# Package 'spatPomp'

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### **Description**

The **spatPomp** package provides facilities for inference on panel data using spatiotemporal partially-observed Markov process (SPATPOMP) models. To do so, it relies on and extends a number of facilities that the **pomp** package provides for inference on time series data using partially-observed Markov process (POMP) models.

The **spatPomp** package concerns models consisting of a collection of interacting units. The methods in **spatPomp** may be applicable whether or not these units correspond to spatial locations.

### Data analysis using spatPomp

The first step in using **spatPomp** is to encode one's model(s) and data in objects of class spatPomp. This can be done via a call to the **spatPomp** constructor function.

#### Extending the pomp platform for developing inference tools

**spatPomp** extends to panel data the general interface to the components of POMP models provided by **pomp**. In doing so, it contributes to the goal of the **pomp** project of facilitating the development of new algorithms in an environment where they can be tested and compared on a growing body of models and datasets.

#### **Documentation**

spatPomp is described by Asfaw et al. (2020)

#### License

spatPomp is provided under the MIT License.

### Author(s)

Kidus Asfaw, Joonha Park, Allister Ho, Edward Ionides, Aaron King

### References

Asfaw, K. et al. (2020) Statistical inference for spatiotemporal partially observed Markov processes via the R package spatPomp. *Manuscript in preparation*.

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#### See Also

pomp package

abf

Adapted Bagged Filter (ABF)

### **Description**

An algorithm for estimating the likelihood of a spatiotemporal partially-observed Markov process model. Running abf causes the algorithm to run bootstrap replicate jobs which each yield an imperfect adapted simulation. Simulating from the "adapted filter" distribution runs into a curse of dimensionality (COD) problem, which is mitigated by keeping particles in each replicate close to each other through resampling down to one particle per replicate at each observation time point. The adapted simulations are then weighted in a way that mitigates COD by making a weak coupling assumption to get an approximate filter distribution. As a by-product, we also get an estimate of the likelihood of the data.

#### Usage

```
## S4 method for signature 'spatPomp'
abf(
  object,
 Nrep,
 Np,
 nbhd,
  tol = 1e-300,
  verbose = getOption("verbose", FALSE)
)
## S4 method for signature 'abfd_spatPomp'
abf(
  object,
 Nrep,
 Nρ,
  nbhd,
  tol = 1e-300,
  verbose = getOption("verbose", FALSE)
)
```

### **Arguments**

object A spatPomp object.

Nrep The number of bootstrap replicates for the adapted simulations.

Np The number of particles used within each replicate for the adapted simulations.

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nbhd	A neighborhood function with three arguments: object, time and unit. The function should return a list of two-element vectors that represent space-time neighbors of $(u,n)$ , which is represented by c(unit, time). See example below for more details.
tol	If the resampling weight for a particle is zero due to floating-point precision issues, it is set to the value of tol since resampling has to be done.
•••	If a params argument is specified, abf will estimate the likelihood at that parameter set instead of at coef(object).
verbose	logical; if TRUE, messages updating the user on progress will be printed to the console.

#### Value

Upon successful completion, abf() returns an object of class 'abfd\_spatPomp' containing the algorithmic parameters used to run abf() and the estimated likelihood.

#### Methods

The following methods are available for such an object:

logLik yields an estimate of the log-likelihood of the data under the model.

#### See Also

Other particle filter methods: abfir(), bpfilter(), enkf(), girf(), ienkf(), igirf(), iubf()

#### **Examples**

```
# Create a simulation of a Brownian motion
b <- bm(U=3, N=10)

# Create a neighborhood function mapping a point in space-time
# to a list of neighboring points in space-time
bm_nbhd <- function(object, time, unit) {
   nbhd_list = list()
   if(time > 1 && unit > 1){
      nbhd_list = c(nbhd_list, list(c(unit-1, time-1)))
   }
   return(nbhd_list)
}

# Run ABF specified number of Monte Carlo replicates and particles per replicate
abfd_bm <- abf(b, Nrep=2, Np=10, nbhd=bm_nbhd)

# Get the likelihood estimate from ABF
logLik(abfd_bm)</pre>
```

abfir 5

abfir

Adapted Bagged Filter with Intermediate Resampling (ABF-IR)

#### **Description**

An algorithm for estimating the filter distribution and likelihood of a spatiotemporal partially-observed Markov process model. Running abfir causes the algorithm to run Monte Carlo replicated jobs which each carry out an adapted simulation using intermediate resampling. Adapted simulation is an easier task than filtering, since particles in each replicate remain close to each other. Intermediate resampling further assists against the curse of dimensionality (COD) problem for importance sampling. The adapted simulations are then weighted in a way that mitigates COD by making a weak coupling assumption to get an approximate filter distribution. As a by-product, we also get an approximation to the likelihood of the data.

### Usage

```
## S4 method for signature 'spatPomp'
abfir(
   object,
   Np,
   Nrep,
   nbhd,
   Ninter,
   tol = (1e-300),
   ...,
   verbose = getOption("verbose", FALSE)
)

## S4 method for signature 'abfird_spatPomp'
abfir(object, Np, Nrep, nbhd, Ninter, tol, ...)
```

A spatPomp object.

### Arguments

object

Np	The number of particles used within each replicate for the adapted simulations.
Nrep	The number of bootstrap replicates for the adapted simulations.
nbhd	A neighborhood function with three arguments: object, time and unit. The function should return a list of two-element vectors that represent space-time neighbors of $(u, n)$ , which is represented by c(unit, time). See example below for more details.

Ninter the number of intermediate resampling time points.

tol If the resampling weight for a particle is zero due to floating-point precision

issues, it is set to the value of tol since resampling has to be done.

... If a params argument is specified, abf will estimate the likelihood at that pa-

rameter set instead of at coef(object).

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verbose

logical; if TRUE, messages updating the user on progress will be printed to the console.

#### Value

Upon successful completion, abfir() returns an object of class 'abfird\_spatPomp' containing the algorithmic parameters used to run abfir() and the estimated likelihood.

#### Methods

The following methods are available for such an object:

logLik yields a biased estimate of the log-likelihood of the data under the model.

#### See Also

```
Other particle filter methods: abf(), bpfilter(), enkf(), girf(), ienkf(), igirf(), iubf()
```

### **Examples**

```
# Create a simulation of a Brownian motion
b < -bm(U=3, N=10)
# Create a neighborhood function mapping a point in space-time
# to a list of ``neighboring points" in space-time
bm_nbhd <- function(object, time, unit) {</pre>
  nbhd_list = list()
  if(time > 1 && unit > 1){
    nbhd_list = c(nbhd_list, list(c(unit-1, time-1)))
  return(nbhd_list)
}
# Run ABFIR with specified number of Monte Carlo replicates and particles per replicate
abfird_bm <- abfir(b,</pre>
                  Nrep = 2,
                  Np=20,
                  nbhd = bm_nbhd,
                  Ninter = length(unit_names(b)))
# Get the likelihood estimate from ABFIR
logLik(abfird_bm)
```

as.data.frame

Coerce to data frame

#### **Description**

**spatPomp** objects can be recast as data frames.

as\_spatPomp 7

### Usage

```
## S3 method for class 'spatPomp'
as.data.frame(x, ...)
```

### **Arguments**

x a spatPomp object.

... additional arguments to be passed to or from methods.

#### **Details**

When object is a simple 'spatPomp' object, as(object, "data.frame") or as.data.frame(object) results in a data frame with the times, units, observables, states (if known), and interpolated covariates (if any).

