

Image Processing & Vision

Week 4

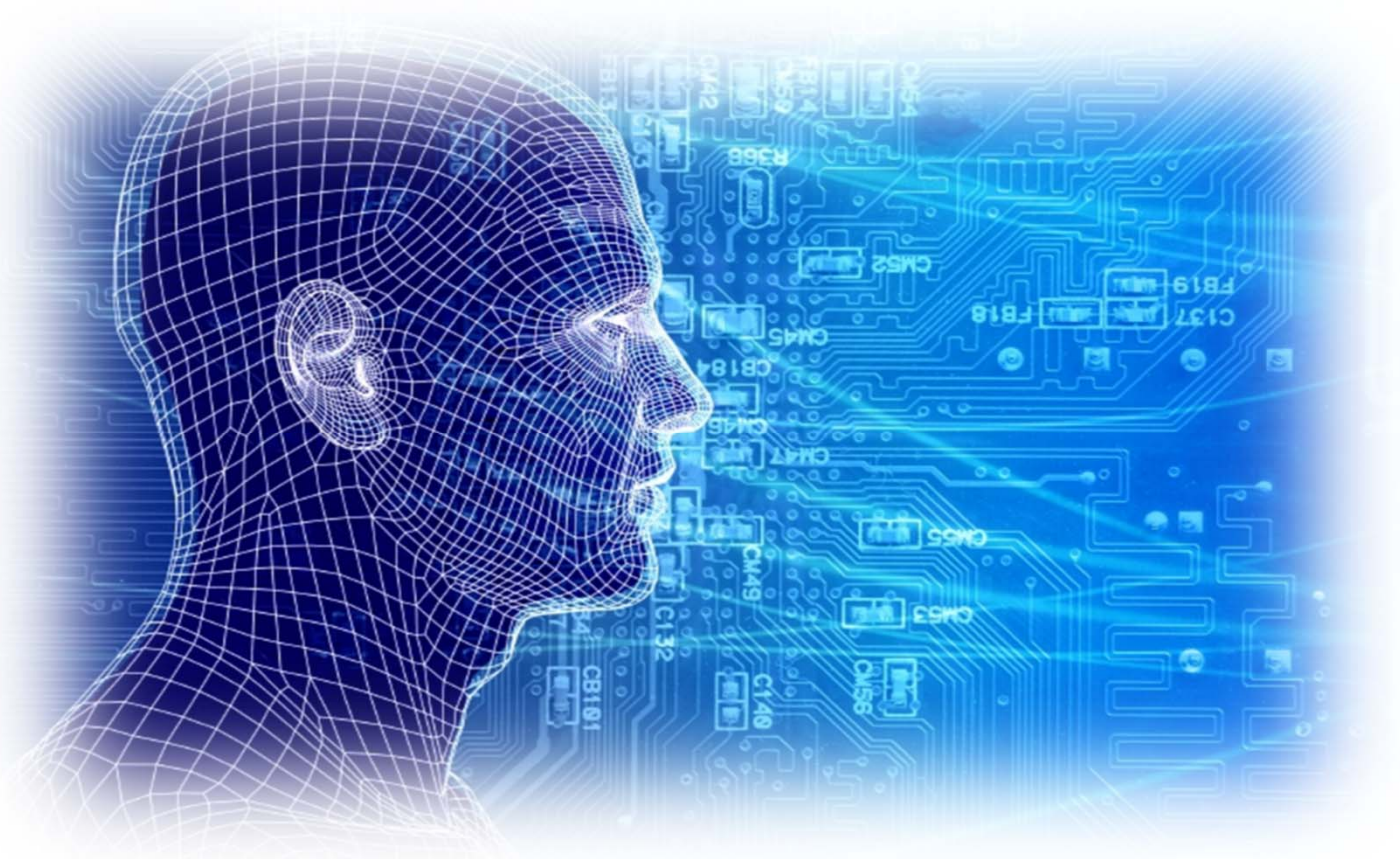
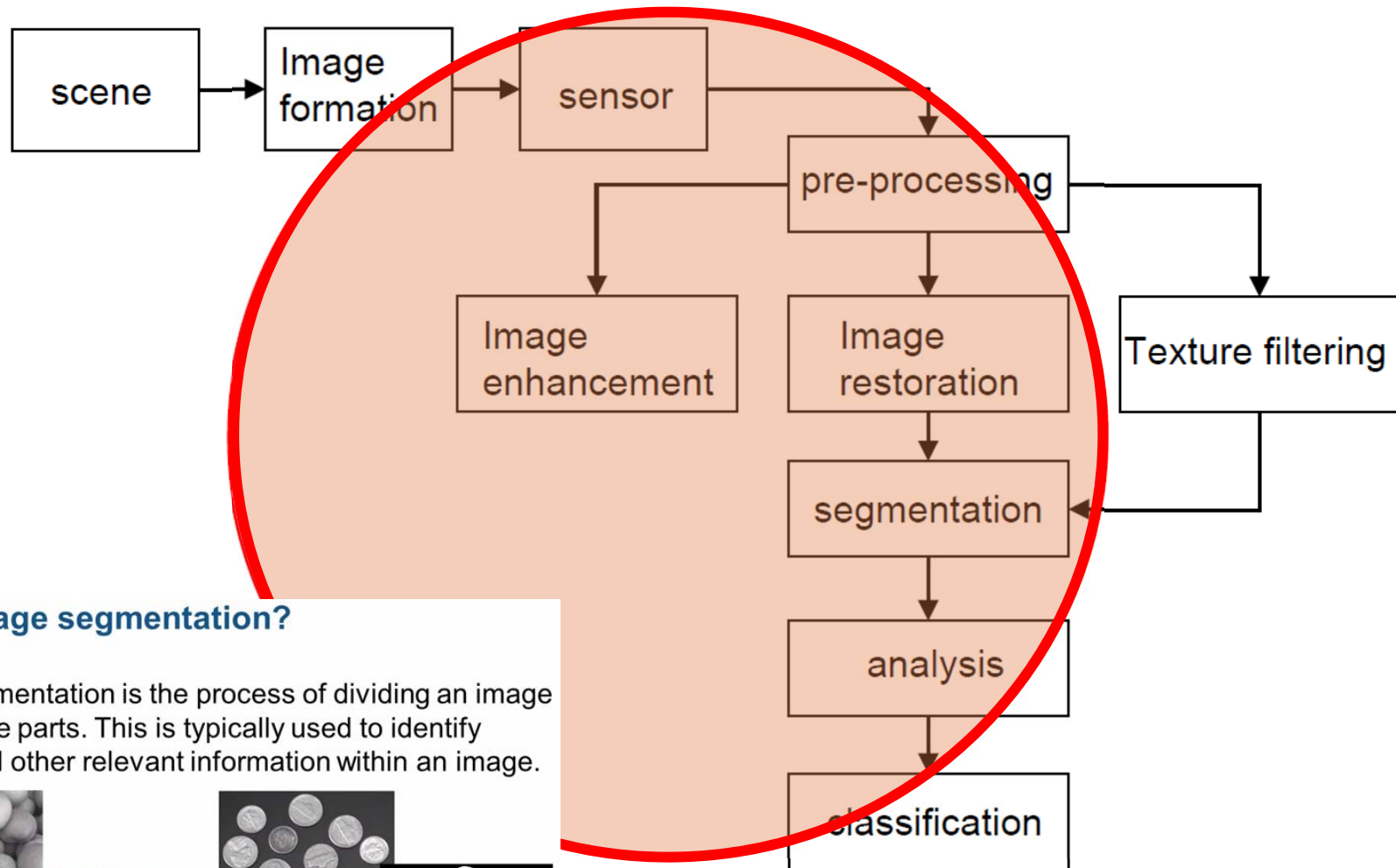
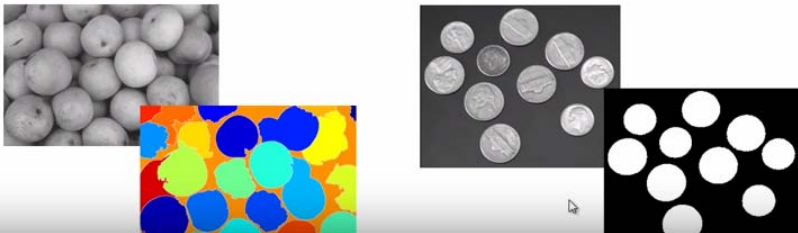


Image Analysis Paradigm—where are we?



What is image segmentation?

- Image segmentation is the process of dividing an image into multiple parts. This is typically used to identify objects and other relevant information within an image.



