

Learned from tap academy

<https://www.youtube.com/watch?v=lyfMNHoOwJ0&list=PLU83Ru7iGtAvP1rqt65MCDSBPFCzUKGXG&index=5>

We are finding time complexity using a method called “FREQUENCY COUNT METHOD”

This is based on condition that

- 1) Eliminate constants
- 2) Retain highest order term

1)

Here for statement frequency is $n+1$ because on $n+1$ only the termination condition is reached. But the inner statements inside for loop will run only for n time.

Eg: $n=3$. So I will reach till 0,1,2,3[ie 4 times] for the termination condition, but sum will be calculated 3 times inside the for loop .Ans is $O(n)$



code	frequency
<code>int arr[] = {1,5,2};</code>	1
<code>int n = arr.length;</code>	1
<code>int sum = 0;</code>	1
<code>for(int i=0; i<n; i++){</code>	$n+1$
<code> sum = sum + arr[i];</code>	n
<code>}</code>	

$O(n)$

- 2) Next loop example, here inner for loop is $n(n+1)$ is because due to outer for loop it will run n times and the inner for loop itself will execute for $n+1$ times , hence $n*(n+1)$. Answer is $O(n^2)$

*	*	*
*	*	*
*	*	*

code	frequency
<pre>for(int i=0; i<n ; i++){ for(int j=0; j<n ; j++){ System.out.print("*"); } System.out.println(); }</pre>	$n+1$ $n*(n+1)$ $n*n$ n
	$n+1 + n^2 + n + n^2 + n$

n 3

i	j
0	0
1	1
2	2
3	3

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Conditions:

01

Eliminate constants

02

Retain the highest ordered term

3) Three nested loop

A

1	2	2
1	3	1
2	1	1

\times

B

2	3	2
1	2	3
2	1	2

code

```
for(int i=0; i<n ; i++){
    for(int j=0; j<n ; j++){
        c[i][j] = 0;
        for(int k=0; k<n; k++){
            c[i][j] = c[i][j] + a[i][k] * b[k][j];
        }
    }
}
```

frequency

 $n+1$
 $n*(n+1)$
 $n*n$
 $n*n*(n+1)$
 $n*n*n$

$n+1 + n^2 + n + n^2 + n^3 + n^2 + n^3$

n 3

4) Ans O(n). +1 in each row is to denote the termination condition. Summation of n natural numbers is written as $n(n+1)/2$

0 1 2 3 4

★				
★	★			
★	★	★		
★	★	★	★	
★	★	★	★	★

$(1+2+3+4+5) + 5$

$\frac{n(n+1)}{2} + n$

n 5

Σ

Code

```
for(int i = 0; i<n ;i++)
{
    for(int j = 0; j<=i ; j++)
    {
        System.out.print("*");
    }
    System.out.println();
}
```

Frequency

$n+1$
$\frac{n(n+1)}{2} + n$
$\frac{n(n+1)}{2}$
n

$n+1+n^2+n+n+n$

i	j	No of times j executed
0	0	+1
1	0,1	+1
2	0,1,2	+1
3	0,1,2,3	+1
4	0,1,2,3,4	+1

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5)

