional arguments supply new or modify existing model characteristics or components. See pomp for a full list of recognized arguments.

When named arguments not recognized by pomp are provided, these are made available to all basic components via the so-called *userdata* facility. This allows the user to pass information to the basic components outside of the usual routes of covariates (covar) and model parameters (params). See ?userdata for

information on how to use this facility.

verbose

logical; if TRUE, diagnostic messages will be printed to the console.

## **Details**

This function is experimental and should be considered in alpha stage. Both interface and underlying algorithms may change without warning at any time. Please explore the function and give feedback via the pomp Issues page.

## Value

An object of class 'wpfilterd\_pomp', which extends class 'pomp'. Information can be extracted from this object using the methods documented below.

wpfilter 139

# Methods

```
logLik the estimated log likelihood
cond.logLik the estimated conditional log likelihood
eff.sample.size the (time-dependent) estimated effective sample size
as.data.frame coerce to a data frame
plot diagnostic plots
```

## Author(s)

Aaron A. King

#### References

M.S. Arulampalam, S. Maskell, N. Gordon, & T. Clapp. A Tutorial on Particle Filters for Online Nonlinear, Non-Gaussian Bayesian Tracking. *IEEE Transactions on Signal Processing* **50**, 174–188, 2002.

## See Also

```
Other elementary POMP methods: pfilter(), pomp-package, probe(), simulate(), spect()
Other particle filter methods: bsmc2(), cond.logLik(), eff.sample.size(), filter.mean(),
filter.traj(), mif2(), pfilter(), pmcmc(), pred.mean(), pred.var()
```

# **Index**

* datasets	rinit_spec,96
blowflies, 18	rmeasure_spec, 99
bsflu, 20	rprocess_spec, 102
dacca, 31	skeleton_spec, 114
ebola, 42	transformations, 130
gompertz, 48	userdata, 131
measles, 55	* low-level interface
ou2, 65	hitch, 49
parus, 70	workhorses, 136
pomp_examples, 83	* models
ricker, 95	blowflies, 18
rw2, 106	dacca, 31
sir_models, 111	gompertz, 48
* design	ou2, 65
design, 33	pomp-package, 5
* diagnostics	pomp_examples, 83
basic_probes, 16	ricker, 95
* distribution	rw2, 106
distributions, 35	sir_models, 111
* elementary POMP methods	* multivariate
pfilter,71	pomp-package, 5
pomp-package, 5	* optimize
probe, 87	sannbox, 107
simulate, 108	* parameter transformations
spect, 115	transformations, 130
wpfilter, 137	* particle filter methods
* extending the pomp package	bsmc2, 21
hitch, 49	cond.logLik, 25
workhorses, 136	eff.sample.size,44
* information on model implementation	filter.mean,45
accumulators, 10	filter.traj,46
covariate_table, 27	mif2, 56
Csnippet, 29	pfilter, 71
distributions, 35	pmcmc, 76
dmeasure_spec, 38	pred.mean,84
dprocess_spec, 41	pred.var, 85
parameter_trans, 67	wpfilter, 137
pomp-package, 5	* particle filtering methods
prior_spec,86	kalman, 51

* pomp examples	?accumulators, 81
blowflies, 18	?dmeasure_spec, 22, 59, 73, 78, 81, 127, 138
bsflu, 20	?dprocess_spec, 81
dacca, 31	?parameter_trans, 22, 59, 81, 92, 121, 127
ebola, 42	?prior_spec, 8, 22, 78, 81
gompertz, 48	?rinit_spec, 8, 22, 52, 58, 63, 73, 78, 80, 88,
measles, 55	91, 110, 117, 120, 127, 138
ou2, 65	?rmeasure_spec, 8, 63, 81, 88, 91, 110, 117,
parus, 70	120
pomp_examples, 83	?skeleton_spec, <i>81</i> , <i>127</i>
ricker, 95	?userdata, <i>8</i> , <i>22</i> , <i>52</i> , <i>59</i> , <i>63</i> , <i>73</i> , <i>78</i> , <i>80</i> , <i>88</i> ,
rw2, 106	92, 110, 117, 121, 138
sir_models, 111	
verhulst, 134	abc, 6, 7, 17, 23, 27, 53, 61, 64, 79, 89, 92, 95,
* pomp parameter estimation methods	118, 121, 132
abc, 7	abc,abcd_pomp-method(abc),7
bsmc2, 21	abc, ANY-method (abc), 7
kalman, 51	abc, data.frame-method(abc), 7
mif2, 56	abc, missing-method (abc), 7
nlf, 61	abc, pomp-method (abc), 7
pmcmc, 76	abc, probed_pomp-method (abc), 7
pomp-package, 5	abc-data.frame(abc),7
probe.match, 90	abc-pomp (abc), 7
spect.match, 118	accumulators, 6, 10, 28, 30, 37, 39, 42, 69,
* pomp workhorses	87, 97, 100, 105, 115, 131, 133
dmeasure, 37	accumvars (accumulators), 10
dprior, 39	as, bsmcd_pomp-method (as.data.frame), 12
dprocess, 40	as, Csnippet-method (Csnippet), 29
flow, 47	as, kalmand_pomp-method(as.data.frame),
partrans, 70	12
rinit, 96	as, listie-method (as.data.frame), 12
rmeasure, 98	as, pfilterd_pomp-method
rprior, 100	(as.data.frame), 12
rprocess, 101	as,probed_pomp-method(as.data.frame),
skeleton, 113	as,wpfilterd_pomp-method
workhorses, 136	(as.data.frame), 12
* probability distributions	as-csnippet (Csnippet), 29
distributions, 35	as.data.frame, 12, 22, 74, 139
* smooth	ds. udtd. 11 dille, 12, 22, 74, 139
bsplines, 23	bake, 14
* summary statistics methods	basic model component, <i>132</i>
abc, 7	basic probes, 8, 88, 91
basic_probes, 16	basic_probes, 9, 16, 89, 92, 118
probe, 87	blowflies, 18, 20, 32, 43, 49, 56, 66, 71, 83,
probe.match, 90	84, 95, 106, 112, 135
spect, 115	blowflies1, 83
* ts	blowflies1 (blowflies), 18
pomp-package, 5	blowflies2, 83

