

# Interval Temporal Logic

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[HTML version of the ITL home page](#)  
[ITL-course: A not so short introduction to ITL](#)

## Abstract

Interval Temporal Logic (ITL) is a flexible notation for both propositional and first-order reasoning about periods of time found in descriptions of hardware and software systems. Unlike most temporal logics, ITL can handle both sequential and parallel composition and offers powerful and extensible specification and proof techniques for reasoning about properties involving safety, liveness and projected time[15]. Timing constraints are expressible and furthermore most imperative programming constructs can be viewed as formulas in a slightly modified version of ITL [25]. Tempura provides an executable framework for developing and experimenting with suitable ITL specifications. In addition, ITL and its mature executable subset Tempura [9] have been extensively used to specify the properties of real-time systems where the primitive circuits can directly be represented by a set of simple temporal formulae. In addition, various researchers have applied Tempura to hardware simulation and other areas where timing is important.

## 1 Syntax

The key notion of ITL is an *interval*. An interval  $\sigma$  is considered to be a (in)finite sequence of states  $\sigma_0, \sigma_1 \dots$ , where a state  $\sigma_i$  is a mapping from the set of variables  $\text{Var}$  to the set of values  $\text{Val}$ . The length  $|\sigma|$  of an interval  $\sigma_0 \dots \sigma_n$  is equal to  $n$  (one less than the number of states in the interval (this has always been a convention in ITL), i.e., a one state interval has length 0).

The syntax of ITL is defined in Table 1 where

$z$  is an integer value,  
 $a$  is a static integer variable (doesn't change within an interval),  
 $A$  is a state integer variable (can change within an interval),  
 $v$  a static or state integer variable,  
 $g$  is a integer function symbol,

Table 1: Syntax of ITL

<i>Expressions</i>	
$e ::=$	$z \mid a \mid A \mid g(e_1, \dots, e_n) \mid \bigcirc A \mid \text{fin } A$
<i>Formulae</i>	
$f ::=$	$\text{true} \mid q \mid Q \mid h(e_1, \dots, e_n) \mid \neg f \mid f_1 \wedge f_2 \mid \forall \mathbf{v} \cdot f \mid$ $\text{skip} \mid f_1 ; f_2 \mid f^*$

$q$  is a static Boolean variable (doesn't change within an interval),  
 $Q$  is a state Boolean variable (can change within an interval),  
 $h$  is a predicate symbol.

## 2 Semantics

The informal semantics of the most interesting constructs are as follows:

- $\bigcirc A$ : if interval is non-empty then the value of  $A$  in the next state of that interval else an arbitrary value.
- $\text{fin } A$ : if interval is finite then the value of  $A$  in the last state of that interval else an arbitrary value.
- $\text{skip}$  unit interval (length 1).
- $f_1 ; f_2$  holds if the interval can be decomposed (“chopped”) into a prefix and suffix interval, such that  $f_1$  holds over the prefix and  $f_2$  over the suffix, or if the interval is infinite and  $f_1$  holds for that interval.
- $f^*$  holds if the interval is decomposable into a finite number of intervals such that for each of them  $f$  holds, or the interval is infinite and can be decomposed into an infinite number of finite intervals for which  $f$  holds.

Let  $\llbracket \dots \rrbracket^e$  be the “meaning” (semantic) function from  $Expressions \times (\Sigma^+ \cup \Sigma^\omega)$  to  $Val$  and let  $\llbracket \dots \rrbracket$  be the “meaning” function from  $Formulae \times (\Sigma^+ \cup \Sigma^\omega)$  to  $Bool$  (set of Boolean values,  $\{\text{tt}, \text{ff}\}$ ) and let  $\sigma = \sigma_0 \sigma_1 \dots$  be an interval. We write  $\sigma \sim_v \sigma'$  if the intervals  $\sigma$  and  $\sigma'$  are identical with the possible exception of their mappings for the variable  $v$ . The formal semantics is listed in Table 2:

## 3 Derived Constructs

Frequently used derived constructs are listed in table 3–6.

