



THE UNIVERSITY
of ADELAIDE



CRICOS PROVIDER 00123M

School of Computer Science

COMP SCI 1103/2103 Algorithm Design & Data Structure

Graph Traversals

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seek LIGHT

Graph Traversal

- We want to have algorithms that visit every node of a given graph in linear time.
 - Breadth-first-search (BFS)
 - Depth-first-search (DFS)

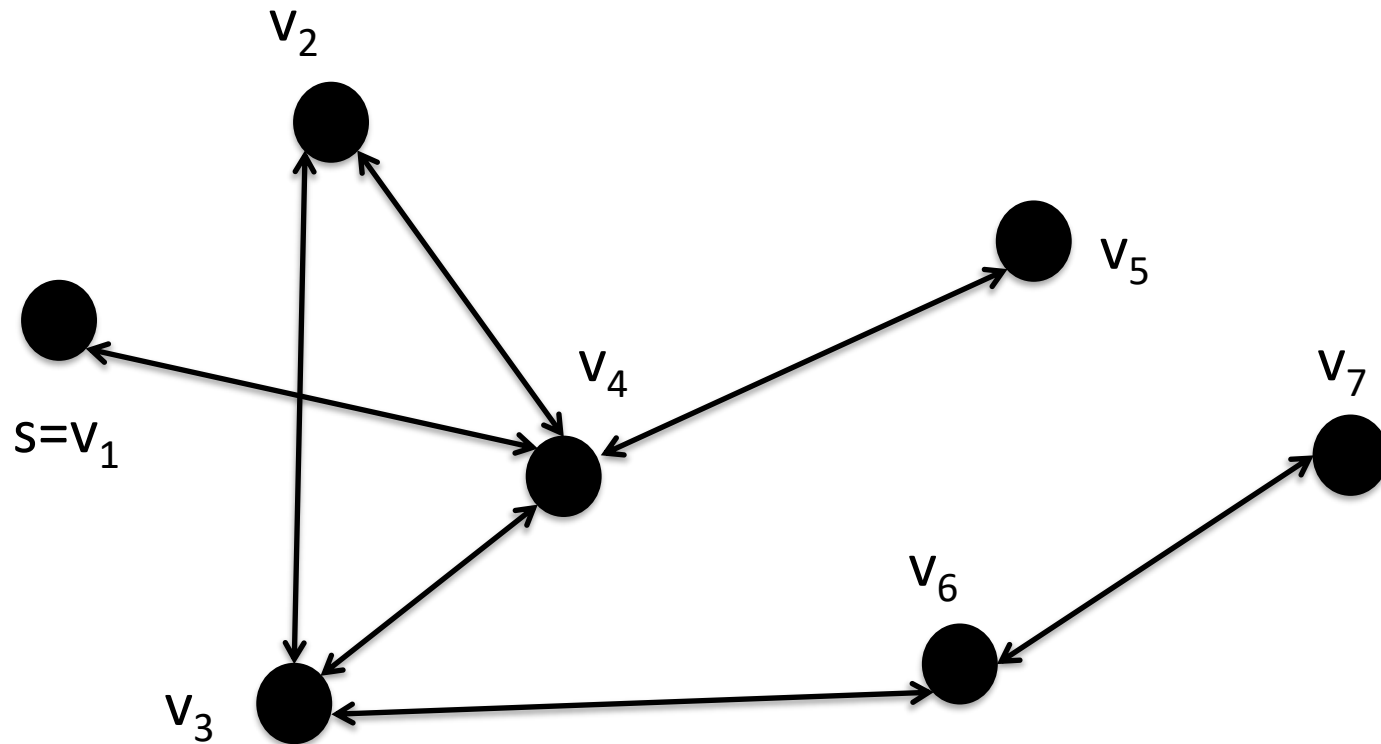
Breadth-First-Search (BFS)

- Idea:
 - Start at a node s
 - Visit a node level by level
 - In iteration i , visit all nodes of distance i to s

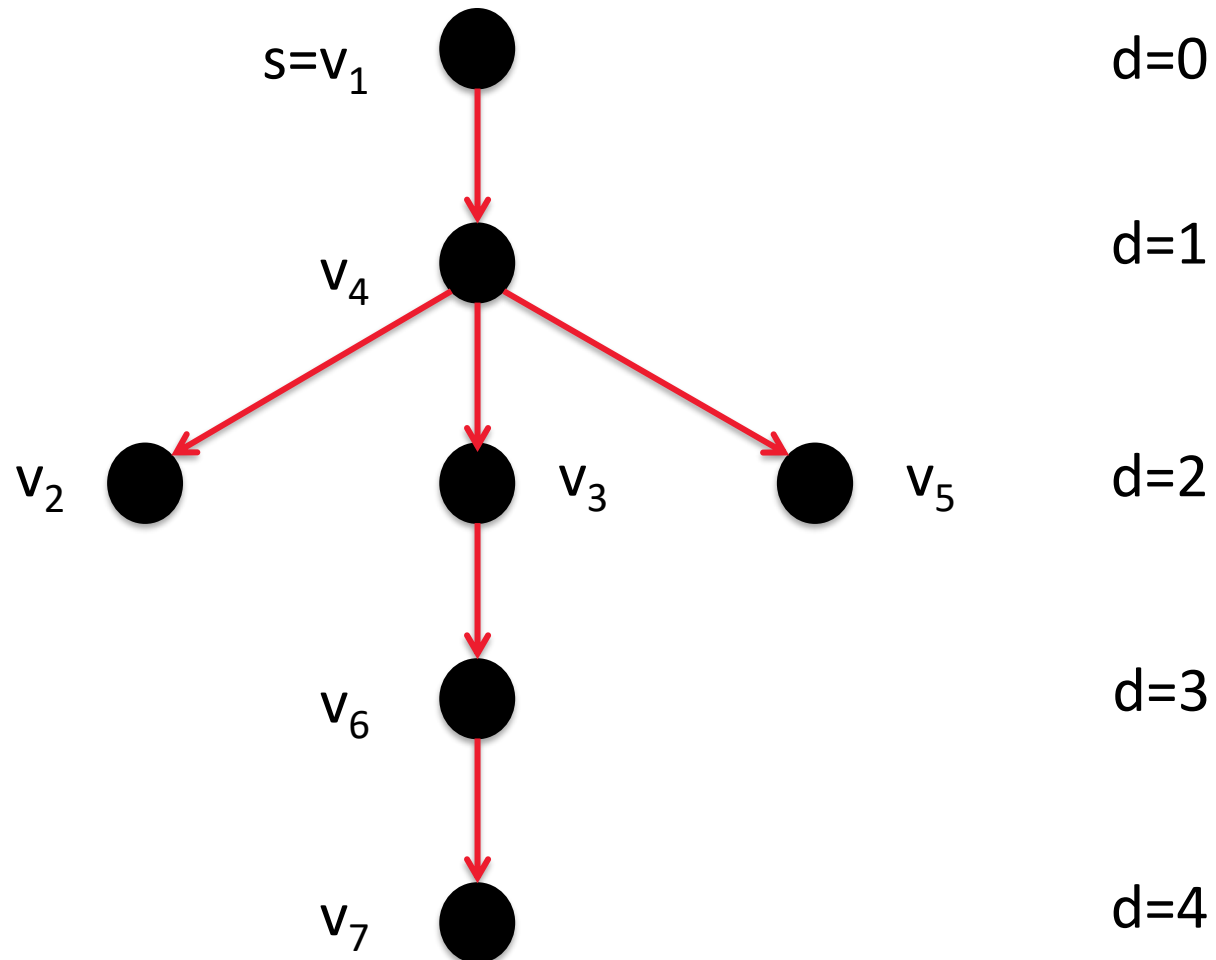
Breadth-First-Search (BFS)

- Idea:
 - Start at a node s
 - Visit a node level by level
 - In iteration i , visit all nodes of distance i to s
- Implementation:
 - Assume graph with n node and m edges
 - Use queue
 - Introduce each node into the queue only once, time $O(n)$
 - Consider a node in the queue with its edges once, time $O(n+m)$
 - Total runtime: $O(n+m)$

Breadth-First-Search (BFS)



Breadth-First-Search Tree



Depth-First-Search (DFS)

- Idea:
 - When visiting a node, mark it as visited and recursively call DFS for one of its non-visited neighbors
 - If there is no non-visited neighbor end recursive call.

