ENTMLGY 6702 Entomological Techniques and Data Analysis

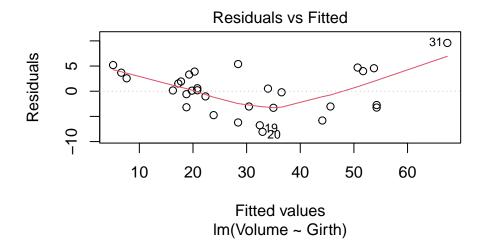
Transformations and Curvilinear Models

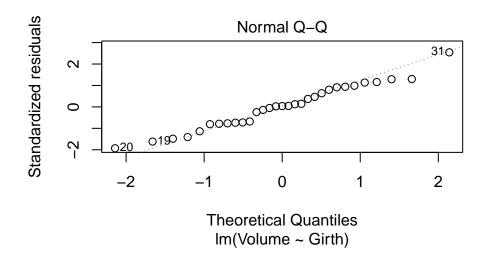
We will use the trees data from the datasets package for this tutorial. Fit a simple linear regression:

```
fit_trees_1 <- lm(Volume~Girth, data=trees)</pre>
summary(fit_trees_1)
##
## Call:
## lm(formula = Volume ~ Girth, data = trees)
##
## Residuals:
     {	t Min}
              1Q Median
                            3Q
                                  Max
## -8.065 -3.107 0.152 3.495 9.587
##
## Coefficients:
##
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) -36.9435
                            3.3651 -10.98 7.62e-12 ***
                            0.2474
                                     20.48 < 2e-16 ***
                 5.0659
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 4.252 on 29 degrees of freedom
## Multiple R-squared: 0.9353, Adjusted R-squared: 0.9331
## F-statistic: 419.4 on 1 and 29 DF, p-value: < 2.2e-16
```

And then take a look at the residuals again, which as you might recall from the simple linear regression tutorial, do not look so great: whereas I'd be okay with that qq-plot, there is some curvature in the residual plot.

```
plot(fit_trees_1, which=c(1,2))
```





We typically deal with residuals that violate assumptions by transforming the response variable and/or predictor and/or by fitting "higher order" (e.g., squared or quadratic) terms. We cover these approaches below.

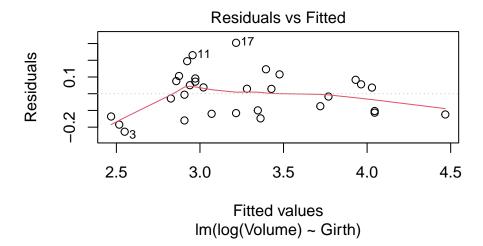
1 Transformations

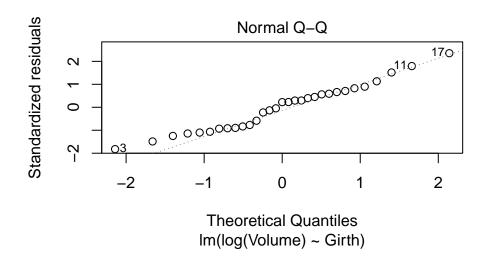
A log or square-root transformation of the response variable can often help with correcting issues of normality and heteroscedasticity. Here, we will just try log-transforming.

```
fit_trees_log_1 <- lm(log(Volume)~Girth, data=trees)
summary(fit_trees_log_1)

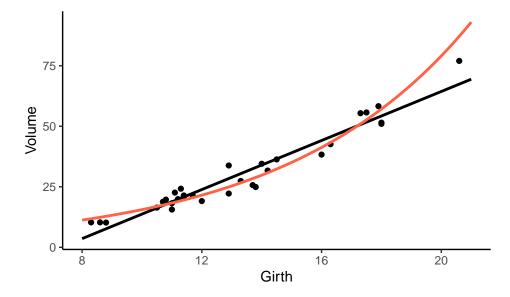
##
## Call:
## lm(formula = log(Volume) ~ Girth, data = trees)</pre>
```

```
##
## Residuals:
##
        Min
                  1Q
                       Median
   -0.22719 -0.11468
                      0.02889
                               0.07930
                                        0.30436
##
##
##
  Coefficients:
##
               Estimate Std. Error t value Pr(>|t|)
## (Intercept) 1.118997
                          0.104021
                                     10.76 1.23e-11 ***
  Girth
               0.162566
                          0.007647
                                     21.26 < 2e-16 ***
##
                   0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Signif. codes:
##
## Residual standard error: 0.1314 on 29 degrees of freedom
## Multiple R-squared: 0.9397, Adjusted R-squared: 0.9376
## F-statistic:
                  452 on 1 and 29 DF, p-value: < 2.2e-16
plot(fit_trees_log_1, which=c(1,2))
```





