ENTMLGY 6707 Entomological Techniques and Data Analysis

R Activity 7: Multiple Linear Regression (MLR)

We have been using simple linear regression (SLR) to evaluate bivariate relationships, such as quantifying the effect of one predictor on our response variable (i.e., the effect of X on Y, Y as a function of X, or, in R speak, lm(Y~X)):

$$Y_i = \beta_0 + \beta_1 X_1 + \epsilon_i$$

Plant height ~ DBH

In multiple linear regression (MLR), we are investigating the explanatory power of two or more predictors, also referred to as "covariates" (note the subscripts for X are different, meaning these variables represent different predictors):

$$Y_i = \beta_0 + \beta_1 X_1 + \beta_2 X_2 + \epsilon_i$$

Plant height $\sim DBH + soil \ nitrogen$

1 Assumptions and collinearity

The same assumptions for SLR ($Y \sim X_1$) apply to MLR ($Y \sim X_1 + X_2$) but there are some additional assumptions in MLR. If you fit a MLR model, you should also check for **collinearity** (aka multicollinearity): correlation between your predictors. If two predictors are highly correlated, they end up explaining the same "type" of variation in your response. For example, if you were trying to predict weight of puppies using age and height, the strong relationship between puppy age and height would cause a problem; when collinearity is present, strange things can happen in the model. For example, the estimate of a slope for a given predictor might flip from positive to negative when that predictor is fit alone (= SLR) vs. when it is fit with a second predictor (= MLR) with which it is strongly correlated.

In MLR, we interpret coefficients as follows: "holding all else equal, a one unit increase in X_1 was associated with a B_1 unit increase in Y." That is part of the reason collinearity causes problems. If predictors X_1 and X_2 are highly correlated, it is difficult to "hold X_2 equal" while estimating what happens to the expected value of Y with a one unit change in X_1 .

2 Fitting a MLR model

I will use the CO2 data set from the datasets package in R. This data set reports changes in CO_2 uptake $(\mu \text{mol}/m^2 \ sec)$ with (i) conc (ambient CO_2 in mL/L), (ii) Type (origin of the plant: Quebec or Mississippi), and (iii) Treatment (chilled or nonchilled overnight before the experiment).

Please note a few things here. These models (Y ~ continuous X + categorical Z) are often referred to as analysis of covariance, or ANCOVA, whether an interaction term is included or not. We are going to ignore the repeated measures and Treatment and just look at the effects of conc and Type. There is no interaction term in the below model, and so we say we are just including "main effects" (a bit more on this b elow). I also provide a graphical depiction of the model, in which you should see that the fit lines corresponding to each level of Type are perfectly parallel (just FYI, MLR models with >3 predictors are often presented in tables rather than graphs).

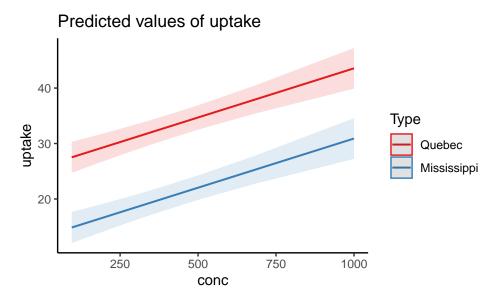
```
library(datasets)
fit_plants_1_nointeraction <- lm(uptake~conc+Type,data=CO2)
anova(fit plants 1 nointeraction)
## Analysis of Variance Table
##
## Response: uptake
##
                                          Pr(>F)
            Df Sum Sq Mean Sq F value
## conc
              1 2285.0
                       2285.0 45.627 1.997e-09 ***
                        3365.5
                                67.204 3.061e-12 ***
## Type
              1 3365.5
## Residuals 81 4056.4
                          50.1
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

summary(fit plants 1 nointeraction)

```
##
## Call:
## lm(formula = uptake ~ conc + Type, data = CO2)
##
## Residuals:
##
       Min
                  1Q
                       Median
                                    3Q
                                            Max
## -18.2145 -4.2549
                       0.5479
                                5.3048
                                       12.9968
##
## Coefficients:
##
                     Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                    25.830052
                                1.579918
                                          16.349 < 2e-16 ***
                     0.017731
                                0.002625
                                           6.755 2.00e-09 ***
## conc
## TypeMississippi -12.659524
                                1.544261
                                         -8.198 3.06e-12 ***
##
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 7.077 on 81 degrees of freedom
## Multiple R-squared: 0.5821, Adjusted R-squared: 0.5718
## F-statistic: 56.42 on 2 and 81 DF, p-value: 4.498e-16
```

In our model with no interaction, our interpretation would be that plants from Quebec had higher uptake than plants from Mississippi AND that the differences in uptake were constant across all values of conc (the lines are parallel!). Said another way, the relationship (i.e., slope) between uptake and conc does not change with plant Type - the intercept does change with plant Type, however (that is apparent from looking at the graph).

