

2.

Priority Queue

A data structure for maintaining a set S of elements, each with an associated value called a key

— A max. priority queue uses max-heap, and supports the following operations:

— Insert (S, x, k): insert element x with key k into S

Equiv. to: $S = S \cup \{x\}$

— Maximum (S): returns element with largest key

— Extract-Max(): removes & returns the element with largest key

— Increase-key (S, x, k): Increases value of element x 's key to the new value k ($k \geq x.\text{key}$)

Max - Heap - Maximum (A)

if $A.\text{heap-size} < 1$

error "heap underflow"

return $A[1]$

Max-Heap-Extract-Max (A)

max = Max-Heap-Maximum(A)

A[1] = A[A.heap-size]

A.heap-size = A.heap-size - 1

Max-Heapify(A)

return max

$O(\lg n)$

Max-Heap-Increase-Key (A, x, k)

if $k < x.key$

error "New key is smaller than current key"

$x.key = k$

find the index i in array A where object x occurs

while $i > 1$ and $A[\text{Parent}(i)].key < A[i].key$

exchange $A[i]$ with $A[\text{Parent}(i)]$

Update the information that maps
Priority Queue objects to array indices

$i = \text{Parent}(i)$

$O(\lg n) + \text{overhead of mapping Pr. Que. obj to index}$

Max-Heap-Insert(A, x, n)

if $A.\text{heap-size} == n$

error "heap overflow"

$A.\text{heap-size} = A.\text{heap-size} + 1$

$k = x.\text{key}$

$x.\text{key} = -\infty$

$A[A.\text{heap-size}] = x$

map x to index heap-size in array

Max-Heap-Increase-key(A, x, k)

 $O(\lg n) + \text{overhead} \dots$