Do SAT Solvers Make Good Configurators?

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ASPL at SPLC 2008

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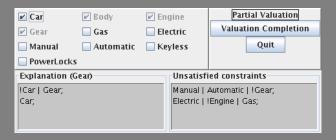
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Introduction

Configuration

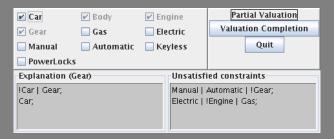
- a feature models represent the set of products we are interested in and the dependencies between them
- customer selects a product in the configuration process
- the product should fulfill the desires of the customer but must respect the constraints imposed by the feature model

∠ Car	∠ Body	✓ Eng	gine	Partial Valuation
✓ Gear	Gas	Electric		Valuation Completion
Manual	Automatic	Keyless		Quit
☐ PowerLocks				
Explanation (Gear)			Unsatisfied constraints	
!Car Gear;			Manual Automatic !Gear;	
Car;			Electric !Engine Gas;	



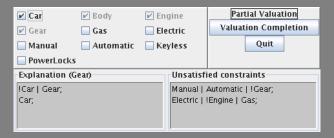
Functionality

feedback takes place as the choices are being made



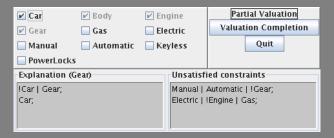
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- disabling choices that do not lead to a solution
- never let the user violate the constrains (backtrack freeness)
- explaining why a value is locked

How Do We Go About This?

Use a SAT Solver

- determines the satisfiability of a given Boolean formula
- operates on Conjunctive Normal Form (CNF)
- a certification of the response is produced
- nowadays SAT solvers are very efficient

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Assumptions

- constraints encoded in a CNF
- decisions so far encoded as a conjunction of literals

$$\phi \equiv f_1 \wedge \neg f_8 \wedge \dots$$

SAT Solver for Configuration

Testing all free features after each user's decision

```
Test-Vars()
    foreach x that was not assigned to by the user
          do CanBeTrue \leftarrow TEST-SAT(\phi, x)
 3
              CanBeFalse \leftarrow TEST-SAT(\phi, \neg x)
 4
             if \neg CanBeTrue \land \neg CanBeFalse
                then error "Unsatisfiable constraint!"
             if \neg CanBeTrue then Set(x, False)
 6
             if \neg CanBeFalse then Set(x, True)
             if CanBeTrue ∧ CanBeFalse
 8
                then Reset(x)
 9
                      Unlock(x)
10
                else Lock(x)
```

Can We Improve This?

SAT

- For satisfiable queries, the SAT solver returns with a satisfying assignment.
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UNSAT

- Can a negative response of the solver help in the future?
- Example

$$\begin{vmatrix}
f_1 => f_2 \\
\neg f_2 \\
\dots
\end{vmatrix} \neg f_1$$

Recording disabled values may help with further queries.

Satisfiability with Caching

- KnownValues represent values known to be SAT
- DisabledValues represent values known to be UNSAT

```
TEST-SAT(\phi: Formula, l: Literal) : Boolean

1 if l \in KnownValues then return TRUE

2 if l \in DisabledValues then return FALSE

3 L \leftarrow SAT(\phi \land l \land \bigwedge_{k \in DisabledValues} \neg k)

4 if L \neq null

5 then KnownValues \leftarrow KnownValues \cup L

6 else DisabledValues \leftarrow DisabledValues \cup \{l\}

7 return L \neq null
```

Explanations

- The solver produces a unsatisfiable subset of given formulas.
- This may not be minimal, several techniques how to minimize.
- In the tool an iterative technique by Zhang and Malik.

Discussion and Future Work

Comparing to Binary Decision Diagrams (BDDs)

- It is expected to be slower than *but* much less likely to choke.
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- Requires CNF however any formula can be clausified in polynomial size.

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- Use proofs for more efficient cache discarding.
- Could this approach work for non-Boolean domains?

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A java implementation, including a SAT solver, available at

kind.ucd.ie

When to Discard Caches?

- With a new decision asserted, *KnownValues* may change and thus get discarded whereas *DisabledValues* remain the same.
- When a decision is retracted, *KnownValues* remain whereas *DisabledValues* are discarded.