```
library(tidyverse)
library(sjPlot)
library(sjmisc)
plot_model(fit_plants_1_nointeraction, type = "pred", terms = c("conc", "Type"))+
    theme_classic()
```



3 Interactions

Residuals 80 3848.4

Interactions between our predictors indicate whether the effect of one predictor (X_1) on our response variable (Y) is influenced by another predictor (X_2) . Note this is different from collinearity, because when fitting an interaction our goal is actually to quantify how one predictor affects the relationship between our response and other predictor. In R, we code interactions using an asterisk, "*". In the case of uptake, we might be interested to know if the relationship between uptake and conc changes between plants from Quebec vs. Mississippi (i.e., levels of Type).

Note that we always include the so-called main effects when fitting interaction terms: you would not fit a variable in an interaction term without also fitting that variable alone (i.e., as a main effect). Indeed, you will notice below that conc*Type forces R to provide estimates of main effects for conc and Type in the summary().

```
fit_plants_1_interaction <- lm(uptake~conc*Type,data=CO2)</pre>
anova(fit_plants_1_interaction)
## Analysis of Variance Table
##
## Response: uptake
##
             Df Sum Sq Mean Sq F value
                                            Pr(>F)
                         2285.0 47.4995 1.143e-09 ***
## conc
              1 2285.0
## Type
              1 3365.5
                         3365.5 69.9614 1.560e-12 ***
## conc:Type
             1
                 208.0
                          208.0
                                4.3238
                                          0.04079 *
```

summary(fit_plants_1_interaction)

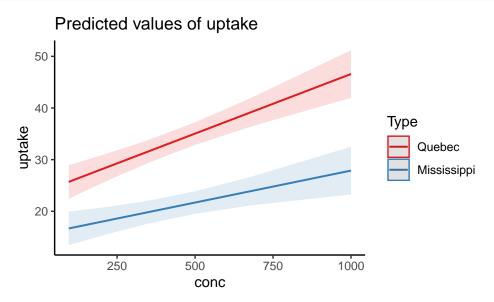
48.1

Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1

```
##
## Call:
## lm(formula = uptake ~ conc * Type, data = CO2)
##
## Residuals:
##
       Min
                  1Q
                      Median
                                    3Q
                                            Max
##
  -16.3956 -5.5250
                     -0.1604
                                5.5724
                                        12.0072
##
## Coefficients:
##
                         Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                        23.503038
                                    1.910531
                                              12.302 < 2e-16 ***
                                               6.344 1.25e-08 ***
                         0.023080
                                    0.003638
## conc
## TypeMississippi
                        -8.005495
                                    2.701899
                                              -2.963
                                                      0.00401 **
## conc:TypeMississippi -0.010699
                                    0.005145
                                             -2.079 0.04079 *
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 6.936 on 80 degrees of freedom
## Multiple R-squared: 0.6035, Adjusted R-squared: 0.5887
## F-statistic: 40.59 on 3 and 80 DF, p-value: 4.78e-16
```

In the graph below, note the lines are no longer parallel! With the interaction term, we are now evaluating whether the effect of conc on uptake changes with plant Type. In this case, we would conclude that Type influenced the uptake ~ conc relationship because of the conc:Type line in the above anova table $(F_{1,80}=4.32,p=0.0408)$. In the next section, I go into more detail on how to interpret summary() output of models with interactions.

