

## Contents

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```
clear; close all; clc;
```

## Problem 1

---

```
figure(1);
Ts = 0.4;

Gs = tf(0.5, [1 0.5])
Gsc1 = feedback(Gs,1)

Gz = c2d(Gs, Ts)
Gzc1 = feedback(Gz, 1)
hold on;
step(Gsc1);
step(Gzc1);

hold off;
```

Gs =

$$\frac{0.5}{s + 0.5}$$

Continuous-time transfer function.

Gsc1 =

$$\frac{0.5}{s + 1}$$

Continuous-time transfer function.

Gz =

$$\frac{0.1813}{z - 0.8187}$$

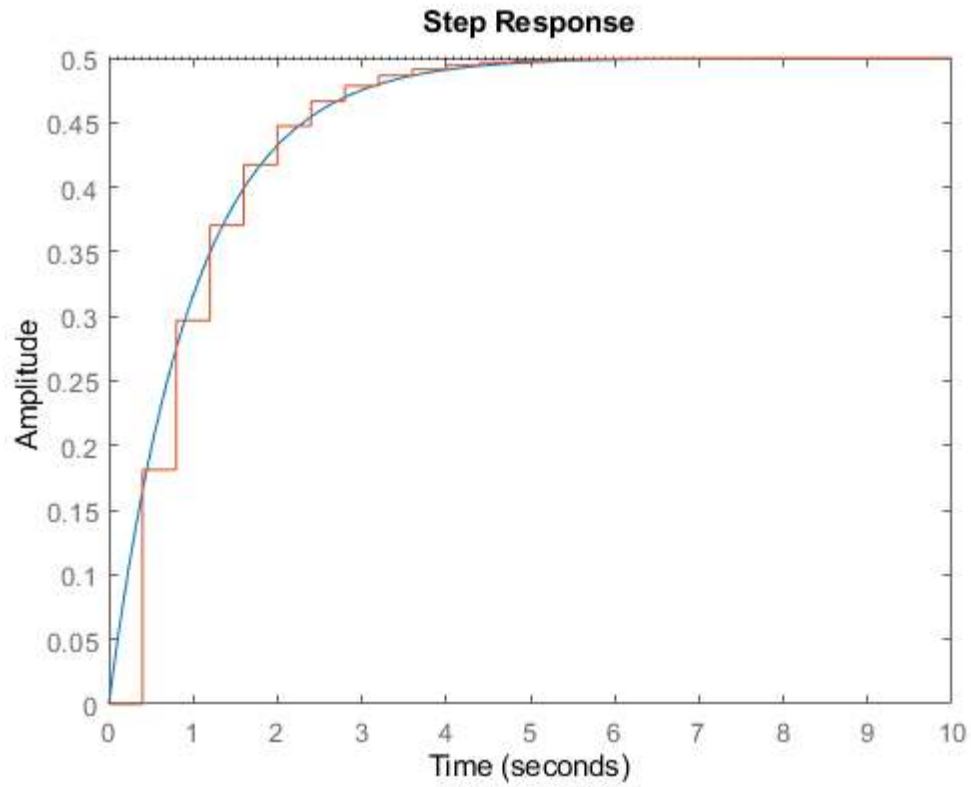
Sample time: 0.4 seconds  
Discrete-time transfer function.

Gzcl =

$$\frac{0.1813}{z - 0.6375}$$

Sample time: 0.4 seconds

Discrete-time transfer function.



## problem 2

```
figure(2);  
Ts = 0.6;  
  