#### Value

A 'data.frame' with columns for time, spatial unit and observations.

as\_spatPomp

Coerce to spatPomp

### **Description**

Convert to class spatPomp object

#### **Details**

When object is a simple 'pomp' object, construct and return a one-dimensional 'spatPomp' object.

#### Value

a class 'spatPomp' representation of the object.

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bm

Brownian motion spatPomp simulator

### **Description**

Generate a class 'spatPomp' object representing a U-dimensional Brownian motion with spatial correlation decaying geometrically with distance around a circle. The model is defined in continuous time though in this case an Euler approximation is exact at the evaluation times.

### Usage

```
bm(U = 5, N = 100, delta_t = 0.1)
```

#### Arguments

U A length-one numeric signifying dimension of the process.

N A length-one numeric signifying the number of observation time steps to evolve

the process.

delta\_t Process simulations are performed every delta\_t time units whereas observa-

tions occur every one time unit

#### Value

An object of class 'spatPomp' representing a simulation from a U-dimensional Brownian motion

#### **Examples**

```
b \leftarrow bm(U=4, N=20) # See all the model specifications of the object spy(b)
```

**bpfilter** 

Block particle filter (BPF)

### **Description**

An implementation of the block particle filter algorithm of Rebeschini and van Handel (2015), which is used to estimate the filter distribution of a spatiotemporal partially-observed Markov process. bpfilter requires a partition of the spatial units which can be provided by either the block\_size or the block\_list argument. The elements of the partition are called blocks. We perform resampling for each block independently based on sample weights within the block. Each resampled block only contains latent states for the spatial components within the block which allows for a "cross-pollination" of particles where the highest weighted segments of each particle are more likely to be resampled and get combined with resampled components of other particles. The method mitigates the curse of dimensionality by resampling locally.

bpfilter 9

#### Usage

```
## S4 method for signature 'spatPomp'
bpfilter(
  object,
  Np,
  block_size,
  block_list,
  save_states,
    ...,
  verbose = getOption("verbose", FALSE)
)
```

#### **Arguments**

object	A spatPomp object.
Np	The number of particles used within each replicate for the adapted simulations.
block_size	The number of spatial units per block. If this is provided, the method subdivides units approximately evenly into blocks with size block_size.
block_list	List that specifies an exact partition of the spatial units. Each partition element, or block, is an integer vector of neighboring units.
save_states	logical. If True, the state-vector for each particle and block is saved.
•••	If a params argument is specified, bpfilter will estimate the likelihood at that parameter set instead of at coef(object).
verbose	logical; if TRUE, messages updating the user on progress will be printed to the console.

#### Value

Upon successful completion, bpfilter() returns an object of class 'bpfilterd\_spatPomp' containing the algorithmic parameters used to run bpfilter() and the estimated likelihood.

### **Details**

Only one of block\_size or block\_list should be specified. If both or neither is provided, an error is triggered.

#### Methods

The following methods are available for such an object:

logLik yields an estimate of the log-likelihood of the data under the model.

### References

Rebeschini, P., & Van Handel, R. (2015). Can local particle filters beat the curse of dimensionality?. *The Annals of Applied Probability*, **25(5)**, 2809-2866.

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#### See Also

```
Other particle filter methods: abfir(), abf(), enkf(), girf(), ienkf(), igirf(), iubf()
```

#### **Examples**

city\_data\_UK

City data in the United Kingdom

### Description

Population and birth information about cities in England and Wales during the measles pre-vaccine era.

#### **Details**

Data includes births and population at bi-weekly observations from 40 cities and towns.

#### Value

a 'data.frame' of the 40 largest cities and towns in the UK and Wales, their latitude, longitude and mean population during the measles pre-vaccine period.

#### References

Dalziel, Benjamin D. et al. (2016) Persistent chaos of measles epidemics in the prevaccination United States caused by a small change in seasonal transmission patterns. *PLoS computational biology*, **12(2)**, e1004655. DOI: 10.5061/dryad.r4q34

#### See Also

Other datasets: measlesUK

dunit\_measure 11

dunit_measure	dunit_measure dunit_measure evaluates the unit measurement den- sity of a unit's observation given the entire state

#### **Description**

dunit\_measure dunit\_measure evaluates the unit measurement density of a unit's observation given the entire state

#### Usage

```
## S4 method for signature 'spatPomp'
dunit_measure(object, y, x, unit, time, params, log = TRUE, ...)
```

#### **Arguments**

object	An object of class spatPomp
у	A U by 1 matrix of observations for all units
x	A state vector for all units
unit	The unit for which to evaluate the unit measurement density
time	The time for which to evaluate the unit measurement density
params	parameters at which to evaluate the unit measurement density
log	logical; should the density be returned on log scale?
• • •	additional arguments will be ignored

### Value

A class 'matrix' with the unit measurement density for spatial unit unit corresponding to the corresponding measurement in y and states in x.

### **Examples**

```
b <- bm(U=3)
s <- states(b)[,1,drop=FALSE]
rownames(s) -> rn
dim(s) <- c(3,1,1)
dimnames(s) <- list(variable=rn, rep=NULL)
p <- coef(b); names(p) -> rnp
dim(p) <- c(length(p),1); dimnames(p) <- list(param=rnp)
o <- obs(b)[,1,drop=FALSE]
dunit_measure(b, y=o, x=s, unit=1, time=1, params=p)</pre>
```

12 enkf

e	n	k	f

Generalized Ensemble Kalman filter (EnKF)

### **Description**

A function to perform filtering using the ensemble Kalman filter of Evensen, G. (1994). This function is generalized to allow for an measurement covariance matrix that varies over time. This is useful if the measurement model varies with the state.

### Usage

```
## S4 method for signature 'spatPomp'
enkf(data, Np, ..., verbose = getOption("verbose", FALSE))
```

### **Arguments**

data	A spatPomp object.
Np	The number of Monte Carlo particles used to approximate the filter distribution.
	If a params argument is specified, abf will estimate the likelihood at that parameter set instead of at coef(object).
verbose	logical; if TRUE, messages updating the user on progress will be printed to the console.

#### Value

An object of class 'enkfd\_spatPomp' that contains the estimate of the log likelihood (via the loglik attribute), algorithmic parameters used to run enkf(). Also included are estimated filter means, prediction means and forecasts that are generated during an enkf() run.

#### References

- G. Evensen. Sequential data assimilation with a nonlinear quasi-geostrophic model using Monte Carlo methods to forecast error statistics. *Journal of Geophysical Research: Oceans* **99**, 10143–10162, 1994.
- G. Evensen. Data assimilation: the ensemble Kalman filter. Springer-Verlag, 2009.
- J.L. Anderson. An Ensemble Adjustment Kalman Filter for Data Assimilation. *Monthly Weather Review* **129**, 2884–2903, 2001.

#### See Also

```
Other particle filter methods: abfir(), abf(), bpfilter(), girf(), ienkf(), igirf(), iubf()
```

eunit\_measure 13

#### **Examples**

```
# Create a simulation of a Brownian motion
b <- bm(U=6, N=10)

# Run EnKF
enkfd_bm <- enkf(b, Np = 100)

# Get a likelihood estimate
logLik(enkfd_bm)</pre>
```

eunit\_measure

eunit\_measure

### **Description**

eunit\_measure evaluates the expectation of a unit's observation given the entire state

### Usage

```
## S4 method for signature 'spatPomp'
eunit_measure(object, x, unit, time, params, Np = 1, log = FALSE)
```

### **Arguments**

object	An object of class spatPomp
X	A state vector for all units
unit	The unit for which to evaluate the expectation
time	The time for which to evaluate the expectation
params	parameters at which to evaluate the unit expectation
Np	numeric; defaults to 1 and the user need not change this
log	logical; should the density be returned on log scale?