Depth-First-Search (DFS)

- Idea:
 - When visiting a node, mark it as visited and recursively call DFS for one of its non-visited neighbors
 - If there is no non-visited neighbor end recursive call.
- Implementation:
 - Assume graph with n node and m edges
 - Use stack
 - Push each non-visited neighbors into stack only once, time $O(n)$
 - Consider a node with its edges once, time $O(n+m)$
 - Total runtime: $O(n+m)$

Depth-First-Search (DFS)

Three types of nodes



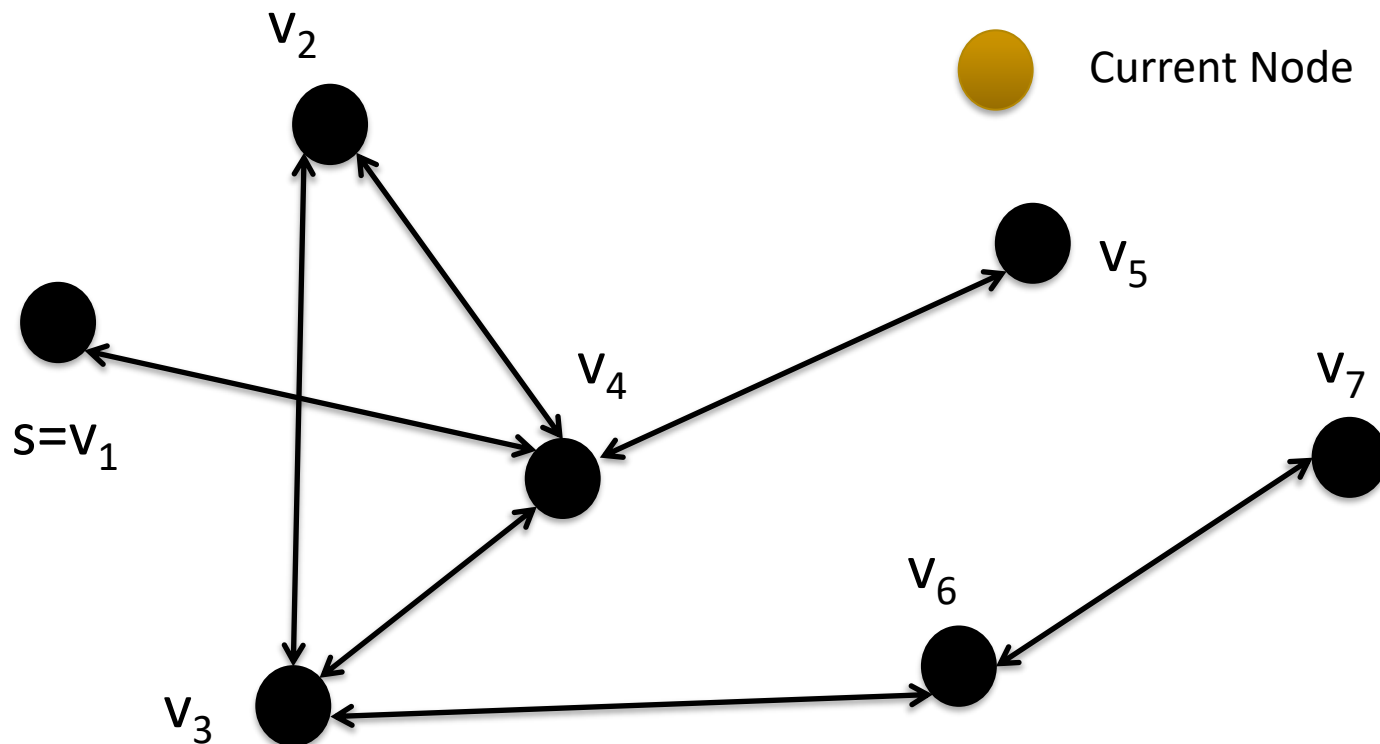
Finished Node



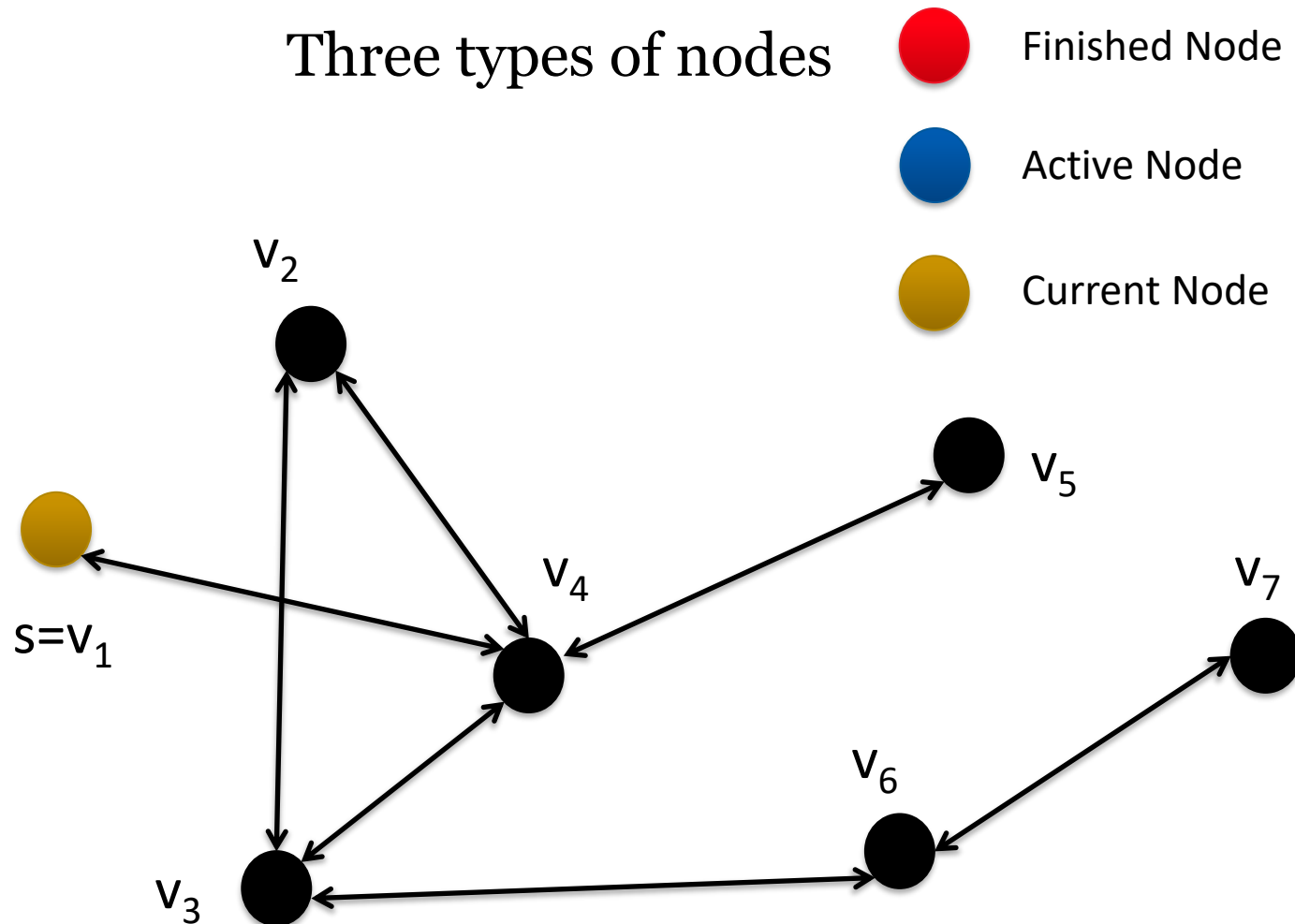
Active Node



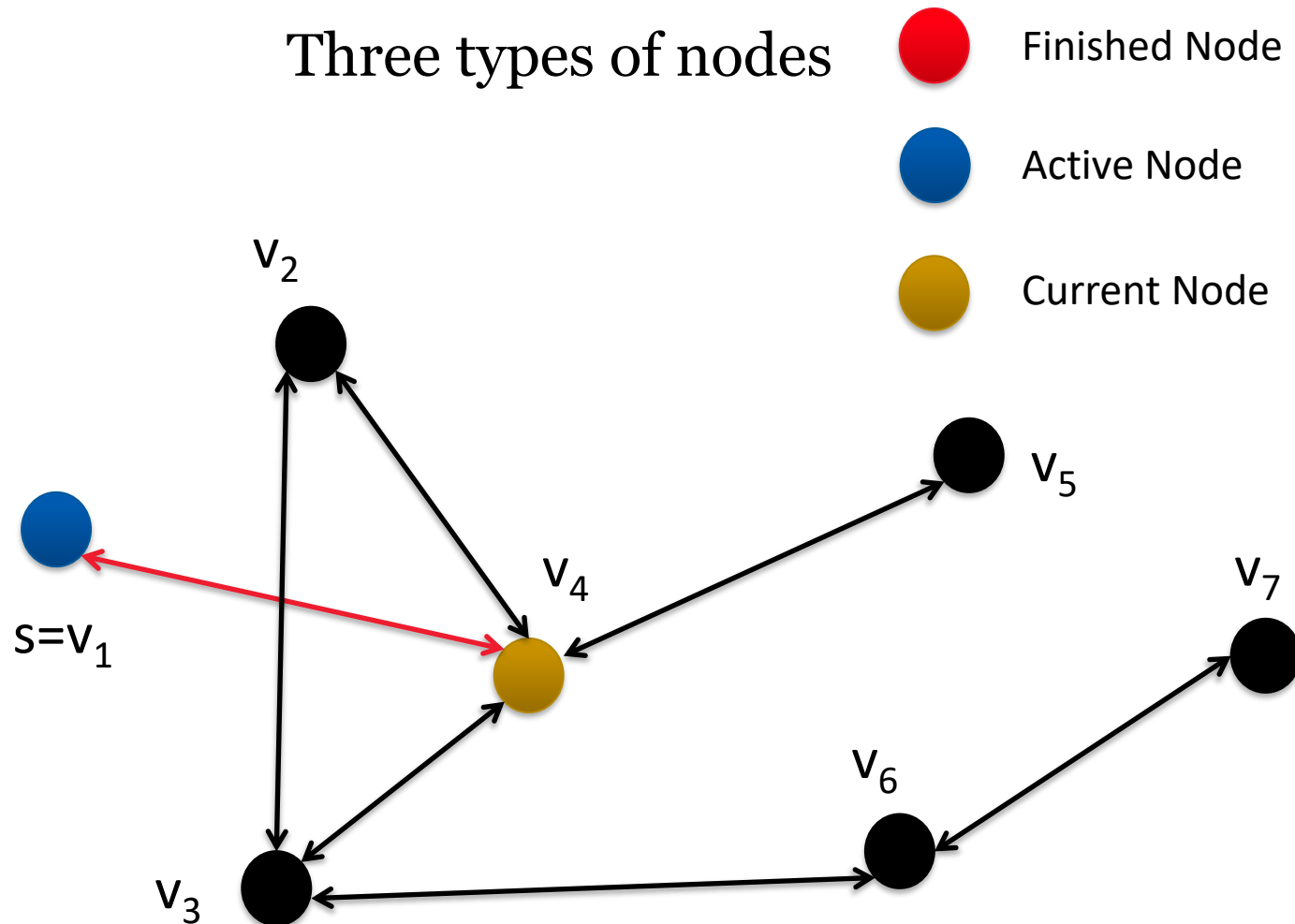
Current Node



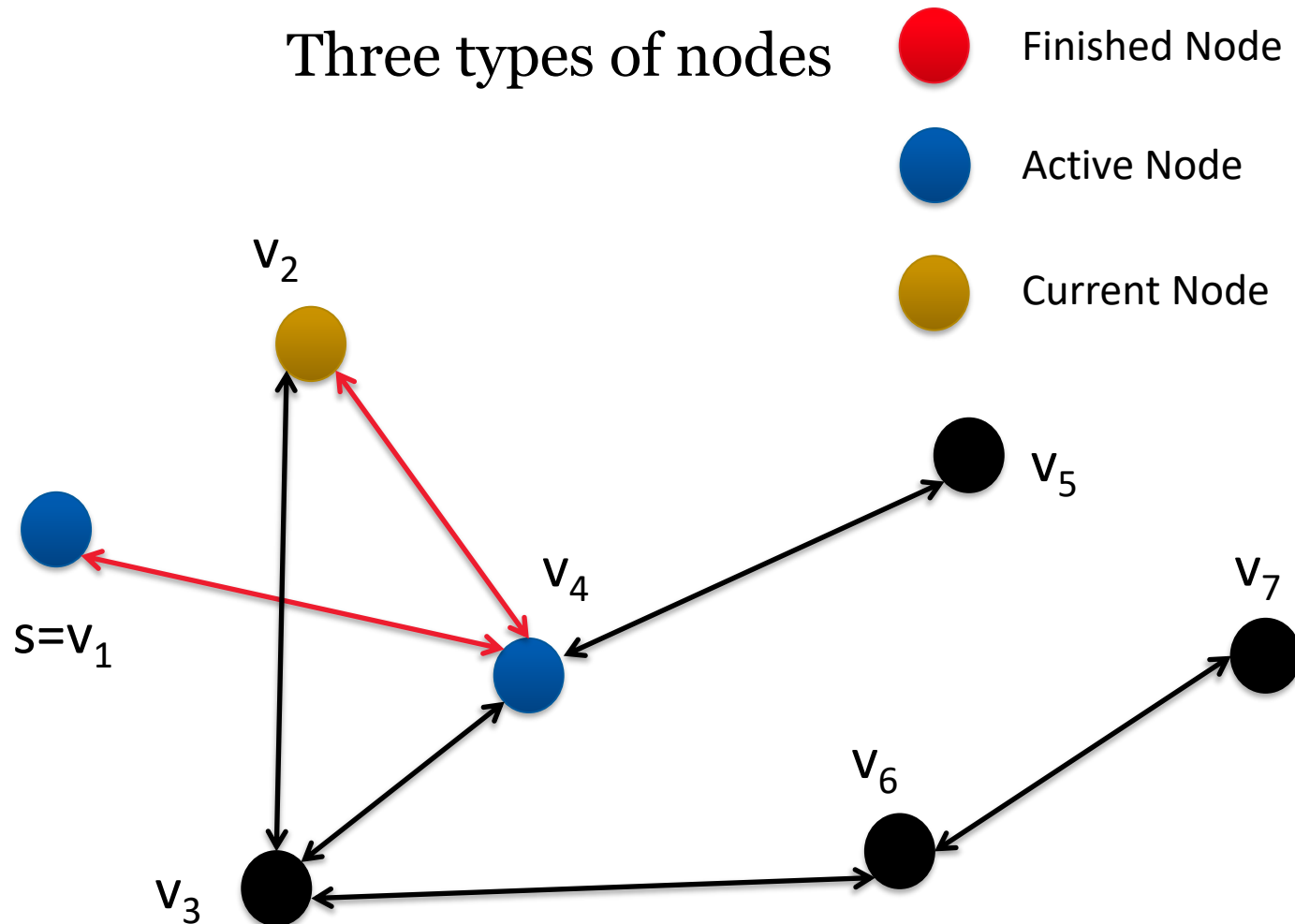
Depth-First-Search (DFS)



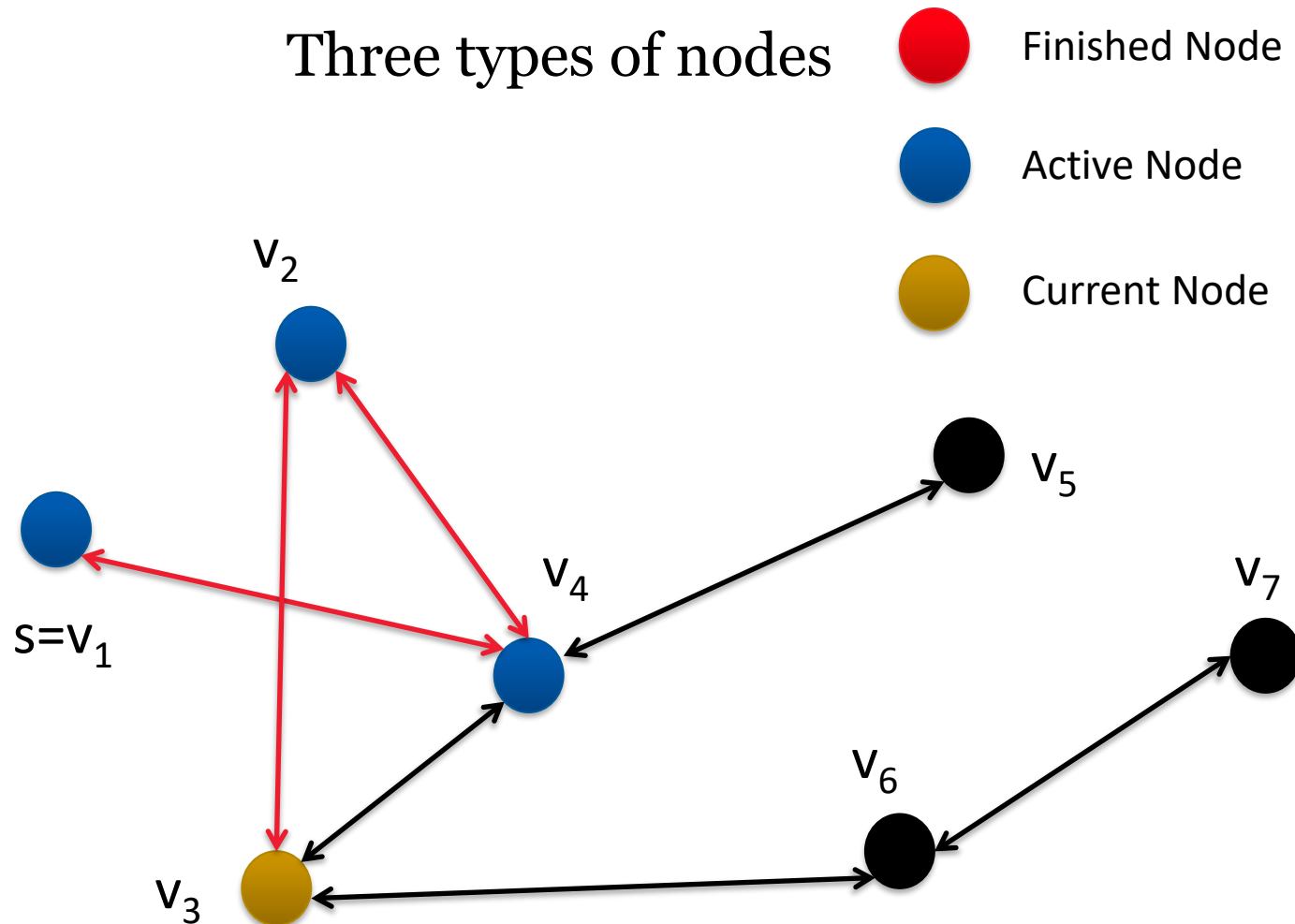
Depth-First-Search (DFS)