Gs = tf(2,[1 0.5])  
Gz = c2d(Gs, Ts)  
Gzcl = feedback(Gz, 0.04)  
  
hold on;  
step(0.4*Gzcl)  
hold off;
```

Gs =

$$\frac{2}{s + 0.5}$$

Continuous-time transfer function.

Gz =

$$\frac{1.037}{z - 0.7408}$$

Sample time: 0.6 seconds

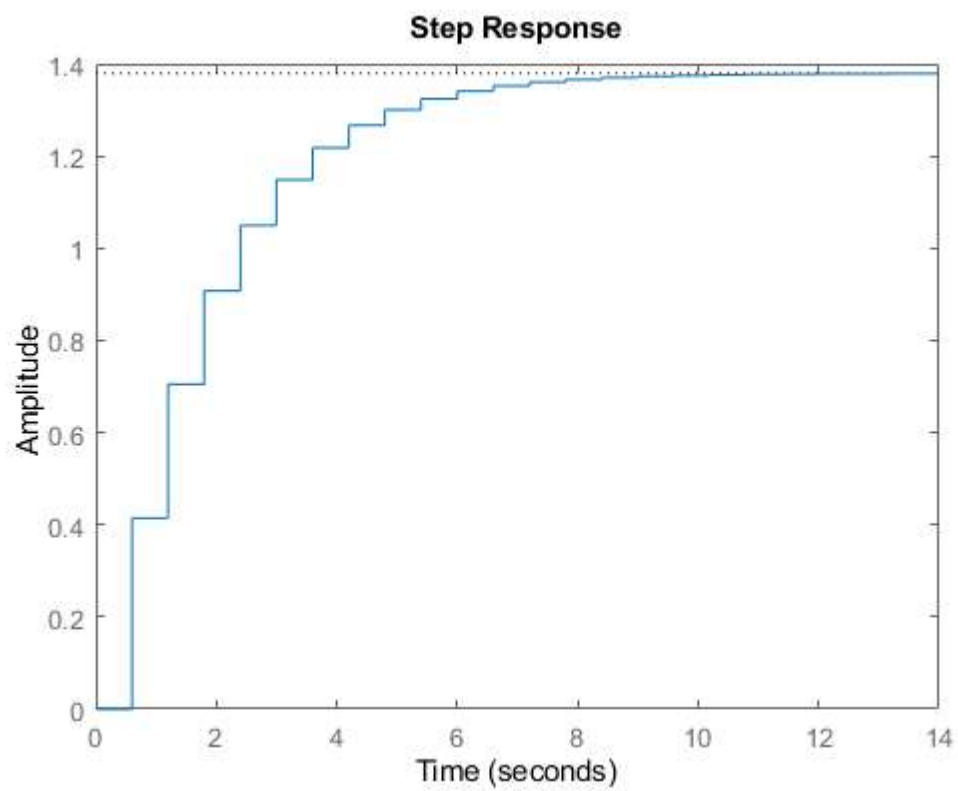
Discrete-time transfer function.

Gzcl =

$$\frac{1.037}{z - 0.6993}$$

Sample time: 0.6 seconds

Discrete-time transfer function.



### problem 3

```
figure(3);  
hold on;  
  
Gs = tf(1, [1 1 0])  
Gsc1 = feedback(Gs, 1)  
step(Gsc1);
```

```

% T = 1s
Ts = 1;
Gz = c2d(Gs, Ts);
Gzcl = feedback(Gz, 1)
log(pole(Gzcl))/Ts
step(Gzcl);

% T = 0.5s
Ts = 0.5;
Gz = c2d(Gs, Ts);
Gzcl = feedback(Gz, 1)
log(pole(Gzcl))/Ts
step(Gzcl);

