B561 Advanced Database Concepts Assignment 2 Fall 2022

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This assignment relies on the lectures

- SQL Part 1 and SQL Part 2 (Pure SQL);
- Tuple Relational Calculus;
- Views;
- Relational Algebra (RA); and
- Joins and semijoins.

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To turn in your assignment, you will need to upload to Canvas 3 files:

- 1. A file with name assignment2.sql which contains the necessary SQL statements that solve the problems in this assignment. The assignment2.sql file must be so that the AI's can run it in their PostgreSQL environment. You should use the Assignment2Script.sql file to construct the assignment2.sql file. (Note that the data to be used for this assignment is included in this file.)
- 2. A file with name assignment2.txt file that contains the results of running the SQL code in the assignment2.sql code.
- 3. A file with name assignment2.pdf that contains the solutions to the problems that require it. You are strongly advised to use Latex to construct this file

The problems that need to be included in the assignment2.sql are marked with a blue bullet •. The problems that need to be included in the assignment2.pdf are marked with a green bullet •. Problems that are marked with a red bullet • are practice problems and they should not be included in the 3 files you need to submit.

Database schema and instances

For the problems in this assignment we will use the following database schema:¹

Student(sid, sname, birthYear)
Book(bno, title, price)
Buys(sid, bno)
Major(major)
hasMajor(sid, major)
Cites(bno1, bno2)

In this database we maintain a set of students (Student), a set of books (Book), and a set of majors (Major). The sname attribute in Student is the name of the student. The birthYear attribute in Student specifies the birth year of the student. The bno attribute in Book is the book number of the book.² The title attribute in Book is the title of the book. The price attribute in Book is the price for the book. The major attribute in Major is the name of a major.

A student can buy books. This information is maintained in the Buys relation. A triple (s, b) indicates that the student with sid s buys the book with bno b. We permit that a student buys multiple books and that a book is bought by multiple students. It is possible that a student buys no books and that a book is bought by no students.

A student can have multiple majors. This information is maintained in the hasMajor relation. A student can have multiple majors and a major can have multiple students. It is possible that a student has no major and that a major has no students.

A book can cite other books. This information is maintained in the Cites relation. A pair (b_1, b_2) in Cites indicates that the book with bno b_1 cites the book with bno b_2 . We permit that a book cites multiple books and that a book is cited by multiple books. It is possible that a book cites no other books and that a book is not cited by any book. The domain for the attributes sid, bno, bno1, bno2, birthYear, and price is integer. The domain for all other attributes is text.

¹The primary key, which may consist of one or more attributes, of each of these relations is underlined.

 $^{^2}$ You should think of bno as the ISBN number of a book. Notice that different physical books may have the same ISBN number.

The primary keys in the relations are the respective underlined attributes.

We assume the following foreign key constraints:

- sid is a foreign key in Buys referencing the primary key sid in Student;
- bno is a foreign key in Buys referencing the primary key bno in Book;
- sid is a foreign key in hasMajor referencing the primary key sid in Student;
- major is a foreign key in hasMajor referencing the primary key major in Major;
- bno1 is a foreign key in Cites referencing the primary key bno in Book; and
- bno2 is a foreign key in Cites referencing the primary key bno in Book.

We assume that a book can not recursively cite itself. In other words, the Cites relation is an acylic directed graph. I.e., there are no cycles in the Cites graph.

Pure SQL and RA SQL

In this assignemt, we distinguish between Pure SQL³ and RA SQL. Below we list the **only** features that are allowed in Pure SQL and in RA SQL.

In particular notice that

- 'join', 'natural join', and 'cross join' are **not** allowed in Pure SQL.
- The subquery expressions 'some', 'all', ['not'] "exists", ['not'] 'exists' are **not** allowed in RA SQL.

The only features allowed in Pure SQL

```
select ... from ... where
with ...
union, intersect, except operations
'some' and 'all' subquery expressions
'exists' and 'not exists' subquery expressions
'in' and not in subquery expressions
'view's that can only use the above Pure SQL features
```

The only features allowed in RA SQL

```
with ...
union, intersect, except operations
join ... on ..., natural join, and cross join operations
'view's that can only use the above RA SQL features
commas in the from clause are not allowed
```

 $^{^3}$ Pure SQL is the fragment of SQL that was covered in the lectures up to but not including the lectures about relational algebra.