```
plot_model(fit_plants_1_interaction, type = "pred", terms = c("conc", "Type"))+
    theme_classic()
```



4 Multiple ANOVA (MANOVA)

We have worked with one-way ANOVAs to quantify variation in a continuous response variable as a function of a single predictor that had multiple levels (e.g., plant growth as a function of "fertilizer", where fertilizer had three different levels or fertilizer types). In the preceding section, we used ANOVA to evaluate the effects of a categorical and a continuous predictor on a continuous response. ANOVA is quite flexible/powerful, and we can also evaluate the effects of multiple categorical predictors - that each have two or more levels - on a continuous response.

It is very typical to fit an interaction term in such models, but that will depend on the specific goals of your analysis. Below we are fitting a two-way interaction (e.g., A*B), but you can fit multi-way interactions (A*B*C) if you have a compelling biological reason, but be warned that the more interactions the more difficult the model is to interpret. Also note that instead of Treatment+Type+Treatment*Type, I could have written Treatment*Type and the same model would have been fit (please re-read the previous section if that coding option seems strange).

```
fit_manova <- lm(uptake~Treatment+Type+Treatment*Type,data=CO2)
anova(fit manova)
## Analysis of Variance Table
##
## Response: uptake
##
                  Df Sum Sq Mean Sq F value
                                               Pr(>F)
## Treatment
                      988.1
                              988.1 15.4164 0.0001817 ***
## Type
                   1 3365.5
                             3365.5 52.5086 2.378e-10 ***
## Treatment:Type
                   1
                      225.7
                              225.7
                                    3.5218 0.0642128 .
## Residuals
                  80 5127.6
                               64.1
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
summary(fit_manova)
##
## Call:
## lm(formula = uptake ~ Treatment + Type + Treatment * Type, data = CO2)
##
## Residuals:
##
       Min
                1Q
                    Median
                                3Q
                                       Max
                                    10.648
  -22.452
           -3.624
                     2.167
                             5.773
##
##
## Coefficients:
                                    Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
                                      35.333
                                                   1.747
                                                          20.225 < 2e-16 ***
## Treatmentchilled
                                      -3.581
                                                   2.471
                                                          -1.449 0.151141
## TypeMississippi
                                      -9.381
                                                  2.471
                                                          -3.797 0.000284 ***
## Treatmentchilled:TypeMississippi
                                      -6.557
                                                  3.494
                                                          -1.877 0.064213 .
##
                   0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Signif. codes:
##
## Residual standard error: 8.006 on 80 degrees of freedom
## Multiple R-squared: 0.4718, Adjusted R-squared: 0.452
## F-statistic: 23.82 on 3 and 80 DF, p-value: 4.106e-11
```

The interpretation is the same for our other ANOVA models, but note that the Estimate column in the above summary() output is providing the difference in means of groups compared to a reference level where that reference level (Intercept) represents the mean of uptake for plants that were nonchilled and from Quebec. The second line compares the uptake of plants that were chilled and from Quebec to the reference group. The third line is comparing uptake of plants that were nonchilled and from Mississippi to the reference group. The last line, the interaction term (Treatmentchilled:TypeMississippi), is comparing uptake of plants that were chilled and from Quebec (which again, is the reference level).

So, to estimate the uptake of plants that were nonchilled and from Mississippi, we would use the following. Note all the numbers are taken from the above summary() output and the 0 or 1 indicates "membership" to a treatment (think back to when we covered "dummy" variables):

```
25.952 = 35.333 - (0 \times 3.581) - (1 \times 9.381) - (0 \times 6.557)
```

And to estimate the uptake of plants that were chilled and from Mississippi, we would use the following: $15.814 = 35.333 - (1 \times 3.581) - (1 \times 9.381) - (1 \times 6.557)$

In a way, our model is just estimating the means of our different treatment groups (nonchilled/Quebec, nonchilled/Mississippi, chilled/Quebec, chilled/Mississippi), which we could also calculate using our raw data (see below). Our formal analyses, however, tell us if any differences in the means are statistically meaningful. Note that to compare all the groups to each other, we would need something like emmeans to account for making multiple comparisons (see next section).

