



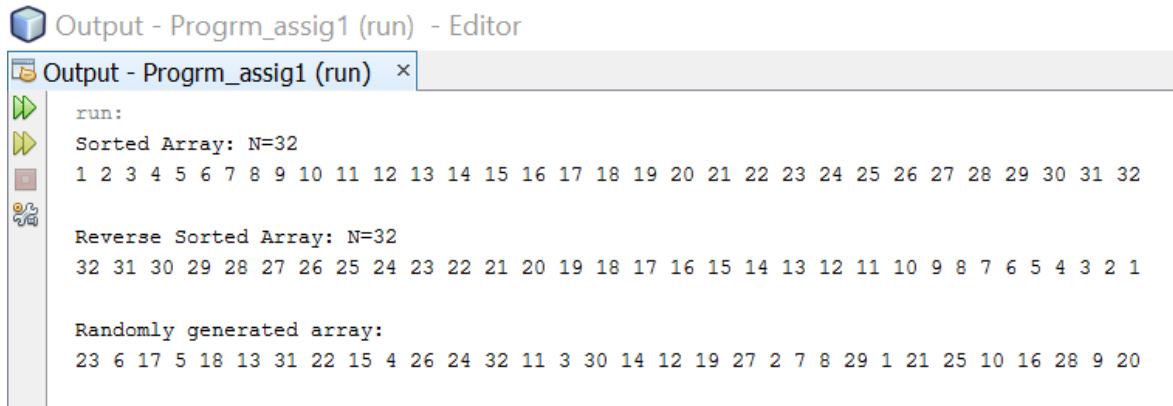
1) N= 32

**NOTE:**

- Run "Progrm\_assign1.java"
- No external Input to be provided.

**o/p**

- 1) Sorted, Reverse Sorted, and Randomly Generated Array

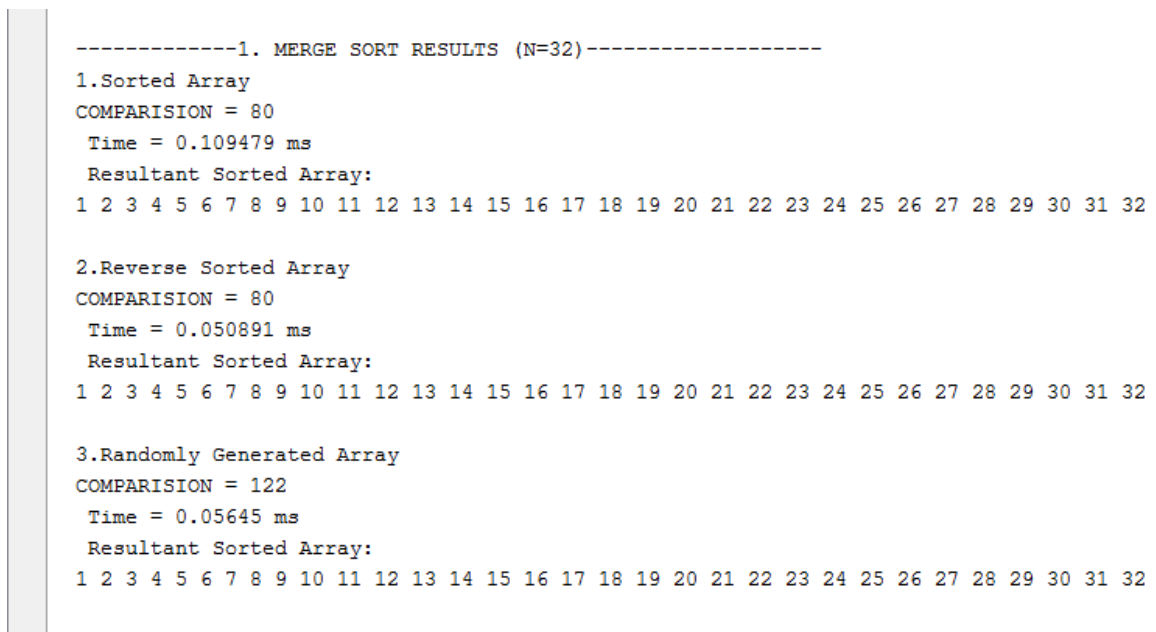


```
Output - Progrm_assign1 (run) - Editor
Output - Progrm_assign1 (run) x
run:
Sorted Array: N=32
1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23 24 25 26 27 28 29 30 31 32

Reverse Sorted Array: N=32
32 31 30 29 28 27 26 25 24 23 22 21 20 19 18 17 16 15 14 13 12 11 10 9 8 7 6 5 4 3 2 1

Randomly generated array:
23 6 17 5 18 13 31 22 15 4 26 24 32 11 3 30 14 12 19 27 2 7 8 29 1 21 25 10 16 28 9 20
```