Table 2: Semantics of ITL

$\llbracket z \rrbracket_\sigma^e$	=	$\hat{z}$
$\llbracket a \rrbracket_\sigma^e$	=	$\sigma_0(a)$ and for all $0 < i \leq  \sigma $ , $\sigma_i(a) = \sigma_0(a)$
$\llbracket A \rrbracket_\sigma^e$	=	$\sigma_0(A)$
$\llbracket g(e_1, \dots, e_n) \rrbracket_\sigma^e$	=	$\hat{g}(\llbracket e_1 \rrbracket_\sigma^e, \dots, \llbracket e_n \rrbracket_\sigma^e)$
$\llbracket \bigcirc A \rrbracket_\sigma^e$	=	$\begin{cases} \sigma_1(A) & \text{if }  \sigma  > 0 \\ \text{choose-any-from}(Val) & \text{otherwise} \end{cases}$
$\llbracket \text{fin } A \rrbracket_\sigma^e$	=	$\begin{cases} \sigma_{ \sigma }(A) & \text{if } \sigma \text{ is finite} \\ \text{choose-any-from}(Val) & \text{otherwise} \end{cases}$
$\llbracket \text{true} \rrbracket_\sigma$	=	tt
$\llbracket q \rrbracket_\sigma$	=	$\sigma_0(q)$ and for all $0 < i \leq  \sigma $ , $\sigma_i(q) = \sigma_0(q)$
$\llbracket Q \rrbracket_\sigma$	=	$\sigma_0(Q)$
$\llbracket h(e_1, \dots, e_n) \rrbracket_\sigma = \text{tt}$	iff	$\hat{h}(\llbracket e_1 \rrbracket_\sigma^e, \dots, \llbracket e_n \rrbracket_\sigma^e)$
$\llbracket \neg f \rrbracket_\sigma = \text{tt}$	iff	not $(\llbracket f \rrbracket_\sigma = \text{tt})$
$\llbracket f_1 \wedge f_2 \rrbracket_\sigma = \text{tt}$	iff	$(\llbracket f_1 \rrbracket_\sigma = \text{tt})$ and $(\llbracket f_2 \rrbracket_\sigma = \text{tt})$
$\llbracket \text{skip} \rrbracket_\sigma = \text{tt}$	iff	$ \sigma  = 1$
$\llbracket \forall v \cdot f \rrbracket_\sigma = \text{tt}$	iff	(for all $\sigma'$ s.t. $\sigma \sim_v \sigma'$ , $\llbracket f \rrbracket_{\sigma'} = \text{tt}$ )
$\llbracket f_1 ; f_2 \rrbracket_\sigma = \text{tt}$	iff	(exists $k$ , s.t. $\llbracket f_1 \rrbracket_{\sigma_0 \dots \sigma_k} = \text{tt}$ and $\llbracket f_2 \rrbracket_{\sigma_k \dots \sigma_{ \sigma }} = \text{tt}$ ) or ( $\sigma$ is infinite and $\llbracket f_1 \rrbracket_\sigma = \text{tt}$ )
$\llbracket f^* \rrbracket_\sigma = \text{tt}$	iff	
if $\sigma$ is finite then		
(exist $l_0, \dots, l_n$ s.t. $l_0 = 0$ and $l_n =  \sigma $ and for all $0 \leq i < n$ , $l_i \leq l_{i+1}$ and $\llbracket f \rrbracket_{\sigma_{l_i} \dots \sigma_{l_{i+1}}} = \text{tt}$ )		
else		
(exist $l_0, \dots, l_n$ s.t. $l_0 = 0$ and $\llbracket f \rrbracket_{\sigma_{l_n} \dots \sigma_{ \sigma }} = \text{tt}$ and for all $0 \leq i < n$ , $l_i \leq l_{i+1}$ and $\llbracket f \rrbracket_{\sigma_{l_i} \dots \sigma_{l_{i+1}}} = \text{tt}$ )		
or		
(exist an infinite number of $l_i$ s.t. $l_0 = 0$ and for all $0 \leq i$ , $l_i \leq l_{i+1}$ and $\llbracket f \rrbracket_{\sigma_{l_i} \dots \sigma_{l_{i+1}}} = \text{tt}$ )		

Table 3: Frequently used non-temporal derived constructs

$\text{false}$	$\hat{=}$	$\neg \text{true}$	false value
$f_1 \vee f_2$	$\hat{=}$	$\neg(\neg f_1 \wedge \neg f_2)$	or
$f_1 \supset f_2$	$\hat{=}$	$\neg f_1 \vee f_2$	implies
$f_1 \equiv f_2$	$\hat{=}$	$(f_1 \supset f_2) \wedge (f_2 \supset f_1)$	equivalent
$\exists v \cdot f$	$\hat{=}$	$\neg \forall v \cdot \neg f$	exists

