# **APTITUDE**

- aptitude for campus placements
- types of ques
  - o quantitive apt., maths
    - number system
    - profit, loss, interest
    - time and work
    - speed, distance, time, etc.
  - o logical apt., critical thinking
    - series
    - odd one out
    - blood relations
    - clock, etc.
- https://www.sheryians.com/courses/coursesdetails/Aptitude%20&%20Reasoning%20for%20Campus%20Placements confirm syllabus

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## Quantitative Aptitude

#### Time and Work

```
- given persons who do same work in some times individually
- now if all person work together, how much time they would take ?
- eg:
  - A work => 2days
    - meaning
      - 1day \Rightarrow 1/2work
  - 1day => 1/2work
  - A work => 3days
    - meaning
      - 1day => 1/3work
      - 1day => 1/3work
      - 1day => 1/3work
  - Together work => x hrs
    - then, Together 1hr => 1/x work
- thus if person A does work in x days, work done per day => 1/x work
- also, A work = A work ALONE
- also, A work ALONE + B work ALONE != A&B Together Work
- A&B Together Work = A&B working simuntaneously as WHOLE SYNERGY
- A work \Rightarrow x days; so A 1day \Rightarrow 1/x work
```

```
- also, A y days \Rightarrow y*(1/x) work
  - eg:
    - B work \Rightarrow 40 days
    - so B 1day => 1/40 work
    - thus, B 23 days => 23*(1/40) work
- case where someone ditch in the way
  - Together A&B for x days + B ALONE 23 days(suppose) = total work = 1
- now if 4 A 1 work => 20 days
  - then, 1 A 1 work => 20/4 days INCORRECT REASONING
  - the thing is that 4 people even identical are working SYNERGY TOGETHER and
complete work in 20 days, they didn't split days for each person, everone work
daily
  - then, 4 A 1 day => 1/20 work CORRECT
  - then, 1 A 1 day \Rightarrow 1/(20*4) work CORRECT
  - always divide the work , not the time
- LCM
```

- LCM stands for Least Common Multiple.
- It is the smallest multiple that two or more numbers have in common.
- A multiple of a number is the product of that number and an integer.
- For example, multiples of 2 are: 2, 4, 6, 8, 10...
- Multiples of 3 are: 3, 6, 9, 12, 15...
- Common multiples of 2 and 3 are: 6, 12, 18...
- The smallest of these common multiples is 6.
- Therefore, LCM of 2 and 3 is 6.
- To find LCM, you can list the multiples of each number and choose the smallest
- Another method is prime factorization: multiply the highest power of all prime factors.
  - Example:
    - Find LCM of 18 and 24 by prime factorization.
      - $-18 = 2 \times 3^{2}$
      - $-24 = 2^3 \times 3$
      - Take highest powers: 23 and 32
      - $LCM = 2^3 \times 3^2 = 8 \times 9 = 72$
- Q. How to add fractions using LCM (Least Common Multiple)?
  - Step 1: Find the LCM of the denominators of the fractions.
  - Step 2: Rewrite each fraction with the denominator equal to the LCM.
- Step 3: Adjust the numerators accordingly by multiplying with what was done to the denominators.
  - Step 4: Add the numerators and keep the common denominator.
  - Step 5: Simplify the fraction if possible.
  - Example:
    - Add 1/3 + 2/5
      - Denominators: 3 and 5
      - LCM of 3 and 5 = 15
      - Rewrite fractions with denominator 15:

$$(1 \times 5) / 15 + (2 \times 3) / 15$$

- = 5/15 + 6/15
- Add numerators: 5 + 6 = 11
- Result: 11/15 (already simplified)

```
when dividing ugly numbers eg: 153/17, start multiple count backwards
17 × 10 = 170 → too big
17 × 9 = 153 → perfect
=> 153/17 = 9
```

- Have clean calculation for acurate calculation

Q. A can do a piece of work in 12 hours and B alone can do it in 15 hours. In how much time will they finish the whole SYNERGY work, working together?

```
- A work \Rightarrow 12hrs
- B work \Rightarrow 15hrs
- A 1hr \Rightarrow 1/12 \text{ work}
- B 1hr \Rightarrow 1/15 work
- Together 1hr => A & B 1hr => A 1hr + B 1hr
- A \& B 1hr => 1/12 + 1/15
  - = (15 + 12) / (12 * 15)
  - = 27 / 180
  - = 9 / 60
  - = 3 / 20
- Together 1hr => 3/20 work
- Together work \Rightarrow 1/(3/20) hrs [like A work \Rightarrow 12hrs;So, A 1hr \Rightarrow 1/12 work ]
- Total time
  - => Together work
  - => 1 /
  - = 1 / (3/20)
  - = 20/3 hrs
  - = 6hrs 40 mins
```