#### Value

A class 'matrix' with the unit expected observation for spatial unit unit corresponding to the corresponding states in x.

### **Examples**

```
b <- bm(U=3)
s <- states(b)[,1,drop=FALSE]
rownames(s) -> rn
dim(s) <- c(3,1,1)
dimnames(s) <- list(variable=rn, rep=NULL)
p <- coef(b); names(p) -> rnp
dim(p) <- c(length(p),1); dimnames(p) <- list(param=rnp)
o <- obs(b)[,1,drop=FALSE]
eunit_measure(b, x=s, unit=2, time=1, params=p)</pre>
```

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gbm

Geometric Brownian motion spatPomp simulator

### Description

Generate a spatPomp object representing a U-dimensional geometric Brownian motion with spatial correlation decaying geometrically with distance around a circle. The model is defined in continuous time, but an Euler approximation is used for this numerical implementation.

#### Usage

```
gbm(U = 5, N = 100, delta_t = 0.1, IVP_values = 1, delta_obs = 1)
```

### **Arguments**

U A length-one numeric signifying dimension of the process.

N A length-one numeric signifying the number of time steps to evolve the process.

delta\_t process simulations are performed every delta\_t time units

IVP\_values initial value parameters for the latent states

delta\_obs observations occur every delta\_obs time units

#### Value

An object of class 'spatPomp' representing a simulation from a U-dimensional geometric Brownian motion

### **Examples**

```
g <- gbm(U=4, N=20)  
# See all the model specifications of the object spy(g)
```

girf

Guided intermediate resampling filter (GIRF)

#### **Description**

An implementation of the algorithm of Park and Ionides (2020), following the pseudocode in Asfaw et al. (2020).

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### Usage

```
## S4 method for signature 'missing'
girf(object, ...)
## S4 method for signature 'ANY'
girf(object, ...)
## S4 method for signature 'spatPomp'
girf(
  object,
  Nρ,
  Ninter,
  lookahead = 1,
  Nguide,
  kind = c("bootstrap", "moment"),
  tol,
  . . . ,
  verbose = getOption("verbose", FALSE)
## S4 method for signature 'girfd_spatPomp'
girf(
  object,
  Nρ,
  Ninter,
  lookahead,
  Nguide,
  kind = c("bootstrap", "moment"),
  tol,
  . . .
)
```

### **Arguments**

object	A spatPomp object.
• • •	If a params argument is specified, abf will estimate the likelihood at that parameter set instead of at coef(object).
Np	The number of particles used within each replicate for the adapted simulations.
Ninter	the number of intermediate resampling time points.
lookahead	The number of future observations included in the guide function.
Nguide	The number of simulations used to estimate state process uncertainty for each particle.
kind	One of two types of guide function construction. Defaults to 'bootstrap'. See Park and Ionides (2020) for more details.
tol	If all of the guide function evaluations become too small (beyond floating-point precision limits), we set them to this value.

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verbose

logical; if TRUE, messages updating the user on progress will be printed to the console.

#### Value

Upon successful completion, girf() returns an object of class 'girfd\_spatPomp' which contains the algorithmic parameters that were used to run girf() and the resulting log likelihood estimate.

#### Methods

The following methods are available for such an object:

logLik yields an unbiased estimate of the log-likelihood of the data under the model.

#### References

Park, J. and Ionides, E. L. (2020) Inference on high-dimensional implicit dynamic models using a guided intermediate resampling filter. *Statistics and Computing*, DOI: 10.1007/s11222-020-09957-3

Asfaw, K. et al. (2020) Statistical inference for spatiotemporal partially observed Markov processes via the R package spatPomp. *Manuscript in preparation*.

#### See Also

```
Other particle filter methods: abfir(), abf(), bpfilter(), enkf(), ienkf(), igirf(), iubf()
```

#### **Examples**

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ienkf

Iterated ensemble Kalman filter (IEnKF)

#### Description

An implementation of a parameter estimation algorithm that uses the ensemble Kalman filter (Evensen, G. (1994)) to perform the filtering step in the parameter-perturbed iterated filtering scheme of Ionides et al. (2015) following the pseudocode in Asfaw, et al. (2020).

### Usage

```
## S4 method for signature 'spatPomp'
ienkf(
  data,
  Nenkf = 1,
  rw.sd,
  cooling.type = c("geometric", "hyperbolic"),
  cooling.fraction.50,
  Np,
   ...,
  verbose = getOption("verbose", FALSE)
)
```

#### **Arguments**

data

an object of class spatPomp

Nenkf

number of iterations of perturbed EnKF.

rw.sd

specification of the magnitude of the random-walk perturbations that will be applied to some or all model parameters. Parameters that are to be estimated should have positive perturbations specified here. The specification is given using the rw.sd function, which creates a list of unevaluated expressions. The latter are evaluated in a context where the model time variable is defined (as time). The expression ivp(s) can be used in this context as shorthand for

```
ifelse(time==time[1],s,0).
```

Likewise, ivp(s,lag) is equivalent to

ifelse(time==time[lag],s,0).

See below for some examples.

The perturbations that are applied are normally distributed with the specified s.d. If parameter transformations have been supplied, then the perturbations are applied on the transformed (estimation) scale.

cooling.type

specifications for the cooling schedule, i.e., the manner and rate with which the intensity of the parameter perturbations is reduced with successive filtering iterations. cooling.type specifies the nature of the cooling schedule. See below (under "Specifying the perturbations") for more detail.

ie

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cooling.fraction.50

specifications for the cooling schedule, i.e., the manner and rate with which the intensity of the parameter perturbations is reduced with successive filtering iterations. cooling.type specifies the nature of the cooling schedule. See below

(under "Specifying the perturbations") for more detail.

Np The number of particles used within each replicate for the adapted simulations.

... If a params argument is specified, abf will estimate the likelihood at that pa-

rameter set instead of at coef(object).

verbose logical; if TRUE, messages updating the user on progress will be printed to the

console.

#### Value

Upon successful completion, ienkf returns an object of class 'ienkfd\_spatPomp'. This object contains the convergence record of the iterative algorithm with respect to the likelihood and the parameters of the model (which can be accessed using the traces attribute) as well as a final parameter estimate, which can be accessed using the coef().

#### Methods

The following methods are available for such an object:

coef gives the Monte Carlo estimate of the maximum likelihood.

#### References

Evensen, G. (1994) Sequential data assimilation with a nonlinear quasi-geostrophic model using Monte Carlo methods to forecast error statistics Journal of Geophysical Research: Oceans 99:10143–10162

Evensen, G. (2009) Data assimilation: the ensemble Kalman filter Springer-Verlag.

Anderson, J. L. (2001) An Ensemble Adjustment Kalman Filter for Data Assimilation Monthly Weather Review 129:2884–2903

#### See Also

```
Other particle filter methods: abfir(), abf(), bpfilter(), enkf(), girf(), igirf(), iubf()
Other spatPomp parameter estimation methods: igirf(), iubf()
```

igirf

Iterated guided intermediate resampling filter (IGIRF)

#### **Description**

An implementation of a parameter estimation algorithm combining the intermediate resampling scheme of the guided intermediate resampling filter of Park and Ionides (2020) and the parameter perturbation scheme of Ionides et al. (2015) following the pseudocode in Asfaw, et al. (2020).