1 Translating SQL queries with query predicates and subquery expressions into safe TRC

We have learned that safe TRC is at the core of the design of SQL. For the problems in the section, you are asked to translate SQL queries into equivalent safe TRC queries. To illustrate what you need to do, consider the following example:

Example 1 Consider the query 'Find each (s, b) pair where s is the sid of a student who bought book b and such that each other book, with price above \$30, that was bought by s is a book cited by b.'

This query can be expressed in SQL as

```
select t.sid, t.bno
from
        Buys t
where true = all (select (t.bno, b.bno) in (select c.bno1, c.bno2
                                                    from
                                                           Cites c)
                      from
                              Book b
                      where b.bno != t.bno and
                              b.price >= 30 and
                              (t.sid, b.bno) in (select t1.sid, t1.bno
                                                    from
                                                            Buys t1));
    Starting from this SQL query, we obtain the safe TRC query
 \{(t.sid, t.bno) \mid Buys(t) \land
     \forall b ((Book(b) \land b.bno \neq t.bno \land b.price \geq 35 \land Buys(t.sid, b.bno)) \rightarrow Cites(t.bno, b.bno)) \}
    Using logical equivalences, this query can also be expressed as the
SQL query
select t.sid, t.bno
from
        Buys t
where not exists (select 1
                      from
                              Book b
                      where b.bno != t.bno and
                              b.price >= 30 and
                              (t.sid, b.bno) in (select t1.sid, t1.bno
                                                    from Buys t1) and
                              (t.bno, b.bno) not in (select c.bno1, c.bno2
                                                         from Cites c));
    Starting from this SQL query, we obtain the safe TRC query
 \{(t.sid, t.bno) \mid Buys(t) \land
     \neg \exists b \in Book \ (b.bno \neq t.bno \land b.price \geq 35 \land Buys(t.sid, b.bno) \land \neg Cites(t.bno, b.bno)) \}
```

We now turn to the problems for this section.

1. • Consider the query 'Find the bno and title of each book that was bought by exactly one student.' This query can be expressed as the SQL query

Starting from this SQL query, express the query in safe TRC. Answer:

```
 \{(t.sid, t.bno) \mid Buys(t) \land \\ \exists S \in (Student(S) \land Buys(t) \land S.sid = t.sid \land b.bno = t.bno) \land \\ \forall (S1, S2(Student(S1) \land Student(S2)) \in Buys(t)(t.sid = S1.sid \land S2.sid = t.sid \land t.bno) \land \\ \land S1 = S2) \}
```

2. • Consider the query 'Find each pair (m,b) where m is a major and b is the bno of a book bought by a student who has major m and such that the price of b is the lowest among the set of books bought by students with major m.'

Starting from this SQL query, express the query in safe TRC.

Answer:

```
 \{(m.major, b.bno) \mid Major(m) \land Book(b) \land \exists t(Buys(t) \land b.bno = b.bno) \land \exists hm(hasMajor(hm) \land t.sid = hm.sid) \land \neg(\exists t \in Buys\exists b1 \in Book(t.bno = b1.bno) \land \exists hm \in hasmajor(t.sid, m.major) \land b1.price > b.price) \}
```

2 Expressing queries in (Extended) Safe TRC and Pure SQL with and without subquery expressions

An important consideration in expressing queries is knowing how they can be written in different, but equivalent, ways. In fact, this is an aspect of programming in general and, as can expected, is also true for database programming languages such as SQL. A learning outcome of this course is to acquire skills for writing queries in different ways. One of the main motivations for this is to learn that different formulations of the same query can dramatically impact performance, sometimes by orders of magnitude.

For the problems in this section, you will need to express queries in Pure SQL with and without subquery expressions. You can use the SQL operators INTERSECT, UNION, and EXCEPT, unless otherwise specified. You are allowed to use views including temporary and user-defined views.

To illustrate what you need to do for the problems in this section, consider the following example.

Example 2 Consider the query 'Find the bno and title of each book that cites a book and that was bought by a student who majors in CS or in Math.'