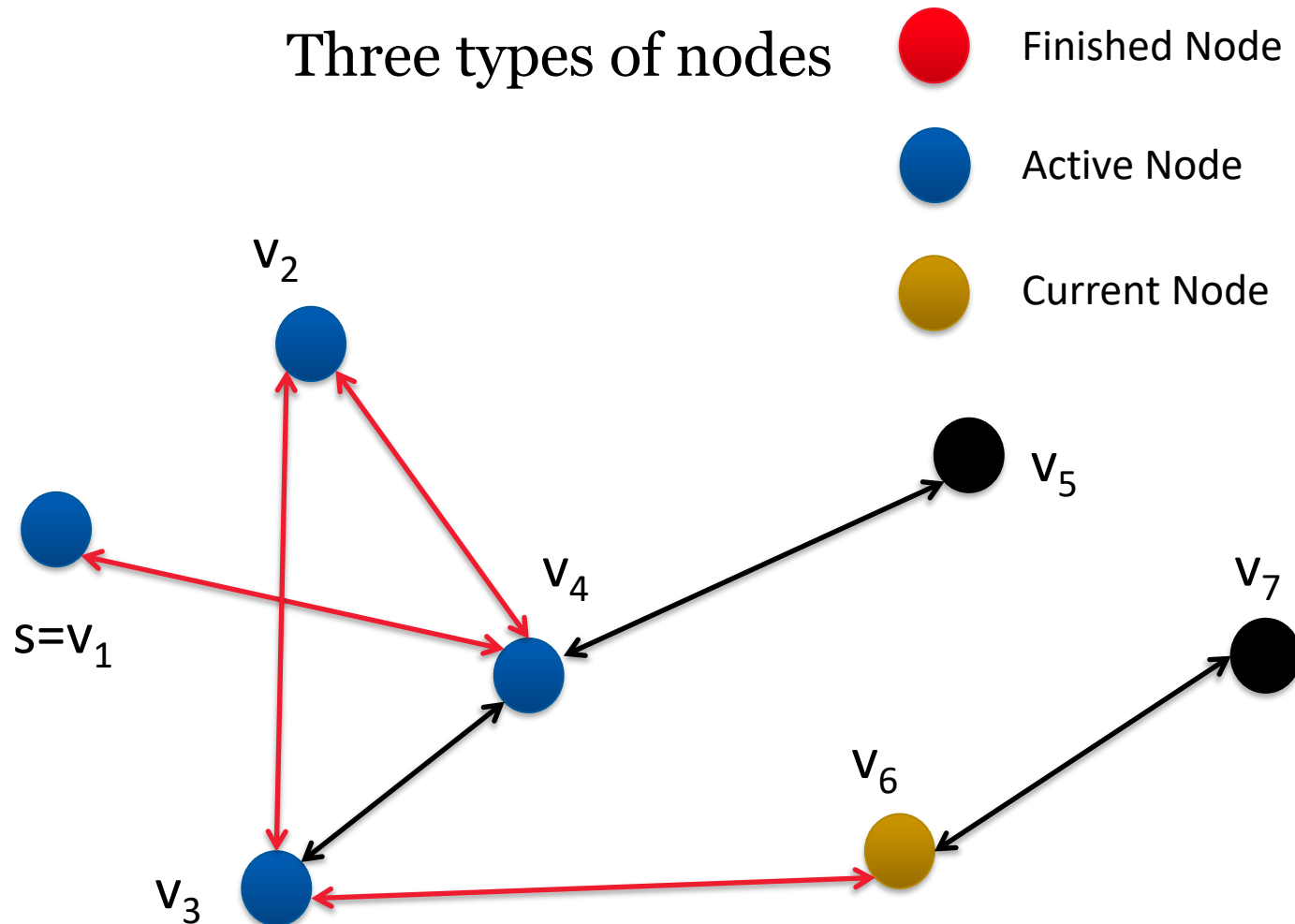
Depth-First-Search (DFS)



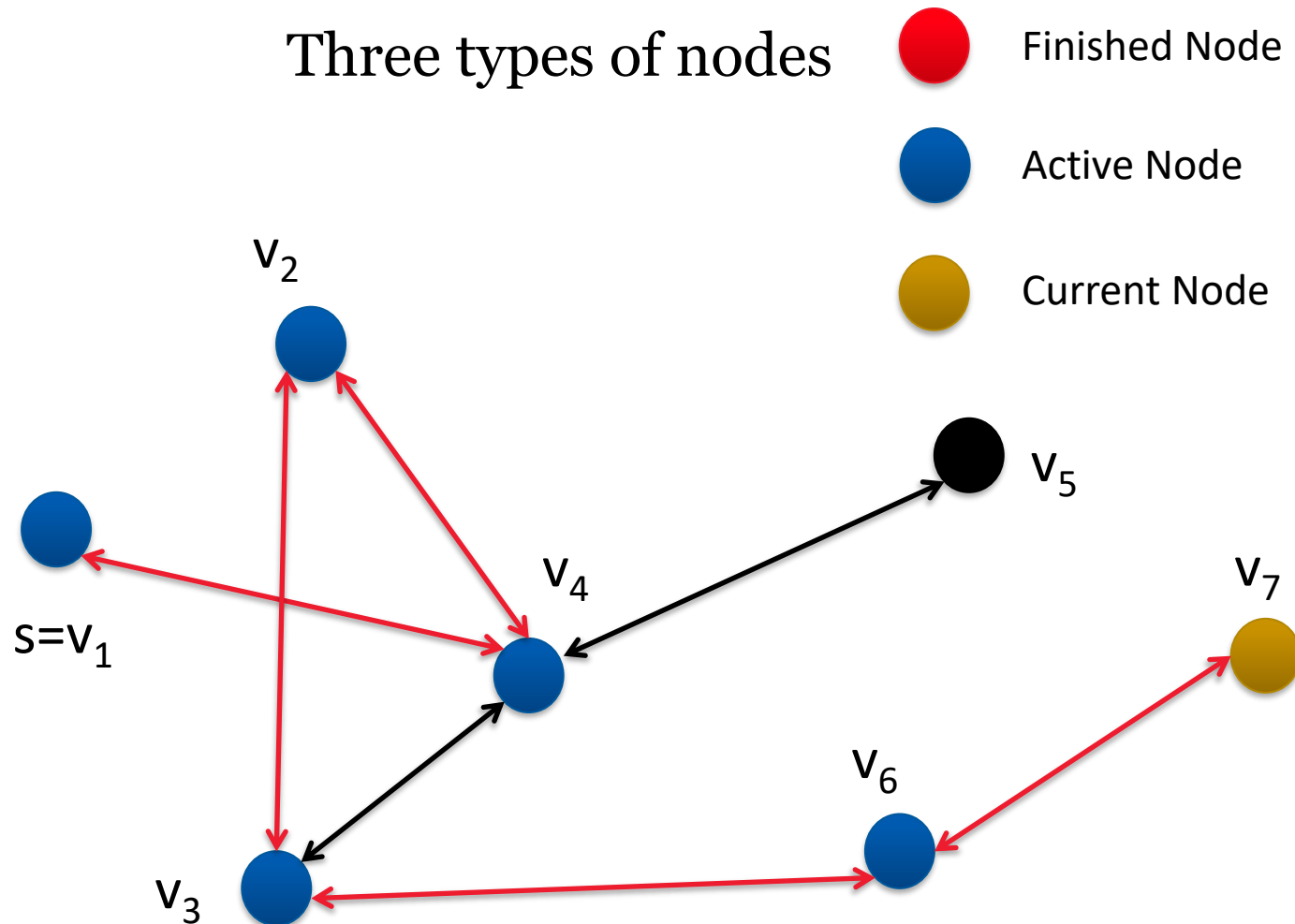
Depth-First-Search (DFS)



