

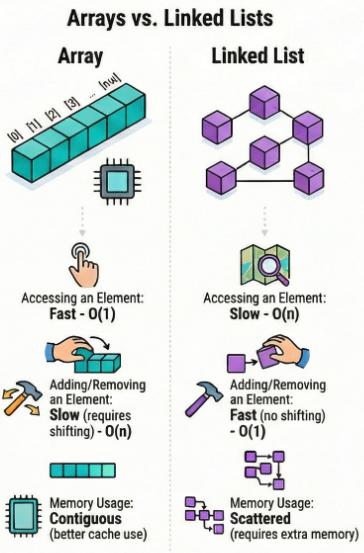
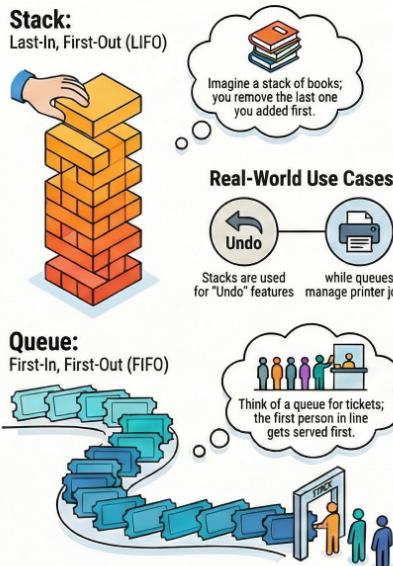
# kintsugi-stack-dsa-cpp: COMPETITIVE\_PROGRAMMING

"Talk is cheap. Show me the time complexity."

- Author: [Kintsugi-Programmer](#)

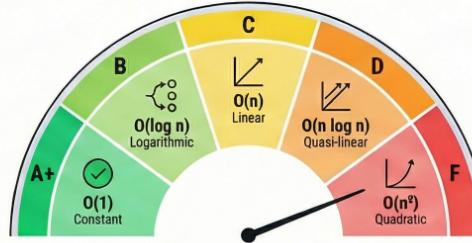
## A Developer's Guide to Data Structures & Algorithms

### Fundamental Data Structures: The Building Blocks



### Measuring Algorithm Efficiency: Understanding Big O

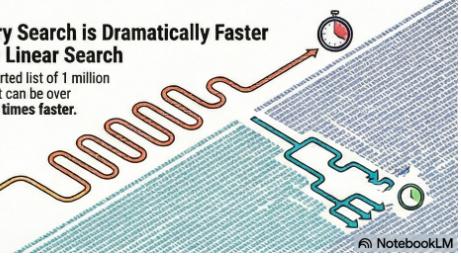
#### Performance Grades on Large Datasets



**What is Big O Notation?** It answers the question: "How does my code slow down as data grows?" Complexities range from excellent ( $O(1)$ ) to extremely poor ( $O(n^2)$ ).

### Binary Search is Dramatically Faster Than Linear Search

On a sorted list of 1 million items, it can be over 38,000 times faster.



Disclaimer: The content presented here is a curated blend of my personal learning journey, experiences, open-source documentation, and invaluable knowledge gained from diverse sources. I do not claim sole ownership over all the material; this is a community-driven effort to learn, share, and grow together.

- <https://codeforces.com/profile/kintsugi-programmer>
- <https://www.tle-eliminators.com/cp-sheet>

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## R800

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### 01 A Halloumi Boxes

- <https://codeforces.com/problemset/problem/1903/A>
- brute force, greedy, sortings, \*800
- Analysis
  - n boxes/array  $a_1 \ a_2 \ \dots \ a_n$
  - $a = \{a_0, a_1, a_2 \ \dots \ a_{n-1}\}$
  - subarray = subsegment = segment taken out of array not manipulated ,no change in order
    - eg:  $\{a_0, a_1\}, \{a_1, a_2, a_3\}$ , etc
  - He wants to sort them in non-decreasing order based on their number
  - non-decreasing = increasing
  - s is atmost k , means :  $s \leq k$
  - however, his machine works in a strange way. It can only reverse any subarray of boxes with length **at most k**
  - subarrsize $\leq k$
  - Find if it's possible to sort the boxes using any number of reverses.
  - So, if  $K \geq 2$  ,Machine's sort is 100%possible at **any number of reverses ANY\_TIMES**
    - if  $k=2$  atleast  $\Rightarrow$  i have power to shift any element anywhere
  - eg:
    - 6421
      - 6421 rev 2 nos sub array my initial thought
      - 6412 rev 2 nos sub array
      - 6142 rev 2 nos sub array
      - 1642 rev 2 nos sub array
      - 1624 rev 2 nos sub array
      - 1264 rev 2 nos sub array
      - 1246 rev 2 nos sub array
      - sorting done :0
    - 6421
      - 1246 rev 4 nos sub array optimal from tuts
  - atq : according to question
  - tl per test = 1sec atq
    - 1sec =  $10^8$  Operations = per test operations
    - $1 \leq k \leq n$  (minitest) $\leq 100$  acc.to ques (atq)
    - consider  $n=100$  upperbound
    - tl per mini test = 1sec /100

- per mini test operations =  $10^8 / 100 = 10^6$
- if tc per mini test =  $O(n^3)$ 
  - so  $n=100$ , then operation =  $O(n^3) = O(100^3) = O(10^9)$  = per mini test operations
  - so  $O(n^3)$  is the upper bound
  - even sol. can have  $O(n^2)$ ,  $O(n)$ ,  $O(n\log n)$  etc. anything below  $O(n^3)$ , but not above  $O(n^3)$
- Expected TC =  $O(n^3)$
- ml per test = 256mB atq
- at  $k=1$ , no sorting is possible
  - because the foundation of reverse is actually swap any atleast 2 stuff
  - if stuff is only one then it wont make sense to reverse as we lost power to shift any element
- Approach
  - Passing Condition where return YES
    - $K \geq 2$
    - or given array is already sorted
  - else, return False

```
#include<bits/stdc++.h>
using namespace std;
int main(){
    // at extreme proof case use :
    // long long t;
    int t;
    cin>>t;
    while(t--){
        int n,k;
        cin>>n>>k;
        vector<int> v(n);
        int i=0;
        //input
        while(i<n){
            cin>>v[i]; // n order
            i++;
        }
        vector<int> v2=v; // copy // n order
        sort(v2.begin(), v2.end()); // n logn order
        if ((v2==v)or(k>=2)){ // to check whether initial array is sorted
        or not // n order
            cout<<"YES\n";
        } else {
            cout<<"NO\n";
        }
    }
    return 0;
}
// tc O(n logn) // highest order here
// at n = 100 , tc = 100 log100 = 100*7 = 700
// 2^7 ~ 100
```

```
// log2(n) = ln n / ln 2
// sc O(n)
```

## 02 A Line Trip

- <https://codeforces.com/problemset/problem/1901/A>
- greedy, math, \*800
- Analysis
  - location&road on number line
    - 0 , a<sub>1</sub> , a<sub>2</sub> , ... , x
    - Round Trip i.e. total path => 0, a<sub>1</sub>, ... a<sub>n</sub>, x, a<sub>n</sub>, ..., a<sub>1</sub>,0
    - a<sub>1</sub>,a<sub>2</sub> ... Gas station for Tanki Full/ Refill
    - 0 start point
    - if stop at non-station location due to gas empty = gameover
    - no refuel at dest x
  - In this ques, we have to find the capacity of gas tank car should take it for journey, efficiently without stopping
  - tl per test = 2secs
    - 2secs = 2\*(10<sup>8</sup>) operations
    - t=1000 atq
    - time/testcase = O(2\* 10<sup>5</sup>)
    - n=50 max atq
    - then at O(n<sup>3</sup>) = O(125000) = O(1.25 \* 10<sup>5</sup>) <= O(2\* 10<sup>5</sup>)
    - TC for minitest = Expected TC = O(n<sup>3</sup>) upper bound
  - tlpt = time limit per test
  - mlpt = 256mB
  - in test case 1
    - n=3
    - x=7
    - a{1,2,5}
    - 0-1-2-5-7-5-2-1-0
    - output = 4
    - gaschanges=
      - 4 start
      - 3 at 1
      - 4 refill
      - 3 at 2
      - 4 refill
      - 1 at 5
      - 4 refill
      - 2 at 7
      - NO Refill at dest x
      - 0 at 5 ,biggest gas consumption, 5->7->5 , 4 units distance
      - 4 refill
      - 1 at 2
      - 4 refill