```
CO2 %>% group_by(Treatment, Type) %>% summarise(means = round(mean(uptake),3)) %>% as.data.frame()
```

```
## `summarise()` has grouped output by 'Treatment'. You can override using the
## `.groups` argument.
## Treatment Type means
## 1 nonchilled Quebec 35.333
## 2 nonchilled Mississippi 25.952
## 3 chilled Quebec 31.752
## 4 chilled Mississippi 15.814
```

5 Multiple comparisons in MLR

We can still conduct multiple comparisons between levels of a factor in MLR/MANOVA frameworks, including when there are interaction terms. However, before doing so, we often need to adjust for the fact that there are other treatments/variables in our model potentially influencing the response variable...thankfully, R does that for us! Below are two examples, and the interpretations are the same as other multiple comparisons we have covered. Note that if you have interaction terms, you should probably limit your multiple comparisons to the interaction term alone. That is, interpreting main effects is not easy when you fit interactions.

```
library(emmeans)
```

5.1 No interaction, one categorical and one continuous predictor

5.2 Interaction between a categorical and a continuous predictor

Note that this is comparing the *slopes* of the uptake ~ conc relationship between the Quebec group and Mississippi group. So, the slope of uptake ~ conc is steeper by 0.0107 for the Quebec plants.

5.3 No interaction, two categorical predictors

Note that we are just looking at Treatment here but the output acknowledges the presence of Type in the model (Results are averaged over the levels of: Type).

5.4 Interaction between two categorical predictors

```
manova_emm <- emmeans(fit_manova, ~Treatment*Type)
pairs(manova_emm)</pre>
```

```
contrast
                                                            SE df t.ratio p.value
                                                 estimate
                                                                    1.449 0.4728
   nonchilled Quebec - chilled Quebec
                                                     3.58 2.47 80
## nonchilled Quebec - nonchilled Mississippi
                                                    9.38 2.47 80
                                                                   3.797 0.0016
## nonchilled Quebec - chilled Mississippi
                                                   19.52 2.47 80
                                                                   7.900 <.0001
## chilled Quebec - nonchilled Mississippi
                                                                   2.348 0.0960
                                                    5.80 2.47 80
##
   chilled Quebec - chilled Mississippi
                                                   15.94 2.47 80
                                                                    6.451
                                                                          <.0001
## nonchilled Mississippi - chilled Mississippi
                                                   10.14 2.47 80
                                                                   4.103 0.0006
```

##

P value adjustment: tukey method for comparing a family of 4 estimates

6 Sequential vs. marginal fitting

The standard R anova() command uses something called sequential fitting, or Type I sums of squares (the names Type X sums of squares originated with SAS, another stats software). A full description of the different types of sums squares is beyond the scope of this class, but what this means is that the order in which you list the predictors inside the lm() command can influence the statistical output and thus your conclusions... wait, what?! To illustrate this point, I'll use a data set on tick abundance.

6.1 Sequential fitting

Please do not worry about biology here, but notice in the output that the sums of squares are changing *just* because we swapped the order of our predictors. Everything else is *exactly* the same.

When f_YEAR is listed first:

```
grouseticks$f_YEAR <- as.factor(grouseticks$YEAR)</pre>
fit_ex1 <- lm(TICKS ~ f_YEAR + HEIGHT, data=grouseticks)</pre>
anova(fit_ex1)
## Analysis of Variance Table
##
## Response: TICKS
##
              Df Sum Sq Mean Sq F value
                                            Pr(>F)
## f_YEAR
                   7050
                         3524.9
                                  24.995 5.928e-11 ***
## HEIGHT
                   6092
                          6092.0
                                  43.199 1.550e-10 ***
## Residuals 399
                  56268
                           141.0
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
When HEIGHT is listed first:
fit_ex2 <- lm(TICKS ~ HEIGHT + f_YEAR, data=grouseticks)</pre>
anova(fit_ex2)
## Analysis of Variance Table
##
## Response: TICKS
##
              Df Sum Sq Mean Sq F value
                                            Pr(>F)
                   7692
                         7692.2 54.546 8.948e-13 ***
## HEIGHT
               1
               2
                         2724.8 19.321 9.788e-09 ***
## f YEAR
                   5450
## Residuals 399
                  56268
                           141.0
## Signif. codes:
                   0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

What the output is doing for anova(fit_ex1) is presenting the effect of f_YEAR on TICKS and THEN presenting the effect of HEIGHT on TICKS AFTER accounting for the effect of f_YEAR. Think of it this way: f_YEAR explains some variation in TICKS and then we see how good of a job HEIGHT does of explaining the remaining variation. The Residuals indicate the remaining/leftover variation after accounting for both predictors (= unexplained variation).

