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$$f(x) = \frac{x}{x + \frac{c}{x}}$$

$$\frac{df(x)}{dx} = \frac{d}{dx} \left( \frac{x}{x + \frac{c}{x}} \right)$$

$$\frac{(x + \frac{c}{x}) \frac{d}{dx} x - x \cdot \frac{d}{dx} (x + \frac{c}{x})}{(x + \frac{c}{x})^2}$$

$$= \frac{(x + \frac{c}{x}) - x(1 + \frac{-c}{x^2})}{(x + \frac{c}{x})^2}$$

$$= \frac{x + \frac{c}{x} - x + \frac{c}{x^2}}{(x + \frac{c}{x})^2}$$

$$= \frac{\frac{c}{x} + \frac{c}{x^2}}{(x + \frac{c}{x})^2}$$

$$= \frac{\frac{c}{x} + \frac{c}{x^2}}{(x + \frac{c}{x})^2}$$