

Reasoning about Feature Models in Higher-Order Logic

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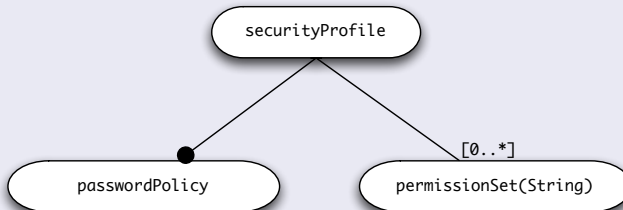


IST-15905

Feature Oriented Domain Analysis

Feature Models

- capture variability and commonality of a product line
- features represent the building blocks



Why Formalize?

Disambiguation

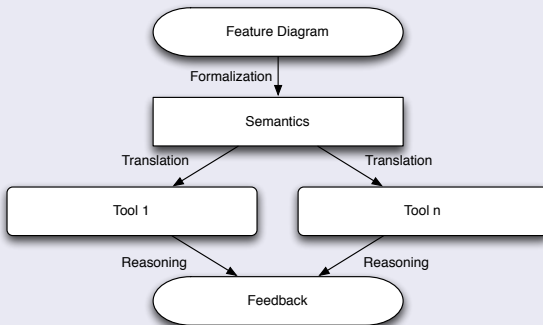
- informal explanation of the meaning might be ambiguous
- for example, absolute vs. relative meaning of *mandatory*

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Reasoning about Feature Models

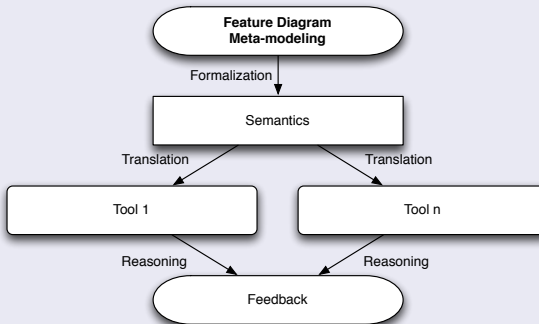


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Reasoning at the Meta Level



Mechanization of the Formalization

PVS

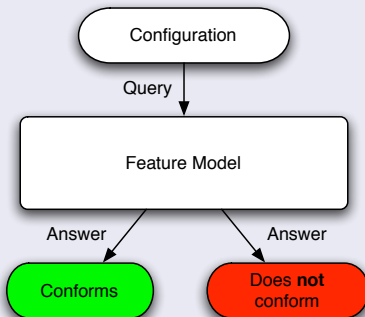
- proof assistant widely used in computer science
- typed higher-order logic language

Pros and Cons

- reason about feature-models that have infinite number of configurations (e.g., feature cloning, attributes)
- express and reason about constraints expressible in HOL
- high level of trustworthiness of the formalization as proofs are checked by a computer
- requires expertise in using a HOL proof-assistant
- some tasks might be tedious

Feature Models as Oracles

- the set of selected features and values of their attributes constitute a *configuration*
- a configuration either does or does not *conform* to the model



Features and Configurations

Features and Attributes

Feature
name : String
size : Integer

$\text{Feature} \rightarrow \mathcal{P}(\text{AttributelIdentifier})$

$\text{AttributelIdentifier} \rightarrow \text{Type}$

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Feature Configurations

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memoryRequirement : Memory

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Feature Configurations

Feature
name = "air-bag"

Feature
name = "cruise-control"

Feature
name = "crash-detection"
memoryRequirement = 100MB

- *value assignment function* assigns values to attributes

$\mathbb{A} \equiv \text{Feature} \rightarrow (\text{AttributeIdentifier} \rightarrow \text{AttributeValues})$

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- *value assignment function* assigns values to attributes
 $\mathbb{A} \equiv \text{Feature} \rightarrow (\text{AttributeIdentifier} \rightarrow \text{AttributeValues})$
- *selection function* determines the selected features
select $\equiv \text{Feature} \rightarrow \text{Boolean}$