- 3 at 1
- 4 refill
- 3 end, fully reached ,gas still remaining
- biggest gas consumption, 5->7->5 , 4 units distance
- thus min threshold gas capacity is 4 units ,as below it , car would stop at 5->7->5
- now the max capacity of gas tank in any journey = max distance of any 2 gas stations throughout journey
- throughout journey means a round trip
  - so, after lastGasStation, car will go to x(dest), and find lastGasStation first in return journey
  - so, that distance is (lastGasStation - x)\*2
- Approach
  - C1= cal. firstGasStation-0
  - C2= max(allDistances(cal. dist b/w eachGasStation))
  - C3= cal. (lastGasStation - x)\*2
  - return max(C1,C2,C3)

```
#include<bits/stdc++.h>
using namespace std;
int main(){
    long long t;
    cin>>t;
    while(t--){
        long long n,x;
        cin>>n>>x;
        long long i=1;
        long long smax=0;
        vector<long long> v1(n+1,0); //initialize safety //O(n)
        v1[0]=0;
        while(i<=n){// O(n)
            cin>>v1[i];
            // cout<<v1[i];
            long long buff=smax;
            smax=max(buff,(v1[i]-v1[i-1]));
            i++;
        }
        long long smax2=(x-v1[n])*2; // O(1)
        cout<< max(smax,smax2)<<endl;
        // cout<< smax<<" "<<v1[n-1]<<" "<<smax2<<endl;
    }
    }return 0;
}
// Time Complexity: O(n)
// Space Complexity: O(n)

// max(a, b); O(1) // just checks (a < b)
// min(a, b); O(1) // just checks (a < b)
// max_element(v.begin(), v.end()); O(n)
// min_element(v.begin(), v.end()); O(n)
```

- my code is more optimal than tut ;)

## 03 A Cover in Water

- <https://codeforces.com/problemset/problem/1900/A>
  - constructive algorithms, greedy, implementation, strings, \*800
  - Analysis
    - Filip has a row of cells, some of which are blocked, and some are empty.
    - He wants all empty cells to have water in them.
    - He has two actions at his disposal
      - 1. place water in an empty cell. **FINITE\_TIMES**
      - 2. remove water from a cell and place it in any other empty cell. **ANY\_TIMES**
    - autoOperation
      - if at some moment cell  $i$  ( $2 \leq i \leq n-1$ ) is empty and both cells  $i-1$  and  $i+1$  contains water, then it becomes filled with water. **ANY\_TIMES**
      - magic autofill
    - $N \Rightarrow s = s_1, s_2, s_3, \dots, s_n$ 
      - $\dots \# \# . \# \dots \# \#$
      - now in ...
        - if we just  $w.w$  ( $w=water$ )  $\Rightarrow www$
        - then we can transfer the middle water to other cells one by one
        - $w.w$  sill it get refill  $\Rightarrow www$
      - $\dots \# \# . \# \dots \# \#$ 
        - $w.w \# \# . \# \dots \# \#$  2times fill water manual
        - $www \# \# . \# \dots \# \#$  autofill
        - $w.w \# \# . \# w \dots \# \#$  swap water
        - $www \# \# . \# w \dots \# \#$  autofill
        - $w.w \# \# w \# w \dots \# \#$  swap water
        - $www \# \# w \# w \dots \# \#$  autofill
        - $w.w \# \# w \# w w \dots \# \#$  swap water
        - $www \# \# w \# w w \dots \# \#$  autofill
        - $w.w \# \# w \# w w w \dots \# \#$  swap water
        - $www \# \# w \# w w w \dots \# \#$  autofill
        - $w.w \# \# w \# w w w \# \#$  swap water
        - $www \# \# w \# w w w \# \#$  auto fill
        - all buckets filled ;0, count=2 operation 1
    - C1: if no. of Consecutive dots(emptyBoxes)  $\geq 3$ 
      - then we only need 1 operation only 2TIMES as we could fill at corner of 3 boxes and middle box will autoOperationAutoFillWater and we can transfer that water to other cells **ANY\_TIMES** 2 operation, and regenerate autoOperationAutoFillWater
    - C2: else we need to fill all boxes by 1 operation only as here autoOperationAutoFillWater fails
    - Expected TC
      - tlpt 1sec atq
        - mt = t max= 100 atq
        - tlpmt =  $10^8 / 100 = 10^6$
        - n = 100 atq
        - TComt =  $O(n^3)$  upperbound

- as  $O(100^3) = O(10^6)$  = order of tlpmt
- mlp 256mB atq
- Approach
  - count no. of dots(emptyBoxes)
  - count no. of Consecutive dots(emptyBoxes)
  - if no. of Consecutive dots(emptyBoxes)  $\geq 3$ 
    - return 2
  - else
    - return no. of dots(emptyBoxes)
- AnotherApproach
  - if i have 3 continuous empty cell, answer is 2 else ,answer is count of all empty cells
  - similar
  - ...  $\Rightarrow (i-1), (i), (i+1)$ 
    - just fill i-1, i+1
  - if (`s[i]=="."` && `i+1<n` && `s[i+1]=="."` && `i+2<n` && `s[i+2]=="."`)
    - return 2
  - else
    - return no. of dots(emptyBoxes)

```
#include<bits/stdc++.h>
using namespace std;
int main(){
    long long t;
    cin>>t;
    while (t--)
    {

        long long n;
        cin>>n;

        string s;
        cin>>s;

        int sum=0;
        int i=0;
        int dot=0;

        while(i<s.size()){
            if (s[i]=='.' & sum!=3)
            {
                sum++;
                dot++;
            }
            else if (s[i]=='#' & sum!=3)
            {
                sum=0;
            }
            i++;
        }
    }
}
```

```

    if ( sum>=3 )
    {
        cout<<2<<endl;
    }
    else
    {
        cout<<dot<<endl;
    }

}

return 0;

}
// TC O(n)
// SC O(n)

```

## 04 A Game with Integers

- <https://codeforces.com/problemset/problem/1899/A>
- games, math, number theory, \*800
- Analysis
  - Vanya and Vova are playing a game. Players are given an integer  $n$ . On their turn, the player can add 1 to the current integer or subtract 1
  - Operations any ne
    - $n=n-1$
    - $n=n+1$
  - The players take turns; Vanya starts. If after Vanya's move the integer is divisible by 3, then he wins. If 10 moves have passed and Vanya has not won, then Vova wins.
  - if both players play optimally
    - then in each of player turn he/she will try move to make other one lose
  - eg: if nos is 5
    - nos = 5
    - 6 ( vanya n++ ) OR 4 ( vanya n--)
    - 5 ( vova n-- ) or 7 ( vova n++ ) OR 3 ( vova n-- ) or 5 ( vova n++ )
    - 6 ( vanya n++ ) OR 4 ( vanya n-- ) or 6 ( vanya n-- ) OR 8 ( vanya n++ ) or 2 ( vanya n-- ) OR 4 ( vanya n++ ) or 4 ( vanya n-- ) OR 6 ( vanya n++ )
    - basically she will counter , to remake it even, repetitive till 10
    - she won
  - Expected TC ?
    - tlpt = 1sec atq
    - mlpt = 256mB atq
    - t = 100 atq
    - n = 1000 atq
    - 1sec =  $10^8$  ops
    - $tlpmt = 10^8 / t = 10^8 / 100 = 10^6$
    - Expected TC =  $O(n^2)$ 
      - not  $O(n^3)$

- as  $1000^3 = 10^9 < tlpmt$
  - as putting n in mt  $O(n^2)$
  - $= 1000^2$
  - $= 10^6$
  - $= tlpmt$
- NOW , if both play most optimal, then they will reverse each other operations and exhaust the turns
  - eg:  $n=6 \Rightarrow 7$  (vanya  $n++$ )  $\Rightarrow 6$  (vova  $n--$ )  $\Rightarrow$  infinite loop
  - $n \% 3 == 0$ 
    - if True, divisible before vanya move
      - even vanya could  $+1/-1$
      - it will not be divisible by 3
      - & vova will cancel the effect  $-1/+1$  of vanya till 10rounds
      - ultimate vova win
    - if False, not divisible before vanya move
      - vanya could  $+1/-1$
      - it will be divisible by 3 after vanya move
      - & vova will do something
      - & vova will cancel the effect  $-1/+1$  of vova
      - and still it will be divisible by 3 after vanya move till 10rounds
      - ultimate vanya win
- numbers
  - 0 DIV
  - 1 ( $-1=0$ )
  - 2 ( $+1=3$ )
  - 3 DIV
  - 4 ( $-1$ )
  - 5 ( $+1$ )
  - 6 DIV
  - 7
  - 8
  - 9 DIV
- Eg: 6
  - $\Rightarrow 7 \Rightarrow 8 \Rightarrow 9 \Rightarrow \dots$  vanya win
  - $\Rightarrow 7 \Rightarrow 6 \Rightarrow 7 \Rightarrow 6 \dots$  vova win if played optimally
- Approach
  - if  $n \% 3 == 0$ 
    - vova win, return Second
  - else if  $n \% 3 != 0$ 
    - vanya win, return Second

```
#include<bits/stdc++.h>
using namespace std;
int main(){
    long long t=0;
    cin>>t;
```

```

while(t--){
    long long n=0;
    cin>>n;
    if (n%3==0){cout<<"Second\n";}
    else{cout<<"First\n";}
}
return 0;
}
// TC O(1)
// SC O(1)

