

# Spring'23 CPSC 323.02 Compilers & Languages

## HW #3 [50 points]

**Submission deadline:** Sunday, May 7, 11:59 PM, submit it on Canvas

*Any HW content shall **NOT** be made publicly accessible without the written consent of the instructor.*

### Top-down Parsers (Reference: Textbook chapters 3.2, 3.3, 3.4)

1. (10 points) Here we have a practical grammar for generating four-function expressions as below. Please remove all left recursions in the grammar (show your elimination steps).

$$E \rightarrow E + T \mid E - T \mid T$$
$$T \rightarrow T * F \mid T / F \mid F$$
$$F \rightarrow \text{int} \mid (E)$$

2. (20 points) Please determine the FIRST and FOLLOW from the revised grammar (*that does not contain left recursions*) in above Question 1.
3. (20 points) Construct the predictive-parser table for the revised grammar in above Question 1 using the FIRST and FOLLOW sets generated in above Question 2.

1. (10 points) Here we have a practical grammar for generating four-function expressions as below. Please remove all left recursions in the grammar (show your elimination steps).

$$E \rightarrow E + T \mid E - T \mid T$$

$$T \rightarrow T * F \mid T / F \mid F$$

$$F \rightarrow \text{int} \mid (E)$$

$$\underline{E \rightarrow E + T \mid E - T \mid T}$$

$$E \rightarrow E + T \text{ (remove direct left-recursion)}$$

$$E \rightarrow TE'$$

$$E' \rightarrow +TE' \mid -TE' \mid \epsilon$$

$$\underline{T \rightarrow T * F \mid T / F \mid F}$$

$$T \rightarrow T * F \text{ (remove direct left-recursion)}$$

$$T \rightarrow FT'$$

$$T' \rightarrow \star FT' \mid / FT' \mid \epsilon$$

Final:

$$E \rightarrow TE'$$

$$E' \rightarrow +TE' \mid -TE' \mid \epsilon$$

$$T \rightarrow FT'$$

$$T' \rightarrow \star FT' \mid / FT' \mid \epsilon$$

$$F \rightarrow \text{int} \mid (E)$$

2. (20 points) Please determine the FIRST and FOLLOW from the revised grammar (*that does not contain left recursions*) in above Question 1.

$$E \rightarrow TE'$$

$$E' \rightarrow +TE' \mid -TE' \mid \epsilon$$

$$T \rightarrow FT'$$

$$T' \rightarrow \star FT' \mid / FT' \mid \epsilon$$

$$F \rightarrow \text{int} \mid (E)$$

FIRST:

$$\text{FIRST}(E) = \text{FIRST}(T) = \text{FIRST}(F) = \{\text{int}, (\}$$

$$\text{FIRST}(E') = \{+, -, \epsilon\}$$

$$\text{FIRST}(T') = \{\star, /, \epsilon\}$$

FOLLOW:

$$\text{FOLLOW}(E) = \{\$, )\}$$

$$\text{FOLLOW}(E') = \{\$, )\}$$

$$\text{FOLLOW}(T) = \{+, -, \$, )\} \text{ (after } T \text{ in } E \rightarrow TE')$$

$$\text{FOLLOW}(T') = \{+, -, \$, )\}$$

$$\text{FOLLOW}(F) = \{\star, /, +, -, \$, )\} \text{ (after } F \text{ in } T \rightarrow FT')$$

3. (20 points) Construct the predictive-parser table for the revised grammar in above Question 1 using the FIRST and FOLLOW sets generated in above Question 2.

$$\text{Table}[E', \$] = \text{Table}[E, )] = \epsilon$$

$$\text{Table}[T', +] = \text{Table}[T', \$] = \text{Table}[T', )] = \epsilon$$

$$\text{Table}[E, \text{int}] = \text{Table}[E, (] = TE'$$

$$\text{Table}[E', +] = +TE'$$

$$\text{Table}[F, \text{int}] = \text{int}$$

$$\text{Table}[F, (] = (E)$$

$$\text{Table}[T', /] = /FT'$$

$$\text{Table}[T', \$] = \epsilon$$

	int	+	-	*	/	(	)	\$
E	TE'					TE'		
E'		+TE'	-TE'				$\epsilon$	$\epsilon$
T	FT'					FT'		
T'		$\epsilon$	$\epsilon$	*FT'	/FT'		$\epsilon$	$\epsilon$
F	int					(E)		