Content

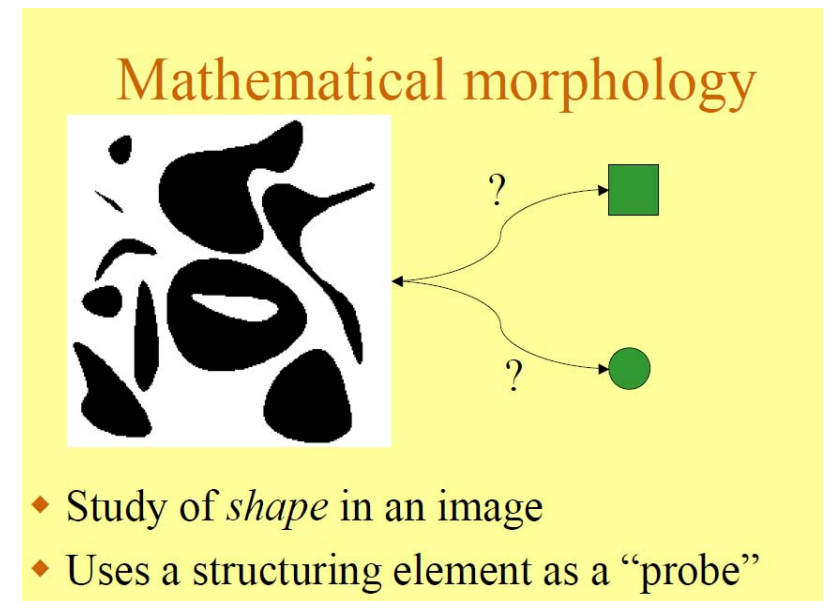
- Morphological operations
 - **Dilation & Erosion**
 - **Opening & Closing**
- Segmentation
- Edge detection

MORPHOLOGICAL OPERATIONS

Dilation & Erosion

What is Morphology in computer vision ?

1. Morphology generally concerned with **shape** and **properties of objects**.
2. Used for **segmentation** and **feature extraction**.
3. Segmentation = used for **cleaning** binary objects.



Morphological operation

Two basic operations

1. **erosion** (opening)

2. **dilation** (closing)

**Mathematical
Morphology**
- Set-theoretic
representation for binary
shapes

Binary Morphology

- Libraries of Structuring Elements(SE)

A **structuring element** is a shape mask used in the basic morphological operations.

They can be any shape and size that is digitally representable, and each has an **origin**.



box

`box(length,width)`



hexagon



disk

`disk(diameter)`

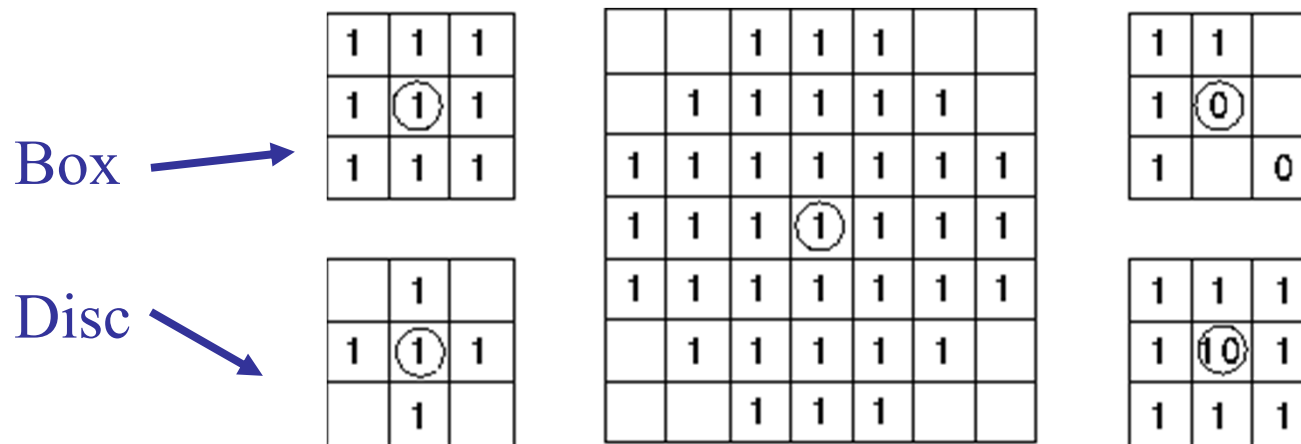


any shape

Application
specific **SE** created
by the user!

Structuring Element (Kernel)

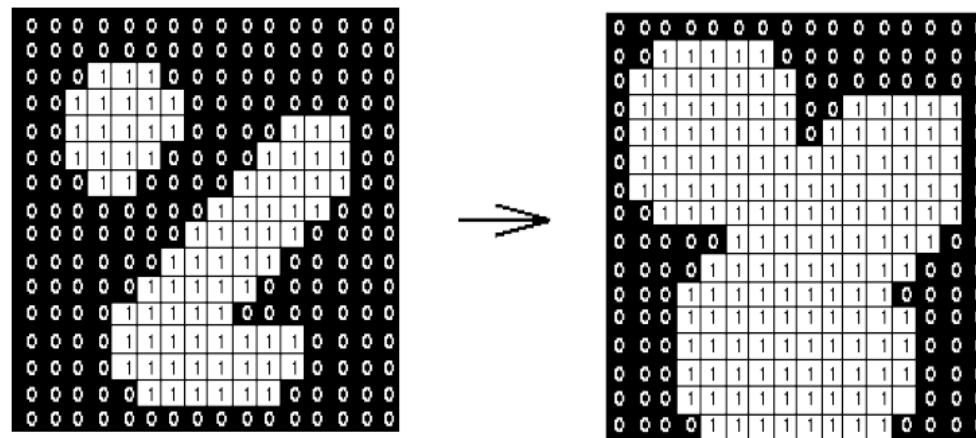
- varying sizes
- element values are 0,1 and none(!)
- Structural Elements have an origin
- For thinning, other values are possible
- Empty spots in the Structuring Elements are *don't care's*!



Examples of structuring elements

DILATION \leftrightarrow EROSION

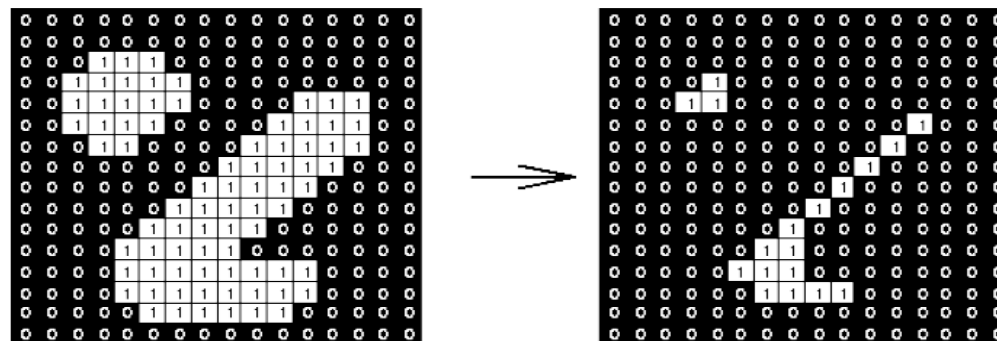
- Dilation (OR)
 - expands binary regions



Effect of dilation using a 3×3 square structuring element

- Erosion (AND)
 - shrinks

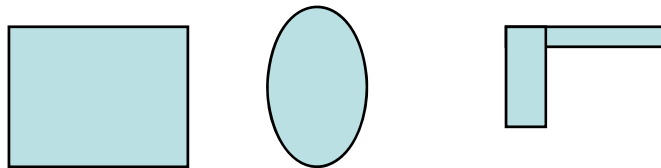
Applications of erosion :
Eliminating unwanted detail



Effect of erosion using a 3×3 square structuring element

DILATION

- Dilation (OR)
 - expands binary regions
- Properties:
 - It grows or thickens objects
 - Thickening is controlled by **Structuring Element (SE)**



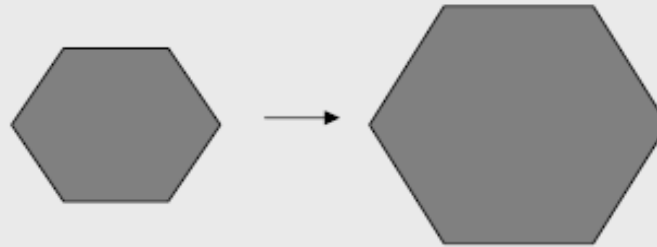
- **Structuring element** is a matrix of 1's and 0's

DILATION : Main Applications

Dilation **expands** the connected sets of 1s of a binary image.

