

Lesson 7:

Case study: forecasting Ebola

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1 Introduction

Objectives

1. To explore the use of POMP models in the context of an outbreak of an emerging infectious disease.
2. To demonstrate the use of diagnostic probes for model criticism.
3. To illustrate some forecasting methods based on POMP models.
4. To provide an example that can be modified to apply similar approaches to other outbreaks of emerging infectious diseases.

This lesson follows King *et al.* (2015), all codes for which are available on datadryad.org.

1.1 2014 West Africa EVD outbreak

An emerging infectious disease outbreak

Let's situate ourselves at the beginning of October 2014. The WHO situation report contained data on the number of cases in each of Guinea, Sierra Leone, and Liberia. Key questions included:

1. How fast will the outbreak unfold?
2. How large will it ultimately prove?
3. What interventions will be most effective?

As is to be expected in the case of a fast-moving outbreak of a novel pathogen in an underdeveloped country, the answers to these questions were sought in a context far from ideal:

- Case ascertainment is difficult and the case definition itself may be evolving.
- Surveillance effort is changing on the same timescale as the outbreak itself.
- The public health and behavioral response to the outbreak is rapidly changing.

Best practices

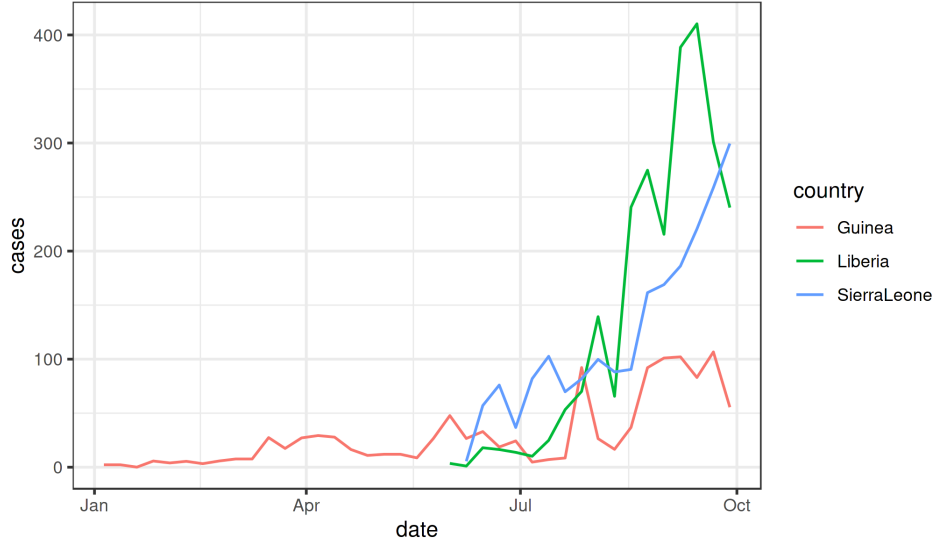
- The King *et al.* (2015) paper focused critical attention on the economical and therefore common practice of fitting deterministic transmission models to cumulative incidence data.
- Specifically, King *et al.* (2015) showed how this practice easily leads to overconfident prediction that, worryingly, can mask their own presence.
- The paper recommended the use of POMP models, for several reasons:
 - Such models can accommodate a wide range of hypothetical forms.
 - They can be readily fit to incidence data, especially during the exponential growth phase of an outbreak.
 - Stochastic models afford a more explicit treatment of uncertainty.
 - POMP models come with a number of diagnostic approaches built-in, which can be used to assess model misspecification.

2 Data and model

2.1 Data

Situation-report data

The data and **pomp** codes used to represent the transmission models are presented in [a supplement](#). The data we focus on here are from the WHO Situation Report of 1 October 2014. Supplementing these data are population estimates for the three countries.



2.2 Model

SEIR model with gamma-distributed latent period

- Many of the early modeling efforts used variants on the simple SEIR model.
- Here, we'll focus on a variant that attempts a more careful description of the duration of the latent period.
- Specifically, this model assumes that the amount of time an infection remains latent is

$$LP \sim \text{Gamma}\left(m, \frac{1}{m\alpha}\right),$$

where m is an integer.