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### Usage

```
## S4 method for signature 'missing'
igirf(data, ...)
## S4 method for signature 'ANY'
igirf(data, ...)
## S4 method for signature 'spatPomp'
igirf(
 data,
 Ngirf,
 Nρ,
  rw.sd,
  cooling.type,
  cooling.fraction.50,
 Ninter,
 lookahead = 1,
 Nguide,
 kind = c("bootstrap", "moment"),
  tol = 1e-300,
  verbose = getOption("verbose", FALSE)
)
## S4 method for signature 'igirfd_spatPomp'
igirf(
 data,
 Ngirf,
 Nρ,
  rw.sd,
  cooling.type,
  cooling.fraction.50,
 Ninter,
  lookahead,
 Nguide,
 kind = c("bootstrap", "moment"),
  tol,
 verbose = getOption("verbose", FALSE)
)
```

### **Arguments**

```
    an object of class spatPomp or igirfd_spatPomp
    If a params argument is specified, abf will estimate the likelihood at that parameter set instead of at coef(object).
    Ngirf the number of iterations of parameter-perturbed GIRF.
```

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Np

The number of particles used within each replicate for the adapted simulations.

rw.sd

specification of the magnitude of the random-walk perturbations that will be applied to some or all model parameters. Parameters that are to be estimated should have positive perturbations specified here. The specification is given using the rw.sd function, which creates a list of unevaluated expressions. The latter are evaluated in a context where the model time variable is defined (as time). The expression ivp(s) can be used in this context as shorthand for

ifelse(time==time[1],s,0).

Likewise, ivp(s,lag) is equivalent to

ifelse(time==time[lag],s,0).

See below for some examples.

The perturbations that are applied are normally distributed with the specified s.d. If parameter transformations have been supplied, then the perturbations are applied on the transformed (estimation) scale.

cooling.type

specifications for the cooling schedule, i.e., the manner and rate with which the intensity of the parameter perturbations is reduced with successive filtering iterations. cooling.type specifies the nature of the cooling schedule. See below (under "Specifying the perturbations") for more detail.

cooling.fraction.50

specifications for the cooling schedule, i.e., the manner and rate with which the intensity of the parameter perturbations is reduced with successive filtering iterations. cooling.type specifies the nature of the cooling schedule. See below (under "Specifying the perturbations") for more detail.

Ninter the number of intermediate resampling time points.

lookahead The number of future observations included in the guide function.

Nguide The number of simulations used to estimate state process uncertainty for each

particle.

kind One of two types of guide function construction. Defaults to 'bootstrap'. See

Park and Ionides (2020) for more details.

tol If all of the guide function evaluations become too small (beyond floating-point

precision limits), we set them to this value.

verbose logical; if TRUE, messages updating the user on progress will be printed to the

console.

#### Value

Upon successful completion, <code>igirf()</code> returns an object of class 'igirfd\_spatPomp'. This object contains the convergence record of the iterative algorithm with respect to the likelihood and the parameters of the model (which can be accessed using the traces attribute) as well as a final parameter estimate, which can be accessed using the <code>coef()</code>. The algorithmic parameters used to run <code>igirf()</code> are also included.

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#### Methods

The following methods are available for such an object:

coef gives the Monte Carlo maximum likelihood parameter estimate.

#### References

Park, J. and Ionides, E. L. (2020) Inference on high-dimensional implicit dynamic models using a guided intermediate resampling filter. *Statistics and Computing*, DOI: 10.1007/s11222-020-09957-3

Asfaw, K. et al. (2020) Statistical inference for spatiotemporal partially observed Markov processes via the R package spatPomp. *Manuscript in preparation*.

#### See Also

```
Other particle filter methods: abfir(), abf(), bpfilter(), enkf(), girf(), ienkf(), iubf()
Other spatPomp parameter estimation methods: ienkf(), iubf()
```

iubf

Iterated Unadapted Bagged Filter (IUBF)

#### **Description**

An algorithm for estimating the parameters of a spatiotemporal partially-observed Markov process. Running iubf causes the algorithm to perform a specified number of iterations of unadapted simulations with parameter perturbation and parameter resamplings. At each iteration, unadapted simulations are performed on a perturbed version of the model, in which the parameters to be estimated are subjected to random perturbations at each observation. After cycling through the data, each replicate's weight is calculated and is used to rank the bootstrap replicates. The highest ranking replicates are recycled into the next iteration. This extra variability introduced through parameter perturbation effectively smooths the likelihood surface and combats particle depletion by introducing diversity into particle population. As the iterations progress, the magnitude of the perturbations is diminished according to a user-specified cooling schedule.

### Usage

```
## $4 method for signature 'spatPomp'
iubf(
  object,
  Nubf = 1,
  Nrep_per_param,
  Nparam,
  nbhd,
  prop,
  rw.sd,
  cooling.type = c("geometric", "hyperbolic"),
```

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```
cooling.fraction.50,
  tol = (1e-18)^17,
  verbose = getOption("verbose"),
)
```

#### **Arguments**

nbhd

object A spatPomp object.

Nubf The number of iterations to perform

Nrep\_per\_param The number of replicates used to estimate the likelihood at a parameter

The number of parameters that will undergo the iterated perturbation **Nparam** 

> A neighborhood function with three arguments: object, time and unit. The function should return a list of two-element vectors that represent space-time neighbors of (u, n), which is represented by c(unit, time). See example below

for more details.

A numeric between 0 and 1. The top prop\*100% of the parameters are resamprop

pled at each observation

rw.sd specification of the magnitude of the random-walk perturbations that will be

applied to some or all model parameters. Parameters that are to be estimated should have positive perturbations specified here. The specification is given using the rw. sd function, which creates a list of unevaluated expressions. The latter are evaluated in a context where the model time variable is defined (as time). The expression ivp(s) can be used in this context as shorthand for

ifelse(time==time[1],s,0).

Likewise, ivp(s, lag) is equivalent to

ifelse(time==time[lag],s,0).

See below for some examples.

The perturbations that are applied are normally distributed with the specified s.d. If parameter transformations have been supplied, then the perturbations are applied on the transformed (estimation) scale.

cooling.type

specifications for the cooling schedule, i.e., the manner and rate with which the intensity of the parameter perturbations is reduced with successive filtering iterations. cooling.type specifies the nature of the cooling schedule. See below (under "Specifying the perturbations") for more detail.

cooling.fraction.50

specifications for the cooling schedule, i.e., the manner and rate with which the intensity of the parameter perturbations is reduced with successive filtering iterations. cooling.type specifies the nature of the cooling schedule. See below (under "Specifying the perturbations") for more detail.

tol

If the resampling weight for a particle is zero due to floating-point precision

issues, it is set to the value of tol since resampling has to be done.

logical; if TRUE, diagnostic messages will be printed to the console. verbose

logLik 23

• • •

additional arguments supply new or modify existing model characteristics or components. See pomp for a full list of recognized arguments.

When named arguments not recognized by pomp are provided, these are made available to all basic components via the so-called *userdata* facility. This allows the user to pass information to the basic components outside of the usual routes of covariates (covar) and model parameters (params). See userdata for information on how to use this facility.

#### Value

Upon successful completion, iubf() returns an object of class 'iubfd\_spatPomp'. This object contains the convergence record of the iterative algorithm with respect to the likelihood and the parameters of the model (which can be accessed using the traces attribute) as well as a final parameter estimate, which can be accessed using the coef(). The algorithmic parameters used to run iubf() are also included.

#### Methods

The following methods are available for such an object:

coef extracts the point estimate

#### See Also