The normality assumption looks okay, and the residual plot, in my opinion, is close enough. If we wanted to plot the line from our model with a log-transformation onto the graph, we would need to back-transform our predictions: our model actually fit the regression line to a log-transformed version of Volume as a function of Girth.

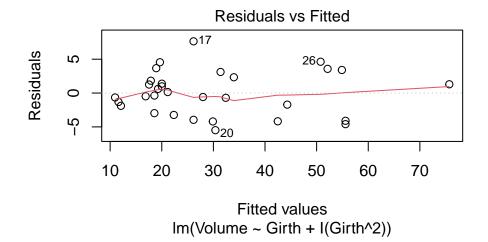


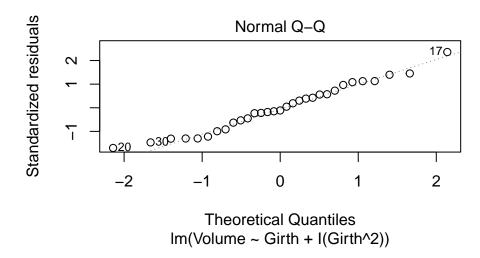
2 Curvilinear fits

If on initial plotting or in the residual plots you notice some curvature, a curvilinear model might provide a better fit. This can be achieved by fitting a quadratic or squared term to the model. Note: when one includes higher order terms (x^2, x^3, x^4) , it is convention to include all lower order terms in the model. For example, you would rarely ever fit $Y \sim X^3$, as the appropriate model would be $Y \sim X + X^2 + X^3$.

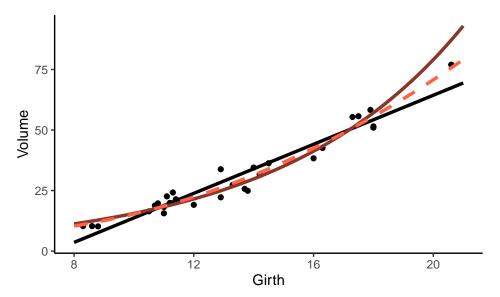
I fit polynomials as follows. The I() syntax is required and lets R know that you are performing a transformation on that variable (here, it is getting squared).

```
fit_trees_poly <- lm(Volume ~ Girth + I(Girth^2), data=trees)</pre>
summary(fit trees poly)
##
## Call:
## lm(formula = Volume ~ Girth + I(Girth^2), data = trees)
##
## Residuals:
##
                10 Median
                                3Q
                                       Max
       Min
  -5.4889 -2.4293 -0.3718 2.0764
                                   7.6447
##
##
  Coefficients:
##
               Estimate Std. Error t value Pr(>|t|)
##
  (Intercept) 10.78627
                          11.22282
                                     0.961 0.344728
##
##
  Girth
               -2.09214
                           1.64734
                                    -1.270 0.214534
## I(Girth^2)
                0.25454
                           0.05817
                                     4.376 0.000152 ***
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 3.335 on 28 degrees of freedom
## Multiple R-squared: 0.9616, Adjusted R-squared: 0.9588
## F-statistic: 350.5 on 2 and 28 DF, p-value: < 2.2e-16
plot(fit trees poly, which=c(1,2))
```





Here is a plot comparing our three fits. The straightline fit is in black, the model with a log transformation is solid tomato, and the model with a second order term is dashed/light tomato.



2.1 Interpreting curvilinear fits

When you transform either your response or predictor, the interpretation of the model changes. For example, following a log-transformation, you can make broad statements about the nature of the correlation (positive vs. negative), but a one unit change in X is now a β_1 unit change in log(Y). Be cognizant of these changes as you write up results for publication.