It can be used for

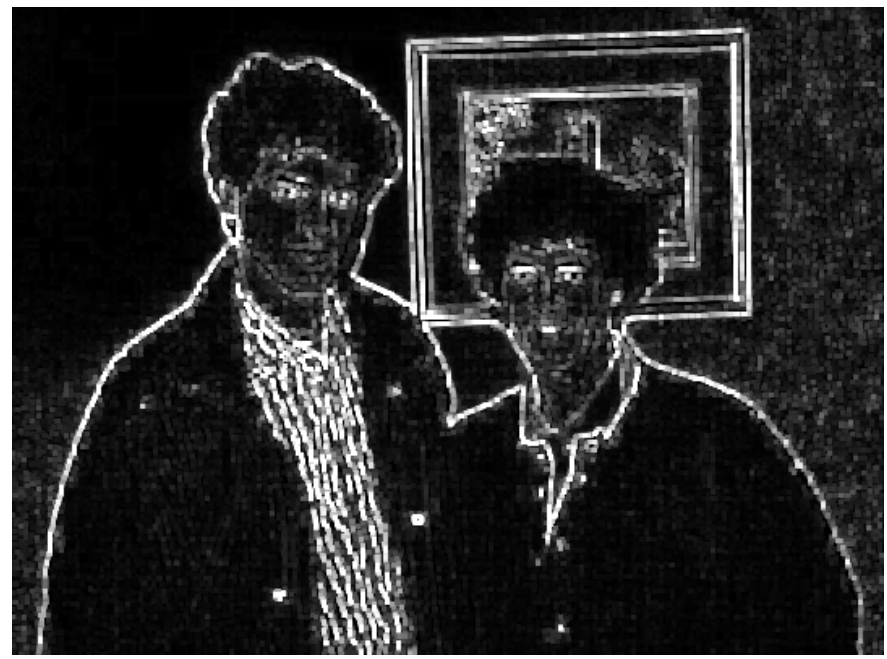
1. expanding shapes:



2. filling holes, gaps and gulfs:



DILATION EXAMPLE



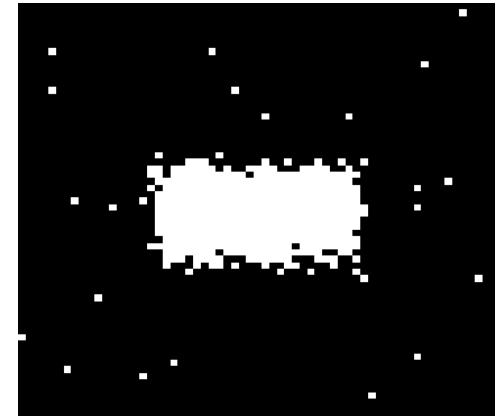
EROSION

- Erosion (AND)
 - Shrinks
- Properties:
 - Erosion removes **spiky edges**
 - objects are light (white in binary)
 - decreases geometrical area of object
 - sets contour pixels of object to background value



EROSION: Main Applications

1. Remove isolated noisy pixels.
2. Smooth object boundary.
3. Remove the outer layer of object pixels, so object becomes slightly smaller.

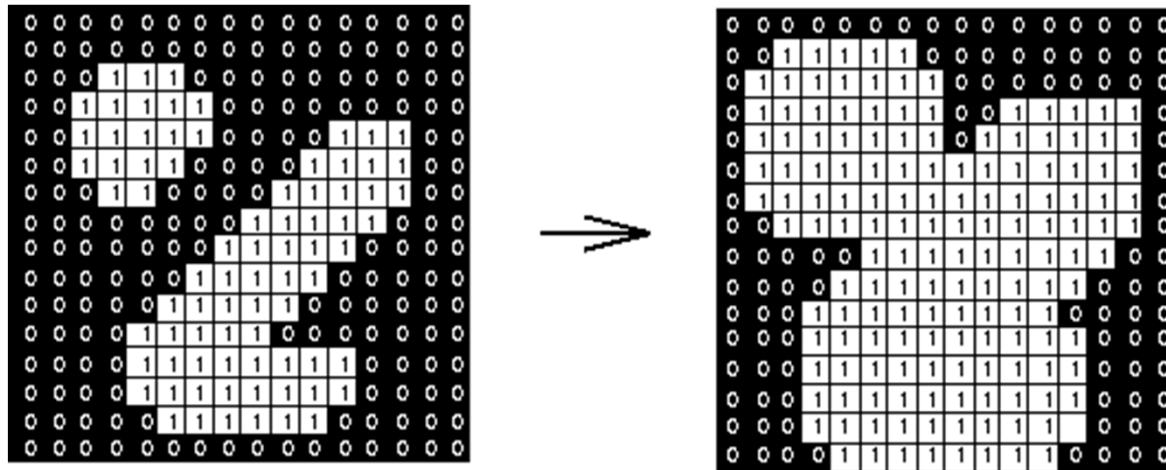


DEMO

- <https://www.youtube.com/watch?v=8Ta-OcdJMMo>

Example: Dilation

- **Dilation** is an important morphological operation



- Applied **Structuring Element**:

1	1	1
1	1	1
1	1	1

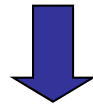
Set of coordinate points =

{ (-1, -1), (0, -1), (1, -1),
(-1, 0), (0, 0), (1, 0),
(-1, 1), (0, 1), (1, 1) }

Let's do it together!

Input image

1	0	0	0	1	1	1	0	1	1
---	---	---	---	---	---	---	---	---	---



Structuring Element

1	1	1
---	---	---



Output Image

	1								
--	---	--	--	--	--	--	--	--	--

Let's do it together!

Input image

1	0	0	0	1	1	1	0	1	1
---	---	---	---	---	---	---	---	---	---



Structuring Element

1	1	1
---	---	---



Output Image

	1	0							
--	---	---	--	--	--	--	--	--	--

Let's do it together!

Input image

1	0	0	0	1	1	1	0	1	1
---	---	---	---	---	---	---	---	---	---



Structuring Element

1	1	1
---	---	---



Output Image

	1	0	1						
--	---	---	---	--	--	--	--	--	--

Let's do it together!

Input image

1	0	0	0	1	1	1	0	1	1
---	---	---	---	---	---	---	---	---	---



Structuring Element

1	1	1
---	---	---



Output Image

	1	0	1	1					
--	---	---	---	---	--	--	--	--	--

Let's do it together!

Input image

1	0	0	0	1	1	1	0	1	1
---	---	---	---	---	---	---	---	---	---



Structuring Element

1	1	1
---	---	---



Output Image

	1	0	1	1	1				
--	---	---	---	---	---	--	--	--	--

Let's do it together!

Input image

1	0	0	0	1	1	1	0	1	1
---	---	---	---	---	---	---	---	---	---



Structuring Element

1	1	1
---	---	---



Output Image

	1	0	1	1	1	1			
--	---	---	---	---	---	---	--	--	--

Let's do it together!

Input image

1	0	0	0	1	1	1	0	1	1
---	---	---	---	---	---	---	---	---	---



Structuring Element

1	1	1
---	---	---



Output Image

	1	0	1	1	1	1	1		
--	---	---	---	---	---	---	---	--	--

Let's do it together!

Input image

1	0	0	0	1	1	1	0	1	1
---	---	---	---	---	---	---	---	---	---



Structuring Element

1	1	1
---	---	---

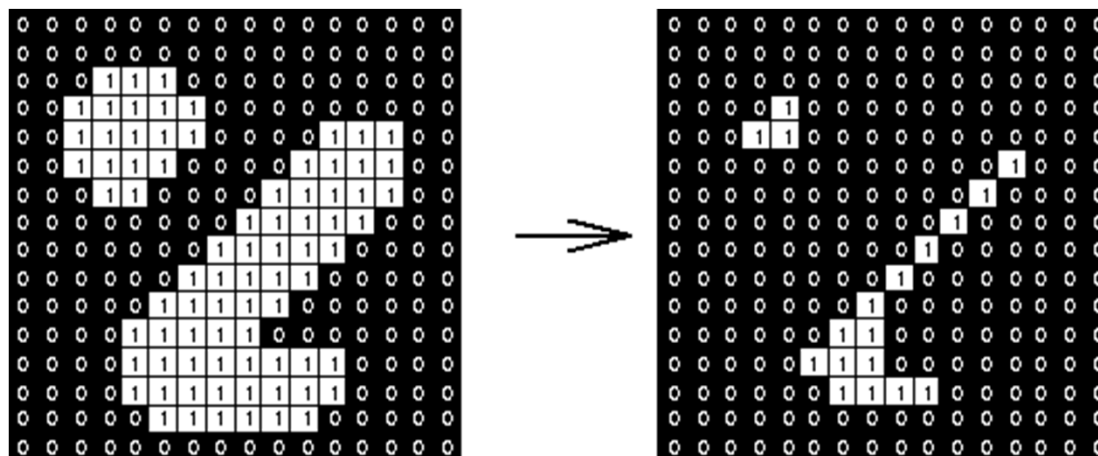


Output Image

	1	0	1	1	1	1	1	1	
--	---	---	---	---	---	---	---	---	--

Example: Erosion

- **Erosion** is an important morphological operation



- Applied **Structuring Element**:

1	1	1
1	1	1
1	1	1

Set of coordinate points =

{ (-1, -1), (0, -1), (1, -1),
(-1, 0), (0, 0), (1, 0),
(-1, 1), (0, 1), (1, 1) }

Let's do it together!