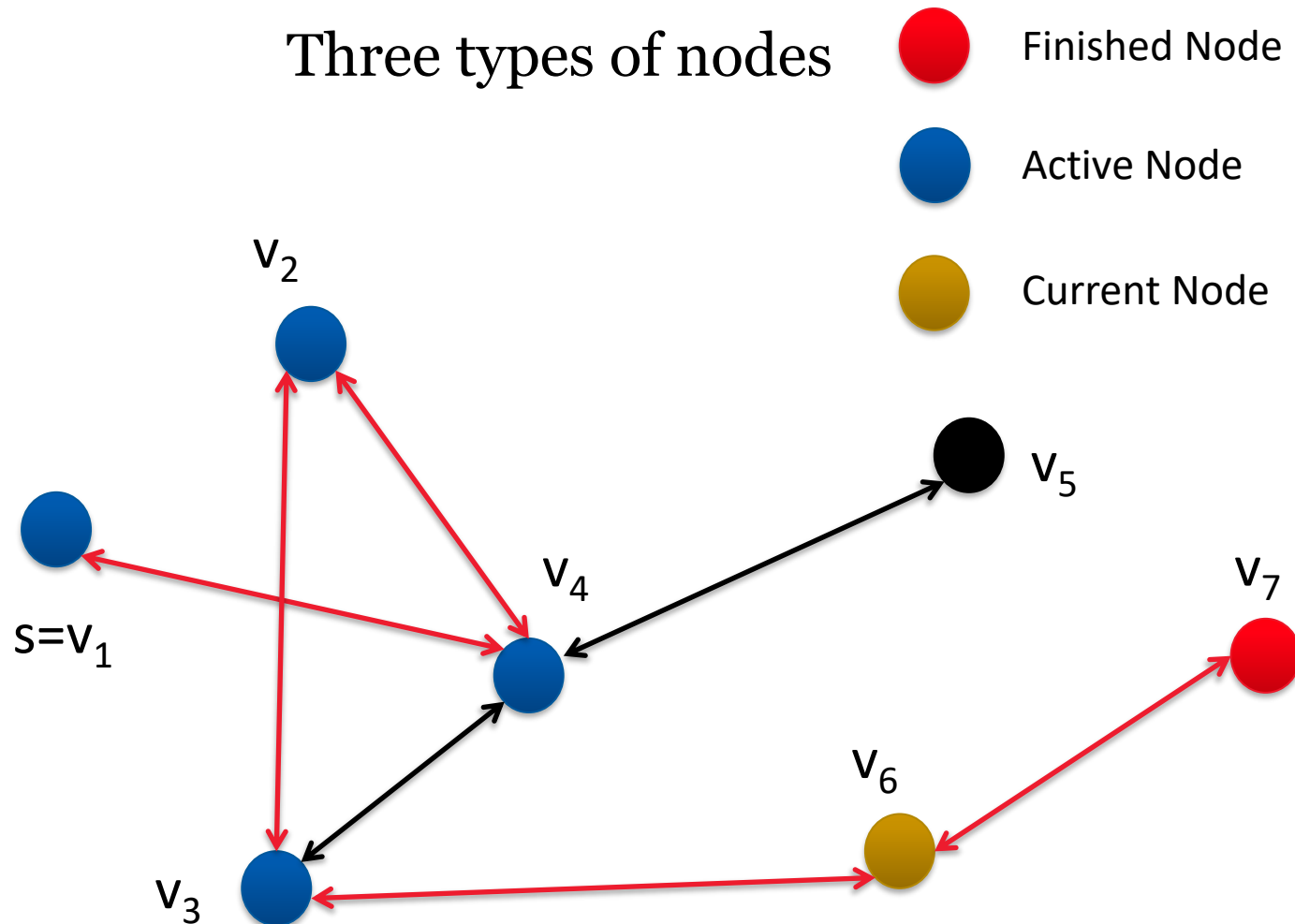
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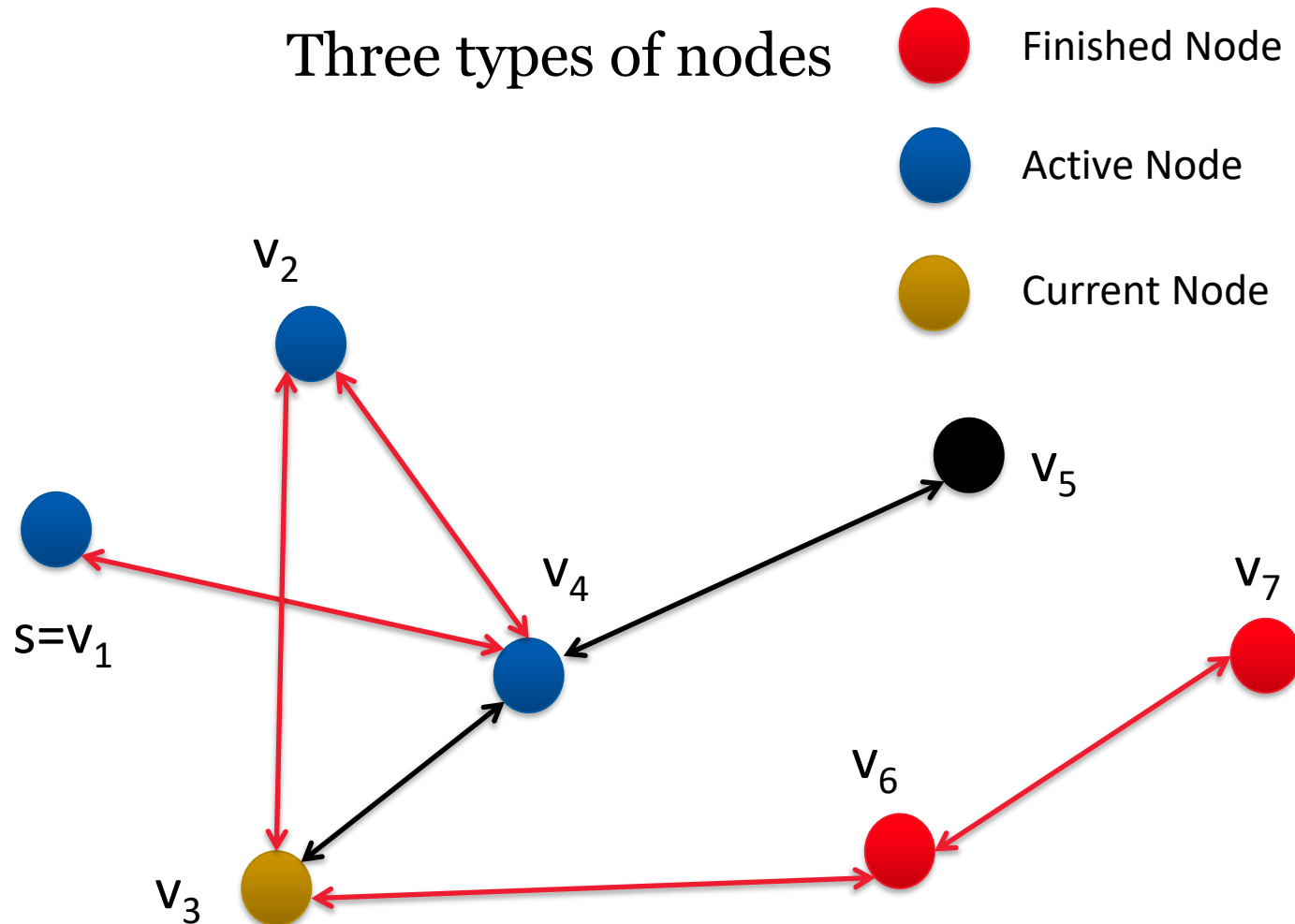
Depth-First-Search (DFS)