- 2) Merge Sort Results – In below result for merge 1. Shows the Best Case, 2. Shows the Worst Case, 3. Shows the Average case



```
-----1. MERGE SORT RESULTS (N=32)-----
1.Sorted Array
COMPARISION = 80
Time = 0.109479 ms
Resultant Sorted Array:
1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23 24 25 26 27 28 29 30 31 32

2.Reverse Sorted Array
COMPARISION = 80
Time = 0.050891 ms
Resultant Sorted Array:
1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23 24 25 26 27 28 29 30 31 32

3.Randomly Generated Array
COMPARISION = 122
Time = 0.05645 ms
Resultant Sorted Array:
1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23 24 25 26 27 28 29 30 31 32
```

- 3) Heap Sort Result- In below result for heap 1. Shows the Best Case, 2. Shows the Worst Case, 3. Shows the Average case

```
-----1. HEAP SORT RESULTS (N=32)-----
1.Sorted Array
  Comparision = 163
  Time = 0.045331 ms
  Resultant Sorted Array:
1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23 24 25 26 27 28 29 30 31 32

2.Reverse Sorted Array
  Comparision = 129
  Time = 0.031218 ms
  Resultant Sorted Array:
1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23 24 25 26 27 28 29 30 31 32

3.Randomly Array
  Comparision = 152
  Time = 0.036351 ms
  Resultant Sorted Array:
1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23 24 25 26 27 28 29 30 31 32
```

- 4) Quick Sort Result- In below result for quick 1. Shows the Best Case, 2. Shows the Worst Case, 3. Shows the Average case

```
-----3. QUICK SORT RESULTS (N=32)-----
1.Sorted Array
  Comparision=496
  Time = 0.043621 ms
  Resultant Sorted Array:
1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23 24 25 26 27 28 29 30 31 32

2.Reverse Sorted Array
  Comparision=496
  Time = 0.0402 ms
  Resultant Sorted Array:
1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23 24 25 26 27 28 29 30 31 32

3.Randomly Array
  Comparision=135
  Time = 0.02908 ms
  Resultant Sorted Array:
1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23 24 25 26 27 28 29 30 31 32

BUILD SUCCESSFUL (total time: 0 seconds)
```

## TABULATED RESULT

### a. Comparisons

<b>SORTING ALGO</b>	<b>Sorted</b>	<b>Rev. Sorted</b>	<b>Random</b>
<b>MERGE</b>	80	80	122
<b>HEAP</b>	163	129	152
<b>QUICK</b>	496	496	135

### b. Time in ms

<b>SORTING ALGO</b>	<b>Sorted</b>	<b>Rev. Sorted</b>	<b>Random</b>
<b>MERGE</b>	0.109479	0.050891	0.05645
<b>HEAP</b>	0.045331	0.031218	0.036351
<b>QUICK</b>	0.043621	0.0402	0.02908

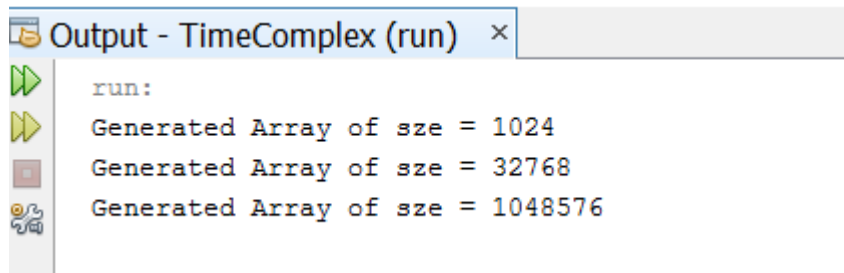
## 2) ANALYSIS OF LARGE SIZE ARRAY

### NOTE:

- Run "TimeComplex.java"
- TimeComplex.java takes longer time to run.
- No external Input to be provided.