Input image

1	0	0	0	1	1	1	0	1	1
---	---	---	---	---	---	---	---	---	---



Structuring Element

1	1	1
---	---	---



Output Image

	0								
--	---	--	--	--	--	--	--	--	--

Let's do it together!

Input image

1	0	0	0	1	1	1	0	1	1
---	---	---	---	---	---	---	---	---	---



Structuring Element

1	1	1
---	---	---



Output Image

	0	0							
--	---	---	--	--	--	--	--	--	--

Let's do it together!

Input image

1	0	0	0	1	1	1	0	1	1
---	---	---	---	---	---	---	---	---	---



Structuring Element

1	1	1
---	---	---



Output Image

	0	0	0						
--	---	---	---	--	--	--	--	--	--

Let's do it together!

Input image

1	0	0	0	1	1	1	0	1	1
---	---	---	---	---	---	---	---	---	---



Structuring Element

1	1	1
---	---	---



Output Image

	0	0	0	0					
--	---	---	---	---	--	--	--	--	--

Let's do it together!

Input image

1	0	0	0	1	1	1	0	1	1
---	---	---	---	---	---	---	---	---	---



Structuring Element

1	1	1
---	---	---



Output Image

	0	0	0	0	1				
--	---	---	---	---	---	--	--	--	--

Let's do it together!

Input image

1	0	0	0	1	1	1	0	1	1
---	---	---	---	---	---	---	---	---	---



Structuring Element

1	1	1
---	---	---



Output Image

	0	0	0	0	1	0			
--	---	---	---	---	---	---	--	--	--

Let's do it together!

Input image

1	0	0	0	1	1	1	0	1	1
---	---	---	---	---	---	---	---	---	---



Structuring Element

1	1	1
---	---	---



Output Image

	0	0	0	0	1	0	0		
--	---	---	---	---	---	---	---	--	--

Let's do it together!

Input image

1	0	0	0	1	1	1	0	1	1
---	---	---	---	---	---	---	---	---	---



Structuring Element

1	1	1
---	---	---



Output Image

	0	0	0	0	1	0	0	0	
--	---	---	---	---	---	---	---	---	--

DEMO in matlab: DILATION \leftrightarrow EROSION

Example: Suppose that the structuring element is a 3x3 square with the origin at its center

$$K = \begin{array}{|c|c|c|} \hline 1 & 1 & 1 \\ \hline 1 & 1 & 1 \\ \hline 1 & 1 & 1 \\ \hline \end{array} \quad \left\{ \begin{array}{l} (-1,-1), (0,-1), (1,-1), \\ (-1,0), (0,0), (1,0), \\ (1,1), (0,1), (1,1) \end{array} \right\}$$

$$X = \begin{array}{|c|c|c|c|c|} \hline & & & & \\ \hline & & & & \\ \hline & & & & \\ \hline & & & & \\ \hline & & & & \\ \hline \end{array}$$

Opening & Closing

- ✓ derived from the fundamental operations: erosion and dilation
- ✓ normally applied to binary images

Opening & Closing

- Opening → An Erosion followed by a dilation
- Closing → A dilation followed by an erosion

