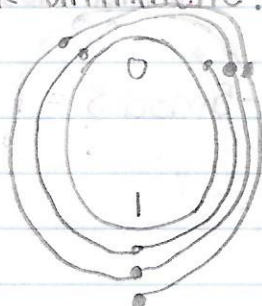


# CIS405: Mod 4 Modular Arithmetic Journal

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Visualize  $7 \bmod 2$  and  $-7 \bmod 6$  using clock arithmetic and Barrett reduction. Show the calculation on how you arrived at the answer in both cases.

Clock arithmetic:  $7 \bmod 2$



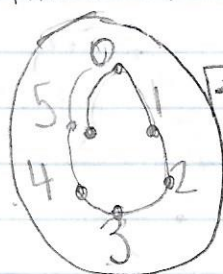
$$7 \bmod 2 = 1$$

Barrett Reduction:  $7 \bmod 2$

$$\begin{aligned} &= 7 - 2 \cdot \lfloor 7/2 \rfloor = 7 - 2 \cdot \lfloor 3.5 \rfloor \\ &= 7 - 2 \cdot 3 \\ &= 7 - 6 = 1 \end{aligned}$$

$$7 \bmod 2 = 1$$

Clock arithmetic:  $-7 \bmod 6$



$$-7 \bmod 6 = 5$$

Barrett Reduction:  $-7 \bmod 6$

$$\begin{aligned} &= -7 - (6 \cdot \lfloor -7/6 \rfloor) \\ &= -7 - (6 \cdot \lfloor -1.16 \rfloor) \\ &= -7 - (6 \cdot (-2)) \\ &= -7 - (-12) \\ &= -7 + 12 = 5 \end{aligned}$$

$$-7 \bmod 6 = 5$$