Q. A and B together can do a piece of work in 12 days. B alone can do it in 30 days. In how many days will A alone finish the work?

```
- A & B work => 12 days

- B work => 30 days

- A & B 1 day => 1/12 work

- B 1 day => 1/30 work

- A 1 day => A & B 1 day - B 1 day

- = 1/12 - 1/30

- = (30 - 12) / (12 * 30)

- = 18 / 360

- = 1 / 20
```

```
- A 1 day => 1/20 work
- A work => 20 days
```

## Q. A & B $\rightarrow$ 18 days, B & C $\rightarrow$ 24 days, C & A $\rightarrow$ 36 days; A, B & C $\rightarrow$ ?, A $\rightarrow$ ?

```
- A \& B \Rightarrow 18 \text{ days}
- B & C => 24 days
- C \& A \Rightarrow 36 days
- A & B 1 day => 1/18 work
- B & C 1 day => 1/24 work
- C & A 1 day => 1/36 work
- Sum => 1/18 + 1/24 + 1/36
 - = (4 + 3 + 2) / 72 [LCM 72]
 - = 9 / 72
 - = 1 / 8
- Sum = (A \& B)1day + (B \& C)1day + (C \& A)1day
 - = 2 * (A + B + C)1day
-2 * (A + B + C)1day => 1/8
- (A + B + C)1day => 1/16
- A, B & C \Rightarrow 1 / (1/16)
 - = 16 days
- A 1 day => (A + B + C)1day - (B + C)1day
 - = 1/16 - 1/24
 - = (3 - 2) / 48
 - = 1 / 48
- A work => 48 days
- B 1 day => (A + B + C)1day - (C + A)1day
 - = 1/16 - 1/36
 - = (9 - 4) / 144
 - = 5 / 144
- B work => 1 / (5/144)
 - = 144 / 5 days
 - = 28 4/5  days
 - = 28 days 19 hrs 12 mins
- C 1 day => (A + B + C)1day - (A + B)1day
 - = 1/16 - 1/18
  - = (9 - 8) / 144
  - = 1 / 144
- C work => 144 days
```

Q. A & B can do a piece of work in 45 & 40 days respectively. They began the work together but A leaves after some days & B finished the remaining work in 23 days. After how many days did A leave?

```
- case where someone ditch in the way
- Together A&B for x days + B ALONE 23 days = total work = 1
- Together work
- A work \Rightarrow 45 days
- B work \Rightarrow 40 days
- A 1 day => 1/45 work
- B 1 day => 1/40 \text{ work}
- B 23 days => (1/40)*3 work
- Together 1 day => A 1 day + B 1 day
 - = 1/45 + 1/40
 - = (40 + 45) / (45 * 40)
 - = 85 / 1800
 - = 17 / 360
- Suppose A left after x days
- Work done in x days by (A + B) \Rightarrow x * (17/360)
- Work done in 23 days by B ALONE => 23 * (1/40) = 23/40
- Total work = 1
- Equation \Rightarrow (17x / 360) + (23 / 40) = 1
- Take LCM 360
  -(17x / 360) + (207 / 360) = 1
 -(17x + 207) / 360 = 1
 -17x + 207 = 360
  -17x = 153
  - x = 9
- when dividing ugly numbers eg: 153/17, start multiple count backwards
  - 17 × 10 = 170 \rightarrow too big
  - 17 × 9 = 153 → perfect
  - \Rightarrow 153/17 = 9
- also, A work = A work ALONE
- also, A work ALONE + B work ALONE != A&B Together Work
- A&B Together Work = A&B working simuntaneously as WHOLE SYNERGY
- A work \Rightarrow x days; so A 1day \Rightarrow 1/x work
  - also, A y days => y*(1/x) work
  - eg:
    - B work => 40 days
    - so B 1day \Rightarrow 1/40 work
    - thus, B 23 days => 23*(1/40) work
```