Table 4: Frequently used temporal derived constructs

$\bigcirc f$	$\hat{=}$	$\text{skip} ; f$	next
$\text{more}$	$\hat{=}$	$\bigcirc \text{true}$	non-empty interval
$\text{empty}$	$\hat{=}$	$\neg \text{more}$	empty interval
$\text{inf}$	$\hat{=}$	$\text{true} ; \text{false}$	infinite interval
$\text{isinf}(f)$	$\hat{=}$	$\text{inf} \wedge f$	is infinite
$\text{finite}$	$\hat{=}$	$\neg \text{inf}$	finite interval
$\text{isfin}(f)$	$\hat{=}$	$\text{finite} \wedge f$	is finite
$\text{fmore}$	$\hat{=}$	$\text{more} \wedge \text{finite}$	non-empty finite interval
$\Diamond f$	$\hat{=}$	$\text{finite} ; f$	sometimes
$\Box f$	$\hat{=}$	$\neg \Diamond \neg f$	always
$\textcircled{w} f$	$\hat{=}$	$\neg \bigcirc \neg f$	weak next
$\Diamond_I f$	$\hat{=}$	$f ; \text{true}$	some initial subinterval
$\Box_I f$	$\hat{=}$	$\neg(\Diamond_I \neg f)$	all initial subintervals
$\Diamond_S f$	$\hat{=}$	$\text{finite} ; f ; \text{true}$	some subinterval
$\Box_S f$	$\hat{=}$	$\neg(\Diamond_S \neg f)$	all subintervals

## 4 Propositional proof system

In table 7 we list the propositional axioms and rules for ITL.

## 5 First order proof system

Some axioms for the first order case are shown in Table 8.

Let  $v$  refer to both static and state variables.

We denote by  $f_v^e$  that in formula  $f$  expression  $e$  is substituted for variable  $v$ .

Table 5: Frequently used concrete derived constructs

$\text{if } f_0 \text{ then } f_1 \text{ else } f_2$	$\hat{=}$	$(f_0 \wedge f_1) \vee (\neg f_0 \wedge f_2)$	if then else
$\text{if } f_0 \text{ then } f_1$	$\hat{=}$	$\text{if } f_0 \text{ then } f_1 \text{ else empty}$	if then
$\text{fin } f$	$\hat{=}$	$\Box(\text{empty} \supset f)$	final state
$\text{sfin } f$	$\hat{=}$	$\neg(\text{fin } (\neg f))$	strong final state
$\text{halt } f$	$\hat{=}$	$\Box(\text{empty} \equiv f)$	terminate interval when
$\text{shalt } f$	$\hat{=}$	$\neg(\text{halt } (\neg f))$	strong terminate interval when
$\text{keep } f$	$\hat{=}$	$\Box(\text{skip} \supset f)$	all unit subintervals
$\text{keepnow } f$	$\hat{=}$	$\Diamond(\text{skip} \wedge f)$	initial unit subinterval
$f^\omega$	$\hat{=}$	$\text{isinf}(\text{isfin}(f)^*)$	infinite chopstar
$fstar(f)$	$\hat{=}$	$\text{isfin}(\text{isfin}(f)^*) \vee$ $\text{isinf}(\text{isfin}(f)^*) ; \text{isinf}(f)$	finite chopstar
$\text{while } f_0 \text{ do } f_1$	$\hat{=}$	$(f_0 \wedge f_1)^* \wedge \text{fin } \neg f_0$	while loop
$\text{repeat } f_0 \text{ until } f_1$	$\hat{=}$	$f_0 ; (\text{while } \neg f_1 \text{ do } f_0)$	repeat loop

Table 6: Frequently used derived constructs related to expressions

$A := exp$	$\hat{=}$	$\bigcirc A = exp$	assignment
$A \approx exp$	$\hat{=}$	$\Box(A = exp)$	equal in interval
$A \leftarrow exp$	$\hat{=}$	$\text{finite} \wedge (\text{fin } A) = exp$	temporal assignment
$A \text{ gets } exp$	$\hat{=}$	$\text{keep}(A \leftarrow exp)$	gets
$\text{stable } A$	$\hat{=}$	$A \text{ gets } A$	stability
$\text{padded } A$	$\hat{=}$	$(\text{stable}(A) ; \text{skip}) \vee \text{empty}$	padded expression
$A \llsim exp$	$\hat{=}$	$(A \leftarrow exp) \wedge \text{padded } A$	padded temporal assignment
$\text{goodindex } A$	$\hat{=}$	$\text{keep}(A \leftarrow A \vee A \leftarrow A + 1)$	increasing index
$\text{intlen}(exp)$	$\hat{=}$	$\exists I \bullet (I = 0) \wedge (I \text{ gets } I + 1) \wedge (I \leftarrow exp)$	interval length

Table 7: Propositional Axioms and Rules for ITL.