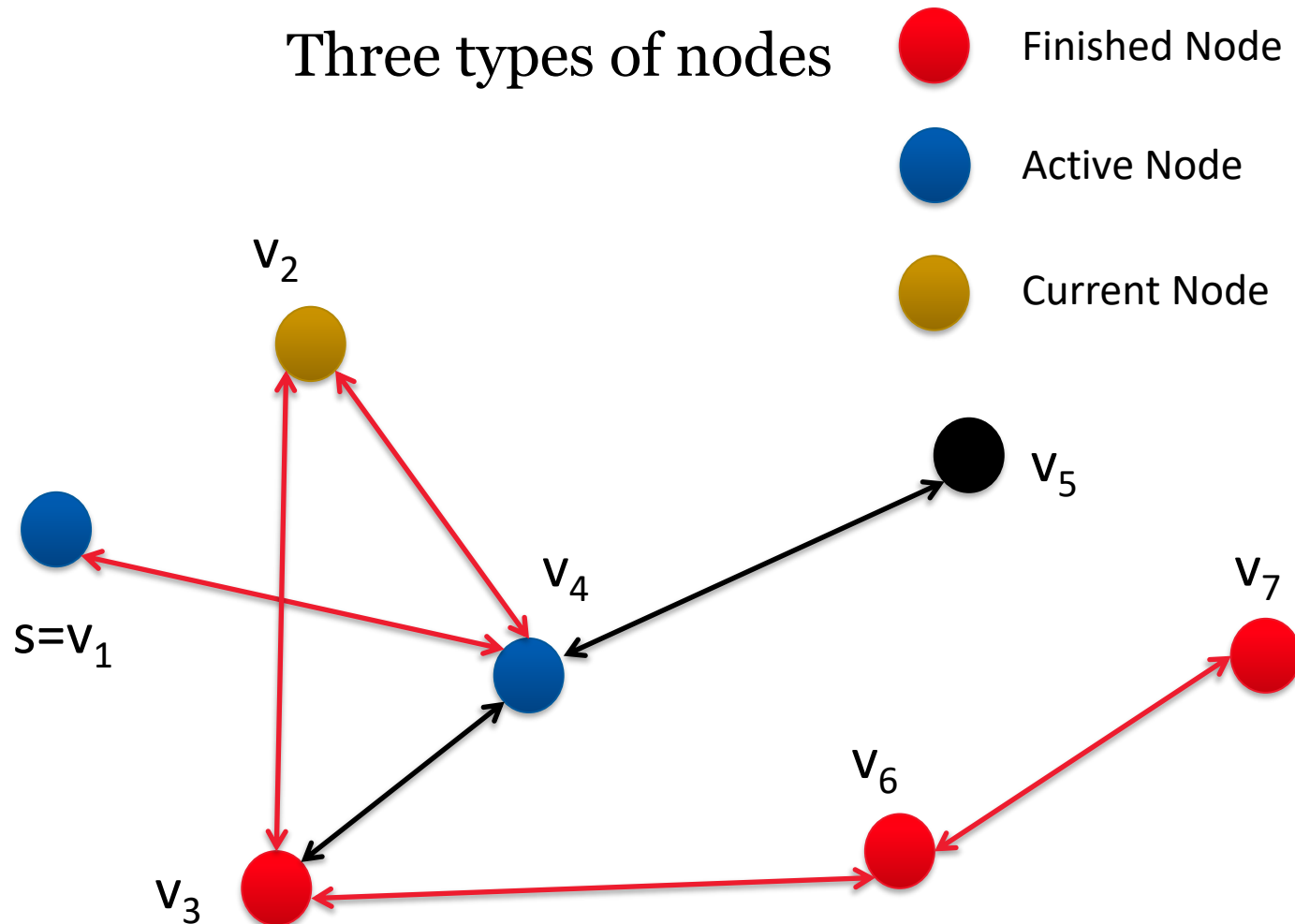
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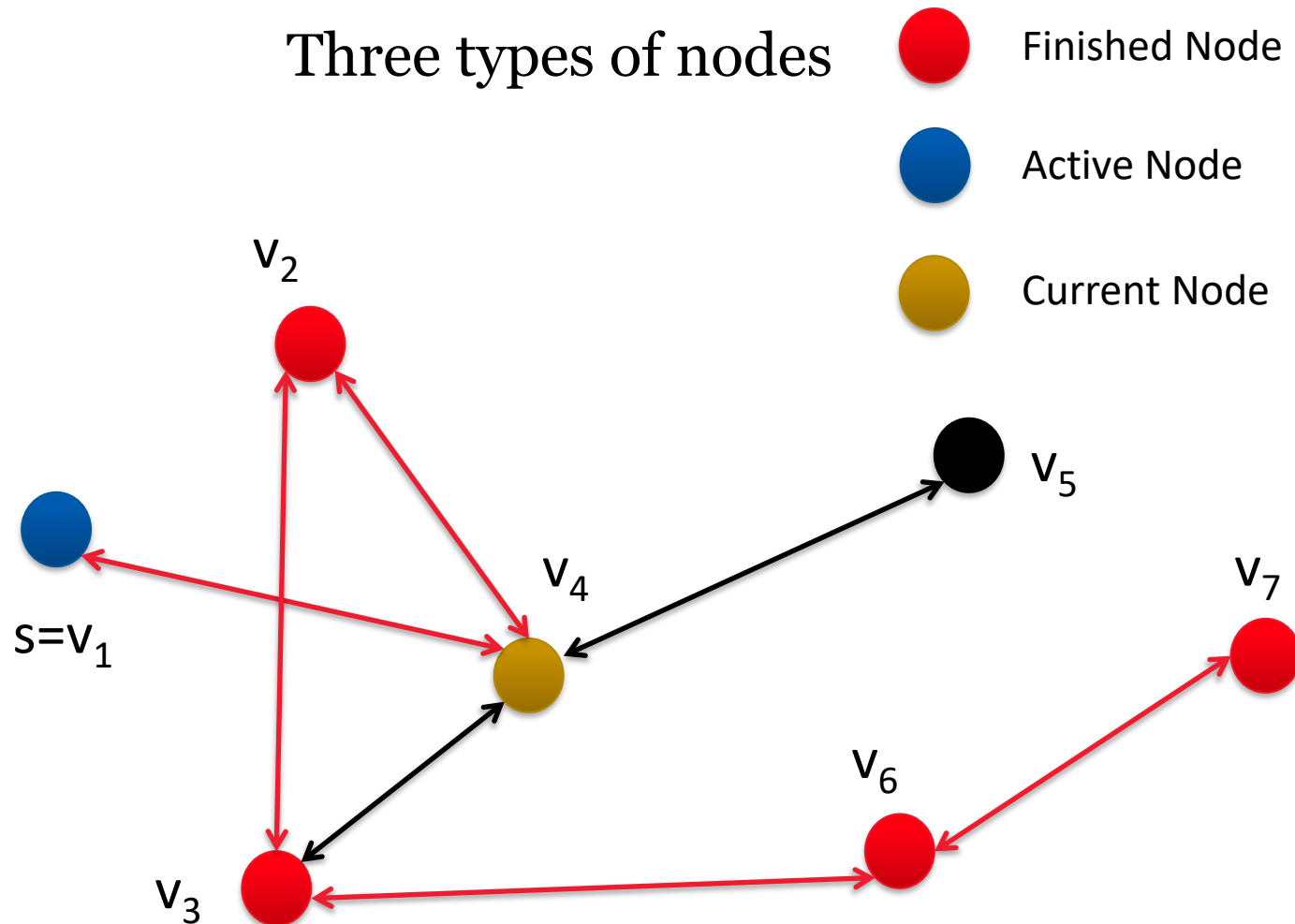
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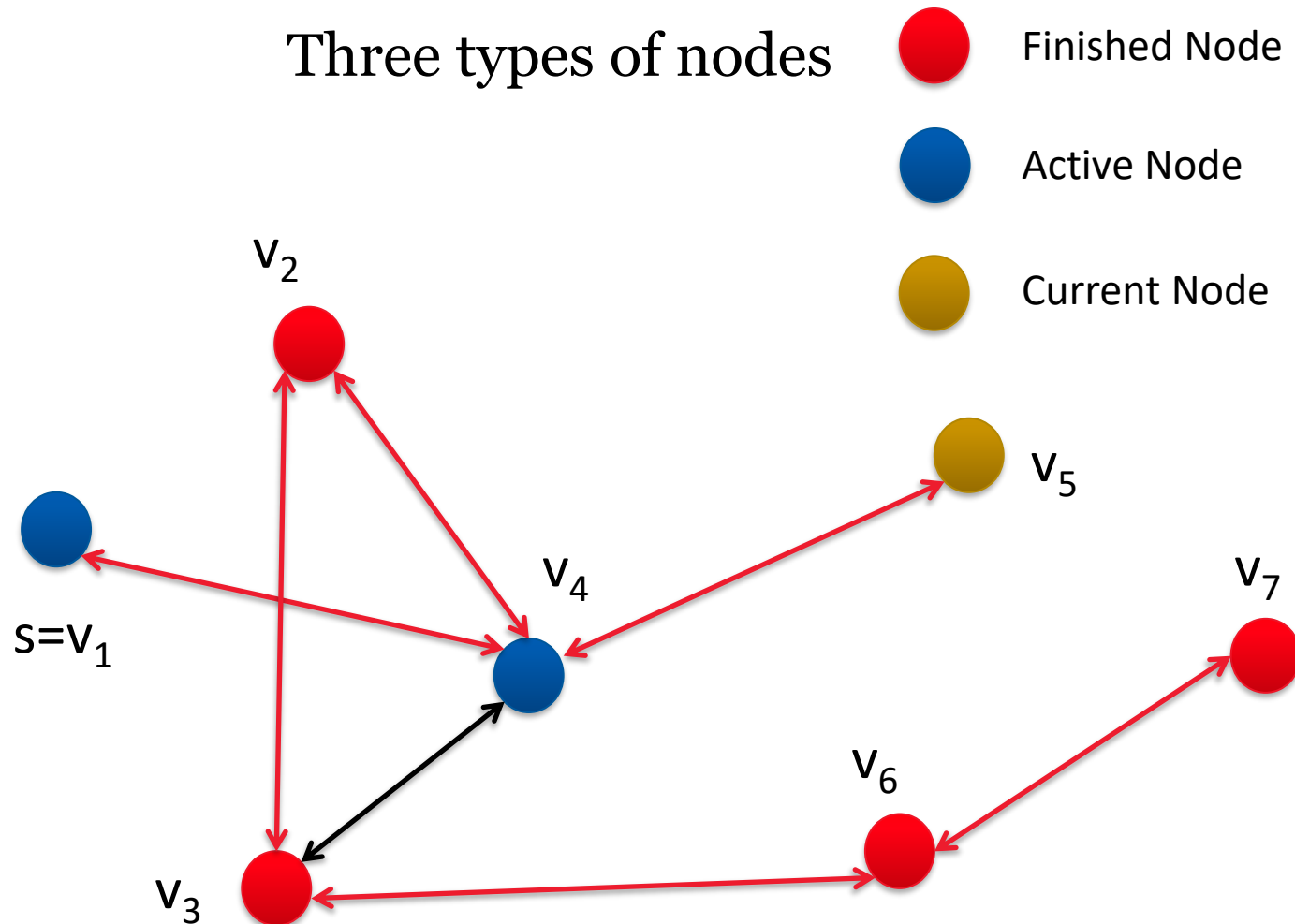