blowflies2 (blowflies), 18	coerce-objfun-data.frame
bsflu, 19, 20, 32, 43, 49, 56, 66, 71, 83, 84,	(as.data.frame), 12
95, 106, 112, 135	<pre>coerce-pomp-data.frame (as.data.frame),</pre>
bsmc2, 6, 9, 21, 26, 45, 46, 53, 54, 61, 64, 74,	12
79, 85, 92, 121, 139	<pre>coerce-probe_match_objfun-probed_pomp</pre>
bsmc2, ANY-method (bsmc2), 21	(probe), 87
bsmc2,data.frame-method(bsmc2),21	<pre>coerce-spect_match_objfun-spectd_pomp</pre>
bsmc2, missing-method (bsmc2), 21	(spect), 115
bsmc2,pomp-method(bsmc2),21	cond.logLik, 23, 25, 45, 46, 61, 74, 79, 85,
bsmc2-data.frame (bsmc2), 21	139
bsmc2-pomp (bsmc2), 21	<pre>cond.logLik, ANY-method (cond.logLik), 25</pre>
bspline.basis (bsplines), 23	<pre>cond.logLik,bsmcd_pomp-method</pre>
bsplines, 23	(cond.logLik), 25
	<pre>cond.logLik,kalmand_pomp-method</pre>
coef, 24, 59	(cond.logLik), 25
coef, listie-method (coef), 24	<pre>cond.logLik,missing-method</pre>
coef, missing-method (coef), 24	(cond.logLik), 25
coef, objfun-method (coef), 24	<pre>cond.logLik,pfilterd_pomp-method</pre>
coef, pomp-method (coef), 24	(cond.logLik), 25
coef-listie (coef), 24	cond.logLik,wpfilterd_pomp-method
coef-objfun (coef), 24	(cond.logLik), 25
coef-pomp (coef), 24	<pre>cond.logLik-bsmcd_pomp (cond.logLik), 25</pre>
coef<- (coef), 24	<pre>cond.logLik-kalmand_pomp (cond.logLik),</pre>
coef<-,missing-method (coef), 24	25
coef<-,pomp-method (coef), 24	<pre>cond.logLik-pfilterd_pomp</pre>
coef <pomp (coef),="" 24<="" td=""><td>(cond.logLik), 25</td></pomp>	(cond.logLik), 25
coerce, bsmcd_pomp, data.frame-method	cond.logLik-wpfilterd_pomp
(as.data.frame), 12	(cond.logLik), 25
coerce, Csnippet, character-method	continue, 26, 59
(Csnippet), 29	continue, abcd_pomp-method (continue), 26
coerce, kalmand_pomp, data.frame-method	continue, ANY-method (continue), 26
(as.data.frame), 12	<pre>continue,mif2d_pomp-method(continue),</pre>
coerce, listie, data. frame-method	26
(as.data.frame), 12	continue, missing-method (continue), 26
coerce, objfun, data.frame-method	continue, pmcmcd_pomp-method (continue),
(as.data.frame), 12	26
coerce,pfilterd_pomp,data.frame-method	continue-abcd_pomp (continue), 26
(as.data.frame), 12	continue-mif2d_pomp (continue), 26
coerce, pomp, data.frame-method	continue-pmcmcd_pomp (continue), 26
(as.data.frame), 12	covariate_table, 6, 10, 27, 30, 37, 39, 42,
coerce, probe_match_objfun, probed_pomp-method	69, 81, 87, 97, 100, 105, 115, 131,
(probe), 87	133
<pre>coerce,probed_pomp,data.frame-method</pre>	covariate_table,ANY-method
(as.data.frame), 12	(covariate_table), 27
<pre>coerce,spect_match_objfun,spectd_pomp-method</pre>	covariate_table,character-method
(spect), 115	(covariate_table), 27
<pre>coerce,wpfilterd_pomp,data.frame-method</pre>	covariate_table,missing-method
(as.data.frame), 12	(covariate_table), 27