```

## 05 A Jagged Swaps

- <https://codeforces.com/problemset/problem/1896/A>
- sortings, \*800
- Analysis
  - here, permutation is an array
    - of unique elements
    - if array of  $n$  integers, then integer exists of all  $1,..,n$
    - => ORDER DOES NOT MATTER
  - we want to check if we could sort the permutation with special operation ANY\_TIMES
  - special operation
    - if  $a[i-1] < a[i] > a[i+1]$ 
      - then swap  $a[i], a[i+1]$
  - eg: 1 3 2 5 4
    - target: 1 2 3 4 5
    - now
      - 1 3 2 5 4
      - 1<3>2 5 4 satisfies spec ops
      - 1 2 3 5 4 swap :0
      - 1 2 3 <5>4 satisfies spec ops
      - 1 2 3 4 5 swap :0
      - = target
  - Expected TC
    - tlpt 1sec atq
      - t max 5000 atq
      - n max 10 atq
      - 1 sec =  $10^8$  ops
      - $tlpmt = 10^8 / 5 * 10^3$ 
        - =  $10^5 / 5$
        - =  $2 * 10^4$  ops
      - $O(10^4) < tlpmt$
      - $O(n^4) = \text{Expected TC} = tlpmt$
    - mlpt 256mB atq
- Approach optimal
  - IF THE FIRST NUMBER IN THE INITIAL ARRAY IS 1, THEN ANSWER IS YES , ELSE ANSWER IS NO
  - if not 1st element is 1 ,then that element can never shift towards its desired side

- this is technically bubble sort
- as if a number is largest, then it would be  $a[i-1] < a[i] > a[i+1]$  obviously
- our input arrays are already a permutation perfect, so no need to crosscheck

```
#include<bits/stdc++.h>
using namespace std;

int main(){

    long long t;
    cin>>t;
    while(t--){
        int n;
        cin>>n;
        vector<int> arr(n, 0);
        for (int i=0; i<n; i++) cin>>arr[i];
        if (arr[0]==1) cout<<"YES\n";
        else cout<<"NO\n";

    }

    return 0;
}
// TC O(n)
// SC O(n)
```

- Approach Brute Force
  - if this is permutation
    - if permutation is already sorted
      - return "YES"
    - else
      - try sort by special operation n times
      - if sorted
        - return "YES"
      - else
        - return "NO"
  - else
    - return "NO"
    - TTYL

```
#include<bits/stdc++.h>
using namespace std;

string checkSort(vector<int> arr, vector<int> arr2, int n){
    for ( int faltu=0; faltu<n; faltu++){
        for ( int idx=0; idx<n; idx++){
            if (
                arr[idx]<arr[idx+1] &&
```

```

        arr[idx+1]>arr[idx+2] &&
        idx+2<n
    ){
        int temp= arr[idx+1];
        arr[idx+1]= arr[idx+2];
        arr[idx+2]=temp;

    }
}
if(arr2==arr) { return "YES"; }
}
return "NO";
}

// NO NEED
string checkPert(int n){
    vector<int> arr(n);
    for (int i=0; i<n; i++) cin>>arr[i];

    vector<int> arr2=arr;
    sort(arr2.begin(),arr2.end());

    for ( int idx=0; idx<n; idx++){if (arr2[idx]!=idx+1) {return "NO";}
    if(arr2==arr) { return "YES"; } // already sorted
    return checkSort(arr,arr2, n); // we dont feed data types as arguements
}

int main(){
    long long t;
    cin>>t;
    while(t--){
        int n;
        cin>>n;
        cout<<checkPert(n)<<"\n";

    }
    return 0;
}

```

## 06 A Doremy's Paint 3

- <https://codeforces.com/problemset/problem/1890/A>
- constructive algorithms, \*800
- Analysis
  - array a = { a1,a2,a3...an}
  - n sized array
  - you want equality among the adjacent sums

- array is good for this ques as
- there exists a k such that  $a_1+a_2=a_2+a_3=\dots=a_{n-1}+a_n=k$
- Can you reorder the elements such that the condition becomes true ???
- **permute its element** = change its order
- eg : {1,1,2}
  - 1,2,1 permute done
  - now  $1+2 = 2+1 = 3 : 0$  Done
  - "YES"
- Expected TC?
  - $tlpt = 1\text{sec}$  atq
  - $= 10^8 \text{ ops}$
  - $t \max=100 = mt$  atq
  - $tlmt = 10^8 / 100 = 10^6$
  - $n = 100$
  - $O(n^3) = 100^3 = 10^6 = tlmt$
  - Expected TC =  $O(n^3)$
  - $mlpt = 256\text{mB}$  atq
  - if Expected TC =  $O(n^3)$  ,then
    - $O(n^4)$  NO ABOVE UPPER BOUND
    - $O(n^3)$  YES UPPER BOUND
    - $O(n^2)$  YES BELOW UPPER BOUND
    - $O(n)$  YES BELOW UPPER BOUND
    - $O(n\log_2(n))$  YES BELOW UPPER BOUND
    - $O(n^1)$  YES BELOW UPPER BOUND
    - this helps in thinking solution limits and optimisation
    - solution can be minimal, not exact  $O(n^3)$
    - but still we got to know our limits
- Approach optimal
  - => Generalise the condition
    - $a_1 + a_2 = a_2 + a_3 = \dots = a_{n-1} = a_n$  atq
    - $\Rightarrow a_{i-1} + a_i = a_i + a_{i+1}$
    - $\Rightarrow a_{i-1} + a_i(\text{cancelled}) = a_i(\text{cancelled}) + a_{i+1}$
    - $\Rightarrow a_{i-1} = a_{i+1} !!!$
    - i.e.  $a_1=a_3=a_4=a_5=\dots \&& a_2=a_4=a_6=\dots$
  - odd index positions should have same nos && even index positions should have same nos
  - NO when i have more than or equal to 3 distinct integers in my array, eg: 1 1 2 3 => no, you cant create any fair ordering
    - => Case of 3 Distinct Integers
  - ELSE NOW if we have N1 & N2, freq. f1, f2
    - we want either of both cases in n=6
      - { N1 N2 N1 N2 N1 N2 }
      - { N2 N1 N2 N1 N2 N1 }
      - $\Rightarrow f1=f2$  AT ODD N
      - YES
    - n=7
      - { N1 N2 N1 N2 N1 N2 N1 }

- { N2 N1 N2 N1 N2 N1 N2 }
- => f1=f2 +1
- => f2=f1 +1
- => abs(f1-f2) = 1 AT EVEN N
- if not then we cant achieve our **ai-1 = ai+1** !!!, then NO
- => Case of 2 Distinct Integers
- => Case of 1 Distinct Integers
  - N1 , any n
  - then N1 N1 N1 N1 ...
  - whole array same
  - direct YES
- else NO

```
#include<bits/stdc++.h>
using namespace std;
int main(){

    // t
    // mini tests
    int t;
    cin>>t;
    while (t--){
        long long n;
        cin>>n;
        vector<long long> a(n, 0);
        // vector input
        for (long long i=0; i<n; i++) {cin>>a[i];} //n

        // freq map
        map<long long, long long> freq_map;
        for (long long i =0; i<n; i++){//n
            freq_map[a[i]]++; //logn
        }
        //nlogn

        if (freq_map.size()>=3) cout<<"No"<<endl;
        else {

            // begin- first element
            // rbegin- last element

            long long freq1 = freq_map.begin()->second;
            long long freq2 = freq_map.rbegin()->second;

            //odd size array
            if (freq1==freq2) cout<<"Yes"<<endl;
            else if ( n%2 ==1 && abs(freq1-freq2)==1) cout<<"Yes"<<endl;
            else cout<<"No"<<endl;
        }
    }
}
```

```

    return 0;
}

// TC O(nlog2n) = O(100*log2(100)) = O(100*7) = O(700)
// SC O(n+n) = O(2n) = O(200)

// this problem is imp to teach map,begin,rbegin iterators

```

- this problem is imp to teach map,begin,rbegin iterators

```

// freq map
map<long long, long long> freq_map;
for (long long i = 0; i < n; i++){//n
freq_map[a[i]]++; //logn
}

```

```
if (freq_map.size() >= 3) cout << "No" << endl;
```

```

// begin- first element
// rbegin- last element

long long freq1 = freq_map.begin() -> second;
long long freq2 = freq_map.rbegin() -> second;

