

In[2]:=

**ord = 2**

Out[2]= 2

In[3]:= **left = Sort[Join[{{0, DC}}, Table[{-k dx, VL[k]}, {k, 1, ord}]]]**

Out[3]= {{0, DC}, {-2 dx, VL[2]}, {-dx, VL[1]}}

In[4]:= **right = Join[{{0, DC}}, Table[{k dx, VR[k]}, {k, 1, ord}]]**

Out[4]= {{0, DC}, {dx, VR[1]}, {2 dx, VR[2]}}

In[5]:= **poL = Simplify[InterpolatingPolynomial[left, x]]**

Out[5]= 
$$\frac{DC (2 dx^2 + 3 dx x + x^2) + x (dx (-4 VL[1] + VL[2]) + x (-2 VL[1] + VL[2]))}{2 dx^2}$$

In[6]:= **poR = Simplify[InterpolatingPolynomial[right, x]]**

Out[6]= 
$$\frac{DC (2 dx^2 - 3 dx x + x^2) + x (4 dx VR[1] - 2 x VR[1] - dx VR[2] + x VR[2])}{2 dx^2}$$

In[7]:= **deL = Simplify[D[poL, x] /. x -> 0]**

Out[7]= 
$$\frac{3 DC - 4 VL[1] + VL[2]}{2 dx}$$

In[8]:= **deR = Simplify[D[poR, x] /. x -> 0]**

Out[8]= 
$$-\frac{3 DC - 4 VR[1] + VR[2]}{2 dx}$$

In[9]:= **sold = Simplify[Solve[deL / eL - deR / eR == 0, DC][[1, -1, -1]]]**

Out[9]= 
$$-\frac{eR (-4 VL[1] + VL[2]) + eL (-4 VR[1] + VR[2])}{3 (eL + eR)}$$

In[10]:= **sole = Simplify[Solve[deL - deR == 0, DC][[1, -1, -1]]]**

Out[10]= 
$$\frac{1}{6} (4 VL[1] - VL[2] + 4 VR[1] - VR[2])$$

In[11]:= **lapL = Simplify[(D[poL, {x, 2}]) /. x -> -dx]**

Out[11]= 
$$\frac{DC - 2 VL[1] + VL[2]}{dx^2}$$

In[12]:= **lapR = Simplify[D[poR, {x, 2}] /. x -> +dx]**

Out[12]= 
$$\frac{DC - 2 VR[1] + VR[2]}{dx^2}$$

In[13]:= **Simplify[Apart[lapR /. DC -> sold]]**

Out[13]= 
$$\frac{2 eL (-VR[1] + VR[2]) + eR (4 VL[1] - VL[2] - 6 VR[1] + 3 VR[2])}{3 dx^2 (eL + eR)}$$

In[14]:= **Simplify**[**Apart**[lapL /. DC → sold]]

Out[14]= 
$$\frac{2 eR (-VL[1] + VL[2]) - eL (6 VL[1] - 3 VL[2] - 4 VR[1] + VR[2])}{3 dx^2 (eL + eR)}$$