```
Other particle filter methods: abfir(), abf(), bpfilter(), enkf(), girf(), ienkf(), igirf()
Other spatPomp parameter estimation methods: ienkf(), igirf()
```

logLik

Log likelihood

### **Description**

Extract the estimated log likelihood.

#### Usage

```
## S4 method for signature 'girfd_spatPomp'
logLik(object)

## S4 method for signature 'bpfilterd_spatPomp'
logLik(object)

## S4 method for signature 'abfd_spatPomp'
logLik(object)

## S4 method for signature 'iubfd_spatPomp'
logLik(object)
```

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```
## S4 method for signature 'abfird_spatPomp'
logLik(object)
## S4 method for signature 'igirfd_spatPomp'
logLik(object)
```

### **Arguments**

object

fitted model object

#### Value

a numeric which is the estimated log likelihood

lorenz

Lorenz '96 spatPomp simulator

#### **Description**

Generate a spatPomp object representing a U-dimensional stochastic Lorenz '96 process with N measurements made at times  $t_n = n*delta_obs$ , simulated using an Euler method with time increment delta\_t.

### Usage

```
lorenz(
    U = 5,
    N = 100,
    delta_t = 0.01,
    delta_obs = 0.5,
    regular_params = c(F = 8, sigma = 1, tau = 1)
)
```

#### **Arguments**

U A length-one numeric signifying the number of spatial units for the process.

N A length-one numeric signifying the number of observations.

delta\_t A length-one numeric giving the Euler time step for the numerical solution.

delta\_obs A length-one numeric giving the time between observations.

regular\_params A named numeric vector containing the values of the F, sigma and tau parame-

ters. F=8 is a common value that causes chaotic behavior.

#### Value

An object of class 'spatPomp' representing a simulation from a U-dimensional Lorenz 96 model

mcap 25

#### References

Lorenz, E. N. (1996) Predictability: A problem partly solved. *Proceedings of the seminar on predictability* 

#### **Examples**

```
l <- lorenz(U=5, N=100, delta\_t=0.01, delta\_obs=1) # See all the model specifications of the object spy(1)
```

mcap

Monte Carlo adjusted profile

### **Description**

Given a collection of points maximizing the likelihood over a range of fixed values of a focal parameter, this function constructs a profile likelihood confidence interval accommodating both Monte Carlo error in the profile and statistical uncertainty present in the likelihood function.

### Usage

```
mcap(lp, parameter, confidence = 0.95, lambda = 1, Ngrid = 1000)
```

#### **Arguments**

1p a vector of profile likelihood evaluations.

parameter the corresponding values of the focal parameter.
confidence the required level of the confidence interval.
lambda the loess parameter used to smooth the profile.

Ngrid the number of points to evaluate the smoothed profile.

#### Value

mcap() returns a list including the smoothed profile, a quadratic approximation, and the constructed confidence interval.

#### Author(s)

Edward L. Ionides

26 measles

measles

Measles in UK spatPomp generator

### Description

Generate a spatPomp object for measles in the top-U most populous cities in England and Wales. The model is adapted from He et al. (2010) with gravity transport following Park and Ionides (2019). The data in the object is simulated using the process and measurement models of He et al. (2010).

### Usage

```
measles(
    U = 6,
    dt = 2/365,
    fixed_ivps = TRUE,
    shared_ivps = TRUE,
    S_0 = 0.032,
    E_0 = 5e-05,
    I_0 = 4e-05
)
```

### Arguments

U	A length-one numeric signifying the number of cities to be represented in the spatPomp object.
dt	a numeric (in unit of years) that is used as the Euler time-increment for simulating measles data.
fixed_ivps	a logical. If TRUE initial value parameters will be declared in the globals slot and will not be part of the parameter vector.
shared_ivps	a logical. If TRUE and fixed_ivps=TRUE the values of S_0, E_0 and I_0 in the call to measles will be used as initial value parameters for all spatial units.
S_0	a numeric. If shared_ivps=TRUE and fixed_ivps=TRUE this is the initial proportion of all of the spatial units that are susceptible.
E_0	a numeric. If shared_ivps=TRUE and fixed_ivps=TRUE this is the initial proportion of all of the spatial units that are exposed.
I_0	a numeric. If shared_ivps=TRUE and fixed_ivps=TRUE this is the initial proportion of all of the spatial units that are infected.

#### Value

An object of class 'spatPomp' representing a U-dimensional spatially coupled measles POMP model.

measlesUK 27

#### Note

This function goes through a typical workflow of constructing a typical spatPomp object (1-4 below). This allows the user to have a file that replicates the exercise of model building as well as function that creates a typical nonlinear model in epidemiology in case they want to test a new inference methodology. We purposely do not modularize this function because it is not an operational piece of the package and is instead useful as an example.

- 1. Getting a measurements data frame with columns for times, spatial units and measurements.
- 2. Getting a covariates data.frame with columns for times, spatial units and covariate data.
- 3. Constructing model components (latent state initializer, latent state transition simulator and measurement model). Depending on the methods used, the user may have to supply a vectorfield to be integrated that represents the deterministic skeleton of the latent process.
- 4. Bringing all the data and model components together to form a spatPomp object via a call to spatPomp().

#### References

Robert J. Hijmans (2019). The **geosphere** spherical trigonometry package. https://CRAN.R-project.org/package=geosphere.

#### **Examples**

```
m \ \mbox{\footnotesize <-} \ measles(U = 5) 
 # See all the model specifications of the object spy(m)
```

measlesUK

Measles in the United Kingdom

#### **Description**

Measles case data from various cities and towns in England and Wales during the pre-vaccine era.

#### **Details**

Data includes bi-weekly case counts as well as births and population from 40 cities and towns.

#### Value

a 'data.frame' of the 40 largest cities and towns in the UK and Wales, their latitude, longitude and bi-weekly measles case counts, population and birthrates.

#### References

Dalziel, Benjamin D. et al. (2016) Persistent chaos of measles epidemics in the prevaccination United States caused by a small change in seasonal transmission patterns. *PLoS computational biology*, **12(2)**, e1004655. DOI: 10.5061/dryad.r4q34

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#### See Also

Other datasets: city\_data\_UK

munit\_measure munit\_measure

### Description

munit\_measure returns a moment-matched parameter set given an empirically calculated measurement variance and latent states. This is used in girf() and igirf() when they are run with kind='moment'.

### Usage

```
## S4 method for signature 'spatPomp'
munit_measure(object, x, vc, unit, time, params, Np = 1)
```

### **Arguments**

object	An object of class spatPomp
X	A state vector for all units
VC	The empirically calculated variance used to perform moment-matching
unit	The unit for which to obtain a moment-matched parameter set
time	The time for which to obtain a moment-matched parameter set
params	parameters to use to obtain a moment-matched parameter set
Np	Number of particle replicates for which to get parameter sets

#### Value

An array with dimensions  $\dim(\operatorname{array.params})[1]$  by  $\dim(x)[2]$  by  $\operatorname{length}(\operatorname{unit})$  by  $\operatorname{length}(\operatorname{time})$  representing the moment-matched parameter  $\operatorname{set}(s)$  corresponding to the variance of the measurements, vc, and the states, x.