```

- Approach Brute force

- Similar thinking but not organised enough at first try out of clue
- Read number of test cases **t**
- For each test case:
  - Read array size **x**
  - Read **x** elements into array **v1**
  - Make a copy **v2** and sort it
  - Make a copy **v3** from **v2** and remove duplicates from **v3**
  - If **v3.size() > 2**, return "NO"
  - If all elements are equal, return "YES"
  - If array size is even:
    - If frequency of smallest and largest elements is equal, return "YES"
  - If array size is odd:
    - If the frequency difference between smallest and largest elements is exactly 1, return "YES"
    - If array size is 2, return "YES"
    - Else, return "NO"

```

#include<bits/stdc++.h>
using namespace std;
string goodAPCheck(int x){
    vector<int> v1(x);
    for ( int i=0; i<x; i++) cin>>v1[i];
    vector<int> v2=v1;
    sort(v2.begin(),v2.end());

    vector<int> v3=v2;
    // remove duplicates
    v3.erase(unique(v3.begin(),v3.end()),v3.end());
    if (v3.size()>2 ) return "NO";

    if (count(v1.begin(), v1.end(),v2[0])==x) return "YES";
    if (x%2==0 && count(v1.begin(), v1.end(),v2[0])==count(v1.begin(),
v1.end(),v2[x-1])) return "YES";
    if(x%2!=0 && (count(v1.begin(), v1.end(),v2[0])==count(v1.begin(),
v1.end(),v2[x-1])+1 ||count(v1.begin(),
v1.end(),v2[0])+1==count(v1.begin(), v1.end(),v2[x-1]))) return "YES";
    if(x==2) return "YES";
    else return "NO";
}

int main(){

    long long t;
    cin>>t;
    while(t--) {
        int x = 0;
        cin>>x;
        cout<<goodAPCheck(x)<<"\n";
    }
    return 0;
}

```

## 07 A Don't Try to Count

- <https://codeforces.com/problemset/problem/1881/A>
- brute force, strings, \*800
- Analysis
  - string x, len n
  - string s, len m
  - $n*m \leq 25$ 
    - 1, 25
    - 5, 5
    - 25, 1
  - operation ANY\_TIMES

- if  $x = "abc"$
- $x = x+x = "abcabc"$
- Find
  - min. no of operation by which
  - $s$  is substring of  $x$
- Expected TC?
  - tlpt 2sec atq
    - $t = 10^4$  max atq
    - $1\text{sec} = 2 \times 10^8$  ops per test
    - $\text{ops/minitest} = 2 \times 10^8 / 10^4 = 210^4$  ops = 20000 ops =  $25 \times 10^2$  ops
    - $n \times m = 25$  max atq
    - $O(nm10^2)$  Upper bound Expected TC
  - mlpt 256mB atq
- Approach Brute Force Tuts
  - where do i finally say ,this is the end ?
    - $x \rightarrow x+x \rightarrow x+x + x+x \rightarrow \dots \rightarrow$  not infinity but a upperbound
    - arguement = upper bound is 5
    - should not go beyond 5
    - $n \rightarrow x, m \rightarrow s$
    - worst,  $n=1, m=25$
    - eg :  $x='a', s='aa\dots 25times\dots a'$
    - $x.size() < s.size()$ , till this condition is true, you can never find  $s$  within  $x$
    - $a \Rightarrow aa \Rightarrow aaaa \Rightarrow a..8..a \Rightarrow a..16..a \Rightarrow a..32..a$
    - $1 \Rightarrow 2 \Rightarrow 4 \Rightarrow 8 \Rightarrow 16 \Rightarrow 32$ (its enough ,more than 25 to become super set ), these changes done within 5 operation
    - if not done in even 5 operations then ,at 6,  $x=a\dots 64..a$
    - if couldnt find str in 25 ,then you can't find in 64 or more ... .answer is impossible => -1

```
#include<bits/stdc++.h>
using namespace std;
bool check(string s, string x)
{
    if (x.size() < s.size()) return false;
    for (int i=0; i < x.size() - s.size() + 1; i++) if (x.substr(i, s.size()) == s)
        return true; // x.substr(i, s.size()) == s substring extract
    return false;
}// O((n-m+1)*m) = O(n*m)
int main(){
    int t;
    cin >> t;
    while (t--) {
        long long n, m;
        cin >> n >> m;
        string x, s;
        cin >> x >> s;

        string x0 = x;
        string x1 = x0 + x0;
```

```

        string x2 = x1+x1;
        string x3 = x2+x2;
        string x4 = x3+x3;
        string x5 = x4+x4;

        long long ans = -1;
        if(check(s,x0)) ans=0;
        else if (check(s,x1)) ans=1;
        else if (check(s,x2)) ans=2;
        else if (check(s,x3)) ans=3;
        else if (check(s,x4)) ans=4;
        else if (check(s,x5)) ans=5;
        cout<<ans<<endl;

    }return 0;
}
//187 ms    100 KB
// TC O(2^5 *n*m) = O(32*n*m)
// SC O(2^5*n) = O(32*n)

```

- Approach optimal Mine
  - SAME
  - input t testcases
  - each test cases
    - input n,m
    - Wrong, as babb,bbb ,its not -1
    - check if x is substring of s+s
      - if no
        - then x ,even mul by infinite can't be superset or in any combination of s
        - and we took s+s as maybe x="mara", s="rama"
        - return -1
      - if yes
        - then its possible
  - counter=0
  - while counter<=5
    - concatnate till s is substring of x
      - counter++
  - return counter
  - why counter =5 ??
    - counter=m\*n
    - NO, Memory limit exceeded on test 2 1734 ms 262100 KB

```

#include<bits/stdc++.h>
using namespace std;
int checkCount(string x,string s){

```

```

int counter = 0;

while (counter<=5){
    if ((x).find(s) != string::npos){
        return counter;
    }
    counter++;
    x=x+x;
}

return -1;
};

int main(){
    long long t;
    cin >> t;
    while(t--){
        int n=0, m=0;
        string x="", s="";
        cin>>n>>m>>x>>s;

        // if ((s+s).find(x) == string::npos){
        //     cout<<-1<<"\n";
        // }
        // else{
            cout<<checkCount(x,s)<<"\n";
        // }
    }

    return 0;
}

// passed 58 tests containing test cases :)
// 109 ms    100 KB
// Time Complexity: O(n * m)
// Space Complexity: O(n + m) (worst case 32n + m).

```

## 08 A How Much Does Daytona Cost?

- <https://codeforces.com/problemset/problem/1878/A>
- greedy, \*800
- Analysis
  - array a
  - size n
  - int k
  - Find?
    - if exists subsegment(sub array) of a where k is most common element

- $a = \{a_0, a_1, \dots, a_{n-1}\}$
- $n, k$
- subarray
  - $\{a_1, a_2, a_3\}$
  - $\{a_1\}$
  - $\{a_1, a_2\}$
  - $\{a_3, a_4\}$
- eg:  $n=5, k=4, a=\{1, 4, 3, 4, 1\}$ 
  - $\Rightarrow \{4, 3, 4\}$
  - $\Rightarrow \text{YES}$
- Expected TC?
  - tlpt 1sec atq
  - mlpt 256mB atq
  - t max 1000 atq
  - n max 100 atq
  - 1 sec =  $10^8$  ops
  - $tlpmt = 10^8 / 1000 = 10^5$
  - $O(100^3) = 10^6 \text{ NO}$
  - $O(100^2) = 10^4 \text{ YES}$
  - Expected TC =  $tcpmt = O(n^2)$
- Approach optimal
  - IF  $k$  is present in array anywhere, then answer is YES, else no
  - $a = \{a_0, a_1, a_2, k, a_4, \dots, a_n\}$
  - we haven't told lenght of subarray
  - we can take length = 1,  $\{k\}$  is correct too, now in this subarray,  $k$  is the highest occurance as  $k$  is only

```
#include<bits/stdc++.h>
using namespace std;
int main(){
    int t; cin >> t; while(t--){long long n, k; cin >> n >> k;
    long long a[n]; for (int i=0; i<n; i++) cin >> a[i];
    long long number_is_present = 0;
    for (int i=0; i<n; i++){if (a[i]==k) {number_is_present=1; break;}}
    if(number_is_present) cout << "YES" << endl;
    else cout << "NO" << endl;}return 0;
}
// TC O(n)
// SC O(n)
```

- Approach Brute Force
  - SAME nearly
  - One sec,
    - if number exists
      - if array size is 2 or 1
      - or if anywhere  $a[i]=a[i+1]=k$

- or if its > 2
  - if in array bw that 1st occur and last occur ,that number the most occur
- return yes if any satisfy, else no : 0
- FREAKING, the the limits, loopholes are hidden
- functions returns > if else with breaks
- if number exists
  - then its largest at subarray len = 1

```
// template miniTests int1 int2 vectorArrayInt1
#include<bits/stdc++.h>
using namespace std;
string mainGame(int x1, int x2, vector<int> v1){
    // code here
    // x1 n
    // x2 k
    // v1 a
    for ( int i =0; i<x1; i++ ){
        if (x2==v1[i]) {return "YES";}
    }
    return "NO";
}

void eachMiniTest(){
    int x1=0, x2=0;// factor1 factor2
    cin>>x1>>x2;
    vector<int> v1(x1);

    for (int i=0; i<x1; i++ ) cin>>v1[i];
    cout<< mainGame(x1,x2,v1)<<"\n";
}

int main(){
    long long t; //mini test cases
    cin>>t;
    while(t--){
        eachMiniTest();
    }

    return 0;
}
```