- This means that the latent period has expectation $1/\alpha$ and variance $1/(m\alpha)$. In this document, we'll fix $m = 3$.
- We implement Gamma distributions using the so-called *linear chain trick*.



The observations are modeled as a negative binomial process conditional on the number of infections. That is, if C_t are the reported cases at week t and H_t is the true incidence, then we postulate that $C_t|H_t$ is negative binomial with

$$\mathbb{E}[C_t|H_t] = \rho H_t$$

and

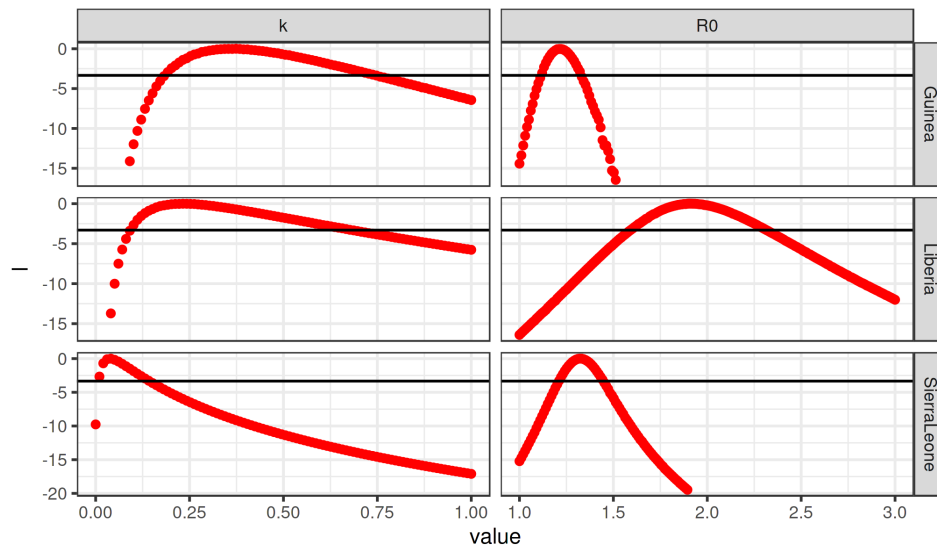
$$\text{Var}[C_t|H_t] = \rho H_t (1 + k \rho H_t).$$

The negative binomial process allows for overdispersion in the counts. This overdispersion is controlled by parameter k .

2.3 Parameter estimates

Parameter estimates

- King *et al.* (2015) estimated parameters for this model for each country.
- A Latin hypercube design was used to initiate a large number of iterated filtering runs.
- Profile likelihoods were computed for each country against the parameters k (the measurement model overdispersion) and R_0 (the basic reproductive ratio).
- Full details are given [on the datadryad.org](https://datadryad.org) site.
- Codes for this document are [available here](#). The results of these calculations are loaded and displayed in the following.
- The following are plots of the profile likelihoods. The horizontal line represents the critical value of the likelihood ratio test for $p = 0.01$.



3 Model Criticism

Diagnostics *or* Model Criticism

- Parameter estimation is the process of finding the parameters that are “best”, in some sense, for a given model, from among the set of those that make sense for that model.
- Model selection, likewise, aims at identifying the “best” model, in some sense, from among a set of candidates.
- One can do both of these things more or less well, but no matter how carefully they are done, the best of a bad set of models is still bad.
- Let’s investigate the model here, at its maximum-likelihood parameters, to see if we can identify problems.
- The guiding principle in this is that, if the model is “good”, then the data are a plausible realization of that model.

- Therefore, we can compare the data directly against model simulations.
- Moreover, we can quantify the agreement between simulations and data in any way we like.
- Any statistic, or set of statistics, that can be applied to the data can also be applied to simulations.
- Shortcomings of the model should manifest themselves as discrepancies between the model-predicted distribution of such statistics and their value on the data.
- **pomp** provides tools to facilitate this process.
- Specifically, the **probe** function applies a set of user-specified summary statistics or *probes*, to the model and the data, and quantifies the degree of disagreement in several ways.
- Let's see how this is done using the model for the Guinean outbreak.