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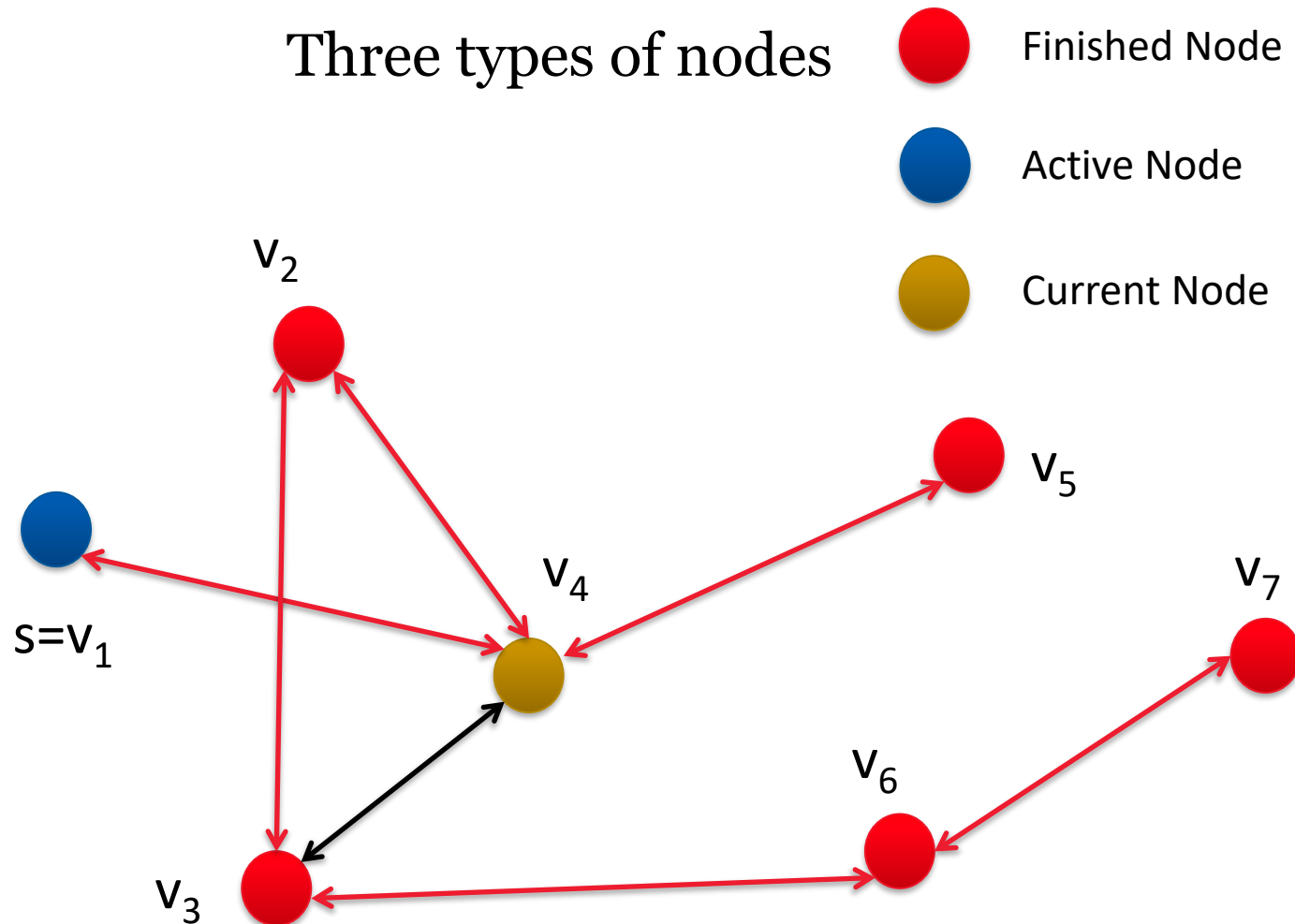
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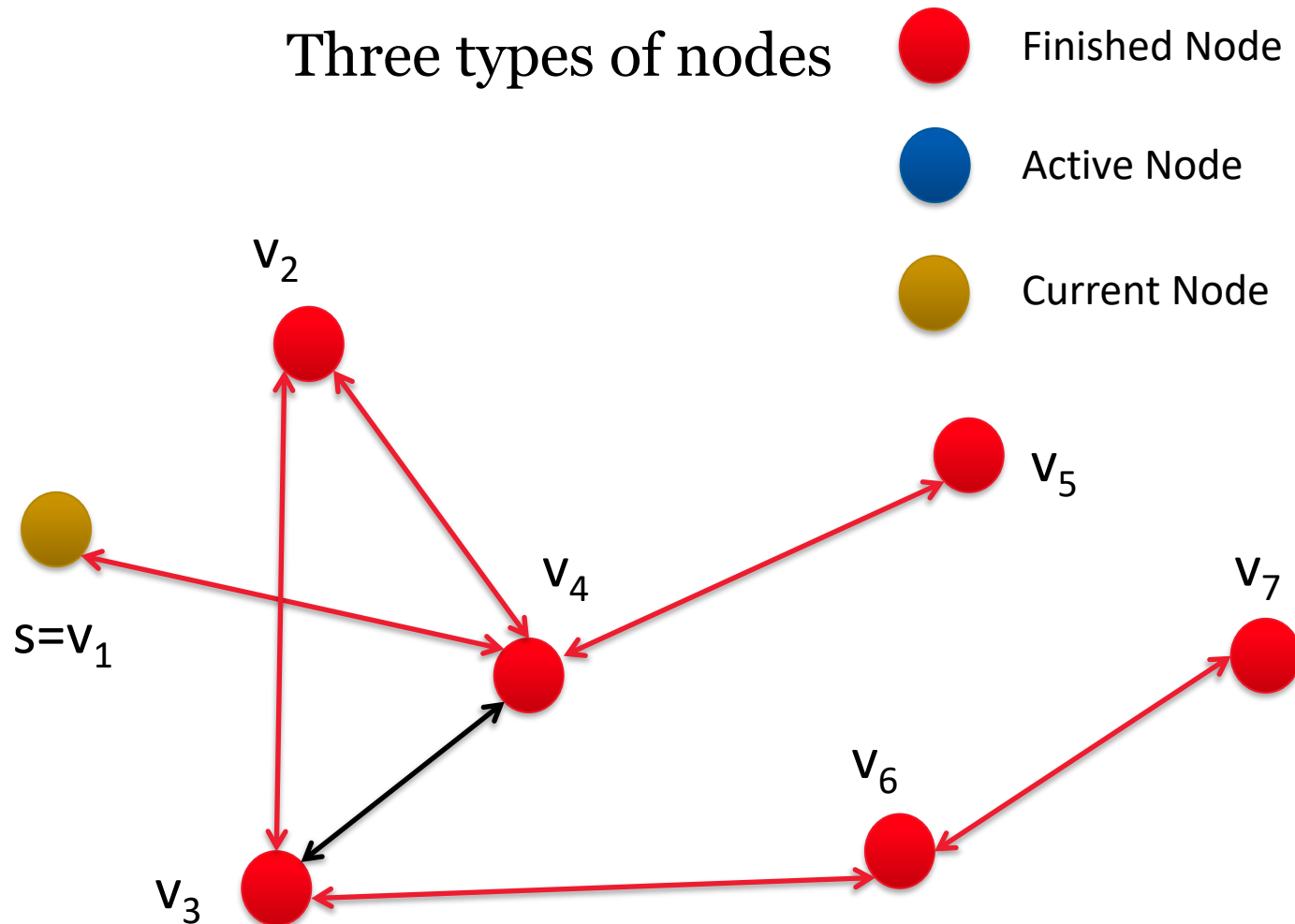
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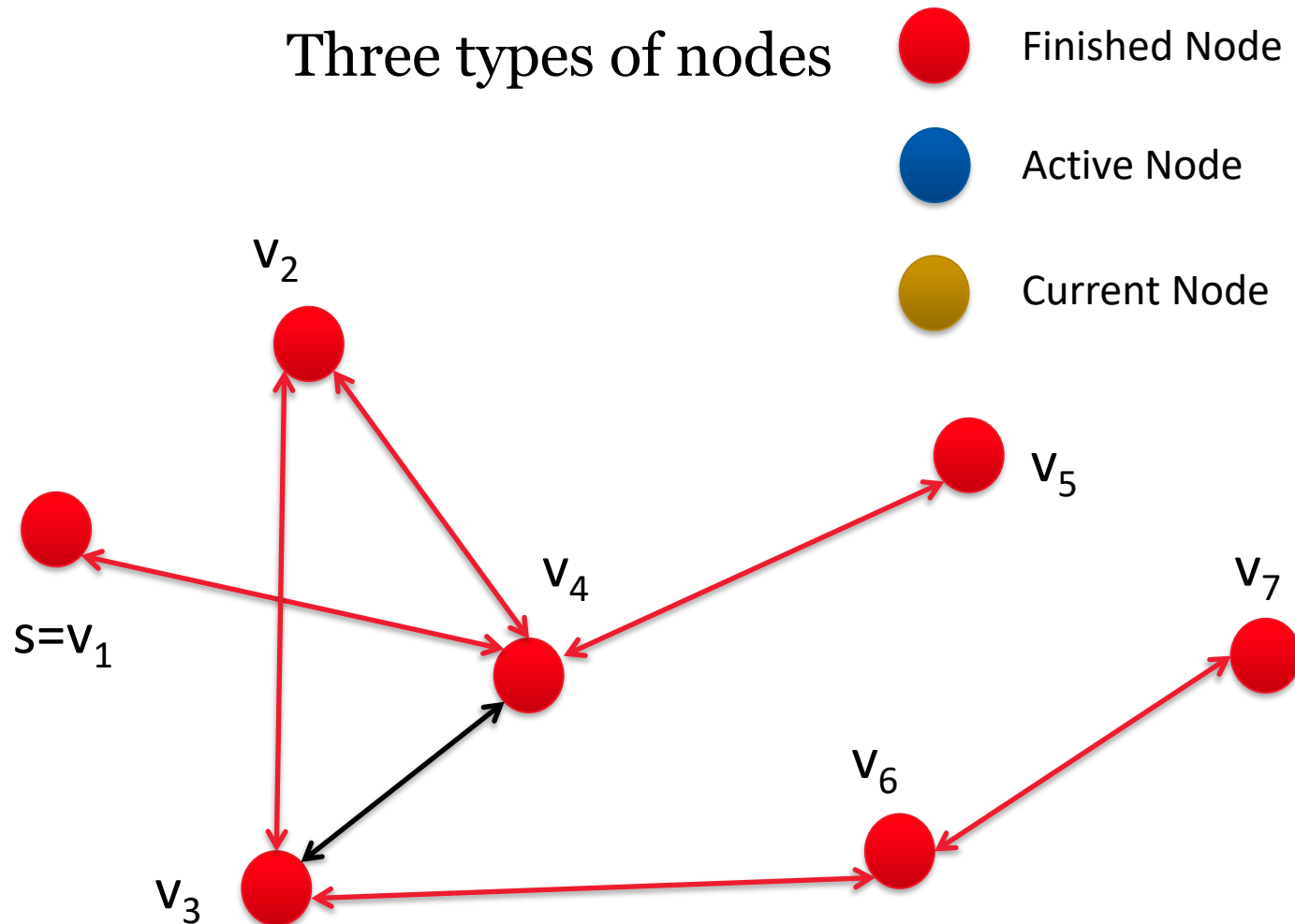