(a) Express this query in Safe TRC (i.e, with quantifiers \exists ' or \forall ').

```
 \{ (b.bno, b.title) \mid Book(b) \land \exists c(Cites(c) \land c.bno1 = b.bno) \land \\ \exists t(Buys(t) \land t.bno = b.bno \land \\ \exists hm(hasMajor(hm) \land hm.sid = t.sid \land (hm.major = \mathbf{CS} \lor hm.major = \mathbf{Math}))) \}
```

```
(b) Express this query in Extended Safe TRC (i.e, with subquery ex-
     pressions).
       \{(b.bno, b.title) \mid Book(b) \land some(\{c.bno1 = b.bno \mid Cites(c)\}) \land \}
         some(\{t.bno = b.bno \mid Buys(t) \land \})
           some(\{hm.sid = t.sid \land (hm.major = CS \lor hm.major = Math) \mid hasMajor(hm)\})\})
      Or, alternatively
       \{(b.bno, b.title) \mid Book(b) \land some(\{c.bno1 = b.bno \mid Cites(c)\}) \land
         some(\{t.bno = b.bno \land some(\{hm.sid = t.sid \land \})\})
           (hm.major = \mathbf{CS} \lor hm.major = \mathbf{Math}) \mid hasMajor(hm)\}) \mid Buys(t)\})\}
(c) Express this query in Pure SQL by only using the 'true = some'
      or 'true = all' subquery expressions.
      A possible solution is
      select b.bno, b.title
     from
            Book b
     where true = some (select c.bno1 = b.bno
                          from Cites c) and
             true = some (select t.bno = b.bno and
                          from Buys t
                           where true = some (select hm.sid = t.sid and
                                                       (hm.major = 'CS' or hm.major = 'Math')
                                                from
                                                       hasMajor hm);
      Or, alternatively
      select b.bno, b.title
           Book b
      where true = some (select c.bno1 = b.bno
                          from Cites c) and
             true = some (select t.bno = b.bno and
                                true = some (select hm.sid = t.sid and
                                                     (hm.major = 'CS' or hm.major = 'Math')
                                             from hasMajor hm)
                           from Buys t);
(d) Express this query in Pure SQL by only using the 'exists' or 'not
      exists' subquery expressions.
      A possible solution is
      select b.bno, b.title
     from
           Book b
      where exists (select 1
```

(e) Express this query in Pure SQL by only using the 'in' or 'not in' subquery expressions. You can not use the set operations INTERSECT, UNION, and EXCEPT.

A possible solution is

(f) Express this query in Pure SQL without using subquery expressions.

A possible solution is

```
select b.bno, b.title
from Book b, Cites c
where b.bno = c.bno1
intersect
select b.bno, b.title
from Book b, Buys t, hasMajor hm
where b.bno = t.bno and
    t.sid = hm.sid and
    (hm.major = 'CS' or hm.major = 'Math');
```

We now turn to the problems for this section.

- 3. Consider the query 'Find the bno and title of each book that is bought by a student who is (strictly) younger than each student who majors in Chemistry and who also bought that book.'
 - (a) Express this query in Safe TRC (i.e, with quantifiers '∃' or '∀').

Answer:

```
 \{(b.bno, b.title) \mid Book(b) \land \exists S \in (Buys(t) \land Student(S) \land t.bno = b.bno \land t.sid = S.sid \land \forall S1 \quad Student(S1) \in hasMajor(hm) \land hm.major =' Chemistry' \\ S.birthyear > S1.birthyear \land t.sid = S1.sid) \}
```

(b) • Express this query in Extended Safe TRC (i.e, with subquery expressions).

Answer:

```
 \{(b.bno, b.title) \mid book(b) \land \\ some(\{t.bno = b.bno \land t.sid = s.sid \mid buys(t)\} \land (some\{t.sid = s.sid \land \\ all(\{s.birthyear > s1.birthyear \land hm.sid = s1.sid \land \\ hm.major =' Chemistry' \mid Student(s) \land Student(s1) \land hasmajor(hm)\})\}))\}
```

- (c) Express this query in Pure SQL by only using the 'true = some' or 'true = all' subquery expressions. You can not use the set operations INTERSECT, UNION, and EXCEPT.
- (d) Express this query in Pure SQL by only using the 'exists' or 'not exists' subquery expressions. You can not use the set operations INTERSECT, UNION, and EXCEPT.
- (e) Express this query in Pure SQL by only using the 'in' or 'not in' subquery expressions. You can not use the set operations INTERSECT, UNION, and EXCEPT.
- (f) Express this query in Pure SQL without using subquery expressions. Now you can use the set operations INTERSECT, UNION, and EXCEPT.
- 4. Consider the query 'Find each student-book pair (s,b) where s is the sid of a student who majors in CS and who bought each book that costs no more than book b.'