3.1 Simulation for diagnosis

Model simulations

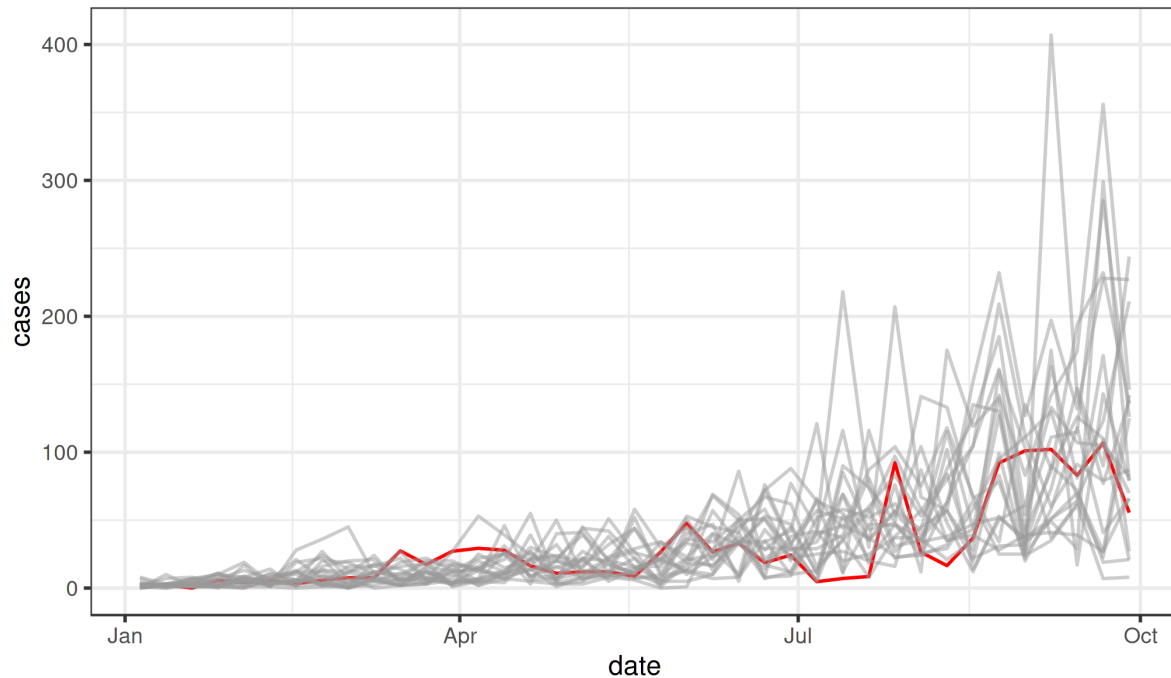
From our profile-likelihood calculations, we extract the MLE:

```
profs %>%
  filter(country=="Guinea") %>%
  filter(loglik==max(loglik)) %>%
  select(-loglik,-loglik.se,-country,-profile) -> coef(gin)
```

Here, **profs** contains the profile-likelihood calculations displayed previously and **gin** is a **pomp** object containing the model and data for Guinea.

The following generates and plots some simulations on the same axes as the data.

```
gin %>%
  simulate(nsim=20,format="data.frame",include.data=TRUE) %>%
  mutate(
    date=min(dat$date)+7*(week-1),
    is.data=ifelse(.id=="data","yes","no")
  ) %>%
  ggplot(aes(x=date,y=cases,group=.id,color=is.data,alpha=is.data))+
  geom_line()+
  guides(color="none",alpha="none")+
  scale_color_manual(values=c(no=gray(0.6),yes="red"))+
  scale_alpha_manual(values=c(no=0.5,yes=1))
```