ChopAssoc	$\vdash (f_0; f_1); f_2 \equiv f_0; (f_1; f_2)$
OrChopImp	$\vdash (f_0 \vee f_1); f_2 \supset (f_0; f_2) \vee (f_1; f_2)$
ChopOrImp	$\vdash f_0; (f_1 \vee f_2) \supset (f_0; f_1) \vee (f_0; f_2)$
EmptyChop	$\vdash \text{empty}; f_1 \equiv f_1$
ChopEmpty	$\vdash f_1; \text{empty} \equiv f_1$
BiBoxChopImpChop	$\vdash \Box(f_0 \supset f_1) \wedge \Box(f_2 \supset f_3) \supset (f_0; f_2) \supset (f_1; f_3)$
StateImpBi	$\vdash p \supset \Box p$
NextImpNotNextNot	$\vdash \bigcirc f_0 \supset \neg \bigcirc \neg f_0$
KeepnowImpNotKeepnowNot	$\vdash \text{keepnow}(f_0) \supset \neg \text{keepnow}(\neg f_0)$
BoxInduct	$\vdash f_0 \wedge \Box(f_0 \supset \textcircled{w} f_0) \supset \Box f_0$
InfChop	$\vdash (f_0 \wedge \text{inf}); f_1 \equiv (f_0 \wedge \text{inf})$
ChopStarEqv	$\vdash f_0^* \equiv (\text{empty} \vee ((f_0 \wedge \text{more}); f_0^*))$
ChopstarInduct	$\vdash (\text{inf} \wedge f_0 \wedge \Box(f_0 \supset (f_1 \wedge \text{fmore}); f_0)) \supset f_1^*$
MP	$\vdash f_0 \supset f_1, \vdash f_0 \Rightarrow \vdash f_1$
BoxGen	$\vdash f_0 \Rightarrow \vdash \Box f_0$
BiGen	$\vdash f_0 \Rightarrow \vdash \Box f_0$

Table 8: Some First Order Axioms and Rules for ITL.

ForallSub	$\vdash \forall \mathbf{v} \cdot f \supset f_v^e$ , where the expression $e$ has the same data and temporal type as the variable $v$ and is free for $v$ in $f$ .
ForallImplies	$\vdash \forall \mathbf{v} \cdot (f_1 \supset f_2) \supset (f_1 \supset \forall \mathbf{v} \cdot f_2)$ , where $v$ doesn't occur freely in $f_1$ .
SubstAxiom	$\vdash \Box(A = B) \supset f \equiv f_A^B$ .
StaticWeakNext	$\vdash w \supset \textcircled{w} w$ , where $w$ only contains static variables.
ExistsChopRight	$\vdash \exists \mathbf{v} \cdot (f_1; f_2) \supset (\exists \mathbf{v} \cdot f_1); f_2$ , where $v$ doesn't occur freely in $f_2$ .
ExistsChopLeft	$\vdash \exists \mathbf{v} \cdot (f_1; f_2) \supset f_1; (\exists \mathbf{v} \cdot f_2)$ , where $v$ doesn't occur freely in $f_1$ .
ForallGen	$\vdash f \Rightarrow \vdash \forall \mathbf{v} \cdot f$ , for any variable $v$ .

## 6 Tools

### 6.1 (Ana)Tempura

Tempura, the C-Tempura interpreter version 2.7 developed originally by Roger Hale and now maintained by Antonio Cau and Ben Moszkowski, is an interpreter for executable Interval Temporal Logic formulae. The first Tempura interpreter was programmed in Prolog by Ben Moszkowski, and was operational around December 2, 1983. Subsequently he rewrote the interpreter in Lisp (mid Mar, 1984), and in late 1984 modified the program to handle a two-level memory and multi-pass scanning. The C-Tempura interpreter was written in early 1985 by Roger Hale at Cambridge University.

