ENTMLGY 6707 Entomological Techniques and Data Analysis

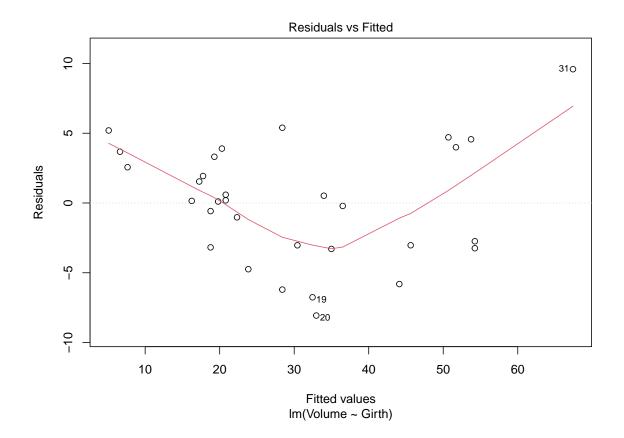
Transformations and Curvilinear Models

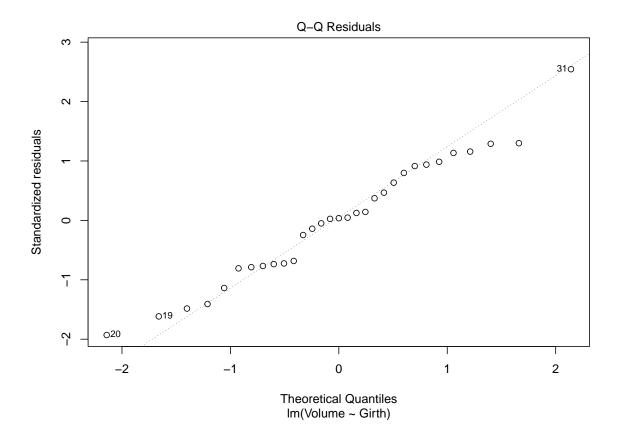
We will use the **trees** data from the **datasets** package for this tutorial. Fit a simple linear regression:

```
fit_trees_1 <- lm(Volume ~ Girth, data = trees)
summary(fit_trees_1)</pre>
```

```
Call:
lm(formula = Volume ~ Girth, data = trees)
Residuals:
  Min
          1Q Median
                        3Q
-8.065 -3.107 0.152 3.495 9.587
Coefficients:
           Estimate Std. Error t value Pr(>|t|)
(Intercept) -36.9435 3.3651 -10.98 7.62e-12 ***
Girth
             5.0659
                        0.2474 20.48 < 2e-16 ***
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Residual standard error: 4.252 on 29 degrees of freedom
Multiple R-squared: 0.9353,
                               Adjusted R-squared: 0.9331
F-statistic: 419.4 on 1 and 29 DF, p-value: < 2.2e-16
```

And then take a look at the residuals again, which as you might recall from the simple linear regression tutorial, do not look so great. While we would be okay with that qq-plot, there is some curvature in the residual plot.





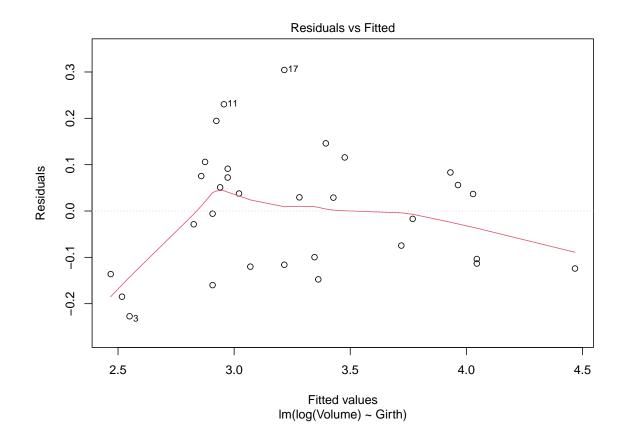
We typically deal with residuals that violate assumptions by transforming the response variable and/or predictor and/or by fitting "higher order" (e.g., squared or quadratic) terms. We cover these approaches below.