## 09 Goals of Victory

- <https://codeforces.com/problemset/problem/1877/A>
- math, \*800
- Analysis
  - Expected TC ?
    - tlpt 1sec atq

- mlpt 256 mB atq
- t max 500 atq = 5\*100
- n max 100 atq
- 1sec =  $10^8$  ops
- tlpmt =  $10^8 / 500$
- Approach
  - given
    - n teams in tournament
    - each match
      - each pair of teams match up once
      - after every match
        - 2 int, as result of match, 2 goals of 2 teams
    - efficiency of team = total no. of goals in each of its matches. - total opponents score in each of its matches.
  - to find
    - efficiency array of each team, one missing
    - a<sub>1</sub>, a<sub>2</sub>, a<sub>3</sub>, ..., a<sub>n-1</sub>
    - n-1 teams
    - efficiency of missing team?
      - it can be uniquely determined
  - input
    - t(tests)
    - n(teams) 1
    - efficiencies of n-1 teams 1
    - n(teams) 2
    - efficiencies of n-1 teams 2
    - ...
  - output
    - missing effiency 1
    - missing effiency 2
    - ...
- Approach 1 -- brute force -- optimal
  - suppose 4 teams
    - n<sub>1</sub> n<sub>2</sub> n<sub>3</sub> n<sub>4</sub> teams
      - matches (in pairs)
        - n<sub>1</sub> n<sub>2</sub> => scores a<sub>1</sub> b<sub>1</sub>
        - n<sub>1</sub> n<sub>3</sub> a<sub>2</sub> c<sub>1</sub>
        - n<sub>1</sub> n<sub>4</sub> a<sub>3</sub> d<sub>1</sub>
        - n<sub>2</sub> n<sub>3</sub> b<sub>2</sub> c<sub>2</sub>
        - n<sub>2</sub> n<sub>4</sub> b<sub>3</sub> d<sub>2</sub>
        - n<sub>3</sub> n<sub>4</sub> d<sub>3</sub> c<sub>3</sub>
      - e<sub>1</sub> e<sub>2</sub> e<sub>3</sub> e<sub>4</sub> eff.s
    - so
      - e<sub>1</sub> = a<sub>1</sub> + a<sub>2</sub> + a<sub>3</sub> - b<sub>1</sub> - c<sub>1</sub> - d<sub>1</sub> = 3
      - e<sub>2</sub> = b<sub>1</sub> + b<sub>2</sub> + b<sub>3</sub> - a<sub>1</sub> - c<sub>2</sub> - d<sub>2</sub> = -4
      - e<sub>3</sub> = c<sub>1</sub> + c<sub>2</sub> + c<sub>3</sub> - a<sub>2</sub> - b<sub>2</sub> - d<sub>3</sub> = 5

- $e4 = d1 + d2 + d3 - a3 - b3 - c3$
- $e1 + e2 + e3 + e4 = 0$  (oh, just found out !!! )
  - $e4 = -(e1+e2+e3)$  (SOLVED!!!)
  - $e4 = -(3-4+5) = -4$
- Formalised
  - Problem Insight
    - Each goal scored by a team increases its own efficiency by 1.
    - The same goal decreases the opponent's efficiency by 1.
    - So for every goal, the total sum of efficiencies changes by +1 and -1.
    - Net change in total efficiency is always 0.
  - Key Observation
    - Initially, before any match, all teams have efficiency 0.
    - So the total sum of efficiencies starts at 0.
    - Since the sum never changes, the final sum of efficiencies is also 0.
  - Given
    - There are n teams.
    - Efficiencies of n – 1 teams are given.
    - One team's efficiency is missing.
  - Logic to Find Missing Efficiency
    - Let the given efficiencies be: A1, A2, A3, ..., An-1
    - Let the missing efficiency be An.
    - Since total sum is 0: A1 + A2 + A3 + ... + An-1 + An = 0
    - Therefore: An = -(A1 + A2 + A3 + ... + An-1)
  - Algorithm
    - Read n.
    - Read the n – 1 efficiencies.
    - Compute their sum.
    - Output the negative of this sum.
  - Complexity
    - Time complexity: O(n)
    - Space complexity: O(1)

```
#include<bits/stdc++.h>
using namespace std;
int main(){
    // Read Question and Analyse it Bit-by-bit
    // write all pts in depth, leave no missing dots
    // then dots will connect easily and will give you answer
    ios::sync_with_stdio(0);
    cin.tie(0);
    int t=0;// safe ,no to garbage entry
    cin>>t;
    while(t--){
        int n=0;// safe ,no to garbage entry
        cin>>n;
        n--;// we have n-1 entries
        int res=0;// safe ,no to garbage entry
        while(n--){
            /
```

```

        int buff=0;// safe ,no to garbage entry
        cin>>buff;
        res+=buff;
    }
    res=res*(-1);
    cout<<res<<"\n";
}

}
return 0;
}

```

```

#include <bits/stdc++.h>
using namespace std;

int main()
{
    int t; // Variable to store the number of test cases
    cin >> t; // Read the number of test cases
    while (t--) // Loop through each test case
    {
        long long n; // Variable to store the number of teams
        cin >> n; // Read the number of teams
        long long a[n]; // Array to store the efficiency of n-1 teams
        for (long long i = 0; i < n - 1; i++) // Loop to read the
efficiency of n-1 teams
            cin >> a[i]; // Read efficiency of each team
        // inputs

        long long sum = 0; // Variable to store the sum of efficiencies of
n-1 teams
        for (long long i = 0; i < n - 1; i++) // Loop to calculate the sum
of efficiencies
            sum += a[i]; // Add each team's efficiency to the sum

        cout << -1 * sum << endl; // Output the efficiency of the missing
team, which is the negative of the sum
    }
    return 0; // Return 0 to indicate successful execution
}

// Time Complexity (TC): O(n) = O(100)
// Space Complexity (SC): O(n) = O(100)

```

## 10 Target Practice

- <https://codeforces.com/problemset/problem/1873/C>
- implementationmath, \*800
- Analysis
  - tc and sc

- 1sec =  $10^8$  ops
- tlpt = 1sec
- 1 test =  $10^8$  ops
- 1 test = 1000 mtest
- => tlpm =  $10^8 / 10^3 = 10^5$  ops =  $O(n^5)$  max allowed and n = 10 (10x10matrix)
- mlpt = 256mb
- given board
- 10x10
- each ring deeper, more points, outermost is 1, innermost is 5
- person shot "X" in grid of 10x10 "."
- Find?
  - Scores
- technically

```
0123456789
```

```
1111111111 0
1222222221 1
1233333321 2
1234444321 3
1234554321 4
1234554321 5
1234444321 6
1233333321 7
1222222221 8
1111111111 9
```

```
0 1234 5678 9
```

```
1 1111 1111 1 0
```

```
1 2222 2222 1 1
1 2333 3332 1 2
1 2344 4432 1 3
1 2345 5432 1 4
```

```
1 2345 5432 1 5
1 2344 4432 1 6
1 2333 3332 1 7
1 2222 2222 1 8
```

```
1 1111 1111 1 9
```

- condition of scoring
  - 1
    - 0,0 to 9,0 L 00 10 20 30 40 50 60 70 80 90
    - 0,9 to 9,9 R 09 19 29 39 49 59 69 79 89 99
    - - 0,0 to 0,9 T 00 01 02 03 04 05 06 07 08 09