covariate_table, numeric-method	dprocess, pomp-method (dprocess), 40
(covariate_table), 27	dprocess-pomp (dprocess), 40
<pre>covariate_table-character,covariate_table,character,covariate_table,character</pre>	афасфевзя <u>е</u> ярес, 6, 10, 28, 30, 37, 39, 41, 41, 69, 87, 97, 100, 105, 115, 131, 133
$covariate\_table-numeric, covariate\_table, numeric, covariate\_table, $	ric-method
(covariate_table), 27	eakf (kalman), 51
covmat, 28	eakf, ANY-method (kalman), 51
<pre>covmat,abcd_pomp-method(covmat), 28</pre>	eakf, data. frame-method (kalman), 51
covmat, abcList-method (covmat), 28	eakf, missing-method (kalman), 51
covmat, ANY-method (covmat), 28	eakf, pomp-method (kalman), 51
covmat, missing-method (covmat), 28	eakf-data.frame(kalman), 51
<pre>covmat, pmcmcd_pomp-method (covmat), 28</pre>	eakf-pomp (kalman), 51
covmat, pmcmcList-method (covmat), 28	
<pre>covmat, probed_pomp-method (covmat), 28</pre>	ebola, 19, 20, 32, 42, 49, 56, 66, 71, 84, 95,
covmat-abcd_pomp (covmat), 28	106, 112, 135
covmat-abcList (covmat), 28	ebolaModel, 83
covmat-pmcmcd_pomp (covmat), 28	ebolaModel (ebola), 42
covmat-pmcmcList (covmat), 28	ebolaWA2014 (ebola), 42
covmat-probed_pomp (covmat), 28	eff.sample.size, 23, 26, 44, 45, 46, 59, 61,
Csnippet, 6, 10, 28, 29, 37, 39, 41, 42, 69, 87,	74, 79, 85, 139
97, 99, 100, 103, 105, 115, 131, 133	eff.sample.size,ANY-method
Csnippet-class (Csnippet), 29	(eff.sample.size), 44
(complete class (complete), 25	eff.sample.size,bsmcd_pomp-method
dacca, 19, 20, 31, 43, 49, 56, 66, 71, 83, 84,	(eff.sample.size), 44
95, 106, 112, 135	eff.sample.size,missing-method
design, 33	(eff.sample.size), 44
deSolve, 47, 130	eff.sample.size,pfilterd_pomp-method
deulermultinom (distributions), 35	(eff.sample.size), 44
discrete_time (rprocess_spec), 102	<pre>eff.sample.size,wpfilterd_pomp-method</pre>
distributions, 6, 10, 28, 30, 35, 39, 42, 69,	(eff.sample.size), 44
87, 97, 100, 105, 115, 131, 133	eff.sample.size-bsmcd_pomp
dmeasure, 37, 39–41, 47, 70, 96, 99–101, 114,	(eff.sample.size), 44
136, 137	eff.sample.size-pfilterd_pomp
dmeasure, ANY-method (dmeasure), 37	(eff.sample.size), 44
dmeasure, missing-method (dmeasure), 37	eff.sample.size-wpfilterd_pomp
dmeasure, pomp-method (dmeasure), 37	(eff.sample.size), 44
dmeasure-pomp (dmeasure), 37	enkf (kalman), 51
dmeasure_spec, 6, 10, 28, 30, 37, 38, 38, 42,	enkf, ANY-method (kalman), 51
69, 87, 97, 100, 105, 115, 131, 133	enkf,data.frame-method(kalman),51
dprior, 38, 39, 41, 47, 70, 96, 99–101, 114,	enkf, missing-method (kalman), 51
136, 137	enkf,pomp-method(kalman), 51
dprior, ANY-method (dprior), 39	enkf-data.frame(kalman), 51
dprior, missing-method (dprior), 39	enkf-pomp (kalman), 51
	euler (rprocess_spec), 102
dprior, pomp-method (dprior), 39	ewcitmeas, 83
dprior-pomp (dprior), 39	
dprocess, 38, 40, 40, 47, 70, 96, 99–101, 114,	ewcitmeas (measles), 55
136, 137	ewmeas, 83
dprocess, ANY-method (dprocess), 40	ewmeas (measles), 55
dprocess, missing-method (dprocess), 40	expit (transformations), 130