The exact reverse is true for the output of anova(fit_ex2), which is presenting the effect of HEIGHT on TICKS and THEN presenting the effect of f_YEAR on TICKS AFTER accounting for the effects of HEIGHT. The Residuals value does not change between analyses, which makes sense: we are using the same two

predictors in both models and they will explain the exact same amount of variability in our response variable (we are just swapping the order in which we fit them).

6.2 Marginal fitting

In practice, we usually - really, always - want to look at the explanatory power of our predictors after accounting for the other predictors in a model (if you have a counter example, I am genuinely curious to hear it!). This process is called marginal fitting, or Type II OR Type III sums of squares.

Again, the nuances of sums of squares are beyond the scope of this class, but here is a short summary. First, remember that interpreting main effects can be very difficult when you have an interaction term in the model (e.g., interpreting effects of A and B when your model is lm(Y~A+B+A*B)). When using Type II sums of squares, the ANOVA table will return the marginal effects of A and B while igoring the interaction term. However, when using Type III sums of squares, the effects of each predictor on our response variable will be returned AFTER the model accounts for the effects of all the other predictors. This means that (i) the order of predictors in your R code will not matter when using Type II or III and (ii) the results using Type III and III will be exactly equivalent when you do not have an interaction term in the model. We will use Type III sums of squares in this class, but here is an example illustrating the differences.

To use Type II or III sums of squares, install and load the car package, which has the function Anova() with a capital "A".

```
library(car)
```

Notice that both models now have the same exact ANOVA table. Bottom line: I recommend always using Type II or III sums of squares unless you have a very compelling reason to do otherwise.

When f_YEAR is listed first:

```
Anova(fit_ex1, type="III")
## Anova Table (Type III tests)
##
## Response: TICKS
##
               Sum Sq Df F value
                                      Pr(>F)
                           52.786 1.970e-12 ***
## (Intercept)
                 7444
                        1
## f_YEAR
                 5450
                           19.321 9.788e-09 ***
## HEIGHT
                 6092
                           43.199 1.550e-10 ***
                        1
## Residuals
                56268 399
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
When HEIGHT is listed first:
Anova(fit ex2, type="III")
## Anova Table (Type III tests)
##
## Response: TICKS
               Sum Sq Df F value
                                      Pr(>F)
                           52.786 1.970e-12 ***
## (Intercept)
                 7444
## HEIGHT
                           43.199 1.550e-10 ***
                 6092
                        1
## f_YEAR
                 5450
                        2
                           19.321 9.788e-09 ***
                56268 399
## Residuals
## ---
```

Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1

Here are the example ANOVA tables for our three approaches. Read the vertical bar in "HEIGHT $|f_YEAR$ " as "given", meaning we are looking at the effect of HEIGHT on TICKS given (or after accounting/adjusting for) the effects of f_YEAR on TICKS.

Table 1: ANOVA Table for fit_ex1_df (sequential fit)

| Predictor | DF | SS | MS | F | P |
|--------------------------------------|---------------|---------|------------------------------|---|------------------|
| f_YEAR HEIGHT f_YEAR Residuals | 2 1 399 | 6091.98 | 3524.86 6091.98 141.02 | | <0.0001 <0.01 |

Table 2: ANOVA Table for fit_ex2_df (sequential fit)

| Predictor | DF | SS | MS | F | P |
|-----------------|-----|----------|---------|-------|----------|
| HEIGHT | 1 | 7692.19 | 7692.19 | 54.55 | < 0.0001 |
| $f_YEAR HEIGHT$ | 2 | 5449.52 | 2724.76 | 19.32 | < 0.0001 |
| Residuals | 399 | 56268.21 | 141.02 | | |

Table 3: ANOVA Table for fit_ex1_df (marginal fit)

| Predictor | DF | SS | MS | F | P |
|---------------|-----|----------|-----------|-------|----------|
| f_YEAR HEIGHT | 2 | 5449.52 | 2724.7600 | 19.32 | < 0.0001 |
| HEIGHT f_YEAR | 1 | 6091.98 | 6091.9800 | 43.2 | < 0.01 |
| Residual | 399 | 56268.21 | 141.0231 | | |