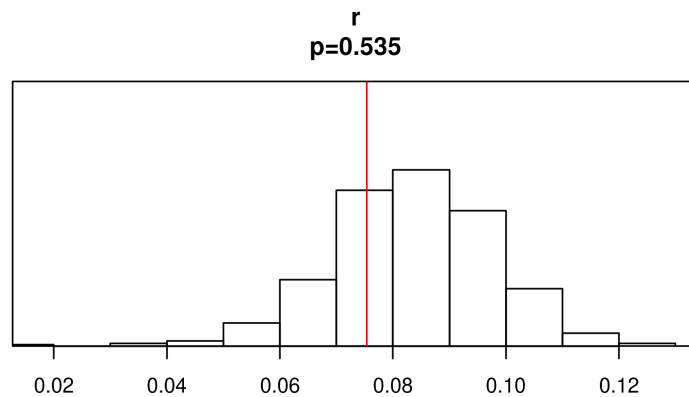
3.2 Diagnostic probes

Diagnostic probes

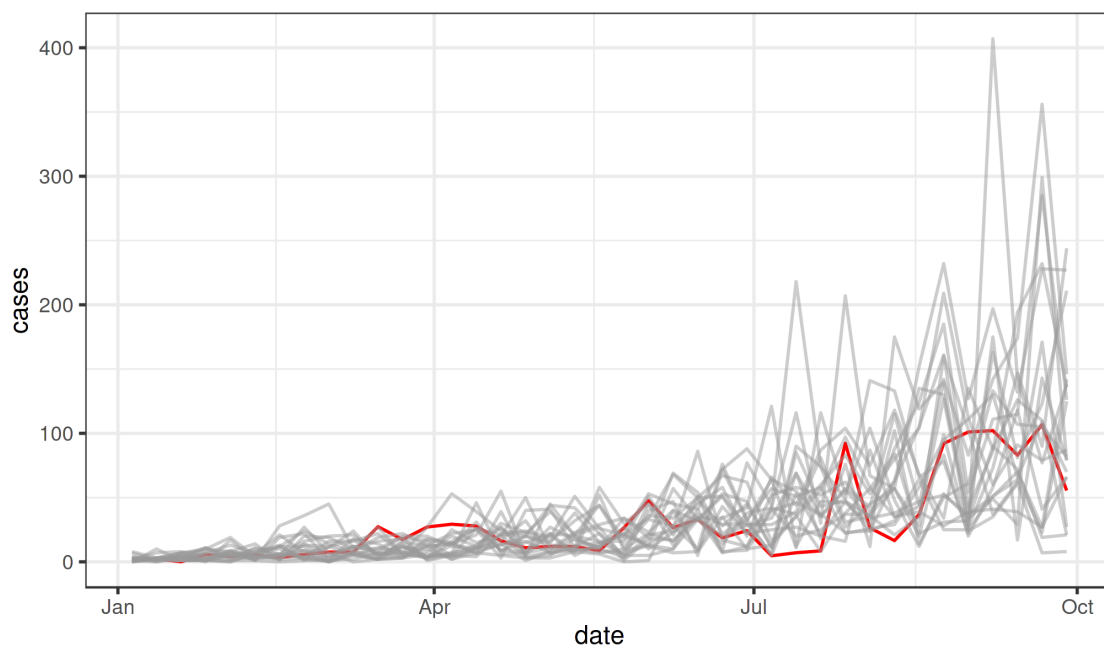
- Does the data look like it could have come from the model?
 - The simulations appear to be growing a bit more quickly than the data.
- Let's try to quantify this.
 - First, we'll write a function that estimates the exponential growth rate by linear regression.
 - Then, we'll apply it to the data and to 500 simulations.
- In the following, `gin` is a pomp object containing the model and the data from the Guinea outbreak.

```
growth.rate <- function (y) {
  cases <- y["cases",]
  fit <- lm(log1p(cases)~seq_along(cases))
  unname(coef(fit)[2])
}

gin %>%
  probe(probes=list(r=growth.rate),nsim=500) %>%
  plot()
```