AnaTempura, which is built upon C-Tempura, is a tool for the runtime verification of systems using Interval Temporal Logic (ITL) and its executable subset Tempura. The runtime verification technique uses assertion points to check whether a system satisfies timing, safety or security properties expressed in ITL. The assertion points are inserted in the source code of the system and will generate a sequence of information (system states), like values of variables and timestamps of value change, while the system is running. Since an ITL property corresponds to a set of sequences of states (intervals), runtime verification is just checking whether the sequence generated by the system is a member of the set of sequences corresponding to the property we want to check. The Tempura interpreter is used to do this membership test.

#### Download Stable Version:

- Version 2.16 (released 08/12/2009): [gzipped tar file](#) or [zip file](#).
  - added floats. Floats have the form `$2.3e+10$` in Tempura. For output: `output($2.3$)` will be `$2.30000e+00$`, i.e., precision is 5 digits after the `'.'`. One can set this via the precision variable. With precision of 2 one gets `$2.30e+00$`. The format command can output floats in two forms: `%f` output will be of the form `2.33333`, `e` output will be of the form `2.33333e+01`. The following operations on floats are defined: unary, `+`, `-`; binary: `+`, `-`, `div`, `mod`, `/`, `*`, `**`, `ceil`, `floor`, `sqrt`, `itof`, `exp`, `log`, `log10`, `sin`, `cos`, `tan`, `asin`, `acos`, `atan`, `atan2`, `sinh`, `cosh`, `tanh`, `fabs`.
  - `anatemura` is now using the new Tile interface
  - when setting system variables with `set`, output both old and new values
  - Added `'frandom'` and `'fRandom'` for float random number between `[0.0,1.0)`
  - Added `defaults` command, `X defaults 1` denotes when `X` is undefined then take as value for `X` the value 1.
  - Added `prev(X)` operator, the value of `X` in the previous state.

- Added mem(X) operator, X is a 'memory' variable, i.e., when undefined take the value in the previous state.
- Added #n history operator, used as option to exists when declaring a variable, it will keep a history of n previous values of a variable.
- Added nprev(X,n) operator, nprev(X,3) for instance is an abbreviation of prev(prev(prev(X))).
- When setting debug\_level to 6 more usefull information is displayed like the state of a variable and reduction rule being applied.
- Included tempura executables tempura\_linux for Linux (compiled on Ubuntu 9.10), tempura\_solaris for Solaris (compiled on Sparc Solaris 10u8), and tempura.exe for Windows (compiled on Windows XP SP3).
- Included anatempura executables anatempura\_solaris, anatempura\_linux and anatempura.exe. These were built using the Tclkit Kitgen build system (<http://wiki.tcl.tk/18146>). Now no need anymore to install tcl/tk and expect in order to run anatempura.
- changed copyright license to GPLv3.0

- Version 2.15 (released 14/08/2008): [gzipped tar file](#) or [zip file](#).

\*\*\*\*\*2.15\*\*\*\*\*

- introduced various node accessor macros so that if one changes the node structure we only have to change the macro.
- if formula can't be reduced in the final state of the prefix of a chop then we will evaluate ((prefix and empty);true) and (suffix). This feature can be switched on/off with hopchop. The default of hopchop is true.
- added integer overflow tests.
- unified/cleaned up the various node data structures.

- Version 2.14 (released 29/11/2007): [gzipped tar file](#) or [zip file](#).

\*\*\*\*\*2.14\*\*\*\*\*

- work around a recent misfeature of windows when started an external program.
- added the io redirections, set infile="some file name", set outfile="some file name", where stdin and stdout can be used to redirect to standard keyboard and screen i/o.
- added the infinite and randlen constructs for respectively an infinite interval and a random length interval (less or equal to max\_randlen).

- Version 2.13 (released 28/08/2007): [gzipped tar file](#) or [zip file](#).

\*\*\*\*\*2.13\*\*\*\*\*



- added reset in file menu to restart tempura.
  - open and reload now also load the file into Tempura.
  - added showstate Tempura command. This will display what is (un)defined in the current state.
  - changed contact email address to tempura@dmu.ac.uk
- Version 2.12 (released 04/05/2007): [gzipped tar file](#) or [zip file](#).

```
*****2.12*****
This version is the first version that compiles both under
Windows and Unix/Linux type of machines. See Changelog for detailed
news/changes.
```

To run the graphical interface you can either

- use the pre-compiled binary:
  - anatempura\_linux (Ubuntu 9.10)
  - anatempura\_solaris (Solaris 10u8)
  - anatempura.exe (Windows XP)
- or use anatempura.tcl:
 

you need to compile tempura, install Tcl/Tk (at least 8.5) and Expect. You can get Tcl/Tk from [Tcl/Tk site](#) and you can get Expect from the [Expect homepage](#). A convenient way of installing these is using the [ActiveTcl](#) package which includes both. ActiveTcl is the complete, ready-to-install Tcl/Tk distribution for Windows, Mac OS X, Linux, Solaris, AIX and HP-UX. Newer versions of the ActiveTcl do not have the Expect package installed. But you can get Expect with the teacup command:

(For Windows you have to do this in a DOS shell.)  
 Type the following command:  
 teacup install Expect

Tempura can be compiled using the Gnu C compiler under a Unix like operating system like Sunos 4.1.3, Solaris 2.5.1 (and higher), Linux etc. For Windows you need to install the [MinGW](#) (Minimalist GNU for Windows). For convenience the pre-compiled binary for Windows (Windows XP) tempura.exe, for Solaris (Solaris 10u8) tempura\_solaris and for Linux (Ubuntu 9.10) are included.

**Contact:** Email [tempura@dmu.ac.uk](mailto:tempura@dmu.ac.uk) in case of problems.

## Publications:

- Analysing C programs is discussed in:  
[A Framework For Analysing The Effect of ‘Change’ In Legacy Code](#), S. Zhou, H. Zedan and A. Cau. In IEEE Proc. of ICSM’99, 1999.
- Analysing Verilog programs is discussed in:  
[A logic-based Approach for Hardware/Software Co-design](#), H. Zedan and A. Cau. Digest of IEE event Hardware-Software Co-design, 8 Dec., 2000.
- A paper describing the run-time verification method used in AnaTempura:  
[Run-time analysis of time-critical systems](#). S. Zhou and H. Zedan and A. Cau. Journal of System Architecture, 51(5):331-345, 2005.
- Slides of seminar talk about AnaTempura:  
[AnaTempura](#), A. Cau, S. Zhou and H. Zedan.

**Overview:** Figure 1 shows an overview of AnaTempura.

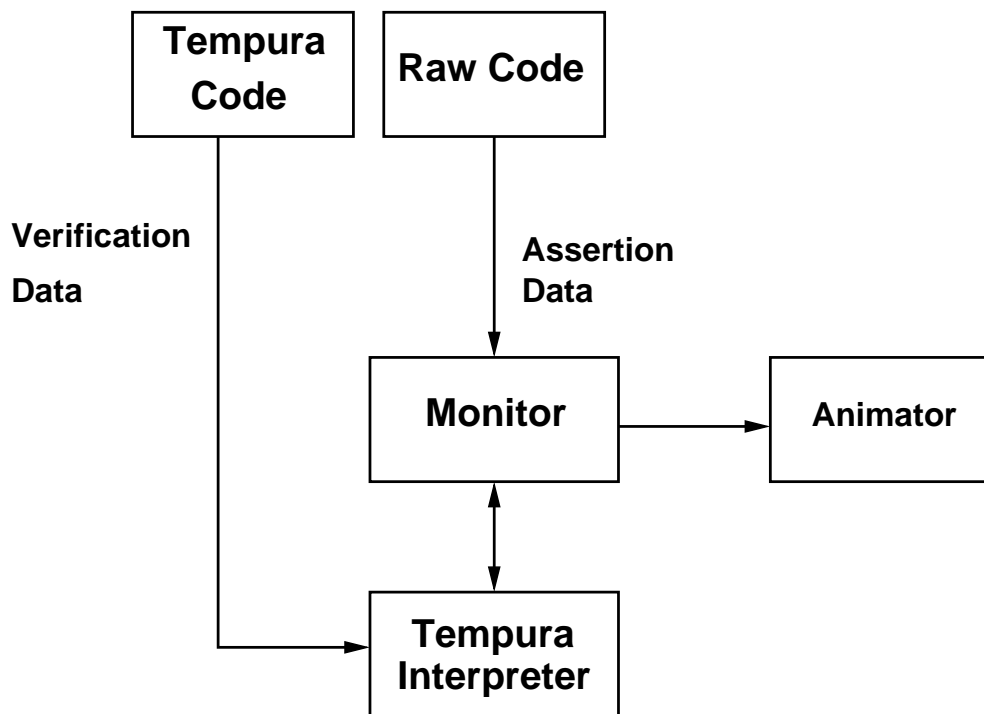


Figure 1: Overview of AnaTempura

Figure 2 shows the interface of AnaTempura.

Figure 3 shows a graphical snapshot of a simulation of the ep/3 microprocessor specified in Tempura.