(a) • Express this query in Extended Safe TRC (i.e, with subquery expressions).

Answer:

```
 \{(t.sid, t.bno) \mid Buys(t) \land hasMajor(hM) \land hM.sid = t.sid \land hM.major =' CS' \land all((\{some(\{t_1.sid = t.sid\} \mid Buys(t_1) \land t_1.bno = b.bno)\} \mid Book(b) \land Book(b_1) \land b.price \leq b_1.price \land b_1.bno = t.bno)) \}
```

- (b) Express this query in Pure SQL by only using the 'true = some' or 'true = all' subquery expressions. You can not use the set operations INTERSECT, UNION, and EXCEPT.
- (c) Express this query in Pure SQL by only using the 'exists' or 'not exists' subquery expressions. You can not use the set operations INTERSECT, UNION, and EXCEPT.
- (d) Express this query in Pure SQL by only using the 'in' or 'not in' subquery expressions. You can not use the set operations INTERSECT, UNION, and EXCEPT.
- (e) Express this query in Pure SQL without using subquery expressions. Now you can use the set operations INTERSECT, UNION, and EXCEPT.
- 5. Consider the query 'Find the sid and name of each student who bought all-but-one book that cost strictly more than \$30.'
 - (a) Express this query in Safe TRC (i.e, with quantifiers '∃' or '∀').

Answer:

```
\{(s.sid, s.sname) \mid Student(s) \land \\ \forall_{s_1} \in Student(Book(b_3) \land b_3.price > 30 \land Book(b_4) \land b_4.price > 30 \land \\ b_3.bno = b_4.bno \land \forall_b \in Book(b_3.bno \neq t.bno \land Buys(s_1.sid, t.bno) \land \\ b_1.bno = t.bno) \land \forall_{b_2} \in Book(b_3bno \neq t_2.bno \land Buys(s_1.sid, b_2.bno) \land \\ b_2.bno = t_2.bno))\}
```

Here $b_3 = b_{-}30_{-}1$ and $b_4 = b_{-}30_{-}2$ as per query, i wrote

(b) • Express this query in Pure SQL by only using the 'true = some' or 'true = all' subquery expressions. You can not use the set operations INTERSECT, UNION, and EXCEPT.

- (c) Express this query in Pure SQL by only using the 'exists' or 'not exists' subquery expressions. You can not use the set operations INTERSECT, UNION, and EXCEPT.
- (d) Express this query in Pure SQL by only using the 'in' or 'not in' subquery expressions. You can not use the set operations INTERSECT, UNION, and EXCEPT.
- (e) Express this query in Pure SQL without using subquery expressions. Now you can use the set operations INTERSECT, UNION, and EXCEPT.

Repeat the sub problems of the type 'a' through 'f' for the following queries

- 6. Consider the query 'Find the sid and sname of each student who majors in CS and who is (strictly) younger than some other student who also majors in CS."
- 7. Consider the query 'Find each (s,b) pair where s is the sid of a student who bought book b and such that each other book bought by s is a book cited by b."
- 8. Consider the query 'Find each major that is not a major of any person who bought a book with title 'Databases' or 'Philosophy'."
- 9. Consider the query 'Find the bno and title of each book that is bought by a student who majors in CS and who is, among all students who major in CS, the next-to-oldest.'

3 Expressing queries in Relational Algebra and RA SQL

Reconsider the queries in Section ?? and Section ??. The objective is to express these queries in Relational Algebra in standard notation and in RA SQL.

There are some restrictions:

- You can only use WHERE clauses that use conditions involving constants. For example conditions of the form ' $t.A\,\theta\,\mathbf{a}$ ', i.e., these involving a constant ' \mathbf{a} ' are permitted, but conditions of the form ' $t.A\,\theta\,s.B$ ', i.e., join conditions, are not allowed. These should be absorbed in JOIN operations in the FROM clause.
- You can not use commas in any FROM clause. Rather, you should use JOIN operations.