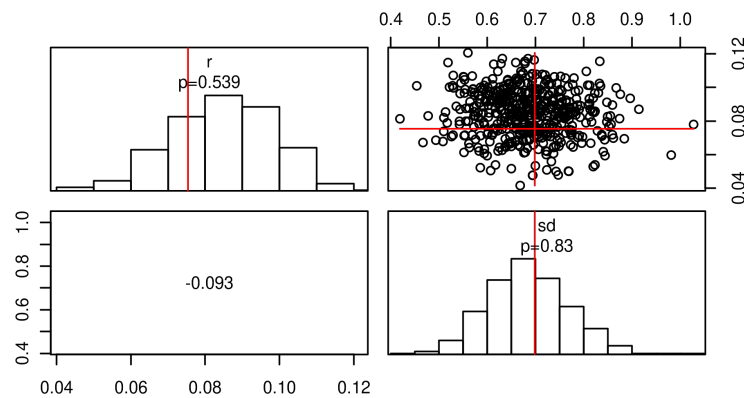
- Do these results bear out our suspicion that the model and data differ in terms of growth rate?



- The simulations also appear to be more highly variable around the trend than do the data.

```
growth.rate.plus <- function (y) {
  cases <- y["cases",]
  fit <- lm(log1p(cases)~seq_along(cases))
  c(r=unname(coef(fit)[2]),sd=sd(residuals(fit)))
}

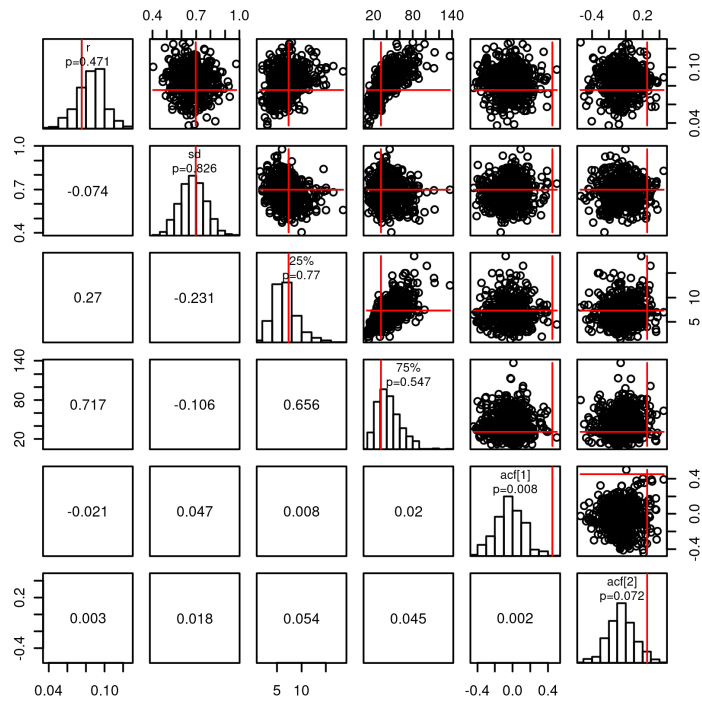
gin %>%
  probe(probes=list(growth.rate.plus),nsim=500) %>%
  plot()
```



- Do we see evidence for lack of fit of model to data?
- Let's also look more carefully at the distribution of values about the trend using the 1st and 3rd quartiles.
- Also, it looks like the data are less jagged than the simulations. We can quantify this using the autocorrelation function (ACF).

```
loglp.detrrend <- function (y) {
  cases <- y["cases",]
  fit <- lm(loglp(cases)~seq_along(cases))
  y["cases",] <- as.numeric(residuals(fit))
  y
}

gin %>%
  probe(nsim=500,
    probes=list(
      growth.rate.plus,
      probe.quantile(var="cases",prob=c(0.25,0.75)),
      probe.acf(var="cases",lags=c(1,2),type="correlation",
        transform=loglp.detrrend))) %>%
  plot()
```

3.3 Exercise

Exercise 7.1. The Sierra Leone outbreak

Apply probes to investigate the extent to which the SEIR model above is an adequate description of the data from the Sierra Leone outbreak. Have a look at the probes provided with **pomp**: `?basic.probes`. Try also to come up with some informative probes of your own. Discuss the implications of your findings.