Feature Models as Restriction Functions

Feature Models as Restriction Functions

a *restriction function* determines whether the given feature selection and attributes' values conform to the model

$$\mathbf{restr} \equiv \mathbf{select} \times \mathbb{A} \rightarrow \text{Boolean}$$

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Examples of Restriction Functions

- f_1 requires f_2 :

$$r_1(s : \mathbf{select}, a : \mathbb{A}) \equiv s(f_1) \Rightarrow s(f_2)$$

- f_2 requires f_3 with a specific version:

$$r_2(s : \mathbf{select}, a : \mathbb{A}) \equiv s(f_2) \Rightarrow (s(f_3) \wedge a(f_3)(\text{version}) = 7)$$

- restriction functions can be combined:

$$r_3(s : \mathbf{select}, a : \mathbb{A}) \equiv r_1(s, a) \wedge r_2(s, a)$$

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More Examples in PVS Notation

- a restriction function that corresponds to a requires relation:

```
require(requiree, required: FEATURE) : RESTRICTION =  
  LAMBDA (select: SELECT, da: DOMAIN_ASSIGNMENT):  
    (select(requiree) IMPLIES select(required))
```

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- combine two given restriction functions:

```
intersect(r1, r2: RESTRICTION) : RESTRICTION =  
  LAMBDA (select: SELECT, da: DOMAIN_ASSIGNMENT):  
    r1(select, da) AND r2(select, da)
```

Meta-Level Property Example

Specialization of a Feature Model via Restriction Functions

$$\begin{aligned} \text{specialization?}(restr_1, restr_2 : \mathbf{restr}) \equiv \\ \forall s : \mathbf{select}; a : \mathbb{A} \bullet restr_1(s, a) \Rightarrow restr_2(s, a) \end{aligned}$$

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Higher-Order Functions on Restriction Functions

assignment to an attribute value:

$$\begin{aligned} \text{assign-value}(r : \mathbf{restr}) \equiv \\ \lambda s : \mathbf{select}, a : \mathbb{A} \bullet r(s, a) \wedge (a(f_1)(\text{version}) = 3) \end{aligned}$$

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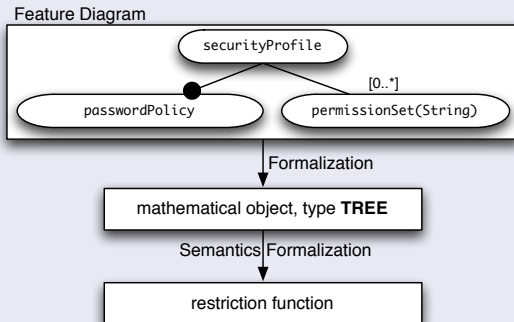
Reasoning

the function *assign-value* returns a specialization:

$$\forall r \bullet \text{specialized?}(\text{assign-value}(r), r)$$

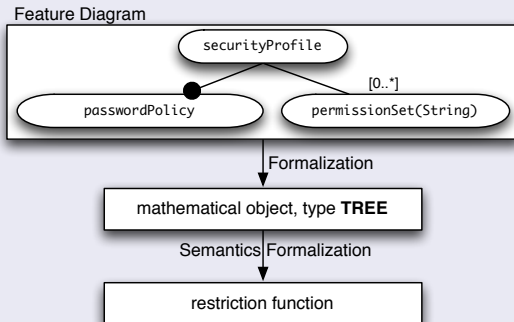
From Feature Diagrams to Restriction Functions

Schematically



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Schematically



A Function From Diagram to Restriction Function

$\text{getRestriction} : \mathbf{TREE} \rightarrow (\text{select} \times \mathbb{A} \rightarrow \text{Boolean})$

Baking Restriction Functions

Modeling Gradual Specialization of Restriction Function

- obtain a restriction function, e.g., from a feature diagram

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...

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Bringing Specializations Together

$$r_n = \text{spec}_n(\dots(\text{spec}_1(\text{getRestriction}(\text{tree})))\dots)$$

Feature Models as Oracles

- the oracle is an important characteristic of the feature model
- enables unified mathematical approach
 - meta-model level, e.g., what is specialization
 - model level, e.g., record constraints in mathematical notation
- oracles are compositional