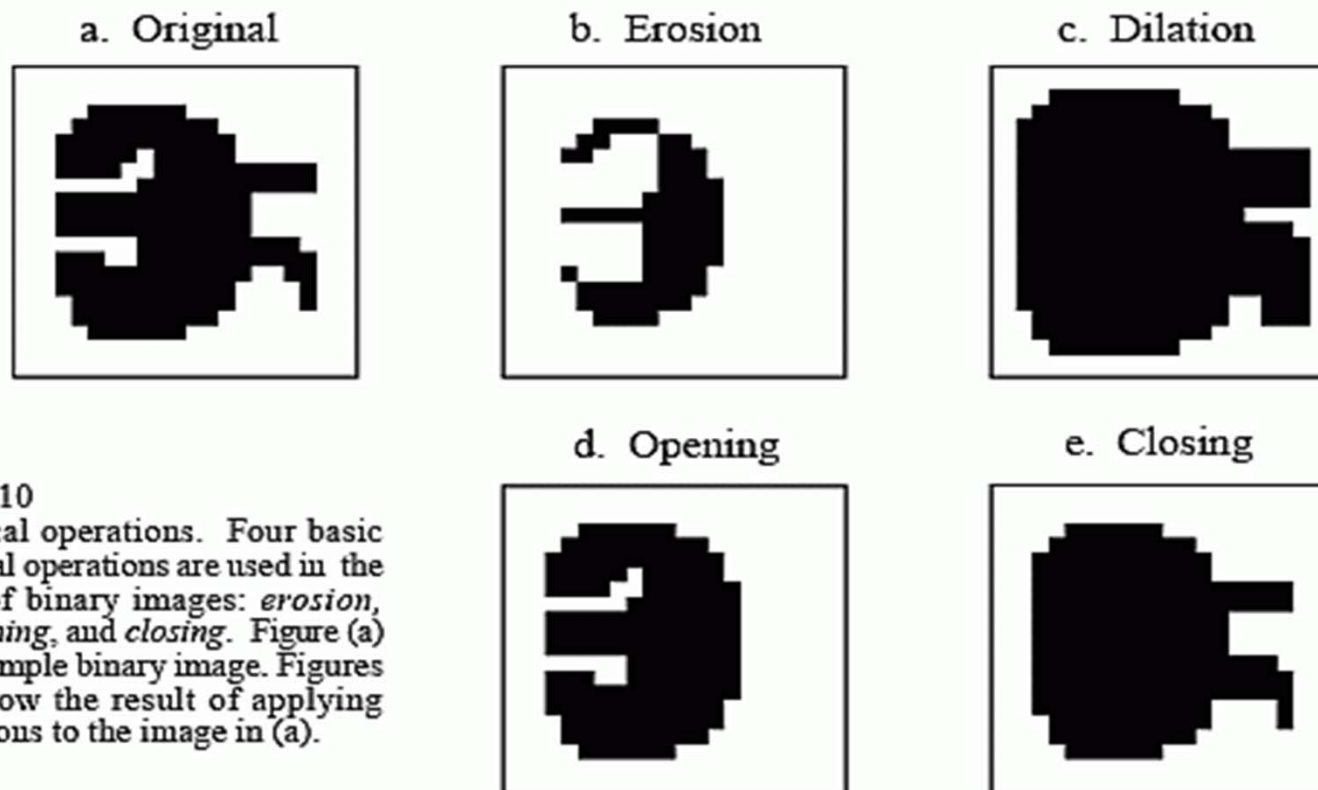
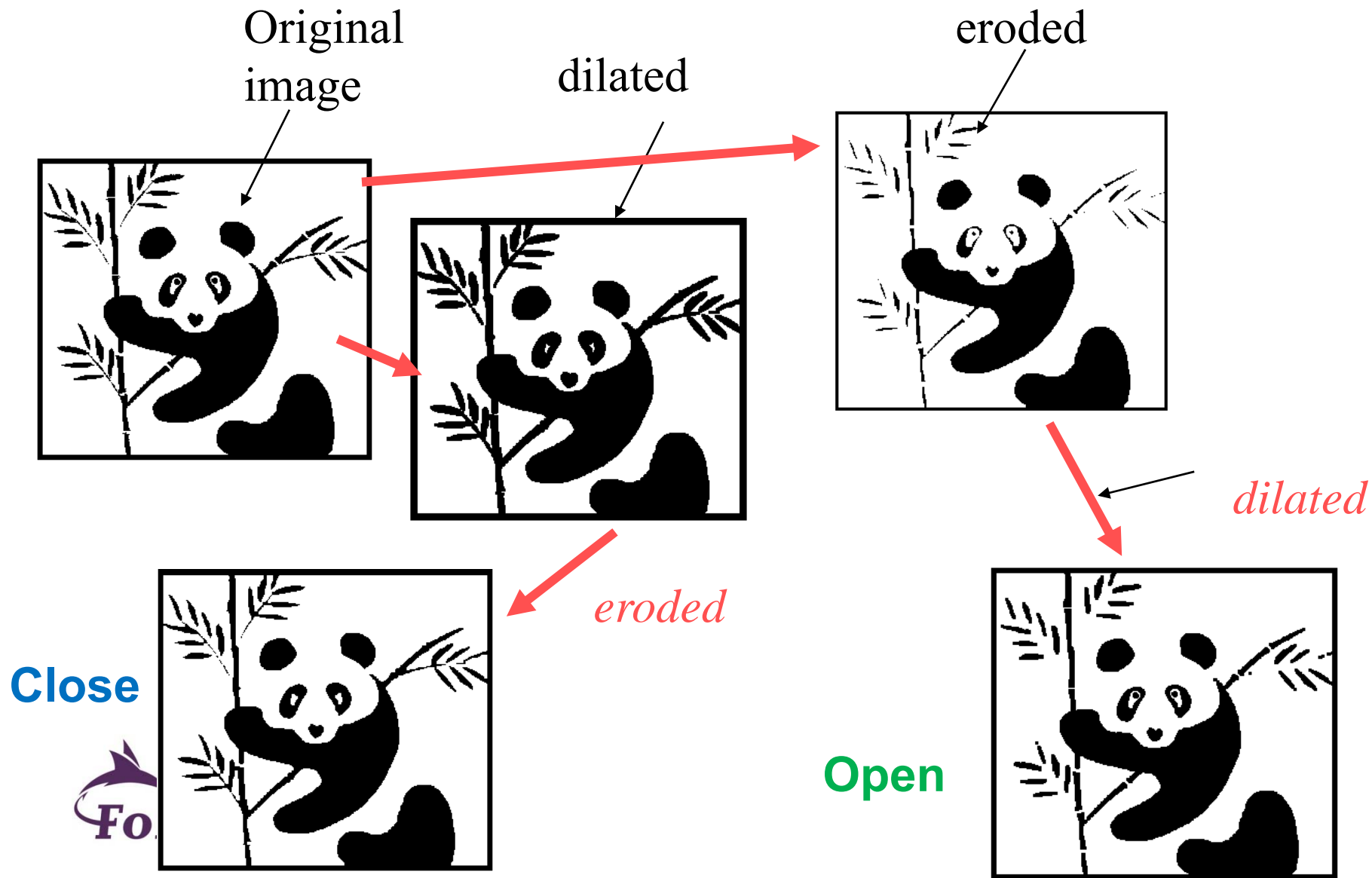
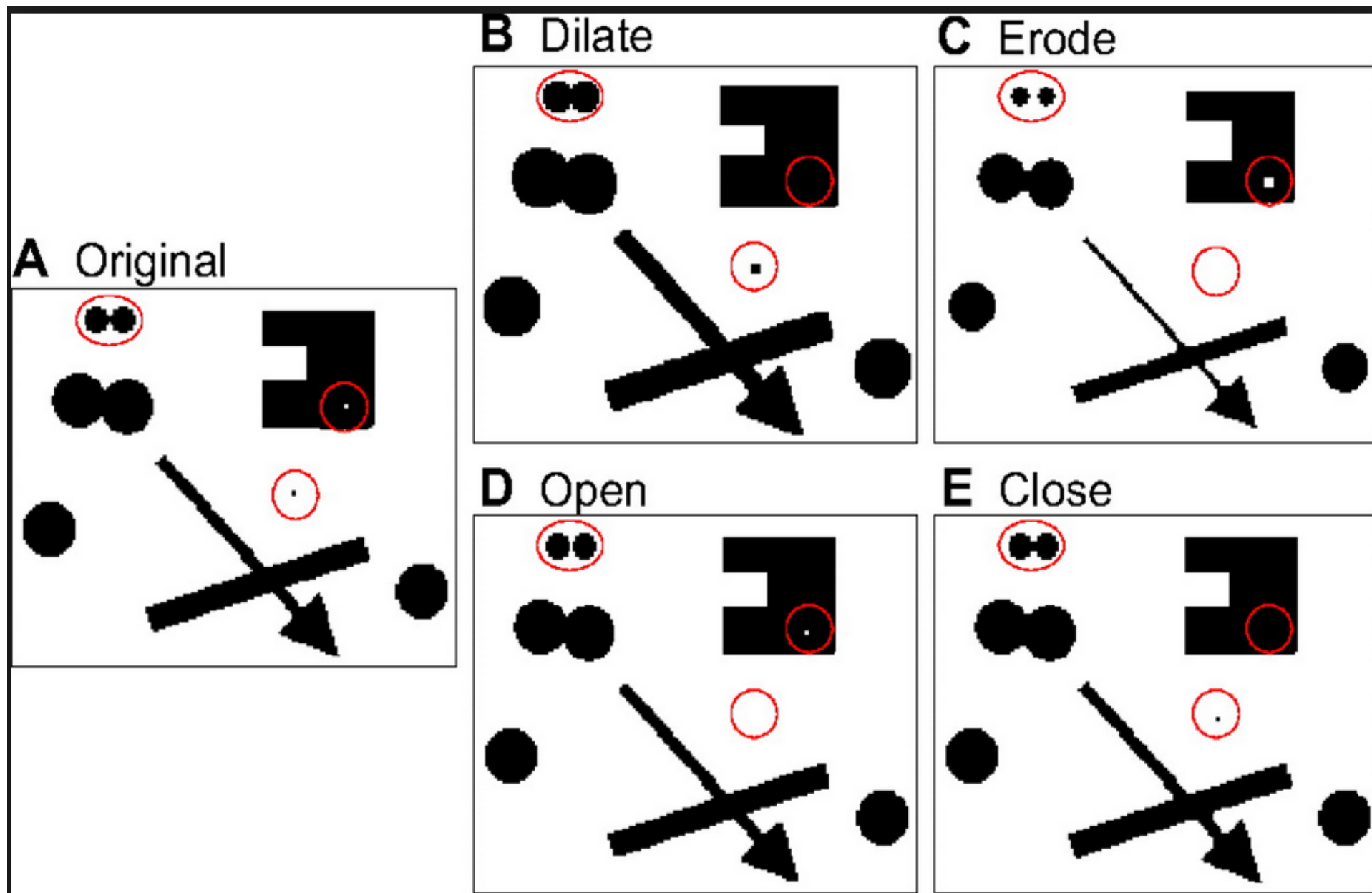


FIGURE 25-10
Morphological operations. Four basic morphological operations are used in the processing of binary images: *erosion*, *dilation*, *opening*, and *closing*. Figure (a) shows an example binary image. Figures (b) to (e) show the result of applying these operations to the image in (a).

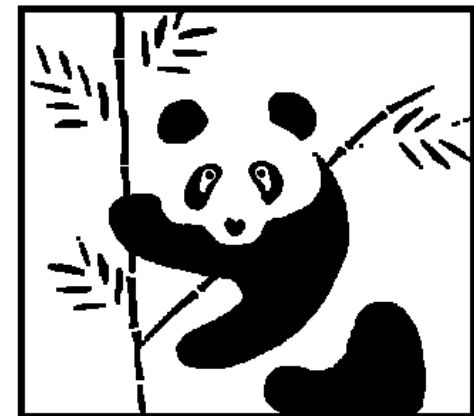
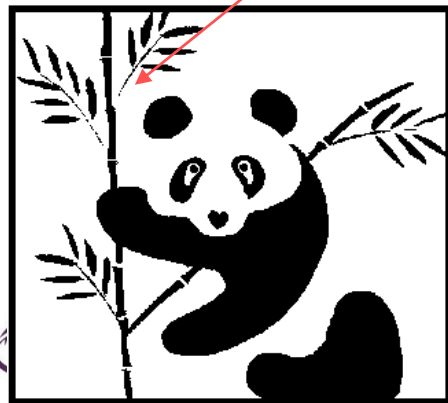
Close = Dilate next Erode
Open = Erode next Dilate





Open

- An erosion followed by a dilation
- It serves to eliminate noise
- Does not significantly change an object's size