4 Forecasting using POMP models

4.1 Sources of uncertainty

Forecasting and forecasting uncertainty

- To this point in the course, we've focused on using POMP models to answer scientific questions, i.e., to compare alternative hypothetical explanations for the data in hand.
- Of course, we can also use them to make forecasts.
- A set of key issues surrounds quantifying the forecast uncertainty.
- This arises from four sources:
 1. measurement error
 2. process noise
 3. parametric uncertainty
 4. structural uncertainty

- Here, we'll explore how we can account for the first three of these in making forecasts for the Sierra Leone outbreak.

4.2 Forecasting Ebola: an empirical Bayes approach

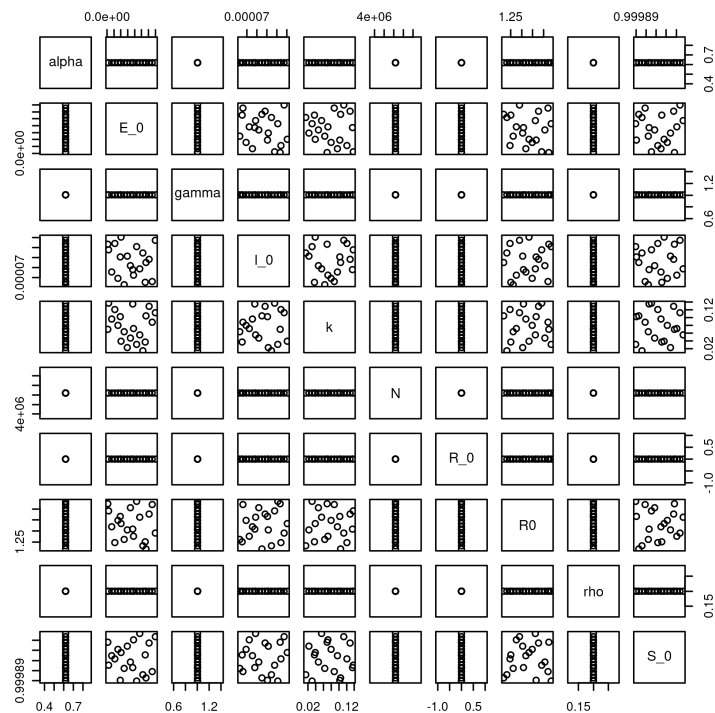
Parameter uncertainty

We take an *empirical Bayes* approach.

First, we set up a collection of parameter vectors in a neighborhood of the maximum likelihood estimate containing the region of high likelihood.

```
profs %>%
  filter(country=="SierraLeone") %>%
  select(-country,-profile,-loglik.se) %>%
  filter(loglik>max(loglik)-0.5*qchisq(df=1,p=0.99)) %>%
  gather(parameter,value) %>%
  group_by(parameter) %>%
  summarize(min=min(value),max=max(value)) %>%
  ungroup() %>%
  filter(parameter!="loglik") %>%
  column_to_rownames("parameter") %>%
  as.matrix() -> ranges
```

```
sobol_design(
  lower=ranges[, "min"],
  upper=ranges[, "max"],
  nseq=20
) -> params
plot(params)
```



Process noise and measurement error

Next, we carry out a particle filter at each parameter vector, which gives us estimates of both the likelihood and the filter distribution at that parameter value.

We extract the state variables at the end of the data for use as initial conditions for the forecasts.

The final states are now stored in `x`.

We simulate forward from the initial condition, up to the desired forecast horizon, to give a forecast corresponding to the selected parameter vector. To do this, we first set up a matrix of parameters:

Then, we generate simulations over the “calibration period” (i.e., the time interval over which we have data). We record the likelihood of the data given the parameter vector:

Now, we create a new pomp object for the forecasting.

We set the initial conditions to the ones determined above and perform forecast simulations.

We combine the calibration and projection simulations into a single data frame.

We repeat this procedure for each parameter vector, binding the results into a single data frame. See [this lesson's R script](#) for details.

We give these prediction distributions weights proportional to the estimated likelihoods of the parameter vectors.