### **Examples**

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```
dimnames = list(params = rownames(p)))
vc <- c(4, 9, 16); dim(vc) <- c(length(vc), 1, 1)
munit_measure(b, x=s, vc=vc, Np=1, unit = 1, time=1, params=array.params)</pre>
```

plot

Plotting spatPomp data

### **Description**

Visualize spatPomp data
Diagnostic plot for igirf()
Visualize spatPomp data

### Usage

```
## S4 method for signature 'igirfd_spatPomp'
plot(x, params = names(coef(x)), ncol = 3)
## S4 method for signature 'spatPomp'
plot(x, type = c("l", "h"), log = F, ...)
```

### **Arguments**

)	(	a spatPomp object
ŗ	oarams	the names of the parameters for which the user would like to see a trace plot
r	ncol	the number of columns in the grid plot
1	туре	for visualizing an object of class spatPomp, the user can obtain a grid of line plots by default ('1') or a heat map by supplying argument 'h'.
]	log	should the data be log-transformed before plotting? This helps in contexts where there are spikes that could take away attention from the dynamics illustrated by the rest of the data.
		for visualizing an object of class spatPomp, the user can add arguments like nrow to specify the number of rows in the grid.

### Value

a ggplot facet plot of class 'gg' and 'ggplot' visualizing the convergence record of running igirf() with respect to the likelihood and the parameters of the model.

a ggplot plot of class 'gg' and 'ggplot' visualizing the time series data over multiple spatial units via a tile-plot.

pStop

print

Print methods

### Description

Prints its argument.

### Usage

```
## S4 method for signature 'spatPomp'
print(x)
```

### Arguments

Х

a spatPomp object

### Value

An object of class 'spatPomp' is returned \*invisibly\*. The user is notified on the console only the class of the object.

### Note

Use spy() to see model components of x instead.

pStop

pStop

### Description

Custom error function

### Usage

```
pStop(fn, ...)
pStop_(...)
pWarn(fn, ...)
pWarn_(...)
```

### Arguments

```
fn name of function (will be enclosed in single quotes)
```

... message

reexports 31

### Value

No return value as this is simply a custom error function.

reexports	Objects exported from other packages	

### Description

These objects are imported from other packages. Follow the links below to see their documentation.

```
magrittr %>%
```

|--|

### Description

runit\_measure simulates a unit's observation given the entire state

### Usage

```
## S4 method for signature 'spatPomp'
runit_measure(object, x, unit, time, params, log = FALSE)
```

### Arguments

object	An object of class spatPomp
х	A state vector for all units
unit	The unit for which to simulate an observation
time	The time for which to simulate an observation
params	parameters to use to simulate an observation
log	logical; should the density be returned on log scale?

#### Value

A matrix with the simulated observation corresponding to state x and unit unit with parameter set params.

32 simulate

### **Examples**

```
b <- bm(U=3)
s <- states(b)[,1,drop=FALSE]
rownames(s) -> rn
dim(s) <- c(3,1,1)
dimnames(s) <- list(variable=rn, rep=NULL)
p <- coef(b); names(p) -> rnp
dim(p) <- c(length(p),1); dimnames(p) <- list(param=rnp)
o <- obs(b)[,1,drop=FALSE]
runit_measure(b, x=s, unit=2, time=1, params=p)</pre>
```

simulate

Simulation of a spatiotemporal partially-observed Markov process

### **Description**

simulate generates simulations of the latent and measurement processes.

### Usage

```
## S4 method for signature 'spatPomp'
simulate(
  object,
  nsim = 1,
  seed = NULL,
  format = c("spatPomps", "data.frame"),
  include.data = FALSE,
  ...
)
```

### Arguments

object	optional; if present, it should be a data frame or a 'pomp' object.
nsim	number of simulations.
seed	optional; if set, the pseudorandom number generator (RNG) will be initialized with seed. the random seed to use. The RNG will be restored to its original state afterward.
format	the format of the simulated results. If the argument is set to 'spatPomps', the default behavior, then the output is a list of spatPomp objects. Options are 'spatPomps' and 'data.frame'.
include.data	if TRUE, the original data and covariates (if any) are included (with .id = "data"). This option is ignored unless format = "data.frame".
• • •	additional arguments supply new or modify existing model characteristics or components. See pomp for a full list of recognized arguments.

When named arguments not recognized by pomp are provided, these are made available to all basic components via the so-called *userdata* facility. This allows the user to pass information to the basic components outside of the usual routes of covariates (covar) and model parameters (params). See userdata for information on how to use this facility.

#### Value

if format='spatPomps' and nsim=1 an object of class 'spatPomp' representing a simulation from the model in object is returned. If format='spatPomps' and nsim>1 a list of class 'spatPomp' objects is returned. If format='data.frame' then a class 'data.frame' object is returned.

### **Examples**

```
# Get a spatPomp object
b <- bm(U=5, N=10)
# Get 10 simulations from same model as data.frame
sims <- simulate(b, nsim=10, format='data.frame')</pre>
```

spatPomp

Constructor of the spatPomp object

### Description

This function constructs a class 'spatPomp' object, encoding a spatiotemporal partially observed Markov process (SPATPOMP) model together with a uni- or multi-variate time series on a collection of units. Users will typically develop a POMP model for a single unit before embarking on a coupled SpatPOMP analysis. Consequently, we assume some familiarity with **pomp** and its description by King, Nguyen and Ionides (2016). The spatPomp class inherits from pomp with the additional unit structure being a defining feature of the resulting models and inference algorithms.

### Usage

```
spatPomp(
  data,
  units,
  times,
  covar,
  t0,
  ...,
  eunit_measure,
  munit_measure,
  vunit_measure,
  dunit_measure,
  runit_measure,
  runit_mea
```

