Statistical Learning - Homework 5 (Conceptual)

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Chapter 6 - Exercise 2

- a) The lass, relative to least squares, is less flexible and hence will give improved prediction accuracy when its increase in bias is less than its decrease in variance.
- b) The ridge regression, relative to least squares, is less flexible and hence will give improved prediction accuracy when its increase in bias is less than its decrease in variance.
- c) The non-linear methods, relative to least squares, is more flexible and hence will give improved prediction accuracy when its increase in variance is less than its decrease in bias.

Chapter 6 - Exercise 3

- a) As we increase s from 0, the training RSS will steadily decrease, since increasing s leads to restricting the coefficients to a lesser extent, and hence making the model more flexible.
- b) As we increase s from 0, the test RSS will decrease initially, and then eventually start increasing in a U shape since the model becomes more flexible and then overestimates/overfits due to extra parameters being involved.
- c) As we increase s from 0, the variance will steadily increase because a more flexible model results in higher variance.
- d) As we increase s from 0, the squared bias will steadily decrease since the model variance will increase and as variance increases, bias decreases due to the bias-variance tradeoff.
- e) As we increase s from 0, the irreducible error will remain constant because the definition of irreducible error means it will remain independent of the chosen model; it's just some small offset showing us that the model isn't the true model.

Chapter 6 - Exercise 4

- a) As we increase λ from 0, the training RSS will steadily increase since the model becomes more flexible as λ increases, naturally leading to a higher RSS.
- b) As we increase λ from 0, the test RSS will decrease initially, and then eventually start increasing in a U shape because the model becomes more flexible, leading to more overestimation/overfitting due to extra parameters being involved.
- c) As we increase λ from 0, the variance will steadily decrease because the model is becoming less flexible since the coefficients are being restricted more and more, leading to lower variance.
- d) As we increase λ from 0, the squared bias RSS will steadily increase because we will be restricting the coefficients to smaller and smaller values, thus the model will become more flexible, leading to higher bias, due to the bias-variance tradeoff.
- e) As we increase λ from 0, the irreducible error will remains constant since the definition of irreducible error means it will be independent of the chosen model.