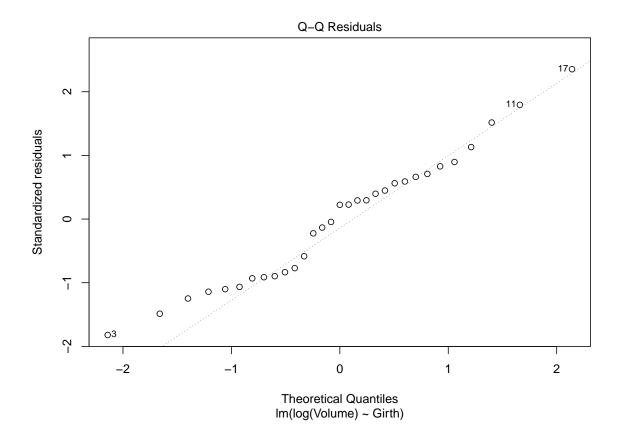
Transformations

A log or square-root transformation of the response variable can often help with correcting issues of normality and heteroscedasticity. Here, we will try log-transforming.

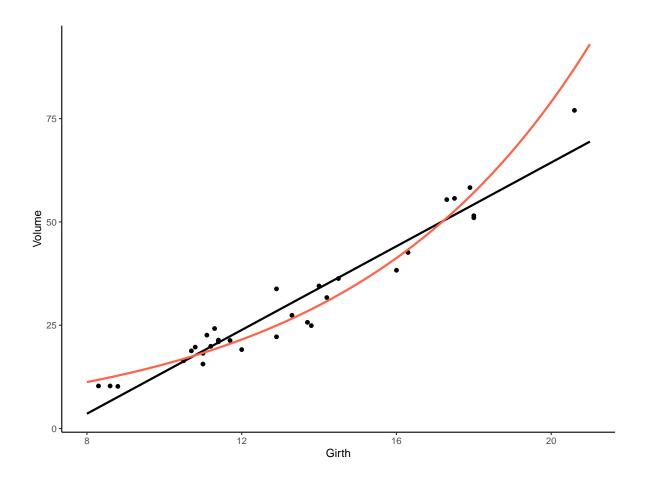
```
fit_trees_log_1 <- lm(log(Volume) ~ Girth, data = trees)</pre>
summary(fit_trees_log_1)
```

```
Call:
lm(formula = log(Volume) ~ Girth, data = trees)
Residuals:
    Min
                                        Max
              1Q
                   Median
                                3Q
-0.22719 -0.11468 0.02889 0.07930 0.30436
Coefficients:
           Estimate Std. Error t value Pr(>|t|)
(Intercept) 1.118997
                      0.104021
                                 10.76 1.23e-11 ***
                      0.007647
                                 21.26 < 2e-16 ***
Girth
           0.162566
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Residual standard error: 0.1314 on 29 degrees of freedom
Multiple R-squared: 0.9397,
                             Adjusted R-squared: 0.9376
F-statistic: 452 on 1 and 29 DF, p-value: < 2.2e-16
plot(fit_trees_log_1, which=c(1,2))
```





The normality assumption looks okay, and the residual plot, in my opinion, is close enough. If we wanted to plot the line from our model with a log-transformation onto the graph, we would need to back-transform our predictions. Our model actually fit the regression line to a log-transformed version of Volume as a function of Girth.