facility, 39	can be found here, 86, 97, 114
filter.mean, 23, 26, 45, 45, 46, 61, 74, 79,	gillespie (rprocess_spec), 102
85, 139	gillespie_hl (rprocess_spec), 102
filter.mean, ANY-method (filter.mean), 45	gompertz, 19, 20, 32, 43, 48, 56, 66, 71, 83,
filter.mean,kalmand_pomp-method	84, 95, 106, 112, 135
(filter.mean), 45	,,,
filter.mean,missing-method	here for a definition of this term, $132$
(filter.mean), 45	hitch, 49
filter.mean,pfilterd_pomp-method	, ,
(filter.mean), 45	<pre>inv_log_barycentric(transformations),</pre>
filter.mean-kalmand_pomp(filter.mean),	130
45	
filter.mean-pfilterd_pomp	kalman, 6, 9, 23, 51, 61, 64, 79, 92, 121
(filter.mean), 45	kernel, <i>17</i>
filter.traj, 23, 26, 45, 46, 61, 73, 74, 79,	
85, 139	load, <i>15</i>
filter.traj,ANY-method(filter.traj),46	log_barycentric(transformations), 130
filter.traj,missing-method	logit (transformations), 130
(filter.traj), 46	logLik, 53, 59, 73, 139
filter.traj,pfilterd_pomp-method	logLik, ANY-method (logLik), 53
(filter.traj), 46	<pre>logLik,bsmcd_pomp-method(logLik),53</pre>
filter.traj,pfilterList-method	<pre>logLik,kalmand_pomp-method(logLik),53</pre>
(filter.traj), 46	<pre>logLik,listie-method(logLik), 53</pre>
filter.traj,pmcmcd_pomp-method	<pre>logLik,missing-method(logLik), 53</pre>
(filter.traj), 46	<pre>logLik,nlf_objfun-method(logLik),53</pre>
filter.traj,pmcmcList-method	logLik,objfun-method(logLik),53
(filter.traj), 46	<pre>logLik,pfilterd_pomp-method(logLik),53</pre>
filter.traj-pfilterd_pomp	<pre>logLik,pmcmcd_pomp-method(logLik),53</pre>
(filter.traj), 46	<pre>logLik,probed_pomp-method(logLik),53</pre>
filter.traj-pfilterList(filter.traj),	<pre>logLik,spect_match_objfun-method</pre>
46	(logLik), 53
<pre>filter.traj-pmcmcd_pomp(filter.traj),</pre>	<pre>logLik,wpfilterd_pomp-method(logLik),</pre>
46	53
filter.traj-pmcmcList(filter.traj),46	<pre>logLik-bsmcd_pomp (logLik), 53</pre>
flow, 38, 40, 41, 47, 70, 96, 99–101, 114, 130,	<pre>logLik-kalmand_pomp (logLik), 53</pre>
136, 137	<pre>logLik-nlf_objfun (logLik), 53</pre>
flow, ANY-method (flow), 47	logLik-objfun(logLik), 53
flow, missing-method (flow), 47	<pre>logLik-pfilterd_pomp(logLik), 53</pre>
flow, pomp-method (flow), 47	<pre>logLik-pmcmcd_pomp (logLik), 53</pre>
flow-pomp (flow), 47	<pre>logLik-probed_pomp (logLik), 53</pre>
forecast, 48	<pre>logLik-spect_match_objfun(logLik), 53</pre>
forecast, ANY-method (forecast), 48	<pre>logLik-wpfilterd_pomp(logLik), 53</pre>
forecast, kalmand_pomp-method	logmeanexp, 54
(forecast), 48	LondonYorke, 83
forecast, missing-method (forecast), 48	LondonYorke (measles), 55
forecast-kalmand_pomp (forecast), 48	
freeze (bake), 14	map, 81, 127
, ,,	map (skeleton_spec), 114
General rules for writing C snippets	mcmc. 9