6.3 A bit more on Type II vs. III Sums of Squares

Let's fit the same model as above (i.e., lm(TICKS ~ f_YEAR + HEIGHT)) but we will include an interaction term: lm(TICKS ~ f_YEAR + HEIGHT + f_YEAR*HEIGHT. Here is a reminder of that model:

Table 4: ANOVA Table for fit_ex1_df (marginal fit)

| Predictor | DF | SS | MS | F | P |
|--|----|----|------------------------------------|---|------------------|
| f_YEAR HEIGHT HEIGHT f_YEAR Residual | 1 | | 2724.7600 6091.9800 141.0231 | | <0.0001 <0.01 |

6.3.1 Type II

Note that in the model below, the estimates for the main effects (f_YEAR, HEIGHT) are the same as the "marginal" fit above in the model that did not have an interaction term (fit_ex1_df). There are slight differences due to rounding in the below output.

```
fit_ex_SS <- lm(TICKS ~ f_YEAR + HEIGHT + f_YEAR*HEIGHT, data=grouseticks)
Anova(fit_ex_SS, type="II")</pre>
```

```
## Anova Table (Type II tests)
##
## Response: TICKS
##
                 Sum Sq Df F value
                                        Pr(>F)
                           2 20.1085 4.804e-09 ***
## f_YEAR
                   5450
## HEIGHT
                   6092
                           1 44.9583 6.937e-11 ***
## f_YEAR:HEIGHT
                   2473
                           2
                             9.1271 0.0001332 ***
## Residuals
                  53795 397
## ---
                   0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Signif. codes:
```

6.3.2 Type III

Note that the below estimates for the main effects (f_{YEAR} , HEIGHT) are NOT the same as the "marginal" fit above in the model that did not have an interaction term (Table 4). The values associated with the interaction are the same, however: the below model provides the effects of f_{YEAR} and HEIGHT after accounting the effect of f_{YEAR} +HEIGHT.

```
Anova(fit_ex_SS, type="III")
```

```
## Anova Table (Type III tests)
##
## Response: TICKS
##
                 Sum Sq
                         Df F value
                                       Pr(>F)
## (Intercept)
                   5915
                          1 43.6540 1.263e-10 ***
## f YEAR
                   2911
                          2 10.7418 2.863e-05 ***
## HEIGHT
                   5210
                          1 38.4525 1.409e-09 ***
                          2
                             9.1271 0.0001332 ***
## f_YEAR:HEIGHT
                   2473
## Residuals
                  53795 397
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

7 R Activity

We will work with the same data set for the next two weeks. The data were generated from a study investigating the effects of animal species, diet, and drug type on blood glucose levels (mg/dl) using a $2 \times 3 \times 2$ factorial arrangement. Note that a factorial design of $A \times B \times C$ means that you designed a study looking at the effects of three factors, one having A levels, one having B levels, and one having C levels.

In this study, two animal species (goats or sheep) were fed one of three diets (control, alfalfa hay, and cottonseed meal) and received a drug injection (slaframine in saline or just saline). The 12 treatment combinations were assigned in a randomized complete block design with twelve blocks (replications). So, each combination of animal \times diet \times drug combination appears twelve times.

We are going to look at the effects of drug and animal on glucose blood levels and entirely ignore diet.

- 1. Load in the glucose_df.txt dataset.
- 2. Create a grouped boxplot of glucose as a function of drug and animal. Use any colors you want, but make sure to overlay the raw data points on top of your boxes. Based on eyeballing the plot, provide a 1-2 sentence description of any pattern(s).
- 3. We are interested in quantifying variation in glucose (our response variable). Note that we could analyze these data in the "historical" way by fitting rep (the column for blocks) as a so-called "fixed effect" (i.e., as a regular old predictor). Next week, you will get practice fitting mixed-effects models, in which rep would be fit as a so-called "random intercept" or "random effect". Do not worry, as I will also further explain the terms fixed, random, and mixed-effect next week. However, for this week, we are going to simplify things: ignore rep and just fit animal, drug, and their interaction (animal × drug) as the predictors (again, we are ignoring the diet column).
- 4. Run an Anova() on the model and ensure you are using marginal fits (Type III sums of squares).
- 5. Conduct a pairwise comparisons of the interaction term
- 6. Write 3-4 sentences interpreting the results of your analyses. Please try to write in biological terms, not statistical, but make sure to include the relevant summary statistics for any claims you make.