```
dmeasure,
  skeleton,
  rinit,
  rprior,
  dprior,
  unit_statenames,
 unit_accumvars,
  shared_covarnames,
  globals,
 paramnames,
 params,
  cdir,
  cfile,
  shlib.args,
 PACKAGE,
  partrans,
 compile = TRUE,
  verbose = getOption("verbose", FALSE)
)
```

### **Arguments**

data either a dataframe holding the spatiotemporal data, or an object of class 'spat-

Pomp', i.e., the output of another **spatPomp** calculation. If dataframe, the user must provide the name of the times column using the times argument and the spatial unit column name using the units argument. The dataframe provided should be sorted in increasing order of time and unit name respectively, i.e. observation 1 in unit A should come before observation 1 in unit B, which should

come before observation 2 in unit A.

units when data is a data. frame this is the name of the column containing the spatial

units.

times the sequence of observation times. times must indicate the column of obser-

vation times by name or index. The time vector must be numeric and non-

decreasing.

covar An optional dataframe for supplying covariate information. If provided, there

must be two columns that provide the observation time and the observation spa-

tial unit with the same names and arrangement as the data.

to The zero-time, i.e., the time of the initial state. This must be no later than the

time of the first observation, i.e.,  $t0 \le times[1]$ .

.. If there are arguments that the user would like to pass to **pomp**'s basic construc-

tor function's  $\dots$  argument, this argument passes them along. Not recommended

for this version of **spatPomp**.

rameters. The unit variable is pre-defined, which allows the user to specify differing specifications for each unit using if conditions. Only C snippets are accepted. The C snippet should assign the scalar approximation to the expected measurement to the pre-defined variable ey given the latent state and the param-

eters. For more information, see the examples section below.

munit\_measure

Evaluator of a moment-matched parameter set (like the standard deviation parameter of a normal distribution or the size parameter of a negative binomial distribution) given an empirical variance estimate, the latent states and all model parameters. Only Csnippets are accepted. The Csnippet should assign the scalar approximation to the measurement variance parameter to the pre-defined variable corresponding to that parameter, which has been predefined with a M\_ pre-fix. For instance, if the moment-matched parameter is psi, then the user should assign M\_psi to the moment-matched value. For more information, see the examples section below.

vunit\_measure

Evaluator of the theoretical measurement variance given the latent states and model parameters. The unit variable is pre-defined, which allows the user to specify differing specifications for each unit using if conditions. Only C snippets are accepted. The C snippet should assign the scalar approximation to the measurement variance to the pre-defined variable vc given the latent state and the parameters. For more information, see the examples section below.

dunit\_measure

Evaluator of the unit measurement model density given the measurement, the latent states and model parameters. The unit variable is pre-defined, which allows the user to specify differing specifications for each unit using if conditions. Only Csnippets are accepted. The Csnippet should assign the scalar measurement density to the pre-defined variable lik. The user is encouraged to provide a logged density in an if condition that checks whether the predefined give\_log variable is true. For more information, see the examples section below.

runit\_measure

Simulator of the unit measurement model given the latent states and the model parameters. The unit variable is pre-defined, which allows the user to specify differing specifications for each unit using if conditions. Only Csnippets are accepted. The Csnippet should assign the scalar measurement density to the pre-defined which corresponds to the name of the observation for each unit (e.g. cases for the measles spatPomp example). For more information, see the examples section below.

rprocess

simulator of the latent state process, specified using one of the rprocess plugins. Setting rprocess=NULL removes the latent-state simulator. For more information, see rprocess specification for the documentation on these plugins.

rmeasure

simulator of the measurement model, specified either as a C snippet, an R function, or the name of a pre-compiled native routine available in a dynamically loaded library. Setting rmeasure=NULL removes the measurement model simulator. For more information, see rmeasure specification.

dprocess

optional; specification of the probability density evaluation function of the unobserved state process. Setting dprocess=NULL removes the latent-state density evaluator. For more information, see dprocess specification.

dmeasure

evaluator of the measurement model density, specified either as a C snippet, an R function, or the name of a pre-compiled native routine available in a dynamically loaded library. Setting dmeasure=NULL removes the measurement density evaluator. For more information, see dmeasure specification.

skeleton

optional; the deterministic skeleton of the unobserved state process. Depending on whether the model operates in continuous or discrete time, this is either a

vectorfield or a map. Accordingly, this is supplied using either the vectorfield or map fnctions. For more information, see skeleton specification. Setting skeleton=NULL removes the deterministic skeleton.

rinit simulator of the initial-state distribution. This can be furnished either as a C

snippet, an R function, or the name of a pre-compiled native routine available in a dynamically loaded library. Setting rinit=NULL sets the initial-state simulator

to its default. For more information, see rinit specification.

rprior optional; prior distribution sampler, specified either as a C snippet, an R function, or the name of a pre-compiled native routine available in a dynamically

loaded library. For more information, see prior specification. Setting rprior=NULL

removes the prior distribution sampler.

dprior optional; prior distribution density evaluator, specified either as a C snippet,

an R function, or the name of a pre-compiled native routine available in a dynamically loaded library. For more information, see prior specification. Setting dprior=NULL resets the prior distribution to its default, which is a flat improper

prior.

unit\_statenames

The names of the components of the latent state. E.g. if the user is constructing an joint SIR model over many spatial units, c('S','I','R') would be passed.

unit\_accumvars a subset of the unit\_statenames argument that are accumulator variables. See accumulator variables for more on the concept of **pomp** accumulator variables.

shared\_covarnames

If covar is supplied, covariates that are shared must still be specified for each unit, i.e., rows with equal values for the same time over all units must be supplied. However, if such covariates exists, supply the names using this argument.

globals optional character; arbitrary C code that will be hard-coded into the shared-

object library created when C snippets are provided. If no C snippets are used,

globals has no effect.

paramnames optional character vector; names of model parameters. It is typically only nec-

essary to supply paramnames when C snippets are in use.

params optional; named numeric vector of parameters. This will be coerced internally

to storage mode double.

cdir optional character variable. cdir specifies the name of the directory within

which C snippet code will be compiled. By default, this is in a temporary directory specific to the R session. One can also set this directory using the

pomp\_cdir global option.

cfile optional character variable. cfile gives the name of the file (in directory cdir)

into which C snippet codes will be written. By default, a random filename is used. If the chosen filename would result in over-writing an existing file, an

error is generated.

shlib.args optional character variables. Command-line arguments to the R CMD SHLIB call

that compiles the C snippets.

PACKAGE optional character; the name (without extension) of the external, dynamically

loaded library in which any native routines are to be found. This is only useful if one or more of the model components has been specified using a precompiled

dynamically loaded library; it is not used for any component specified using C

snippets. PACKAGE can name at most one library.

partrans optional parameter transformations, constructed using parameter\_trans.

Many algorithms for parameter estimation search an unconstrained space of parameters. When working with such an algorithm and a model for which the parameters are constrained, it can be useful to transform parameters. One should supply the partrans argument via a call to parameter\_trans. For more information, see parameter\_trans. Setting partrans=NULL removes the parameter

transformations, i.e., sets them to the identity transformation.

compile logical; if FALSE, compilation of the C snippets will be postponed until they are

needed.

verbose logical; if TRUE, diagnostic messages will be printed to the console.

#### **Details**

One implements a SPATPOMP model by specifying some or all of its basic components, including:

rinit, the simulator from the distribution of the latent state process at the zero-time;

rprocess, the transition simulator of the latent state process;

**dunit\_measure**, the evaluator of the conditional density at a unit's measurement given the unit's latent state;

**eunit\_measure,** the evaluator of the expectation of a unit's measurement given the unit's latent state;

**munit\_measure,** the evaluator of the moment-matched parameter set given a unit's latent state and some empirical measurement variance;

vunit\_measure, the evaluator of the variance of a unit's measurement given the unit's latent state;

runit\_measure, the simulator of a unit's measurement conditional on the unit's latent state;

dprocess, the evaluator of the density for transitions of the latent state process;

**rmeasure**, the simulator of the measurements conditional on the latent state;

**dmeasure**, the evaluator of the conditional density of the measurements given the latent state;

**rprior,** the simulator from a prior distribution on the parameters;

**dprior**, the evaluator of the prior density;

**skeleton**, which computes the deterministic skeleton of the unobserved state process;

partrans, which performs parameter transformations.

The basic structure and its rationale are described in Asfaw et al. (2020).

Each basic component is supplied via an argument of the same name to spatPomp(). The five unit-level model components must be provided via C snippets. The remaining components, whose behaviors are inherited from **pomp** may be furnished using C snippets, R functions, or pre-compiled native routine available in user-provided dynamically loaded libraries.

#### Value

An object of class 'spatPomp' representing observations and model components from the spatiotemporal POMP model.

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#### References

Asfaw, K. et al. (2020) Statistical inference for spatiotemporal partially observed Markov processes via the R package spatPomp. *Manuscript in preparation*.

spatPomp-class

An S4 class to represent a spatiotemporal POMP model and data.

### Description

An S4 class to represent a spatiotemporal POMP model and data.

#### **Slots**

unit\_names A vector containing the spatial units of a spatiotemporal POMP.

unit\_statenames A vector containing the state names such that appending the unit indices to the unit statenames will result in the each unit's corresponding states.

unit\_obsnames A vector of observation types for a spatial unit.

eunit\_measure A pomp\_fun representing the expected measurement for each spatial unit given its states.

dunit\_measure A pomp\_fun representing the unit measurement density for each spatial unit.

runit\_measure A pomp\_fun representing the unit observation simulator.

spatPomp\_Csnippet

C snippets

#### **Description**

spatPomp\_Csnippet() is used to provide snippets of C code that specify model components. It functions similarly to Csnippet() from the **pomp** package; in fact, the output of spatPomp\_Csnippet is an object of class Csnippet. It additionally provides some arguments that allow the user to stay focused on model development in the spatiotemporal context where model size grows.

#### Usage