MCMC proposals, 8, 9, 29, 77, 79	parameter_trans,ANY,missing-method
mean, <i>17</i>	(parameter_trans), 67
measles, 19, 20, 32, 43, 49, 55, 66, 71, 84, 95,	$parameter\_trans, character, character-method$
106, 112, 135	(parameter_trans), 67
mif2, 6, 9, 23, 26, 27, 45, 46, 53, 56, 64, 74,	<pre>parameter_trans,Csnippet,Csnippet-method</pre>
79, 85, 92, 105, 106, 121, 125, 132,	(parameter_trans), 67
139	parameter_trans, function, function-method
mif2, ANY-method (mif2), 56	(parameter_trans), 67
mif2, data.frame-method (mif2), 56	parameter_trans,missing,ANY-method
mif2, mif2d_pomp-method (mif2), 56	(parameter_trans), 67
mif2, missing-method (mif2), 56	parameter_trans,missing,missing-method
mif2,pfilterd_pomp-method(mif2),56	(parameter_trans), 67
mif2, pomp-method (mif2), 56	parameter_trans, NULL, NULL-method
mif2-data.frame (mif2), 56	(parameter_trans), 67
mif2-mif2d_pomp (mif2), 56	parameter_trans,pomp_fun,pomp_fun-method
mif2-pfilterd_pomp (mif2), 56	
	(parameter_trans), 67
mif2-pomp (mif2), 56	parameter_trans-character, character
mvn.diag.rw(proposals), 93	(parameter_trans), 67
mvn.rw(proposals),93	parameter_trans-Csnippet,Csnippet
	(parameter_trans), 67
nlf, 6, 9, 23, 53, 54, 61, 61, 79, 92, 121	parameter_trans-function, function
nlf_objfun (nlf), 61	(parameter_trans), 67
nlf_objfun,ANY-method(nlf),61	parameter_trans-missing,missing
nlf_objfun,data.frame-method(nlf),61	(parameter_trans), 67
nlf_objfun,missing-method(nlf),61	parmat, 69
nlf_objfun,nlf_objfun-method(nlf),61	partrans, 38, 40, 41, 47, 70, 96, 99–101, 114,
nlf_objfun,pomp-method(nlf),61	136, 137
nlf_objfun-data.frame (nlf), 61	partrans, ANY-method (partrans), 70
nlf_objfun-nlf_objfun(nlf), 61	partrans, missing-method (partrans), 70
nlf_objfun-pomp(nlf), 61	partrans, pomp-method (partrans), 70
nloptr, 92, 121, 128	partrans-pomp (partrans), 70
	parus, 19, 20, 32, 43, 49, 56, 66, 70, 83, 84,
obs, 17, 65	95, 106, 112, 135
obs, pomp-method (obs), 65	paste, 24
	periodic.bspline.basis(bsplines), 23
obs-pomp (obs), 65	pfilter, 6, 23, 26, 45, 46, 59, 61, 71, 79, 85,
ode, 47, 127, 129	
onestep (rprocess_spec), 102	89, 111, 118, 132, 137, 139
optim, 64, 92, 108, 121, 128	pfilter, ANY-method (pfilter), 71
ou2, 19, 20, 32, 43, 49, 56, 65, 71, 83, 84, 95,	pfilter, data.frame-method (pfilter), 71
106, 112, 135	pfilter, missing-method (pfilter), 71
	pfilter,objfun-method(pfilter),71
par, <i>76</i>	<pre>pfilter,pfilterd_pomp-method(pfilter),</pre>
parameter_trans, 6, 10, 22, 28, 30, 37, 39,	71
42, 59, 67, 70, 81, 87, 91, 92, 97,	pfilter, pomp-method (pfilter), 71
100, 105, 115, 120, 121, 127, 131,	pfilter-data.frame(pfilter),71
133	pfilter-objfun(pfilter),71
parameter_trans,ANY,ANY-method	pfilter-pfilterd_pomp(pfilter),71
(parameter trans), 67	pfilter-pomp(pfilter),71