- 9,0 to 9,9 B 90 91 92 93 94 95 96 97 98 99
- relation
  - i=0 or 9
  - j=0 or 9
  - 1 = 0+1 == 10-9
- 2
  - 1,1 to 8,1 L 11 21 31 41 51 61 71 81
  - 1,8 to 8,8 R 18 28 38 48 58 68 78 88
  - 
  - 1,1 to 1,8 T 11 12 13 14 15 16 17 18
  - 8,1 to 8,8 B 81 82 83 84 85 86 87 88
  - relation
    - i,j = 1 or 8
    - 1 = 1+1 == 10-8
- 5
  - 4,4
  - 4,5
  - 5,4
  - 5,5
- this not 2D Array
- this is char incoming
- Approach 1 -- brute force
  - The grid is fixed at  $10 \times 10$  and consists of 5 concentric square rings, where the outermost ring gives 1 point and each inner ring gives one more point, up to 5 at the center
    - For every test case, we scan the grid cell by cell
      - When a cell contains 'X', we must determine which ring it belongs to
        - We simulate rings using two boundaries: **bound1** starting at 0 and **bound2** starting at 9
          - Ring 1 checks the outer boundary (row or column equal to 0 or 9)
          - Ring 2 checks the next inner boundary (1 or 8)
          - This continues until ring 5
        - If the current cell lies on any side of the current boundary square
          - (**row == bound1 || row == bound2 || col == bound1 || col == bound2**)
        - The current ring number is returned as the score
      - After each ring check, the boundaries are moved inward (**bound1++**, **bound2--**)
        - The returned ring score is added to the total score
    - After processing all cells, the accumulated score is printed
  - The idea works because each cell belongs to exactly one concentric square ring, and shrinking boundaries correctly model these rings without needing an extra 2D scoring array

```
#include<bits/stdc++.h>
using namespace std;
// 1
/*
```

```
00 01 02 03 04 05 06 07 08 09
10 19
20 29
30 39
40 49
50 59
60 69
70 79
80 89
90 91 92 93 94 95 96 97 98 99
*/
// 2
/*
11 12 13 14 15 16 17 18
21 28
31 38
41 48
51 58
61 68
71 78
81 82 83 84 85 86 87 88
*/
int calScore(int row, int col, char c){
    int bound1 =0;
    int bound2 =9;

    for ( int ring =1; ring<=5; ring++){
        if ( (row==bound1) || (row==bound2) ){ return ring;}
        else if ((col==bound1) || (col==bound2)) {return ring;}

        bound1++;bound2--;
    }
    return 0; // fallback
}
void miniTest(){
    int finalScore=0;
    for (int row=0; row<10; row++){
        for (int col=0; col<10; col++){
            char c;
            cin>>c;
            if (c=='X') finalScore+=calScore(row,col,c);
        }
    }
    cout<<finalScore<<"\n";
}
int main(){
    ios::sync_with_stdio(0);
    cin.tie(0);
    int t;
    cin>>t;
    while(t--){
        /
    }
}
```

```

        miniTest();
    }
    return 0;
}
// Approach 1: Time complexity is O(1) per test case (100 cells × 5 rings,
all constants) and space complexity is O(1).

```

- Approach 2 -- optimal
  - The grid is fixed at 10×10 and forms 5 concentric square rings with scores from 1 (outermost) to 5 (innermost)
    - For each test case, the grid is read cell by cell
      - When a cell contains 'X', its score depends only on how close it is to the nearest border
      - Compute the distance from the cell to all four edges:
        - top → i
        - left → j
        - bottom → 9 - i
        - right → 9 - j
      - The minimum of these four values gives the ring index (0-based)
        - 0 → outer ring, 1 → second ring, ..., 4 → center
      - Add 1 to convert the index into the actual score
        - score += min({i, j, 9 - i, 9 - j}) + 1
      - Repeat for all 100 cells
      - After processing the grid, output the total score
    - The intuition is that every step away from the border moves one ring inward, so the closest border uniquely determines the ring of any cell

```

#include<bits/stdc++.h>
using namespace std;

int calScore(int row, int col, char c){
    int top = row;
    int left = col;
    int bottom = 9 - row;
    int right = 9 - col;
    return min({top, bottom, left, right})+1; // fallback
}

void miniTest(){
    int finalScore=0;
    for (int row=0; row<10; row++){
        for (int col=0; col<10; col++){
            char c;
            cin>>c;
            if (c=='X') finalScore+=calScore(row,col,c);
        }
    }
    cout<<finalScore<<"\n";
}

```

```

}

int main(){
    ios::sync_with_stdio(0);
    cin.tie(0);
    int t;
    cin>>t;
    while(t--){
        miniTest();
    }
    return 0;
}

// Approach 2: Time complexity is O(1) per test case (100 cells, constant
// work per cell) and space complexity is O(1).

```

```

#include <bits/stdc++.h>
using namespace std;

int main() {
    ios::sync_with_stdio(false);
    cin.tie(nullptr);

    int t;
    cin >> t;

    while (t--) {
        int score = 0;
        for (int i = 0; i < 10; i++) {
            for (int j = 0; j < 10; j++) {
                char c;
                cin >> c;
                if (c == 'X') {
                    score += min({i, j, 9 - i, 9 - j}) + 1;
                }
            }
        }
        cout << score << '\n';
    }
}

```

- Approach 3 -- optimal
  - A predefined  $10 \times 10$  **score** matrix stores the score of each cell based on its concentric ring on the target
  - The number of test cases **t** is read, and each test case is processed independently
  - For each test case, a  $10 \times 10$  character grid is read row by row and stored
  - The grid is scanned cell by cell to check for the presence of '**X**' (an arrow hit)
  - Whenever an '**X**' is found, the corresponding value from the **score** matrix is added to **total\_score**
  - After scanning all 100 cells, the final accumulated score is printed for that test case

- Time complexity is  $O(1)$  per test case (fixed  $10 \times 10$  grid), and space complexity is  $O(1)$  since all data structures are of constant size

```
#include<bits/stdc++.h>
using namespace std;

// Predefined score matrix representing the target's rings
// Each element represents the score for that position on the target
const int score[10][10] = {
    {1,1,1,1,1,1,1,1,1,1},
    {1,2,2,2,2,2,2,2,2,1},
    {1,2,3,3,3,3,3,3,2,1},
    {1,2,3,4,4,4,4,3,2,1},
    {1,2,3,4,5,5,4,3,2,1},
    {1,2,3,4,5,5,4,3,2,1},
    {1,2,3,4,4,4,4,3,2,1},
    {1,2,3,3,3,3,3,3,2,1},
    {1,2,2,2,2,2,2,2,2,1},
    {1,1,1,1,1,1,1,1,1,1}
};

int calScore(int row, int col, char c){
    return score[row][col];
}

void miniTest(){
    int finalScore=0;
    for (int row=0; row<10; row++){
        for (int col=0; col<10; col++){
            char c;
            cin>>c;
            if (c=='X') finalScore+=calScore(row,col,c);
        }
    }
    cout<<finalScore<<"\n";
}

int main(){
    ios::sync_with_stdio(0);
    cin.tie(0);
    int t;
    cin>>t;
    while(t--){
        miniTest();
    }
    return 0;
}

// Time complexity is  $O(1)$  per test case (fixed  $10 \times 10$  grid), and space complexity is  $O(1)$  since all data structures are of constant size
```

# 11 Ambitious Kid

- <https://codeforces.com/problemset/problem/1866/A>
- math, \*800
- Analysis
  - What the question gives:
    - An array of N integers (can be positive, negative, or zero)
    - One operation allows increasing or decreasing any single element by 1
    - Unlimited operations are allowed on any elements
  - What the question asks:
    - Find the minimum number of operations needed so that
      - the product of all elements in the array becomes 0
    - eg: [2,3,4] mul = 24
      - op1(-1): [1,3,4] mul = 12
      - op2(-1): [0,3,4] mul = 0 !!!
    - eg: [-2,3,4] mul = -24
      - op1(+1): [-1,3,4] mul = -12
      - op2(+1): [0,3,4] mul = 0 !!!
  - Key observation:
    - A product is 0 if and only if at least one element is 0
    - $\min(A_1, A_2 \dots A_n) = \text{solution}$
  - tc
    - tlpt 1sec
    - mlpt 256mb
    - 1sec =  $10^8$  ops
    - ops per testcase =  $10^8 / 1 = 10^8$
    - total minitests = 1
    - tlpmt =  $10^8$  ops
    - $N = 10^5$
    - $O(N^2) \Rightarrow 10^{10} \Rightarrow \text{NO}$
    - $O(N \log 2N) \Rightarrow \text{YES}$
    - $O(N) \Rightarrow \text{YES}$
    - $O(\log 2N) \Rightarrow \text{YES}$
    - $O(1) \Rightarrow \text{YES}$
    - Expected TC  $\Rightarrow O(N^2)$
- Approach 1 -- brute force -- optimal
  - To make the product of all elements equal to 0, at least one element must be 0
    - So we only need to convert one element to 0 with minimum operations
  - Each operation changes a number by +1 or -1
    - Therefore, converting any element  $A_i$  to 0 takes  $|A_i|$  steps
  - Intuition:
    - The element closest to 0 needs the fewest steps
      - For [2, 3, 4]  $\rightarrow$  closest is 2  $\rightarrow$  2 steps
      - For [-2, -3, -4]  $\rightarrow$  take absolute values [2, 3, 4]  $\rightarrow$  closest is 2  $\rightarrow$  2 steps
  - Steps:
    - Read N

- For each element:
  - Convert it to absolute value (represents steps needed to reach 0)
- Find the minimum value among all absolute values
  - This value is the answer
- Complexity:
  - Time Complexity: O(N)
  - Space Complexity: O(N)

```
#include<bits/stdc++.h>
using namespace std;
int main(){
    int n;
    cin >> n;
    vector<int> v1(n, 0);
    for (int i=0; i<n; i++){
        int i1 = 0;
        cin >> i1;
        v1[i] = (i1 >= 0) ? i1 : (i1 * -1); // or v1[i] = abs(i1);
    }
    cout << *min_element(v1.begin(), v1.end()); // min_element & max_element
    return pointer
    // not sort then v1[1] as its nlogn
    return 0;
}
// TC O(n)
// SC O(n)
```