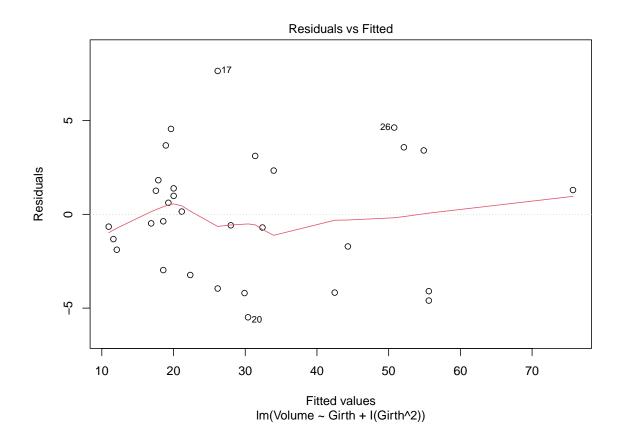


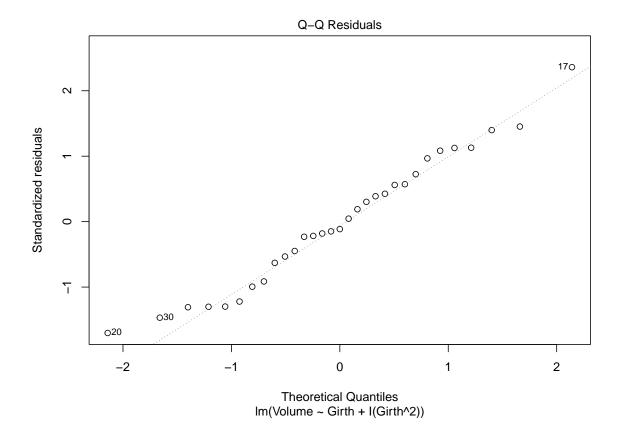
Curvilinear fits

If on initial plotting or in the residual plots you notice some curvature, a curvilinear model might provide a better fit. This can be achieved by fitting a quadratic or squared term to the model. Note: when one includes higher order terms (x^2, x^3, x^4) , it is convention to include all lower order terms in the model. For example, you would rarely ever fit $Y \sim X^3$, as the appropriate model would be $Y \sim X + X^2 + X^3$.

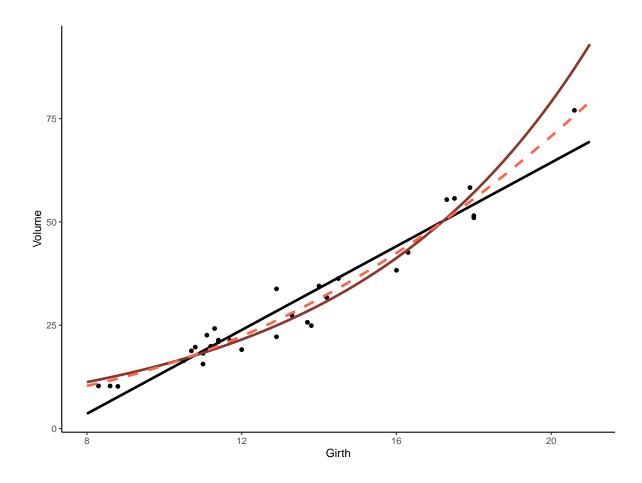
Fit polynomials as follows. The I() syntax is required and lets R know that you are performing a transformation on that variable (here, it is getting squared).

```
fit_trees_poly <- lm(Volume ~ Girth + I(Girth^2), data=trees)</pre>
summary(fit_trees_poly)
Call:
lm(formula = Volume ~ Girth + I(Girth^2), data = trees)
Residuals:
    Min
             1Q Median
                             3Q
                                    Max
-5.4889 -2.4293 -0.3718 2.0764 7.6447
Coefficients:
            Estimate Std. Error t value Pr(>|t|)
(Intercept) 10.78627
                       11.22282
                                  0.961 0.344728
            -2.09214
                        1.64734 -1.270 0.214534
Girth
I(Girth^2)
             0.25454
                        0.05817
                                  4.376 0.000152 ***
                0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Residual standard error: 3.335 on 28 degrees of freedom
Multiple R-squared: 0.9616,
                                Adjusted R-squared: 0.9588
F-statistic: 350.5 on 2 and 28 DF, p-value: < 2.2e-16
plot(fit_trees_poly, which=c(1,2))
```





Here is a plot comparing our three fits. The straight line fit is in black, the model with a log transformation is solid tomato, and the model with a second order term is dashed/light tomato.



Interpreting curvilinear fits

When you transform either your response or predictor, the interpretation of the model changes. For example, following a log-transformation, you can make broad statements about the nature of the correlation (positive vs. negative), but a one unit change in X is now a β_1 unit change in log(Y). Be cognizant of these changes as you write up results for publication.