pfilterd_pomp, 59	pomp, 8, 22, 51, 52, 59, 63, 73, 78, 79, 80, 88,
pfilterd_pomp(pfilter),71	92, 110, 117, 121, 138
pfilterd_pomp-class(pfilter),71	pomp, package (pomp-package), 5
plot, 22, 74, 74, 139	pomp-package, 5
plot, Abc-method (plot), 74	<pre>pomp_example (pomp_examples), 83</pre>
plot,abcd_pomp-method(plot),74	pomp_examples, 19, 20, 32, 43, 49, 56, 66, 71
plot,abcList-method(plot),74	83, 95, 106, 112, 135
plot,bsmcd_pomp-method(plot),74	<pre>pompExample (pomp_examples), 83</pre>
plot, Mif2-method (plot), 74	<pre>pompExamples (pomp_examples), 83</pre>
plot,mif2d_pomp-method(plot), 74	pred.mean, 23, 26, 45, 46, 61, 74, 79, 84, 85,
plot,mif2List-method(plot),74	139
plot, missing-method (plot), 74	pred.mean, ANY-method (pred.mean), 84
plot,pfilterd_pomp-method(plot),74	<pre>pred.mean,kalmand_pomp-method</pre>
plot, Pmcmc-method (plot), 74	(pred.mean), 84
plot,pmcmcd_pomp-method(plot),74	pred.mean, missing-method (pred.mean), 8
plot,pmcmcList-method(plot), 74	<pre>pred.mean,pfilterd_pomp-method</pre>
plot,pomp-method(plot),74	(pred.mean), 84
plot,pomp_plottable-method(plot), 74	<pre>pred.mean-kalmand_pomp(pred.mean), 84</pre>
plot,probe_match_objfun-method(plot),	<pre>pred.mean-pfilterd_pomp (pred.mean), 84</pre>
74	pred.var, 23, 26, 45, 46, 61, 74, 79, 85, 85,
plot,probed_pomp-method(plot),74	139
plot, spect_match_objfun-method (plot),	pred.var, ANY-method (pred.var), 85
74	<pre>pred.var,missing-method(pred.var), 85</pre>
plot, spectd_pomp-method (plot), 74	<pre>pred.var,pfilterd_pomp-method</pre>
plot,wpfilterd_pomp-method(plot),74	(pred.var), 85
plot-Abc (plot), 74	<pre>pred.var-pfilterd_pomp(pred.var), 85</pre>
plot-bsmcd_pomp (plot), 74	print,86
plot-Mif2 (plot), 74	<pre>print,listie-method(print), 86</pre>
plot-pfilterd_pomp(plot), 74	<pre>print,pomp_fun-method(print),86</pre>
plot-Pmcmc (plot), 74	print, unshowable-method (print), 86
plot-pomp (plot), 74	prior_spec, 6, 10, 28, 30, 37, 39, 40, 42, 69,
plot-probe_match_objfun(plot), 74	86, 97, 100, 105, 115, 131, 133
plot-probed_pomp (plot), 74	probe, 6, 9, 17, 54, 74, 87, 92, 111, 118, 137,
plot-spect_match_objfun(plot), 74	139
plot-spectd_pomp (plot), 74	probe, ANY-method (probe), 87
plot-wpfilterd_pomp(plot), 74	probe, data.frame-method (probe), 87
pmcmc, 6, 9, 23, 26, 27, 45, 46, 53, 61, 64, 74,	probe, missing-method (probe), 87
76, 85, 92, 95, 121, 125, 139	probe, objfun-method (probe), 87
pmcmc, ANY-method (pmcmc), 76	probe, pomp-method (probe), 87
pmcmc, data.frame-method (pmcmc), 76	<pre>probe, probe_match_objfun-method</pre>
pmcmc, missing-method (pmcmc), 76	(probe), 87
pmcmc,pfilterd_pomp-method(pmcmc),76	<pre>probe, probed_pomp-method (probe), 87</pre>
pmcmc,pmcmcd_pomp-method(pmcmc),76	probe-data.frame (probe), 87
pmcmc, pomp-method (pmcmc), 76	probe-objfun (probe), 87
pmcmc-data.frame(pmcmc),76	probe-pomp (probe), 87
pmcmc-pfilterd_pomp(pmcmc), 76	probe-probe_match_obfjun(probe), 87
pmcmc-pmcmcd_pomp (pmcmc), 76	probe-probed_pomp (probe), 87
pmcmc-pomp (pmcmc), 76	probe.acf(basic_probes), 16