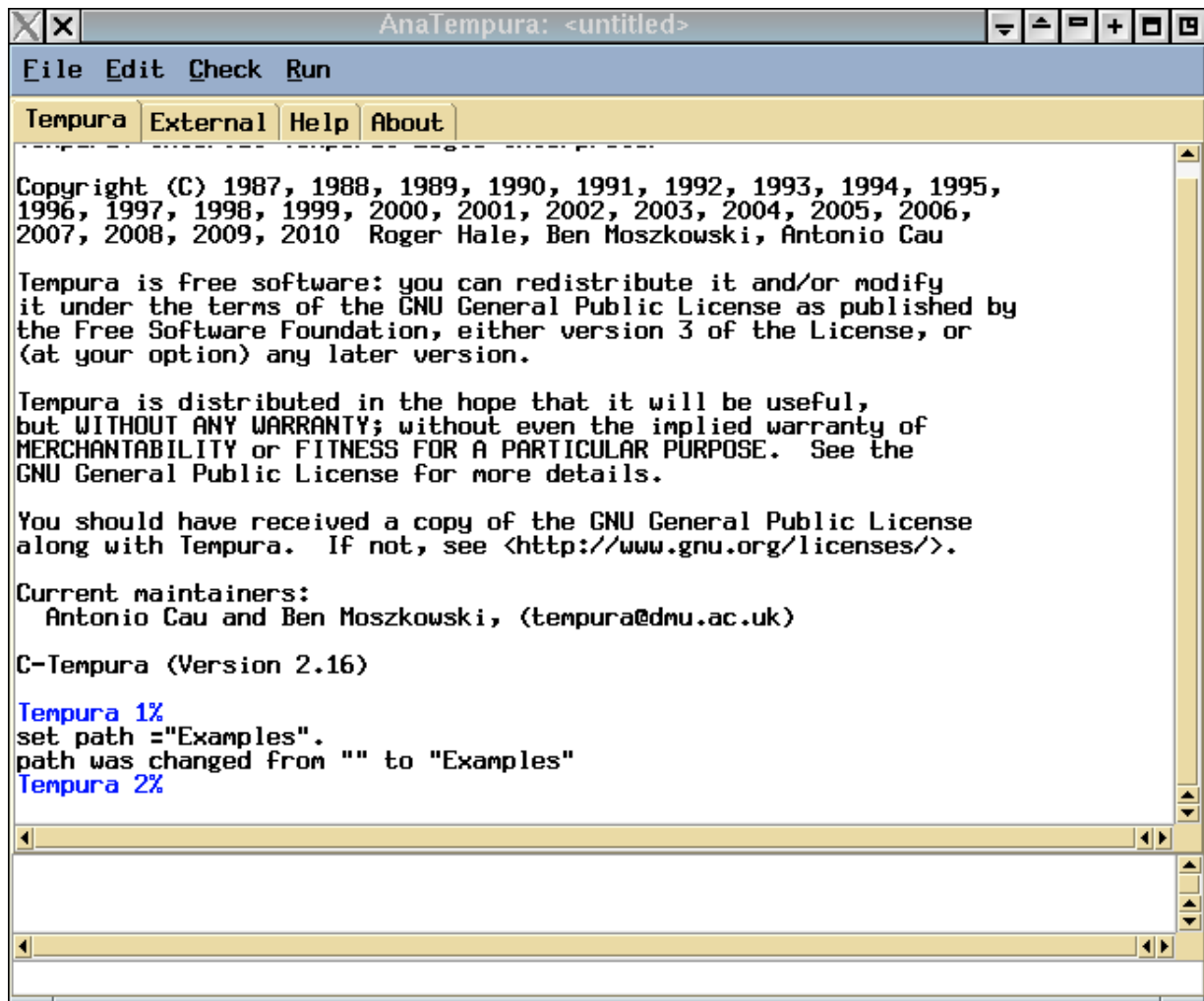


Figure 2: Interface of AnaTempura

## 6.2 ITL Theorem Prover based on Prover9

**Prover9** is a resolution/paramodulation automated theorem prover for first-order and equational logic developed by William McCune.

We have given an algebraic axiom system for Propositional Interval Temporal Logic (PITL): **Interval Temporal Algebra**. The axiom system is a combination of a variant of Kleene algebra and Omega algebra plus axioms for linearity and confluence.