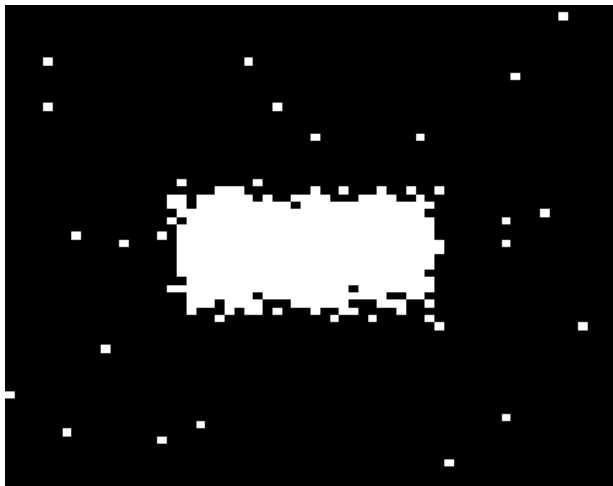


Opening Example

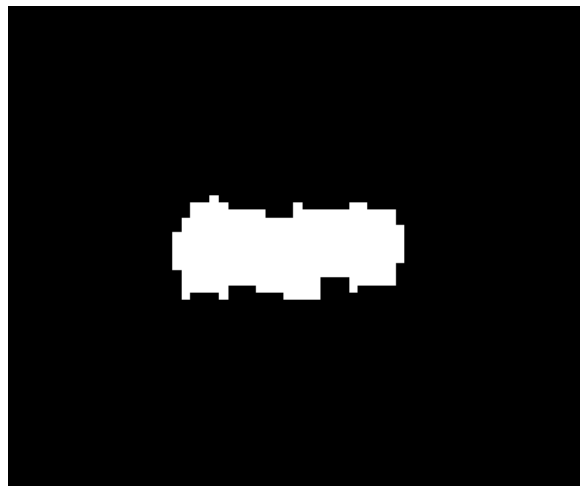
Open = Erode next Dilate

- eliminate noise (isolated pixels)
- smooth boundaries
- object is the same size as in original

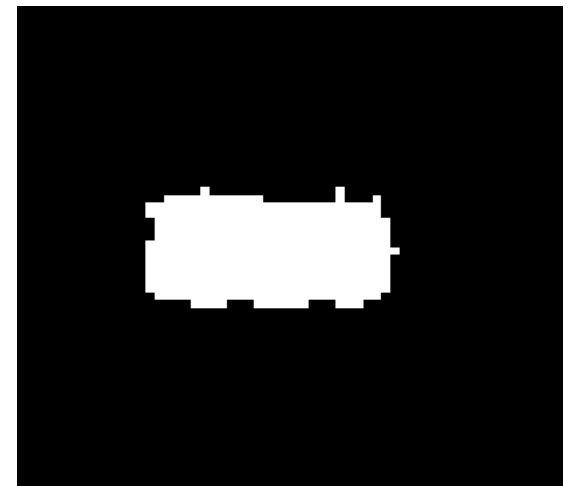
Original



Erode

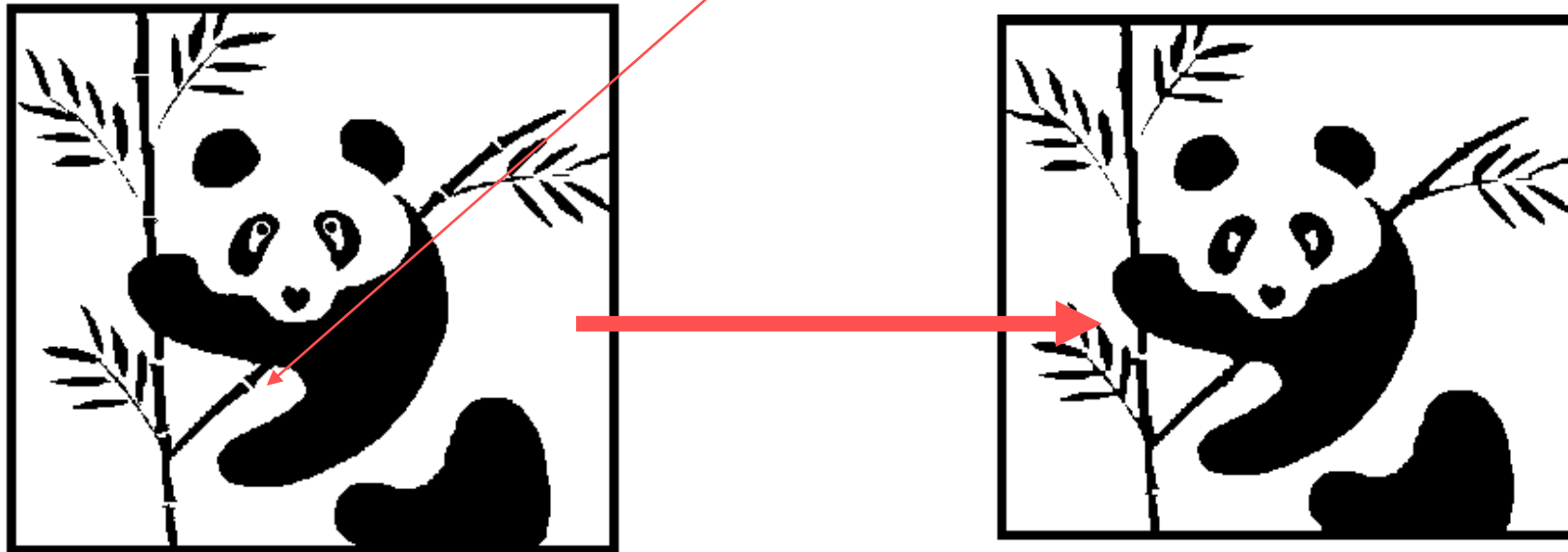


Dilate



Close

- Dilation followed by erosion
- Serves to close up **cracks in objects** and holes due to pepper noise
- Does not significantly change object size