<pre>probe.ccf (basic_probes), 16</pre>	rinit_spec, 6, 10, 28, 30, 37, 39, 42, 69, 87,
<pre>probe.marginal (basic_probes), 16</pre>	96, 96, 100, 105, 115, 131, 133
probe.match, 6, 9, 17, 23, 53, 61, 64, 79, 89,	rmeasure, 38, 40, 41, 47, 70, 96, 98, 100, 101,
90, 108, 118, 121	114, 136, 137
<pre>probe.mean (basic_probes), 16</pre>	rmeasure, ANY-method (rmeasure), 98
probe.median(basic_probes), 16	rmeasure, missing-method (rmeasure), 98
probe.nlar(basic_probes), 16	rmeasure, pomp-method (rmeasure), 98
probe.period (basic_probes), 16	rmeasure-pomp (rmeasure), 98
probe.quantile (basic_probes), 16	rmeasure_spec, 6, 10, 28, 30, 37, 39, 42, 69,
probe.sd (basic_probes), 16	87, 97, 99, 99, 105, 115, 131, 133
probe.var (basic_probes), 16	rprior, 38, 40, 41, 47, 70, 96, 99, 100, 101,
probe_objfun, 17	114, 136, 137
probe_objfun(probe.match), 90	rprior, ANY-method (rprior), 100
	rprior, missing-method (rprior), 100
probe_objfun, ANY-method (probe.match),	rprior, pomp-method (rprior), 100
90	rprior-pomp (rprior), 100
probe_objfun,data.frame-method	rprocess, 38, 40, 41, 47, 70, 96, 99, 100, 101,
(probe.match), 90	114, 136, 137
probe_objfun,missing-method	rprocess plugins, 8, 22, 52, 58, 63, 73, 78,
(probe.match), 90	· -
<pre>probe_objfun,pomp-method(probe.match),</pre>	80, 88, 91, 110, 117, 120, 138
90	rprocess, ANY-method (rprocess), 101
<pre>probe_objfun,probe_match_objfun-method</pre>	rprocess, missing-method (rprocess), 101
(probe.match), 90	rprocess, pomp-method (rprocess), 101
<pre>probe_objfun,probed_pomp-method</pre>	rprocess-pomp (rprocess), 101
(probe.match), 90	rprocess_spec, 6, 10, 28, 30, 37, 39, 42, 69,
<pre>probe_objfun-data.frame (probe.match),</pre>	87, 97, 100, 101, 102, 115, 131, 133
90	runifDesign, 33
<pre>probe_objfun-pomp (probe.match), 90</pre>	runifDesign (design), 33
probe_objfun-probe_match_objfun	rw. sd, <i>58</i> , 105
(probe.match), 90	rw2, 19, 20, 32, 43, 49, 56, 66, 71, 83, 84, 95,
<pre>probe_objfun-probed_pomp (probe.match),</pre>	106, 112, 135
90	
profileDesign (design), 33	sannbox, 107
proposals, 93	see ?rprocess_spec for the
pi oposa13, 75	documentation on these
	plugins, 8, 22, 52, 58, 63, 73, 78,
quantile, 17	80, 88, 91, 110, 117, 120, 138
	set.seed, <i>14</i>
R CMD SHLIB, 29, 30	simulate, 6, 74, 88, 89, 108, 117, 118, 132,
readRDS, 15	137, 139
reulermultinom (distributions), 35	<pre>simulate,data.frame-method(simulate),</pre>
rgammawn (distributions), 35	108
ricker, 19, 20, 32, 43, 49, 56, 66, 71, 83, 84,	simulate, missing-method (simulate), 108
95, 106, 112, 135	simulate, objfun-method (simulate), 108
rinit, 38, 40, 41, 47, 70, 96, 99–101, 114, 137	simulate, pomp-method (simulate), 108
rinit, ANY-method (rinit), 96	simulate-data.frame (simulate), 108
rinit, missing-method (rinit), 96	simulate-missing (simulate), 108
rinit, pomp-method (rinit), 96	simulate-objfun (simulate), 108
rinit-pomp (rinit), 96	simulate-pomp (simulate), 108

sir, 10, 83	<pre>spect_objfun-spect_match_objfun</pre>
sir(sir_models), 111	(spect.match), 118
sir2, <i>84</i>	<pre>spect_objfun-spectd_pomp(spect.match)</pre>
sir2(sir_models), 111	118
sir_models, 19, 20, 32, 43, 49, 56, 66, 71, 84,	sprintf, 24
<i>95</i> , <i>106</i> , 111, <i>135</i>	spy, <i>51</i> , 122
skeleton, 38, 40, 41, 47, 70, 96, 99–101, 113,	spy, ANY-method (spy), 122
130, 136, 137	spy, missing-method(spy), 122
skeleton, ANY-method (skeleton), 113	spy,pomp-method(spy), 122
skeleton, missing-method (skeleton), 113	states, 122
skeleton, pomp-method (skeleton), 113	states, pomp-method (states), 122
skeleton-pomp (skeleton), 113	states-pomp (states), 122
skeleton_spec, 6, 10, 28, 30, 37, 39, 42, 69,	stew (bake), 14
87, 97, 100, 105, 114, 114, 131, 133	subplex, <i>92</i> , <i>121</i> , <i>128</i>
sliceDesign (design), 33	summary (summary-probed_pomp), 123
sobolDesign, 33	summary,objfun-method
sobolDesign (design), 33	(summary-probed_pomp), 123
spect, 6, 9, 17, 74, 89, 92, 111, 115, 121, 139	summary,probed_pomp-method
spect, ANY-method (spect), 115	(summary-probed_pomp), 123
spect, data.frame-method (spect), 115	summary, spectd_pomp-method
spect, missing-method (spect), 115	(summary-probed_pomp), 123
spect, objfun-method (spect), 115	<pre>summary-objfun(summary-probed_pomp),</pre>
spect, pomp-method (spect), 115	123
spect, spect_match_objfun-method	summary-probed_pomp, 123
(spect), 115	summary-spectd_pomp
spect, spectd_pomp-method (spect), 115	(summary-probed_pomp), 123
spect-data.frame(spect), 115	time, 123
spect-objfun (spect), 115	time, missing-method (time), 123
spect-pomp (spect), 115	time, pomp-method (time), 123
spect-spect_match_objfun(spect), 115	time-pomp (time), 123
spect-spectd_pomp (spect), 115	time<- (time), 123
spect.match, 6, 9, 23, 53, 61, 64, 79, 92, 118	time<-, pomp-method (time), 123
spect_objfun(spect.match), 118	time <pomp (time),="" 123<="" td=""></pomp>
spect_objfun, ANY-method (spect.match),	timezero, 124
118	timezero, ANY-method (timezero), 124
spect_objfun,data.frame-method	timezero, missing-method (timezero), 124
(spect.match), 118	timezero, pomp-method (timezero), 124
spect_objfun,missing-method	timezero-pomp (timezero), 124
(spect.match), 118	timezero<- (timezero), 124
<pre>spect_objfun,pomp-method(spect.match),</pre>	timezero<-, ANY-method (timezero), 124
118	timezero<-,missing-method(timezero),
<pre>spect_objfun,spect_match_objfun-method</pre>	124
(spect.match), 118	timezero<-,pomp-method(timezero), 124
spect_objfun, spectd_pomp-method	timezero <pomp (timezero),="" 124<="" td=""></pomp>
(spect.match), 118	traces, 125
<pre>spect_objfun-data.frame (spect.match),</pre>	traces, Abc-method (traces), 125
118	traces, abcd_pomp-method (traces), 125
<pre>spect_objfun-pomp (spect.match), 118</pre>	traces, abcList-method (traces), 125