O/p snaps:

- a) TimeComplex.java o/p three generated array. Array of size 1048576 takes large time to compute.



```
Output - TimeComplex (run) ×
run:
Generated Array of size = 1024
Generated Array of size = 32768
Generated Array of size = 1048576
```

b)

```
----- 1.MERGE SORT RESULTS-----
A) N = 1024
  Comparisions = 8913
  Time = 5.860558 ms

B) N = 32768
  Comparisions = 450243
  Time = 1170.18839 ms

C) N = 1048576
  Comparisions = 19645686
  Time = 1904734.375695 ms
```

c)

```
----- 2.HEAP SORT RESULTS-----  
A) N = 1024  
  Comparision = 9812  
  Time = 1.513464 ms  
  
B) N = 32768  
  Comparision = 478595  
  Time = 7.134536 ms  
  
C) N = 1048576  
  Comparision = 20559946  
  Time = 235.383245 ms
```

d)

```
----- 3.Quick SORT RESULTS-----  
A) N = 1024  
  Comparision =13283  
  Time = 0.846753 ms  
  
B) N = 32768  
  Comparision =581721  
  Time = 7.397543 ms  
  
C) N = 1048576  
  Comparision =25901960  
  Time = 154.965223 ms  
  
BUILD SUCCESSFUL (total time: 81 minutes 34 seconds)
```

## TABULATED RESULT

### 1) COMPARISONS.

<b>SORTING ALGO</b>	<b>N= 1024</b>	<b>N=32768</b>	<b>N=1048576</b>
<b>MERGE</b>	8913	450243	19645686
<b>HEAP</b>	9812	478595	20559946
<b>QUICK</b>	13283	581721	25901960

### 2) TIME (in ms)

<b>SORTING ALGO</b>	<b>N= 1024</b>	<b>N=32768</b>	<b>N=1048576</b>
<b>MERGE</b>	5.860558	1170.18839	1904734.375695
<b>HEAP</b>	1.513464	7.134536	235.383245
<b>QUICK</b>	0.846753	7.397543	154.965223

## Analysis

1)

### MERGE SORT.

Analysis:

① AVERAGE CASE .  $N = 1024$

① Merge Sort.

$$T(n) \leq O(n \log n) \leq A (n \log n).$$

② No. of key comparison = 8913

$$n = 1024$$

$$\therefore n \log n = 1024 \log_2 1024 = 1024 \times 10 = \underline{\underline{10240}}.$$

$$\therefore T(n) = 8913 \leq A * (10240).$$
$$= 0.8704.$$

The constant = 0.8704  
factor

③ ~~Worst case.~~

~~Take  $n = 1024$  as  $n \log n$~~   
~~More key comparisons.~~

②  $N = 32768$ .

$$T(n) \leq O(n \log n)$$

No. of key comparison = 450243.

$$n = \underline{32768}.$$

$$n \log n = 32768 \log_2 32768 = 32768 \times 15 = \underline{\underline{491520}}$$



2)

Finding Constant.

$$T(n) = 450243 \leq B (491520)$$

$$\therefore \boxed{B = 0.91602}$$

$$(3) N = 1048576.$$

$$\text{No. of comparison} = 19645686.$$

$$T(n) = \text{---}$$

$$n \log n = 1048576 \times 20 = 20,971,520$$

$$T(n) = 19645686 \leq C \times (20,971,520).$$

$$\therefore \boxed{C = 0.93677}$$

3)

x HEAD sort

(a)  $N = 1024$ .

$$T(n) \leq O(n \log n) = C * (n \log n)$$

$$n \log n = 1024 \log_2 1024 = 10240$$

$$\text{No. of comparison} = 9812$$

$$\therefore T(n) = 9812 = A * (10240)$$

$$A = 0.958$$

(b)  $N = 32768$ .

$$\text{No. of comparison} = 478595$$

$$n \log n = 32768 \log_2 32768 = 491520$$

$$\therefore T(n) = 478595 = B * 491520$$

$$B = 0.9737$$

(c)  $N = 1048576$ .

$$\text{No. of comparison} = 20559946$$

$$n \log n = 19645686, 20971520$$

$$T(n) = 19645686 = A * 20971520$$

$$T(n) = 20559946 = B * 19645686$$

$$C = 0.9803$$

4)

### Quick Sort

$$T(n) \leq O(n \log n) \leq B(n \log n).$$

(1)  $N = 1024$

no. of comparison = 13283.

$n \log n = 10240.$

$\therefore T(n) = 13283 = A * 10240.$

$A = 1.297$

(2)  $N = 32768$

No. of comparison = 581721

$n \log n = 32768 \cdot \log_2 32768 = 478595$

$(T(n)) = 581721 = B * 478595$

$B = 1.21$



5)

$$\textcircled{4} N = 1048576.$$

$$\text{No. of comparisons} = 25901960$$

$$n \log n = 20971520$$

$$\therefore T(n) = 25901960 = C \times 20971520$$

$$\boxed{C = 1.23}.$$