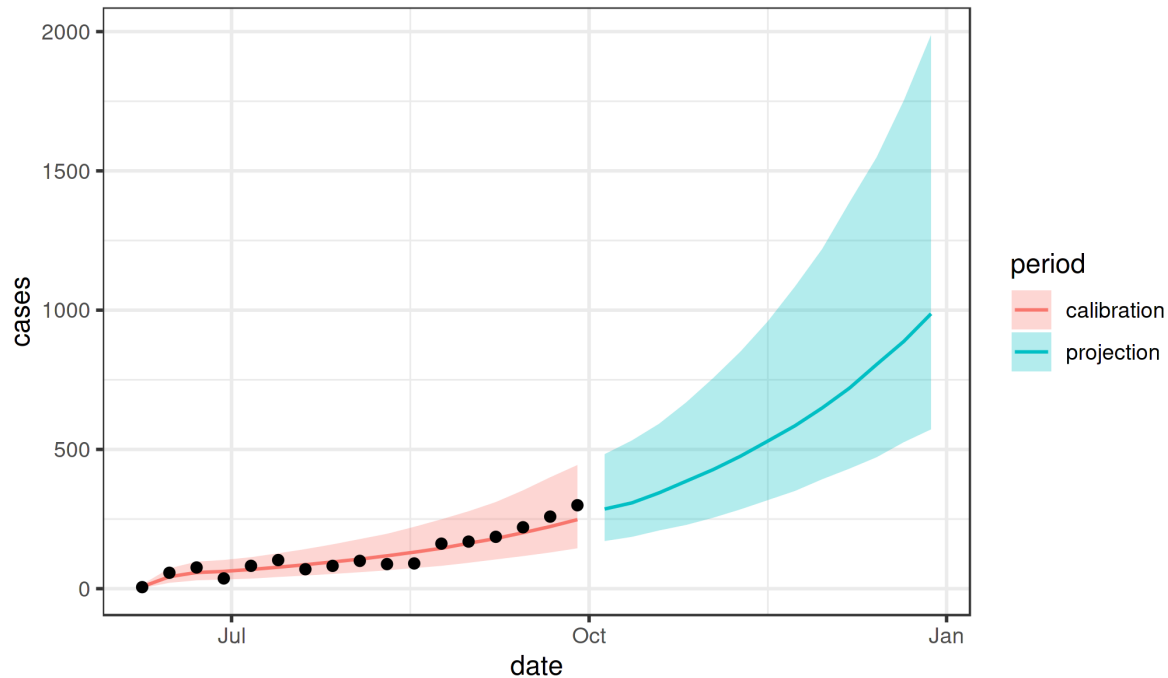
```
sims %>%  
  mutate(weight=exp(loglik-mean(loglik))) %>%  
  arrange(week,.id) -> sims
```

We verify that our effective sample size is large.

```
sims %>%  
  filter(week==max(week)) %>%  
  summarize(ess=sum(weight)^2/sum(weight^2))  
  
      ess  
10617.78
```

Finally, we compute quantiles of the forecast incidence.

```
sims %>%  
  group_by(week,period) %>%  
  summarize(  
    p=c(0.025,0.5,0.975),  
    q=wquant(cases,weights=weight,probs=p),  
    label=c("lower","median","upper")  
  ) %>%  
  select(-p) %>%  
  spread(label,q) %>%  
  ungroup() %>%  
  mutate(date=min(dat$date)+7*(week-1)) -> simq
```



4.3 Exercise


Exercise 7.2. Decomposing the uncertainty

As we have discussed, the uncertainty shown in the forecasts above has three sources: parameter uncertainty, process noise, and measurement error. Show how you can break the total uncertainty into these three components. Produce plots similar to that above showing each of the components.

References

King AA, Domenech de Cellès M, Magpantay FMG, Rohani P (2015). “Avoidable errors in the modelling of outbreaks of emerging pathogens, with special reference to Ebola.” *Proceedings of the Royal Society of London. Series B*, **282**(1806), 20150347. doi: [10.1098/rspb.2015.0347](https://doi.org/10.1098/rspb.2015.0347).

License, acknowledgments, and links

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- The materials build on [previous versions of this course and related courses](#).
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- Produced with R version 4.2.0 and **pomp** version 4.2.1.2.
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