traces, ANY-method (traces), 125	vectorfield(skeleton_spec), 114
traces, Mif2-method (traces), 125	verhulst, 19, 20, 32, 43, 49, 56, 66, 71, 84,
<pre>traces, mif2d_pomp-method (traces), 125</pre>	<i>95, 106, 112,</i> 134
traces, mif2List-method (traces), 125	
traces, missing-method (traces), 125	window, 136
traces, Pmcmc-method (traces), 125	window, pomp-method (window), 136
<pre>traces,pmcmcd_pomp-method(traces), 125</pre>	window-pomp (window), 136
traces, pmcmcList-method (traces), 125	workhorses, 38, 40, 41, 47, 49, 70, 96,
traces-Abc (traces), 125	<i>99–101, 114,</i> 136
traces-abcd_pomp (traces), 125	wpfilter, 6, 23, 26, 45, 46, 61, 74, 79, 85, 89,
traces-abcList (traces), 125	111, 118, 137
traces-Mif2 (traces), 125	wpfilter, ANY-method (wpfilter), 137
traces-mif2d_pomp (traces), 125	<pre>wpfilter,data.frame-method(wpfilter),</pre>
traces-mif2List (traces), 125	137
traces-Pmcmc (traces), 125	wpfilter, missing-method (wpfilter), 137
traces-pmcmcd_pomp (traces), 125	wpfilter, pomp-method (wpfilter), 137
traces-pmcmcList (traces), 125	<pre>wpfilter,wpfilterd_pomp-method</pre>
traj.match, 6, 108, 114, 126	(wpfilter), 137
traj_objfun(traj.match), 126	wpfilter-data.frame(wpfilter), 137
traj_objfun, ANY-method (traj.match), 126	wpfilter-pomp (wpfilter), 137
traj_objfun,data.frame-method	<pre>wpfilter-wpfilterd_pomp(wpfilter), 137</pre>
(traj.match), 126	<pre>wpfilterd_pomp (wpfilter), 137</pre>
traj_objfun,missing-method	<pre>wpfilterd_pomp-class (wpfilter), 137</pre>
(traj.match), 126	
<pre>traj_objfun,pomp-method(traj.match),</pre>	
126	
traj_objfun,traj_match_objfun-method	
(traj.match), 126	
traj_objfun-data.frame (traj.match), 126	
traj_objfun-pomp(traj.match), 126	
traj_objfun-traj_match_objfun	
(traj.match), 126	
trajectory, 47, 113, 114, 128, 129, 137	
trajectory, ANY-method (trajectory), 129	
trajectory, missing-method (trajectory),	
129	
trajectory, pomp-method (trajectory), 129	
trajectory,traj_match_objfun-method	
(trajectory), 129	
trajectory-pomp (trajectory), 129	
trajectory-traj_match_objfun	
(trajectory), 129	
transformations, 6, 10, 28, 30, 37, 39, 42,	
69, 87, 97, 100, 105, 115, 130, 133	
userdata, 6, 10, 28, 30, 37, 39, 42, 69, 87, 97,	
<i>100, 105, 115, 131,</i> 131	
vectorfield, <i>81</i> , <i>127</i>	