This algebraic axiom system for PITL has been encoded in Prover9. So we can use Prover9 to prove the validity of various PITL theorems. The Prover9 encoding of PITL plus examples of more than 300 PITL theorems are available for download as

- Version 1.8 (released 27/08/2009): [gzipped tar file](#).
  - documentation updated to new semantics for

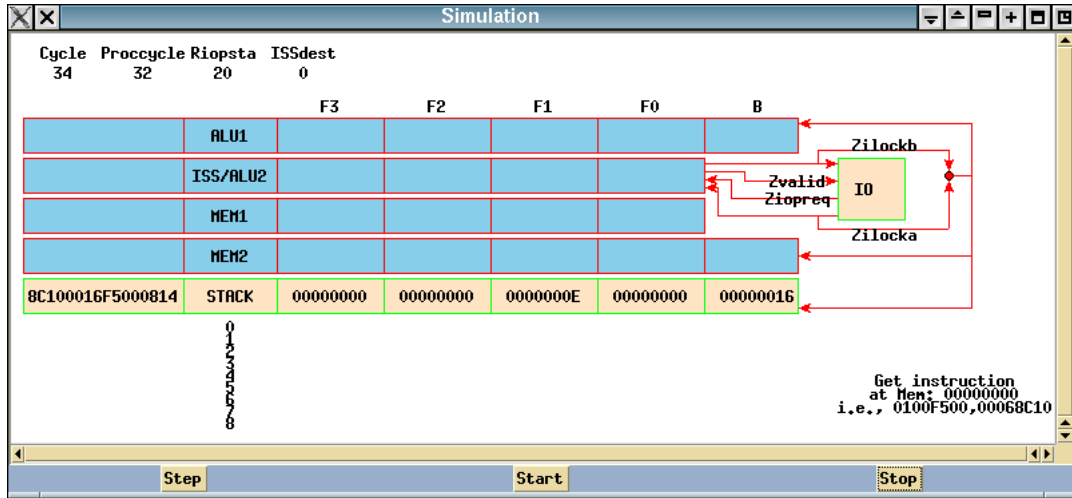


Figure 3: Graphical snapshot of simulation of the EP/3 microprocessor

chopstar and chop omega algebraic operators

- Version 1.7 (released 15/05/2009): [gzipped tar file](#).
  - updated documentation in doc, to use new ITL semantics
- Version 1.6 (released 12/12/2008): [gzipped tar file](#).
  - changed copyright license to GPLv3.0 and added the notice to all files
- Version 1.5 (first public release: 05/12/2008): [gzipped tar file](#).

The README in this tar file contains instructions how to use Prover9 for proving PITL theorems.

### 6.3 ITL Proof Checker based on PVS

PVS is an interactive environment, developed at SRI, for writing formal specifications and checking formal proofs. The specification language used in PVS is a strongly typed higher order logic. The powerful interactive theorem prover/proof checker of PVS has a large set of basic deductive steps and the facility to combine these steps into proof strategies. PVS is implemented in Common Lisp –with ancillary functions provided in C, Tcl/TK and LaTeX– and uses GNU Emacs for its interface. PVS is freely available for IBM RS6000 machines as well as Sun Sparcs under license from SRI. See [PVS homepage](#) for more information.

- The [ITL library for PVS 4.0](#).

- The [ITL library for PVS 3.2](#).
- The [ITL library for PVS 2.4 patchlevel 1](#).
- The [ITL library for PVS 2.3](#).
- The [ITL library for PVS 2.2](#).
- The [ITL library for PVS 2.1 patchlevel 2.417](#).

#### Publications:

- [Technical report](#).

### 6.4 Automatic Verification of Interval Temporal Logic

[Shinji Kono](#) has developed an automatic theorem prover for propositional ITL (LITE). The implementation is in Prolog. Further information can be gathered at [Shinji Kono's Interval Temporal Logic page](#). Shinji Kono has also a Java version of LITE see [CVS repository of JavaLite](#).

## 7 Tempura Book

The book *Executing Temporal Logic Programs* by Dr. B. C. Moszkowski was originally published by Cambridge University Press in 1986. The publishers have kindly given the copyright back to the author. The [pdf version of the book](#) has now been made available. Any comments are welcome. Here is how to reach the author:

[Dr. Ben Moszkowski](#)  
[Software Technology Research Laboratory](#)  
 Gateway House (GH4.55)  
 The Gateway  
 Leicester LE1 9BH  
 Great Britain  
 email: [Ben's email](#)  
 URL: [Dr. Ben Moszkowski www page](#)

## 8 STRL Publications using ITL

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