You can use the following letters, or indexed letters, to denote relation names in RA expressions:

S, S_1, S_2, \cdots	Student
B, B_1, B_2, \cdots	Book
T, T_1, T_2, \cdots	Buys
M, M_1, M_2, \cdots	Major
hM, hM_1, hM_2, \cdots	hasMajor
C, C_1, C_2, \cdots	Cites

To illustrate what you need to do, reconsider the query in Example ?? in Section ??.

Example 3 Consider the query 'Find the bno and title of each book that cites a book and that was bought by a student who majors in 'CS' or in 'Math'.'

(a) Express this query in Relational Algebra in standard notation.

A possible solution is

$$\pi_{bno,title}(Book \bowtie_{bno=bno_1} Cites) \cap$$

 $\pi_{bno,title}(\sigma_{major=\mathbf{CS} \vee major=\mathbf{Math}}(Book \bowtie Buys \bowtie hasMajor))$

If we use the letters in the above box, this expression becomes more succinct:

$$\pi_{bno,title}(B\bowtie_{bno=bno_1} C) \cap \\ \pi_{bno,title}(\sigma_{major=\mathbf{CS}\vee major=\mathbf{Math}}(B\bowtie T\bowtie hM))$$

You are also allowed to introduce letters that denote expressions. For example, let E and F denote the expression

$$\pi_{bno,title}(B\bowtie_{bno=bno_1} C)$$

and

$$\pi_{bno,title}(\sigma_{major=\mathbf{CS}\vee major=\mathbf{Math}}(B\bowtie T\bowtie hM)),$$

respectively. Then we can write the solution as follows:

$$E \cap F$$
.

(b) Express this query in RA SQL.

A possible solution is the following. Note that the WHERE clause only use conditions involving constants.

Another possible solution is the following. In this solution, we have associated the condition involving just constants, i.e., the condition 'major = 'CS' or major = 'Math', with the hasMajor relation.

We conclude with a solution that using a temporary view 'CS_or_Math_Student':

We now turn to the problems in this section.

- 10. Reconsider the query in Problem ?? 'Find the bno and title of each book that was bought by exactly one student.'
 - (a) Express this query in Relational Algebra in standard notation.

Answer:

```
\pi_{B.bno,B.title}(B\bowtie_{B.bno=T.bno}T) - \\ \pi_{B.bno,B.title}(B\bowtie_{B.bno=T.bno}T\bowtie_{B.bno=T_1.bno\land T_1.sid\neq T.sid}T_1)
```

(b) • Express this query in RA SQL.

- 11. Reconsider the query in Problem ?? 'Find each pair (m,b) where m is a major and b is the bno of a book bought by a student who has major m and such that the price of b is the lowest among the set of books bought by students with major m.'
 - (a) Express this query in Relational Algebra in standard notation.

Answer:

```
\pi_{hM.major,B.bno}(B\bowtie_{B.bno=T.bno}T\bowtie_{T.sid=hM.sid}hM) - \pi_{hM.major,B.bno}(B\bowtie_{B.bno=T.bno}T\bowtie_{hM.sid=T.sid}\bowtie_{hM.major=hM_2.major}hM_2\bowtie_{hM_2.sid=T_2.sid}T_2\bowtie_{T_2.bno=B_2.bno\land B.vrice>B_2.price}B_2)
```

- (b) Express this query in RA SQL.
- 12. Reconsider the query in Problem ?? 'Find the bno and title of each book that is bought by a student who is (strictly) younger than each student who majors in Chemistry and who also bought that book.'
 - (a) Express this query in Relational Algebra in standard notation.

Answer:

$$\pi_{B.bno,B.title}(T \bowtie_{T.sid=S.sid} S \bowtie_{B.bno=T.bno} B)$$

 $\bowtie \sigma_{(hM.major='Chemistry')} S_1 \bowtie_{hM.sid=S_1.sid \land S.birthyear} S_1.birthyear hM$

- (b) Express this query in RA SQL.
- 13. Reconsider the query in Problem ?? 'Find each student-book pair (s,b) where s is the sid of a student who majors in CS and who bought each book that costs no more than book b.'
 - (a) Express this query in Relational Algebra in standard notation.