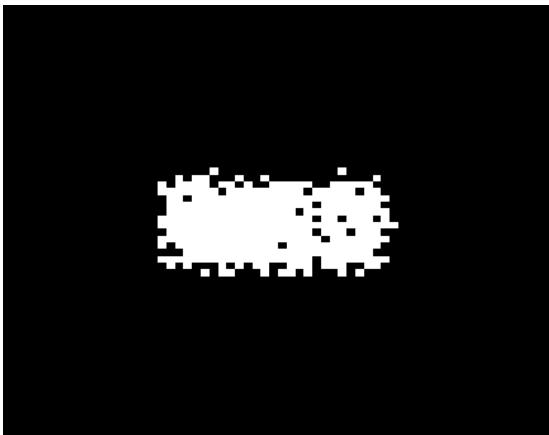


Closing Example

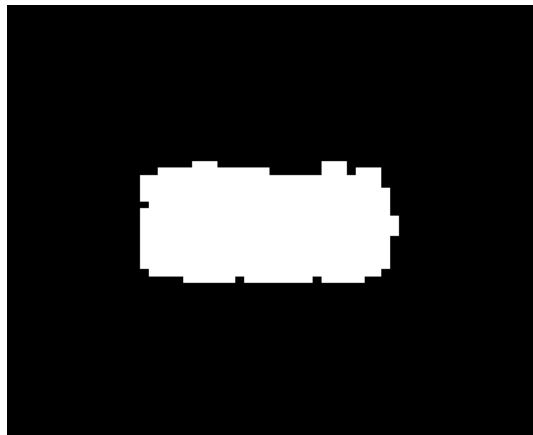
Close = Dilate next Erode

- eliminate noise (holes)
- smooth boundaries
- maintain object size

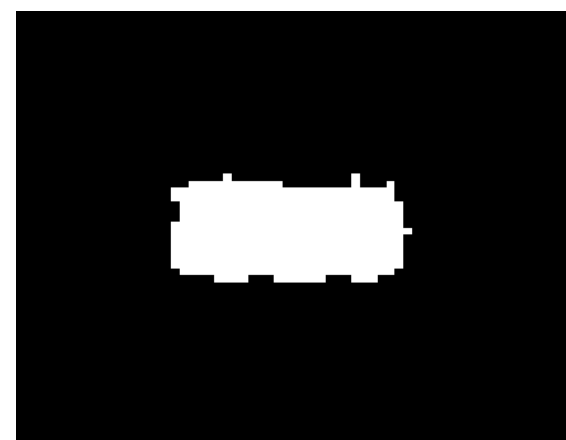
Original



Dilate



Erode

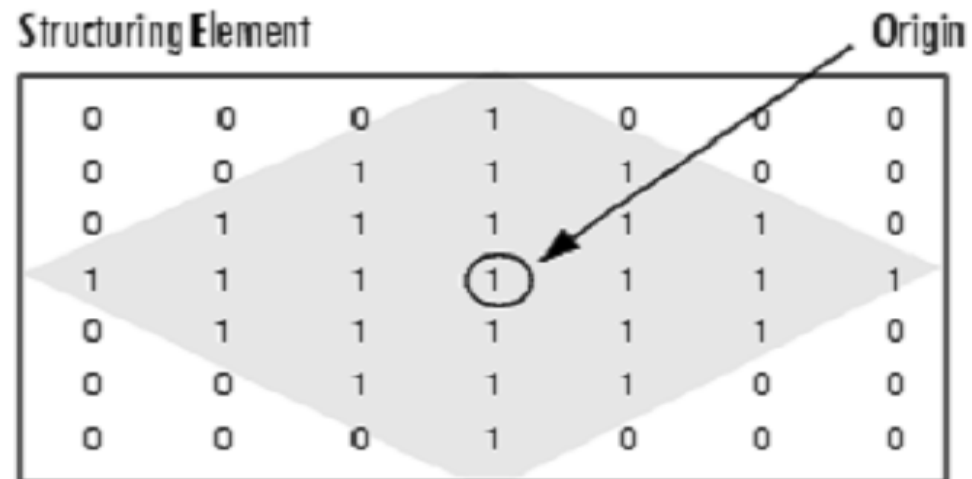


Different view → different way of understanding



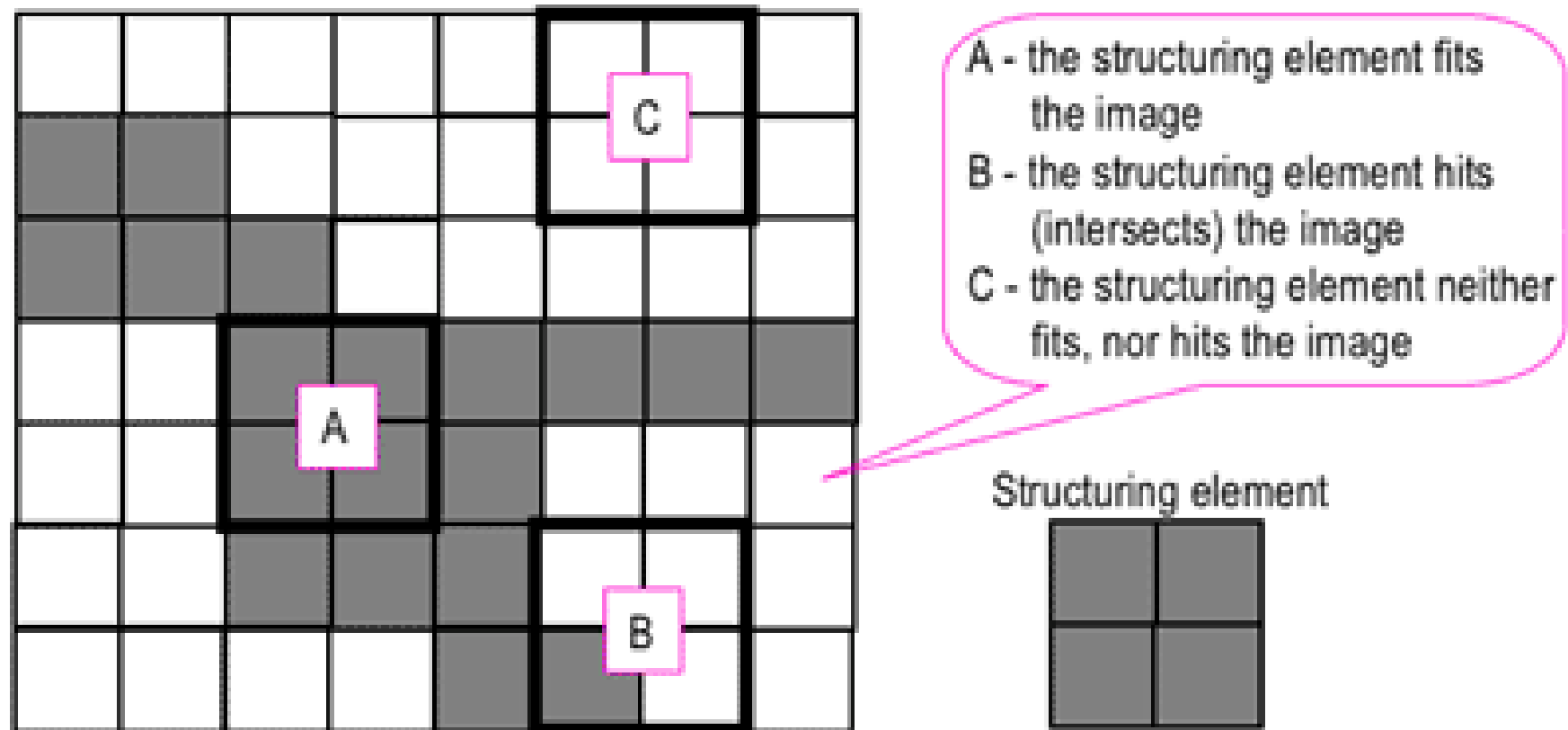
Diamond-Shaped Structuring Element

- *Origin*: the center pixel of the structuring element



Dilation and erosion operation

- **fit—hit—miss**



Probing of an image with a structuring element
(white and grey pixels have zero and non-zero values, respectively).

Dilation

- Miss → No changes
- Hit → at least one pixel matches =>The origin is replaced by 1

0	0	0	0	0	0
0	0	0	0	0	0
0	0	1	1	1	0
0	0	1	1	1	0
0	0	0	0	0	0
0	0	0	0	0	0

Input matrix

1	1	1
---	---	---

**Structuring
element**

0	0	0	0	0	0
0	0	0	0	0	0
0	1	1	1	1	1
0	1	1	1	1	1
0	0	0	0	0	0
0	0	0	0	0	0

Dilated matrix

Dilation in MATLAB

- Dilation Syntax: $Y = \text{imdilate}(A,B)$
 - $A \rightarrow$ input image
 - $B \rightarrow$ Structuring element
 - $Y \rightarrow$ Dilated image
- Structuring element in MATLAB
 - using 'strel' function:
se = strel (shape , parameters)
 - shape can be 'diamond' , 'square' , 'disk' , 'line' etc.

Erosion in MATLAB

- It **shrinks** or **thins** objects in a binary image
- Syntax **se =imerode(A,B)**
- Output is 1 when element completely fits

0	0	0	0	0	0
0	0	0	0	0	0
0	0	1	1	1	0
0	0	1	1	1	0
0	0	0	0	0	0
0	0	0	0	0	0

Input matrix

1	1	1
---	---	---

**Structuring
element**

0	0	0	0	0	0
0	0	0	0	0	0
0	0	0	1	0	0
0	0	0	1	0	0
0	0	0	0	0	0
0	0	0	0	0	0

Eroded matrix

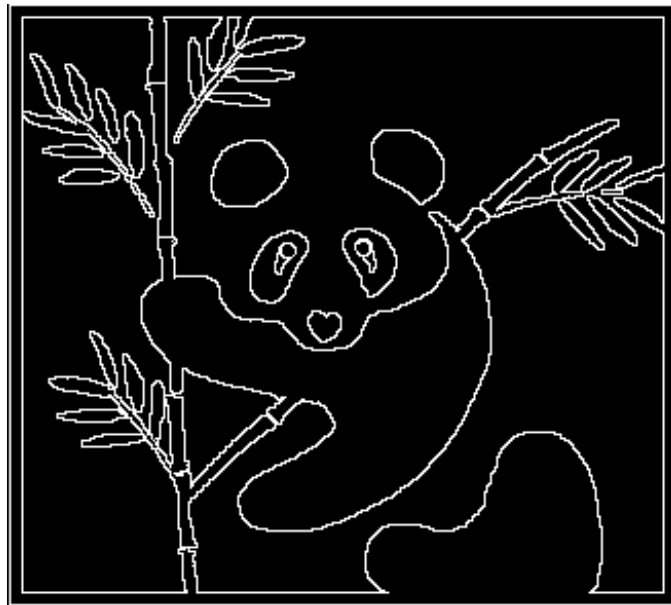
Morphological Operations: Matlab

- In Matlab → help “Morphological Operations

Bonus:

Edge detection

Dilate - original



This subtraction is set theoretical

Now you need to invert the image

There are more methods for edge detection

Binary image contour extraction

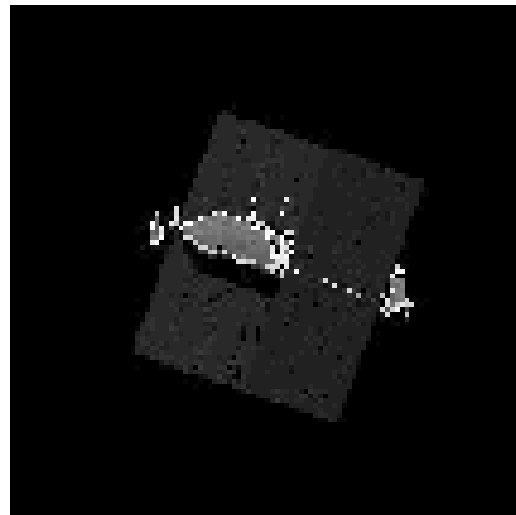
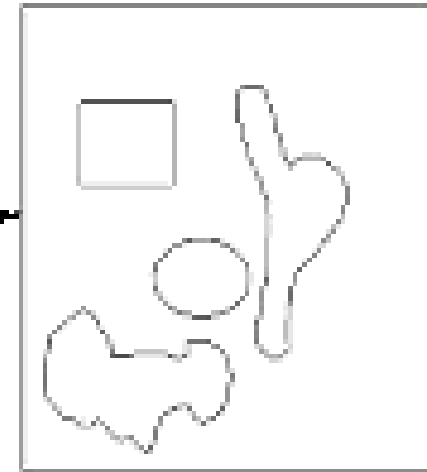
Erode and Binary Contour in Matlab

image



```
Eroded=erode(image);  
Contour=  
double(image)-double(Eroded);  
Contour=~Contour;
```