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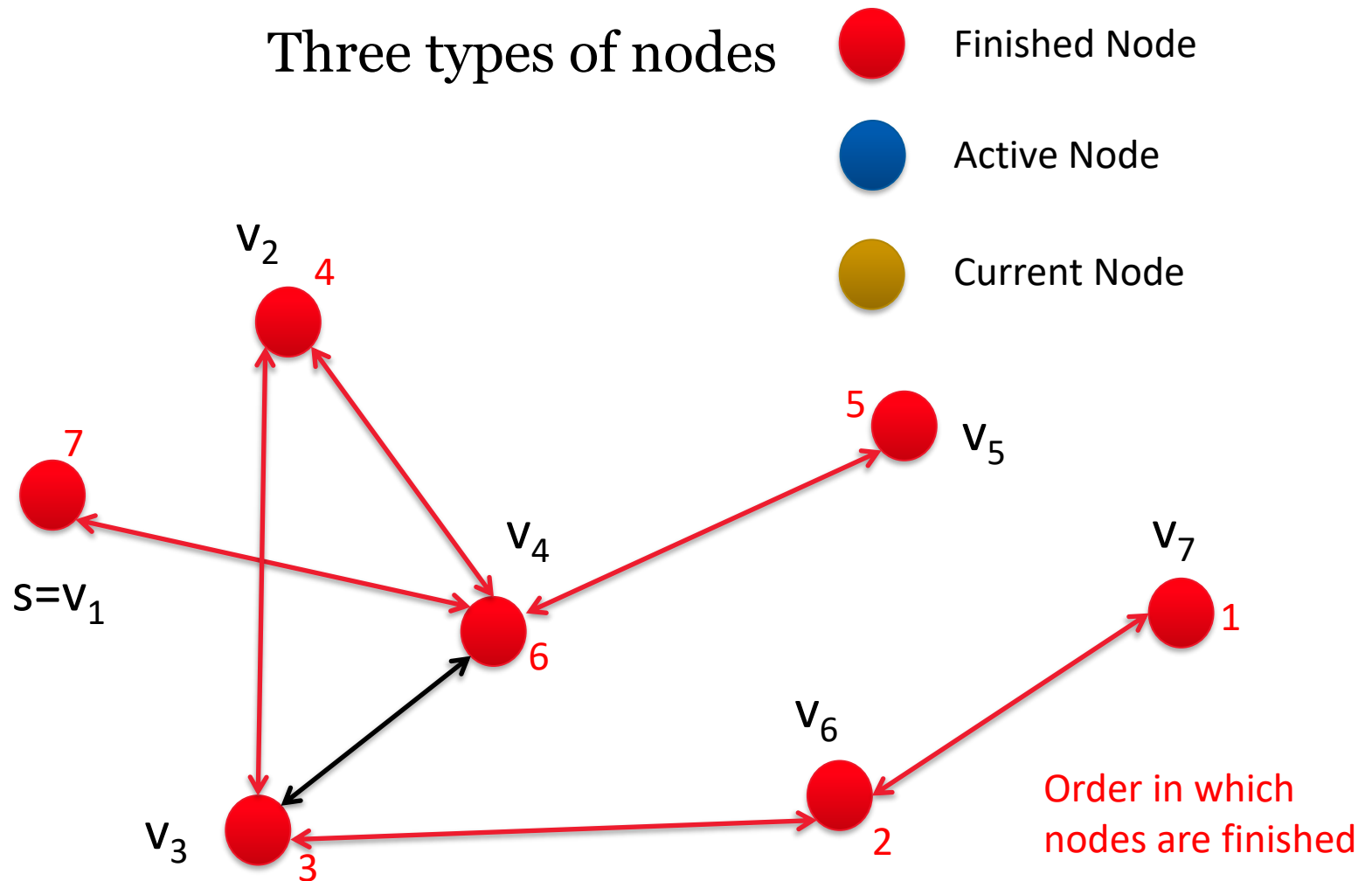
Depth-First-Search (DFS)



Depth-First-Search (DFS)



Depth-First-Search (DFS)



Depth-First-Search Tree