- Approach 2 -- optimal
  - Read integer N
  - Read the array of N integers
  - Initialize a variable min\_ops to a very large value
    - This will store the minimum operations required
  - For each element in the array:
    - Compute the absolute value |Ai|
      - This represents the number of operations needed to make Ai equal to 0
    - Update min\_ops with the minimum of current min\_ops and |Ai|
  - Output min\_ops
    - This is the minimum number of operations needed to make the product of the array equal to 0
  - Reasoning:
    - The product becomes 0 if at least one element is 0
    - Making the element closest to 0 reach 0 requires the fewest operations
  - Complexity:
    - Time Complexity: O(N)
    - Space Complexity: O(N)

```
#include<bits/stdc++.h>
using namespace std;
int main()
{   long long n; cin>>n;
    long long a[n];
    for ( int i=0; i< n; i++){cin>> a[i];} //n
    long long min_ops = INT_MAX;
    for ( int i=0; i< n; i++){min_ops=min(min_ops,abs(a[i]));} //n
    cout<<min_ops;
    return 0;
}
// TC O(n)
// SC O(n)
```

## 12 Sequence Game

- <https://codeforces.com/problemset/problem/1862/B>
- constructive algorithms, \*800
- Analysis
  - backcreate/guessback/reverse engineering!!!
  - tc
    - tlpt = 2 sec
    - 1sec =  $10^8$  ops
    - mlpt = 256 mb
    - mt max =  $10^4$
    - n max =  $2 \times 10^5$
    - Ques Line "The sum of the values of n over all test cases does not exceed  $2 \times 10^5$ "
      - this sum of minitest element length  $\leq 2 \times 10^5$
      - its the main bottleneck
      - so we can assume not  $10^4$ , but only 1 test case with  $n = 2 \times 10^5$ 
        - no need to cal tlpmt
    - 1 test =  $2 \times 10^8$  ops
    - $O(n^2) \Rightarrow (2 \times 10^5)^2 \Rightarrow 4 \times 10^{10} > 2 \times 10^4$
    - $O(n^2)$  No ( $4 \times 10^{10} > 2 \times 10^4$ )
    - $O(n \log 2n)$  Yes ( $< 2 \times 10^4$ )
    - $O(n)$  Yes
    - $O(\log 2n)$  Yes
    - ...  $O(1)$  Yes
    - $\Rightarrow$  so avoid making  $O(n^2) / 2$  nested loops in code!!!
  - Ques
    - Tema and Vika Plays a game
    - Vika : a= +ve int, len m
    - b= new sequence, acc to rule
      - a1 as 1st element
      - then ai ( $2 \leq i \leq m$ ) such that  $a_{i-1} \leq a_i$
      - length of this seq n
    - eg:

- $a = [4, 3, 2, 6, 3, 3]$
- $b = [4, 6, 3]$
- analysis

```
a 6 [4 3 2 6 3 3]
Y N N Y N Y
b 3 [4       6       3]
```

```
4 1st element YES => b1
3>=4 => NO (ai-1 <= ai)
2>=3 => NO
6>=2 => YES => b2
3>=6 => NO
3>=3 => YES => b3
```

- then vika gives b to temu and temu tries to guess seq a
- help vika to guess atleast 1 num.

- Note that the length of the sequence you output should not exceed the input sequence length by more than two times.
- Test Cases
  - input
    - $t (1 \leq t \leq 10^4)$
    - $n$
    - $b_1 b_2 \dots b_n$
    - The sum of the values of  $n$  over all test cases does not exceed  $2 \times 10^5$
  - for each test, output gives 2 lines
    - $m$
    - $a_1 a_2 \dots a_m$
  - mt1
    - 3
    - 4 6 3
    - out
    - 6
    - 4 3 2 6 3 3

```
b [4 6 3]
possibilities
a [4 3 2 6 3 3] (as described in question)
a [4 6 3 3] also possibilities
... so on , make/guess any, if fits the rule then good !!!
```

- mt2
  - 3

- 1 2 3
- out
- 3
- 1 2 3
- In the second sample, Vika could have chosen the original sequence.
- mt3
  - 5
  - 1 7 9 5 7
  - out
  - 6
  - 1 7 9 3 5 7

```
b 1 < 7 < 9 > 5 < 7  
a 1     7     9 ..5     7
```

9 and 5 can't relate as b coming from a  
untill and unless there is unlikely element which exists in  
a which is <9 and <5

possibilities

```
1 7 9 3 5 7  
1 7 9 6 5 7  
1 7 9 5 5 7  
... so on
```

- mt4
  - 1
  - 144
  - out
  - 1
  - 144

- mt5
  - 2
  - 1 1
  - out
  - 2
  - 1 1

- mt6
  - 5
  - 1 2 2 1 1
  - out
  - 6
  - 1 2 2 1 1 1

- If there are multiple suitable sequences, you can output any of them

- Approach 1 -- optimal

- Based on Hint
  - if  $b[i-1] > b[i]$
  - append  $b[i]$  twice

```
a1 a2 a3 a4 ... am
to b1 b2 b3 b4 ... bn
where generally  $b_1 < b_2 < b_3 < b_4 \dots$  ( as only  $a_{i-1} < a_i$  are inserted
in the array of b)
```

there can be numerous possibilities (  $a_1 > a_2 < a_3$ )  
 one of them can be like ( $a_1 > a_2 = a_3$ ), we are only considering this  
 possibility and reverse enginner it..  
 so if  $b_1 < b_2 > b_3 < b_4$  (where  $b_3$  dont make sense)  
 then a would be  $b_1 < b_2 < b_3 = b_3 < b_4$  (to make sense)

- insert all mini test elements into arr b
- then traverse b to append into arr a
  - use the hint
- Reasoning
  - If there are multiple suitable sequences, you can output any of them. (in ques)
  - don't confused by inputs and outputs given, use what question demands and make your own outputs

```
#include<bits/stdc++.h>
using namespace std;
int main(){
    ios::sync_with_stdio(0);
    cin.tie(0);
    int mt=0;
    cin>>mt;
    while(mt--){
        int n=0;
        cin>>n;
        vector<int> b(n);
        for(int i=0; i<n; i++){ //n
            cin>>b[i];
        }
        // input done
        // main output
        vector<int> a;
        a.push_back(b[0]); //1
        for(int i=1; i<n; i++){ // n
            if(b[i-1]>b[i]){
                a.push_back(b[i]); //1
            }
            a.push_back(b[i]);
        }
        cout<<a.size()<<"\n";
        for(int i=0;i<a.size(); i++){ // n
    }}
```

```
        cout<<a[i]<<" ";
    }
    cout<<"\n";
}

// Time Complexity (TC): O(n) = O(2*10^5)
// Space Complexity (SC): O(n) = O(2*10^5)
```

```
#include <bits/stdc++.h>
using namespace std;

int main()
{
    int t; // Number of test cases
    cin >> t;
    while (t--)
    {
        long long n; // Length of sequence b
        cin >> n;
        vector<long long> b(n), a; // Vector b to store input sequence,
vector a to store the reconstructed sequence
        for (int i = 0; i < n; i++) // Loop to read the sequence b
            cin >> b[i];
        // Initial input of sequence b is completed

        a.push_back(b[0]); // Always add the first element of b to a
        for (int i = 1; i < n; i++) // Loop through the rest of the
sequence b
        {
            if (b[i] >= b[i - 1])
                a.push_back(b[i]); // If current element is greater than or
equal to the previous, add it to a
            else
            {
                a.push_back(b[i]); // Add the current element to a
                a.push_back(b[i]); // Add the current element again to a to
ensure a[i-1] <= a[i]
            }
        }
        cout << a.size() << endl; // Output the size of the reconstructed
sequence a
        for (auto it : a) // Output each element of the sequence a
            cout << it << " ";
        cout << endl; // New line after each test case
    }
    return 0;
}
```

```
// Time Complexity (TC): O(n) = O(2*10^5)
// Space Complexity (SC): O(n) = O(2*10^5)
```

# TipsCollectedFromExperiences

---

- Read Question and Analyse it Bit-by-bit
  - write all pts in depth, leave no missing dots
  - reconstruct the test cases with your written logic
    - test cases are misleading and full of confusion
  - then dots will connect easily and will give you answer
- when check TC& SC of program, don't consider TestCasesLoop&Spaces in counting
- 1sec =  $10^8$  Operations
- if 1sec = totalTests
  - operationsPerTestCase =  $10^8 / \text{totalTestCases}$
  - if totalTestCases = 100
    - operationsPerTestCase =  $10^6$  operations
    - $O(n^3)$  is UpperLimit of the question's code
      - as  $O(n^3) = O(100^3) = 10^6 == \text{operationsPerTestCase}$
- always think of extra testcases
- if Expected TC =  $O(n^3)$ , then
  - $O(n^4)$  NO ABOVE UPPER BOUND
  - $O(n^3)$  YES UPPER BOUND
  - $O(n^2)$  YES BELOW UPPER BOUND
  - $O(n)$  YES BELOW UPPER BOUND
  - $O(n\log_2(n))$  YES BELOW UPPER BOUND
  - $O(n^1)$  YES BELOW UPPER BOUND
  - this helps in thinking solution limits and optimisation
  - solution can be minimal, not exact  $O(n^3)$
  - but still we got to know our limits
- and in cp submission, you can see testcases in ID :0
- FREAKING, the the limits, loopholes are hidden
- functions returns>if else with breaks
- => Generalise the condition in question 6R800
  - $a_1 + a_2 = a_2 + a_3 = \dots = a_{n-1} = a_n$  atq
  - $\Rightarrow a_{i-1} + a_i = a_i + a_{i+1}$
  - $\Rightarrow a_{i-1} + a_i(\text{cancelled}) = a_i(\text{cancelled}) + a_{i+1}$

- => ai-1 = ai+1 !!!
- i.e. a1=a3=a4=a5=.... && a2=a4=a6=....