$$CS = \pi_{t.sid,t.bno,b.price}(\sigma_{t.bno=b.bno\land t.sid=hm.sid\land hm.major='CS'}(T \bowtie B \bowtie HM))$$

$$RA = \pi_{sid,bno}(((\pi_{cs.sid,cs.bno,b.bno}(\sigma_{cs.price})_{b.price}(CS(cs) \bowtie BOOK(b)))) - (\pi_{cs.sid,cs.bno,b.bno}(\sigma_{cs.sid=t.sid\land t.bno=b.bno\land cs.price})_{=b.price}(CS(cs) \bowtie BUYS(t) \bowtie BOOK(b)))))$$

Here, $\operatorname{HM}:$ has Major relations, $\operatorname{T}:$ Buys relations, B : Book relations

- (b) Express this query in RA SQL.
- 14. Reconsider the query in Problem ?? 'Find the sid and name of each student who bought all-but-one book that cost strictly more than \$30.'
 - (a) Express this query in Relational Algebra in standard notation.

Answer:

$$morethan 30(M) = \pi_{T.sid,B.bno}(\sigma_{B.price>30}T \bowtie_{B.bno=T.bno} B)$$

$$K = \pi_{M.sid}(M) - (\pi_{M.sid}(M) - (\pi_{m.sid}(M \bowtie_{M.bno=M_1.bno \land M.sid=M_1.sid}))$$

$$\pi_{S.sid,S.sname(S\bowtie_{K.sid=S.sid}K)}$$

(b) • Express this query in RA SQL.

The remaining problems in this section are practice problems (indicated with a red bullet \bullet).

Repeat parts (a) and (b) for these queries.

- 15. Consider the query 'Find the sid and sname of each student who majors in 'CS' and who is (strictly) younger than some other student who also majors in 'CS'.
- 16. Consider the query 'Find each (s,b) pair where s is the sid of a student who bought book b and such that each other book bought by s is a book cited by b.
- 17. Consider the query 'Find each major that is not a major of any person who bought a book with title 'Databases' or 'Philosophy'.
- 18. Consider the query 'Find the bno and title of each book that is bought by a student who majors in CS and who is, among all students who major in CS, the next-to-oldest.'

4 Expressing constraints using Relational Algebra

Recall that it is possible to express constraints as TRC sentences and as boolean SQL queries. It is also possible to express constraints using RA expressions. Let E, F, and G denote RA expressions. Then we can express constraints using set comparisons between RA expressions as follows:

 $E \neq \emptyset$ which is true if E evaluates to an non-empty relation

 $E = \emptyset$ which is true if E evaluates to the empty relation

 $F\subseteq G$ which is true if F evaluates to a relation that is a subset of the relation obtained from G

 $F \not\subseteq G$ which is true if F evaluates to a relation that is not a subset of the relation obtained from G

Here are some examples of writing constraints in this manner.

Example 4 'Some students majors in CS.' This constraint can be expressed as follows:

$$\pi_{sid}(\sigma_{major=\mathbf{CS}}(hasMajor)) \neq \emptyset.$$

Indeed, the RA expression

$$\pi_{sid}(\sigma_{major=\mathbf{CS}}(hasMajor))$$

computes the set of all student sids who major in CS. If this set is not empty then there are indeed students who major in CS.

Incidentally, the constraint 'No one majors in CS' can be written as follows:

$$\pi_{sid}(\sigma_{major=\mathbf{CS}}(hasMajor)) = \emptyset.$$

Example 5 Each student buys at least two books. This constraint can be expressed as follows:

$$\pi_{sid}(S) \subseteq \pi_{T_1.sid}(\sigma_{T_1.bno \neq T_2.bno}(T_1 \bowtie_{T_1.sid = T_2.pid} T_2)).$$

Indeed,

$$\pi_{sid}(S)$$

computes the set of all student sids and

$$\pi_{T_1.sid}(\sigma_{T_1.bno\neq T_2.bno}(T_1\bowtie_{T_1.sid=T_2.pid} T_2))$$

computes the set of all sids of student who buy at least two books. When the first set is contained in the second, we must have that each student buys at least two books.

Incidentally, the constraint 'Some student buys fewer than two books" can be written as follows:

$$\pi_{sid}(S) \not\subseteq \pi_{T_1.sid}(\sigma_{T_1.bno \neq T_2.bno}(T_1 \bowtie_{T_1.sid = T_2.pid} T_2)).$$

We now turn to the problems in this section.

Express each of the following constraints using set comparisons between RA expressions as illustrated in Example ?? and Example ??.

19. • Among the books that cite a book, there are books that cite the same set of other books.