```
## $4 method for signature 'character'
spatPomp_Csnippet(
  code,
  unit_statenames,
  unit_obsnames,
  unit_covarnames,
  unit_ivpnames,
  unit_jaramnames,
  unit_paramnames,
  unit_vfnames
)
```

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### **Arguments**

code

encodes a component of a spatiotemporal POMP model using C code

unit\_statenames

a subset of the unit\_statenames slot of the spatPomp object for which we are writing a model. This argument allows the user to get variables that can be indexed conveniently to update states and measurements in a loop. See examples for more details.

unit\_obsnames

a subset of the unit\_obsnames slot of the spatPomp object for which we are writing a model. This argument allows the user to get variables that can be indexed conveniently to update states and measurements in a loop. See examples for more details.

unit\_covarnames

if the model has covariate information for each unit, the names of the covariates for each unit can be supplied to this argument. This allows the user to get variables that can be indexed conveniently to use incorporate the covariate information in a loop. See examples for more details.

unit\_ivpnames

This argument is particularly useful when specifying the rinit model component. The paramnames argument to the spatPomp() constructor often has names for initial value parameters for the latent states (e.g. S1\_0, S2\_0 for the the quantity of susceptibles at unit 1 and unit 2 at the initial time in an SIR model). By supplying unit\_ivpnames, we can get variables that can be easily indexed to reference the initial value parameters (in the previous example, unit\_ivpnames=c('S') we can get a variable named S\_0 that we can index as S\_0[0] and S\_0[1] to refer to S1\_0 and S2\_0). See examples for more details.

unit\_paramnames

This argument is particularly useful when there are non-initial value parameters that are unit-specific.

unit\_vfnames

This argument is particularly useful when specifying the skeleton model component. For all components of the latent state, the user can assume a variable defining the time-derivative is pre-defined (e.g. DS1 and DS2 for the time-derivative of the quantity of the susceptibles at unit 1 and unit 2 in an SIR model). By supplying unit\_vfnames, we can get variables that can be easily indexed to reference these variables (in the previous example, setting unit\_vfnames=c('S') gets us a variable named DS that we can index as DS[0] and DS[1] to refer to DS1 and DS2). See examples for more details.

### Value

An object of class 'Csnippet' which represents a model specification in C code.

### Examples

```
# Set initial states for Brownian motion
bm_rinit <- spatPomp_Csnippet(
  unit_statenames = c("X"),
  unit_ivpnames = c("X"),
  code = "
   for (int u = 0; u < U; u++) {</pre>
```

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```
X[u]=X_0[u];
}

"
)
# Skeleton for Brownian motion
bm_skel <- spatPomp_Csnippet(
   unit_statenames = c("X"),
   unit_vfnames = c("X"),
   code = "
        for (int u = 0 ; u < U ; u++) {
            DX[u] = 0;
        }
        "
)</pre>
```

undefined

Undefined

### Description

Check for undefined methods.

### Usage

```
undefined(object, ...)
## S4 method for signature '`NULL`'
undefined(object, ...)
## S4 method for signature 'ANY'
undefined(object, ...)
## S4 method for signature 'missing'
undefined(object, ...)
## S4 method for signature 'pomp_fun'
undefined(object, ...)
## S4 method for signature 'partransPlugin'
undefined(object, ...)
## S4 method for signature 'rprocPlugin'
undefined(object, ...)
## S4 method for signature 'covartable'
undefined(object)
## S4 method for signature 'skelPlugin'
undefined(object, ...)
```

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### **Arguments**

```
object object to test.
... currently ignored.
```

#### Value

Returns TRUE if the **pomp** workhorse method is undefined, FALSE if it is defined, and NA if the question is inapplicable.

unit\_names

Unit names of a spatiotemporal model

#### **Description**

unit\_names outputs the contents of the unit\_names slot of a spatPomp object. The order in which the units appear in the output vector determines the order in which latent states and observations for the spatial units are stored.

### Usage

```
## S4 method for signature 'spatPomp'
unit_names(x)
```

### **Arguments**

x a spatPomp object

### Value

A character vector with the unit names used to create the 'spatPomp' object.

vec\_dmeasure

Vector of measurement densities

### **Description**

Evaluate the unit measurement model density function for each unit. This method is used primarily as part of likelihood evaluation and parameter inference algorithms.

### Usage

```
## S4 method for signature 'spatPomp'
vec_dmeasure(object, y, x, units, times, params, log = FALSE, ...)
```

vec\_rmeasure

### **Arguments**

object	a spatPomp object
у	numeric; measurements whose densities given the latent states are evaluated
x	numeric; state at which conditional measurement densities are evaluated
units	numeric; units at which measurement densities are evaluated
times	numeric; time at which measurement densities are evaluated
params	numeric; parameter set at which measurement densities is evaluated
log	logical; should the outputted measurement densities be on log scale?
	additional parameters will be ignored

### Value

An array of dimension length(unit\_names(object)) by dim(x)[2] by dim(x)[3] representing each unit's measurement density assessed for each replicate in x for each observation time.

vec_rmeasure	Vector of simulated measurements

### Description

Simulate from the unit measurement model density function for each unit

### Usage

```
## S4 method for signature 'spatPomp'
vec_rmeasure(object, x, times, params, ...)
```

### **Arguments**

object	a spatPomp object
x	numeric; state at which measurements are simulated
times	numeric; time at which measurements are simulated
params	numeric; parameter set at which measurements are simulated
	additional parameters will be ignored

#### Value

An array of dimension length(unit\_names(object)) by dim(x)[2] by dim(x)[3] representing each unit's simulated measurement assessed for each replicate in x for each observation time.

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vunit_measure	vunit_measure	
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### **Description**

vunit\_measure evaluates the variance of a unit's observation given the entire state

### Usage

```
## S4 method for signature 'spatPomp'
vunit_measure(object, x, unit, time, params, Np = 1)
```

### **Arguments**

object	An object of class spatPomp
X	A state vector for all units
unit	The unit for which to evaluate the variance
time	The time for which to evaluate the variance
params	parameters at which to evaluate the unit variance
Np	numeric; defaults to 1 and the user need not change this

### Value

A matrix with the unit measurement variance implied by the state, x, and the parameter set params for unit unit.

### **Examples**

```
b <- bm(U=3)
s <- states(b)[,1,drop=FALSE]
rownames(s) -> rn
dim(s) <- c(3,1,1)
dimnames(s) <- list(variable=rn, rep=NULL)
p <- coef(b); names(p) -> rnp
dim(p) <- c(length(p),1); dimnames(p) <- list(param=rnp)
o <- obs(b)[,1,drop=FALSE]
vunit_measure(b, x=s, unit=2, time=1, params=p)</pre>
```

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