- put this at 1st line of main() code, to fix bug of compiler at running test cases, not interactive program

```
ios::sync_with_stdio(0);
cin.tie(0);
```

- templates

```
// template miniTests int1 int2 vectorArrayInt1
#include<bits/stdc++.h>
using namespace std;
void mainGame(int x1, int x2, vector<int> v1){
    // code here

}

void eachMiniTest(){
    int x1=0, x2=0;// factor1 factor2
    vector<int> v1;
    cin>>x1>>x2;
    for (int i=0; i<x1; i++ ) cin>>v1[i];
    mainGame(x1,x2,v1);

}

int main(){
    ios::sync_with_stdio(0);
    cin.tie(0);
    long long t; //mini test cases
    cin>>t;
    while(t--){
        eachMiniTest();
    }

    return 0;
}
```

```
// template miniTests int1 int2 string
#include<bits/stdc++.h>
using namespace std;
void mainGame(int x1, int x2, string s){
    // code here

}

void eachMiniTest(){
```

```

        int x1=0, x2=0;// factor1 factor2
        string s;
        cin>>x1>>x2>>s;
        mainGame(x1,x2,s);

    }

int main(){
    ios::sync_with_stdio(0);
    cin.tie(0);
    long long t; //mini test cases
    cin>>t;
    while(t--){
        eachMiniTest();
    }

    return 0;
}

```

- Vectors CPP STL

```

vector<int> v1(n); // create ,with n elements mandatory
cin>>v1[0]; // insert
vector<int> v2 = v1; // copy
sort(v2.begin(),v2.end()); // sorting in stl, asc
bool compare= (v1==v2); // compare

```

```

#include<vector>
#include<iostream>
#include<algorithm>

```

- use `long long` instead of `int` for bigger stuff
- max/min : `max(var1 ,var2),min(var1, var2)`
  - make sure var1,var2 has SAME DATATYPE
  - inbuilt
- subarray = sub segment =segment taken out of array not manipulated ,no change in order
  - eg of a = {a0, a1, a2 ... an-1}, subarrs : {a0, a1}, {a1,a2,a3}, etc
- non-decreasing = increasing
- s is atmost k , means :  $s \leq k$
- atq : according to question
- How to Calculate Expected TC? eg: in 1R800

- tl per test = 1sec atq
  - 1sec =  $10^8$  Operations = per test operations
  - $1 \leq k \leq n$  (minitest)  $\leq 100$  acc.to ques (atq)
  - consider  $n=100$  upperbound
  - tl per mini test = 1sec /100
  - per mini test operations =  $10^8 / 100 = 10^6$
  - if tc per mini test =  $O(n^3)$ 
    - so  $n=100$ , then operation =  $O(n^3) = O(100^6)$  = per mini test operations
    - so  $O(n^3)$  is the upper bound
    - even sol. can have  $O(n^2)$ ,  $O(n)$ ,  $O(n\log n)$  etc. anything below  $O(n^3)$ , but not above  $O(n^3)$
  - Expected TC =  $O(n^3)$

```
// 1R800
// at extreme proof case use :
long long t;
```

```
// 1R800
// at n = 100 , tc = 100log100 = 100*7 = 700
// 2^7 ~ 100
// log2(n) = ln n / ln 2
```

```
// 1R800
// input, n order
cin>>v[i]; // n order

// vector copy, n order
vector<int> v2=v; // copy // n order

// sort stl func, n order
sort(v2.begin(), v2.end()); // nlogn order

// vector compare, n order
if (v2==v) // vector compare // n order
```

- tlpt = time limit per test
- 2secs =  $2 * (10^8)$  operations
- at 2R800 , tl per test = 2secs
  - 2secs =  $2 * (10^8)$  operations
  - t=1000 atq
  - time/testcase =  $O(2 * 10^5)$
  - n=50 max atq

- then at  $O(n^3) = O(125000) = O(1.25 * 10^5) \leq O(2 * 10^5)$
- TC for minitest = Expected TC =  $O(n^3)$  upper bound

```
• // max(a, b); O(1) // just checks (a < b)
  // min(a, b); O(1) // just checks (a < b)
  // max_element(v.begin(), v.end()); O(n)
  // min_element(v.begin(), v.end()); O(n)
```

- `vector<long long> v1(10, 0);` initialize safety vector
- :What the Fish Ques
- Parity
  - Parity is simply whether a number is even or odd.
  - Even parity: divisible by 2 (like 2, 4, 6, 8...)
  - Odd parity: not divisible by 2 (like 1, 3, 5, 7...)
- 6R800 this problem is imp to teach map,begin,rbegin iterators

```
// freq map
map<long long, long long> freq_map;
for (long long i = 0; i < n; i++){//n
    freq_map[a[i]]++; //logn
}
```

```
if (freq_map.size() >= 3) cout << "No" << endl;
```

```
// begin- first element
// rbegin- last element

long long freq1 = freq_map.begin()->second;
long long freq2 = freq_map.rbegin()->second;
```

- 11R800, you can use `INT_MAX INT_MIN` to initialise Extreme Value and compare as reference and play with it

```
long long min_ops = INT_MAX;
for (int i = 0; i < n; i++){min_ops = min(min_ops, abs(a[i]));} //n
```

# Array Coloring [ONSIGHT]

---

- <https://codeforces.com/problemset/problem/1857/A>
- greedy, math, \*800
- Analysis
  - given Array, n integers
  - to do
    - if you can
      - colour array elements in 2 groups/ 2 colors
      - parity of color 1 elements sum = parity of color 2 elements sum
      - print YES
    - else print NO
  - Parity
    - Parity is simply whether a number is even or odd.
    - Even parity: divisible by 2 (like 2, 4, 6, 8...)
    - Odd parity: not divisible by 2 (like 1, 3, 5, 7...)
  - eg: [1,2,4,3,2,3,5,4]
    - c1: [1,2,3] , c1 sum = even parity
    - c2: [4,2,3,5,4], c2 sum = odd parity
    - YES
  - eg: [4,7]
    - NO
  - eg: [3,9,8]
    - YES
    - c1: [3,9]
    - c2: [8]
    - both sum even parity
  - eg: [1,7]
    - YES
    - c1: [1]
    - c2: [7]
    - both sum odd parity
  - eg: [5,4,3,2,1]
    - NO
    - can't make 2color groups with same parity
- Approach
  - if no. of odds = no. of evens
    - YES
  - else if n=3 && no. of odds != 3 or !=1
    - YES
    - actually if [even,even,even] works YES
    - [odd,odd,odd] NO
    - [odd,odd,even] YES
    - [odd,even,even] NO
  - so iff n is odd && odd< even && abs(odd-even)!=1

- YES
- [odd,odd,odd,even,even] NO
- [odd,odd,even,even,even] YES
- [odd,odd,odd,even,even,even] NO

```
#include<bits/stdc++.h>
using namespace std;

int main(){
    ios::sync_with_stdio(0);
    cin.tie(0);
    int t;
    cin>> t;
    while (t--)
    {
        int n,odd=0,even=0;
        cin>>n;
        vector<int> v1(n,0);
        for (int i=0; i<n; i++){
            cin>>v1[i];
            if (v1[i]%2==0) {even++;}
            else {odd++;}
        }
        // cout<<odd<<" "<< even<<endl;
        if (odd==even && n>2) {
            cout<<"YES\n";
        }
        else if ((n==2 && odd!=even) || (n==3 && odd>even) || (n%2!=0 &&
odd<even && abs(odd-even)!=1) || even==1 || odd==1)
        {
            cout<<"YES\n";
        }
        else
        {
            cout<<"NO\n";
        }
    }

    return 0;
}
```

---

## End-of-File

The [kintsugi-stack](#) repository, authored by Kintsugi-Programmer, is less a comprehensive resource and more an Artifact of Continuous Research and Deep Inquiry into Computer Science and Software Engineering. It serves as a transparent ledger of the author's relentless pursuit of mastery, from the foundational algorithms to modern full-stack implementation.

Made with ❤️ Kintsugi-Programmer