Contour

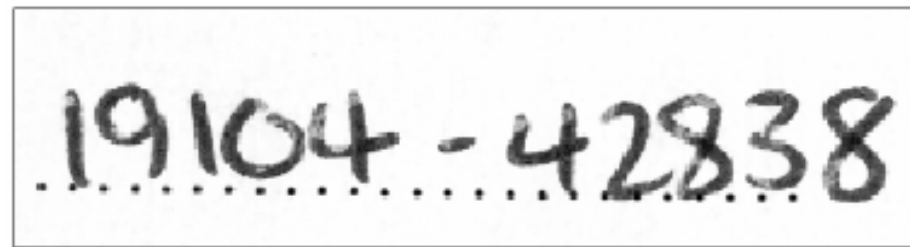


Satellite image
with contour.

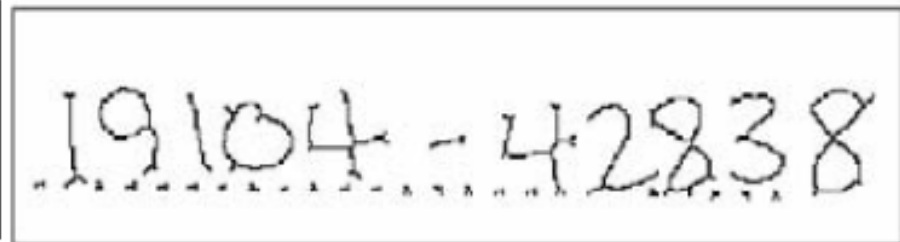
Erosion can be
used to find
contour

Dilation can be
also used for it -
think how?

Morphological Processing of Handwritten Digits

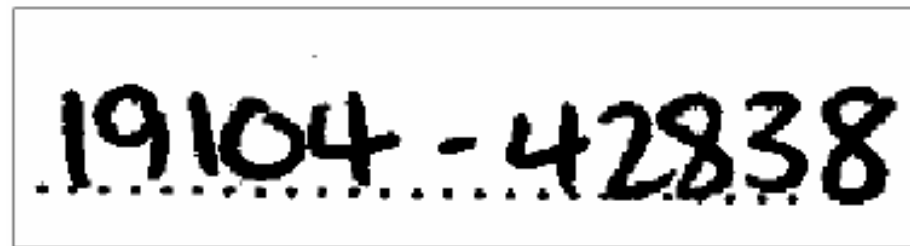


thresholding image I



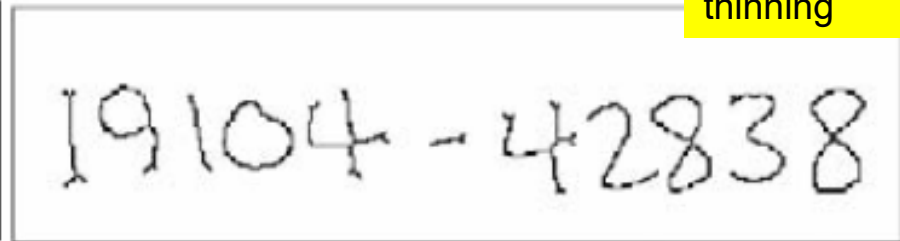
$Y \circ \{L_i\}_{i=1}^8$, repeat till convergence

thinning



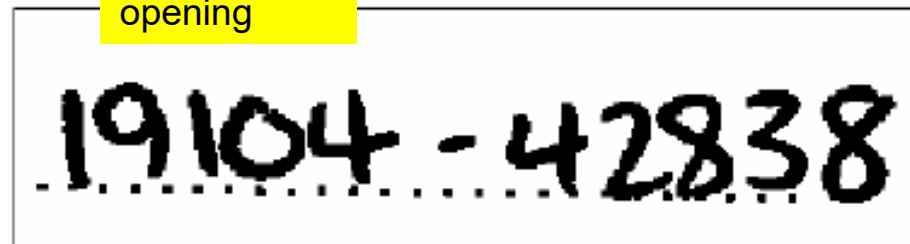
$X = (I < 245)$

opening



smoothed skeleton

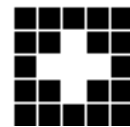
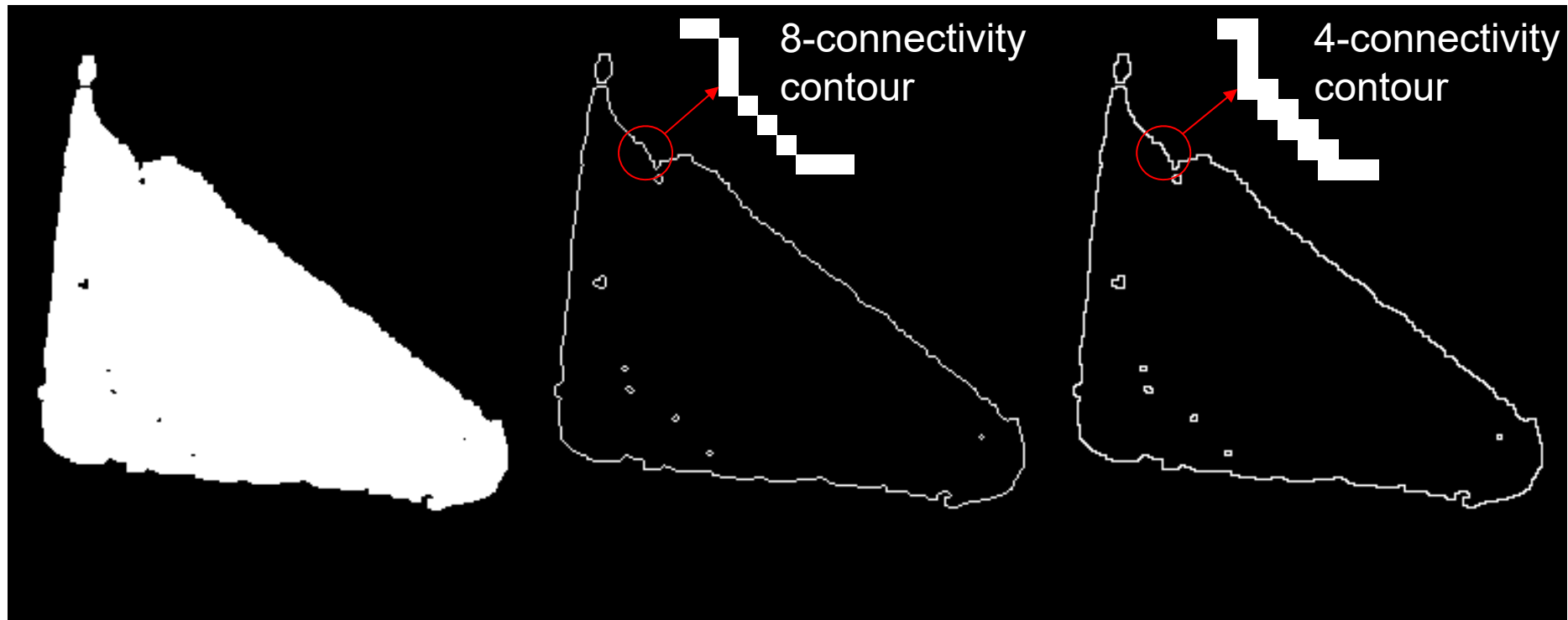
smoothing



$Y = X \circ S_{3,3}$

$$S_{3,3} = \begin{bmatrix} 0 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 0 \end{bmatrix}$$

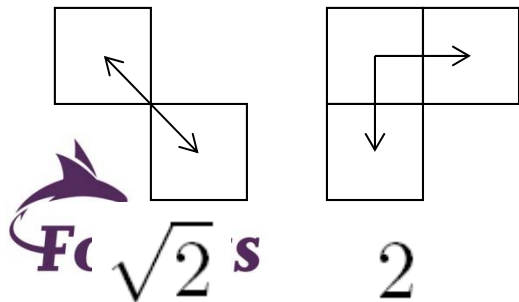
CONTOURS with different connectivity patterns



4-connectivity



8-connectivity



Important for perimeter computation.