% T = 0.1s
Ts = 0.1;
Gz = c2d(Gs, Ts);
Gzcl = feedback(Gz, 1)
log(pole(Gzcl))/Ts
step(Gzcl);
hold off;

```

---

Gs =

$$\frac{1}{s^2 + s}$$

Continuous-time transfer function.

Gscl =

$$\frac{1}{s^2 + s + 1}$$

Continuous-time transfer function.

Gzcl =

$$\frac{0.3679 z + 0.2642}{z^2 - z + 0.6321}$$

Sample time: 1 seconds

Discrete-time transfer function.

ans =

$$\begin{aligned} & -0.2293 + 0.8907i \\ & -0.2293 - 0.8907i \end{aligned}$$

Gzcl =

$$\frac{0.1065 z + 0.0902}{z^2 - 1.5 z + 0.6967}$$

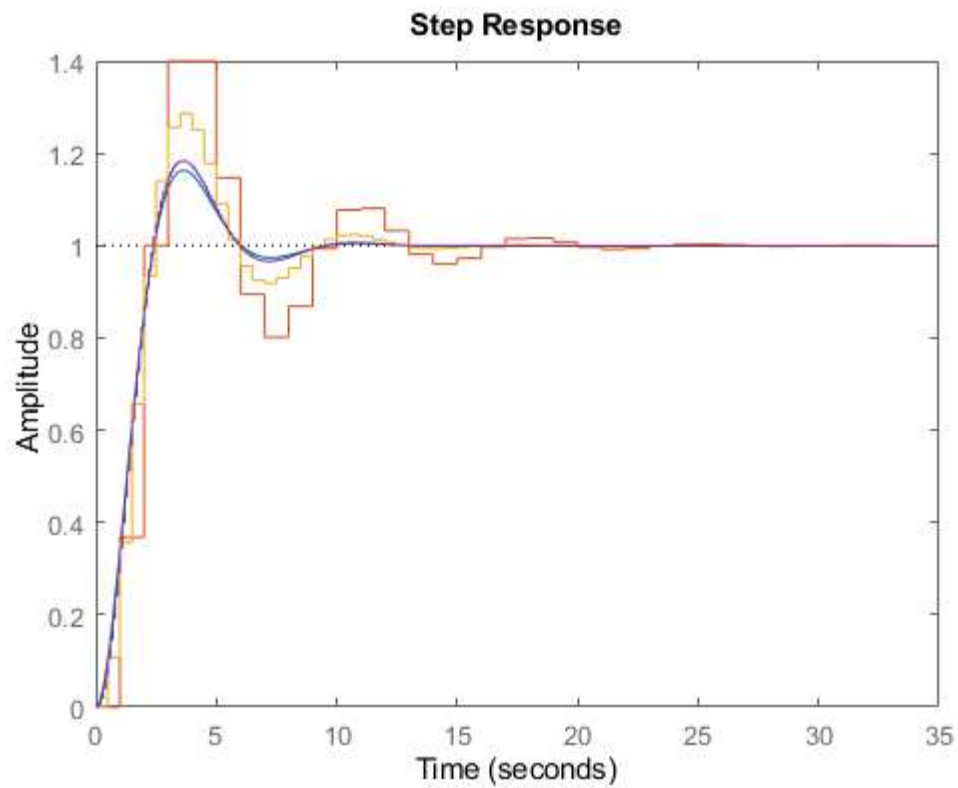
Sample time: 0.5 seconds  
Discrete-time transfer function.

```
ans =  
-0.3614 + 0.9088i  
-0.3614 - 0.9088i
```

```
Gzcl =  
  
0.004837 z + 0.004679  
-----  
z^2 - 1.9 z + 0.9095
```

Sample time: 0.1 seconds  
Discrete-time transfer function.

```
ans =  
-0.4742 + 0.8794i  
-0.4742 - 0.8794i
```



#### problem 4

```
hold on;  
Gs = tf(1, [1 1]);  
Ts = 1;  
Gz = c2d(Gs, Ts)  
  
hold off;
```

Gz =

```
      0.6321  
-----  
z - 0.3679
```

Sample time: 1 seconds

Discrete-time transfer function.

## Problem 5

---

```
syms z  
C = (z-0.9)*(z-0.8)*(z^2-1.9*z+1);  
expand(C)  
roots([1 -3.6 4.95 -3.068 0.72])
```

```
ans =  
z^4 - (18*z^3)/5 + (99*z^2)/20 - (767*z)/250 + 18/25  
ans =  
      0.9500 + 0.3122i  
      0.9500 - 0.3122i  
      0.9000 + 0.0000i  
      0.8000 + 0.0000i
```