Q. If 4 men or 6 boys can finish a piece of work in 20 days, in how many days can 6 men & 11 boys finish it?

```
- 4 men => 20 days
- 6 boys => 20 days
- 4 \text{ men } 1 \text{ day } => 1/20 \text{ work}
-1 \text{ man } 1 \text{ day } => 1/(20 \times 4) = 1/80 \text{ work}
- 6 boys 1 day \Rightarrow 1/20 work
-1 boy 1 day \Rightarrow 1/(20 \times 6) = 1/120 work
- 6 men & 11 boys 1 day => 6*(1/80) + 11*(1/120)
  - = 6/80 + 11/120
  - = 9/120 + 11/120 [LCM 240]
  - = 20/240
  - = 1/12
- 6 \text{ men } \& 11 \text{ boys } \Rightarrow 1 / (1/12)
  - = 12 \text{ days}
- Have clean calculation for acurate calculation
- now if 4 A 1 work => 20 days
  - then, 1 A 1 work => 20/4 days INCORRECT REASONING
  - the thing is that 4 people even identical are working SYNERGY TOGETHER and
complete work in 20 days, they didn't split days for each person, everone work
daily
  - then, 4 A 1 day => 1/20 work CORRECT
  - then, 1 A 1 day \Rightarrow 1/(20*4) work CORRECT
  - always divide the work , not the time
```

#### Practice

- Q1. If Roger can do a piece of work in 8 days and Antony can do the same work in 5 days, in how many days will both of them do it together?
- Q2. To complete a piece of work, A takes 50% more time than B. If together they take 18 days to complete the work, how much time shall B take to do it alone?
- Q3. A takes 3 days to complete a work while B takes 2 days. Both of them finish a work and earn Rs. 150. What is A's share of money? (Hint money should be divided.. in the ratio of how much work a person does in 1 day) Rs 70 Rs 30 Rs 60 Rs 75
- Q4. An exam was conducted and the following was analyzed. 4 men were able to check some exam papers in 8 days working 5 hours regularly. What is the total number of hours taken by 2 men in 20 days to check double the number of exam papers?

```
Q1.
- Roger => 8 days
```

```
- Antony => 5 days
- Roger 1 day => 1/8 work
- Antony 1 day => 1/5 work
- (Roger + Antony) 1 day => 1/8 + 1/5
  - = (5 + 8) / 40
                            [LCM 40]
  - = 13 / 40
- (Roger + Antony) => 1 / (13/40)
  - = 40 / 13 days
 - = 3 \text{ days} + (1/13) \text{ day}
  - = 3 days 1 hour 50 minutes 46 seconds
Q2.
- A takes 50% more time than B \Rightarrow A = 1.5 \times B
- Let B => x days
- Then A \Rightarrow 1.5x days
- A 1 day => 1/(1.5x) = 2/(3x) work
- B 1 day \Rightarrow 1/x work
- (A + B) 1 day => 2/(3x) + 1/x
  - = (2 + 3) / (3x) [LCM 3x]
  - = 5 / (3x)
- (A + B) time => 1 / (5/(3x)) = 3x / 5 days
- Given together they take 18 days:
  -3x / 5 = 18
  - x = 18 \times 5 / 3
  - x = 30
- B \Rightarrow 30 \text{ days}
Q3.
- A \Rightarrow 3 \text{ days}
- B \Rightarrow 2 \text{ days}
- A 1 day \Rightarrow 1/3 work
- B 1 day \Rightarrow 1/2 work
- Ratio of daily work (A : B) \Rightarrow 1/3 : 1/2
  - = (multiply by 6) => 2 : 3
- Total money = Rs. 150
- A's share => 2 / (2 + 3) \times 150
  - = 2/5 \times 150
  - = Rs. 60
- Correct option: Rs 60
Q4.
- 4 men => 8 days × 5 hours/day to check N papers
```

```
Total man-hours for N papers => 4 × 8 × 5

= 160 man-hours

Double the papers => 2N => required man-hours = 2 × 160

= 320 man-hours

2 men working 20 days for 2N papers:

Let daily hours per man = h
Total man-hours available = 2 × 20 × h = 40h
40h = 320
h = 8 hours/day

Total number of hours taken by 2 men in 20 days (man-hours) => 2 × 20 × 8

= 320 hours

Answer: 320 hours (i.e., each works 8 hours/day for 20 days)
```