Answer:

$$\pi_{C_1.bno1}(\sigma_{C_1.bno1\neq C_2.bno}(C_1\bowtie_{C_1.bno2=C_2.bno2}C_2))\neq\emptyset.$$

20. • Some student who majors only bought books that where bought by students who major in Math.

Answer:

$$\pi_{T.sid}(T \bowtie_{T.sid=hM_1.sid} hM_1) \subseteq \pi_{T_2.bno}(\sigma_{hM_2.major='Math'}(T_2 \bowtie_{T_2.sid=hM_2.sid} hM_2))$$

21. • There are pairs of majors that have no common students who have those majors.

Answer:

$$\pi_{hM_1.major,hM_2.major}(\sigma_{hM_1.sid\neq hM_2.sid}(hM_1\bowtie hM_2))\neq\emptyset$$

22. • Attribute 'sid' in the relation has Major is a foreign key referencing the primary key 'sid' in the relation Student.

Answer:

$$\pi_{S.sid}(S) \subseteq \pi_{hM.sid}(hM_{hM.sid=S.sid} \bowtie S)$$

For each of the following practice problem, express constraints using set comparisons between RA expressions as illustrated in Example ?? and Example ??.

- 23. No book cites each book that cost strictly less than \$30.
- 24. Each major is not the major of all students.
- 25. Each pair of different students who share a major buy a book with the same bno.
- 26. The attribute sid is a primary key of the Student relation.

5 Views

Express the following parameterized and recursive views. You are allowed to combine the features of both Pure SQL and RA SQL.

- 27. Define a parameterized view 'PurchasedBookLessPrice(sid int, price integer)' that returns, for a given student identified by 'sid' and a given 'price' value, the subrelation of 'Book' of books that are bought by that student and that cost strictly less than 'price'.
 - Test your view for the parameter values (1001,15), (1001,30), (1001,50), and (1002,30).
- 28. Define a parameterized view 'CitedBookbyMajor(major text)' that returns for a major 'major' the subrelation of 'Book' of books that are cited by a book bought by a the student who majors in 'major'.

Test your view for each major.

- 29. Define a parameterized view 'JointlyBoughtBook(sid1 integer, sid2 integer)' that returns the subrelation of 'Book' of books that are bought by both the students with sids 'sid1' and 'sid2', respectively.
 - Test your view for the parameters (1001, 1002), (1001,1003), and (1002,1003).
- 30. Let PC(parent : integer, child : integer) be a rooted parent-child tree. So a pair (n, m) in 'PC' indicates that node n is a parent of node m. The 'sameGeneration(n1, n2)' binary relation is inductively defined using the following two rules:

- If n is a node in PC, then the pair (n, n) is in the sameGeneration relation. (Base rule)
- If n_1 is the parent of m_1 in PC and n_2 is the parent of m_2 in PC and (n_1, n_2) is a pair in the sameGeneration relation then (m_1, m_2) is a pair in the sameGeneration relation. (Inductive Rule)

Write a recursive view for the sameGeneration relation. Test your view.

6 Theory about safe TRC and Relational Algebra

31. • Prove that each safe TRC formula $F(t_1, \ldots, t_n)$ can be brought into the following normal form

$$\bigvee_{i=1}^{k} R_1^i(t_1) \wedge \cdots \wedge R_n^i(t_n) \wedge G^i jt_1, \dots t_n)$$

where

- R_i^j is a relation name for each $i \in [1, n]$ and $j \in [1, k]$; and
- $G^{j}(t_{1},...,t_{n})$ is a TRC formula wherein no disjunctions (' \vee ') occur for each $i \in [1,k]$.
- 32. Prove that for each RA expression 'E' with attributes (A_1, \ldots, A_k) , there exists a safe TRC formula ' F_E ' such that 'E' and ' $\{(A_1: u_1(t_1), \ldots, A_k: u_k(t_1, \ldots, t_n)) \mid F_E(t_1, \ldots, t_n)\}$ ' express the same query.
- 33. Prove that for each safe TRC formula ' $F(t_1, \ldots, t_k)$ ' there exists a RA expressions ' E_F ' such that ' $\{(A_1 : u_1(t_1), \ldots, A_k : u_k(t_1, \ldots, t_n)) \mid F_E(t_1, \ldots, t_n)\}$ ' and E_F express the same query.