i	p
0	0
1	$0+1$
2	$0+1+2$
3	$0+1+2+3$
...	
K	$0+1+2+3+\dots+K$

Termination condition

$$p > n$$

$$\frac{k(k+1)}{2} > n$$

$$\frac{k^2+k}{2} > n$$

$$k^2+k > n$$

$$k^2 > n$$

Code

```
for(int i = 0; p <= n; i++)
{
    p = p+i;
}
```

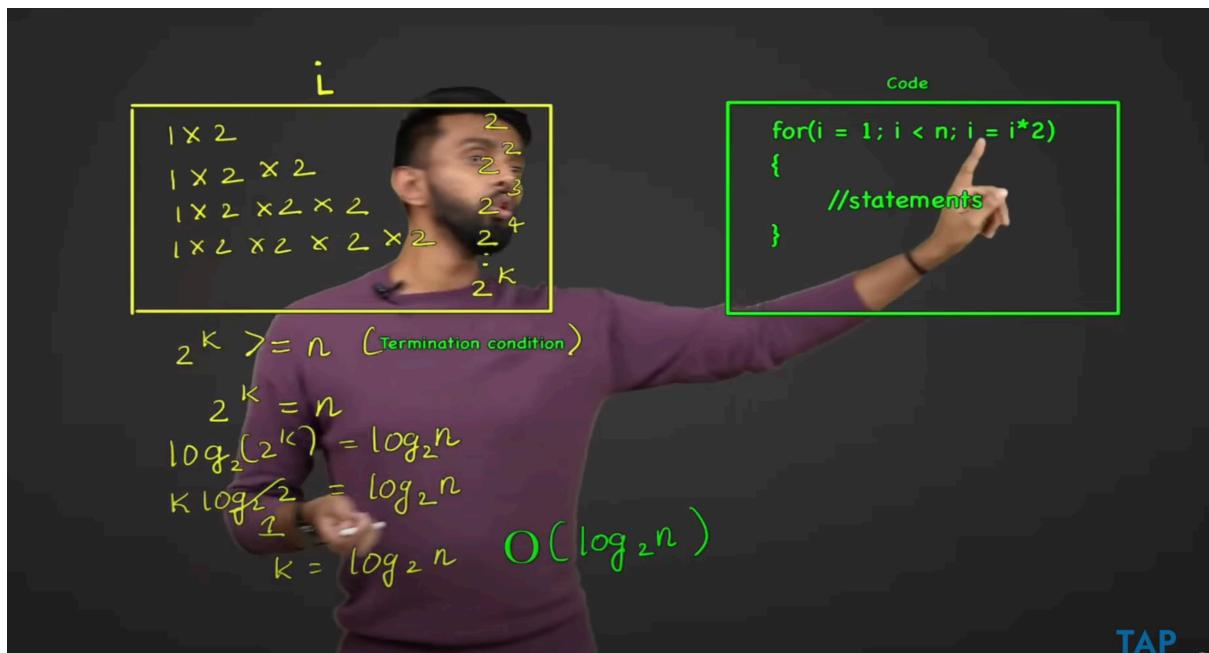
$\sqrt{k^2} > \sqrt{n}$

$k > \sqrt{n}$

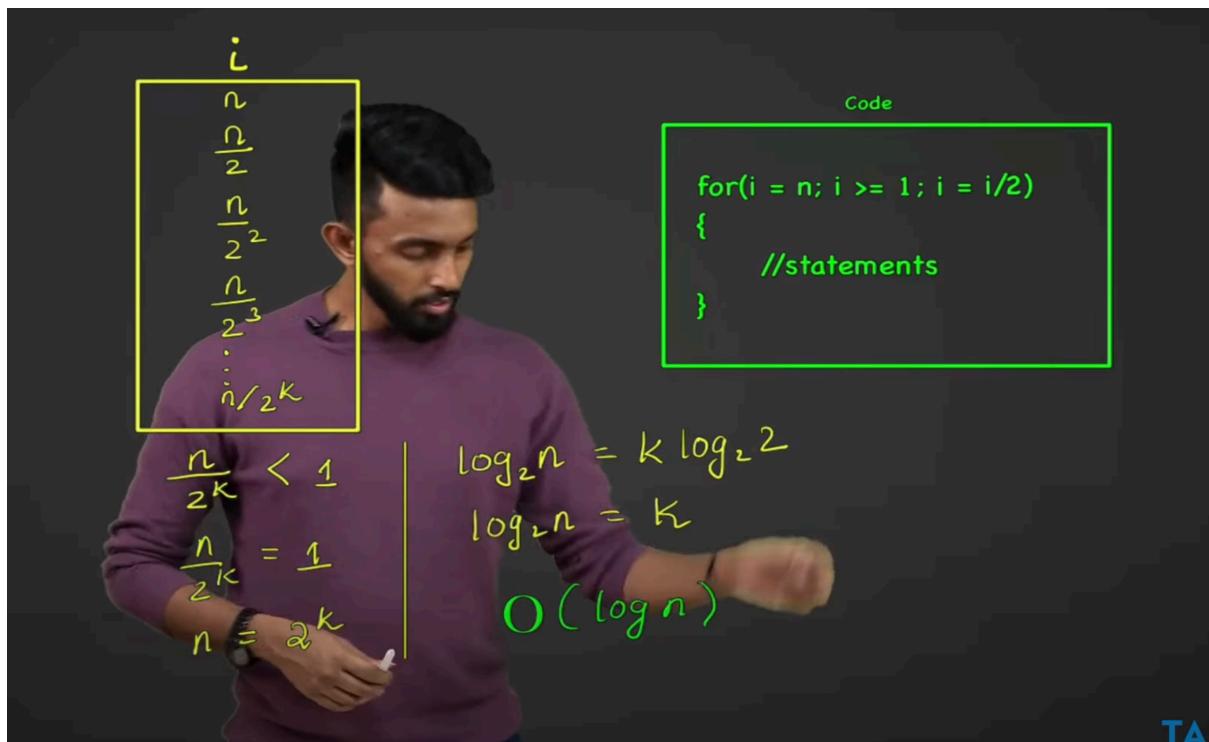
$O(\sqrt{n})$

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6) Ans $O(\log n)$



7)



8)

$$\begin{aligned}k &\geq n \\i^2 &\geq n \\\sqrt{i^2} &\geq \sqrt{n} \\i &\geq \sqrt{n} \\O(\sqrt{n})\end{aligned}$$

Code

```
for(i = 0; i*i < n; i++)  
{  
    //statements  
}
```

$$\begin{array}{ll}0 & 0^2 \\1 & 1^2 \\2 & 2^2 \\3 & 3^2 \\4 & 4^2 \\5 & 5^2 \\\vdots & \vdots \\k & i^2\end{array}$$

9)ANS : $O(n)$

$O(n)$ ←
+
 $O(n)$ ←
 $O(n)$

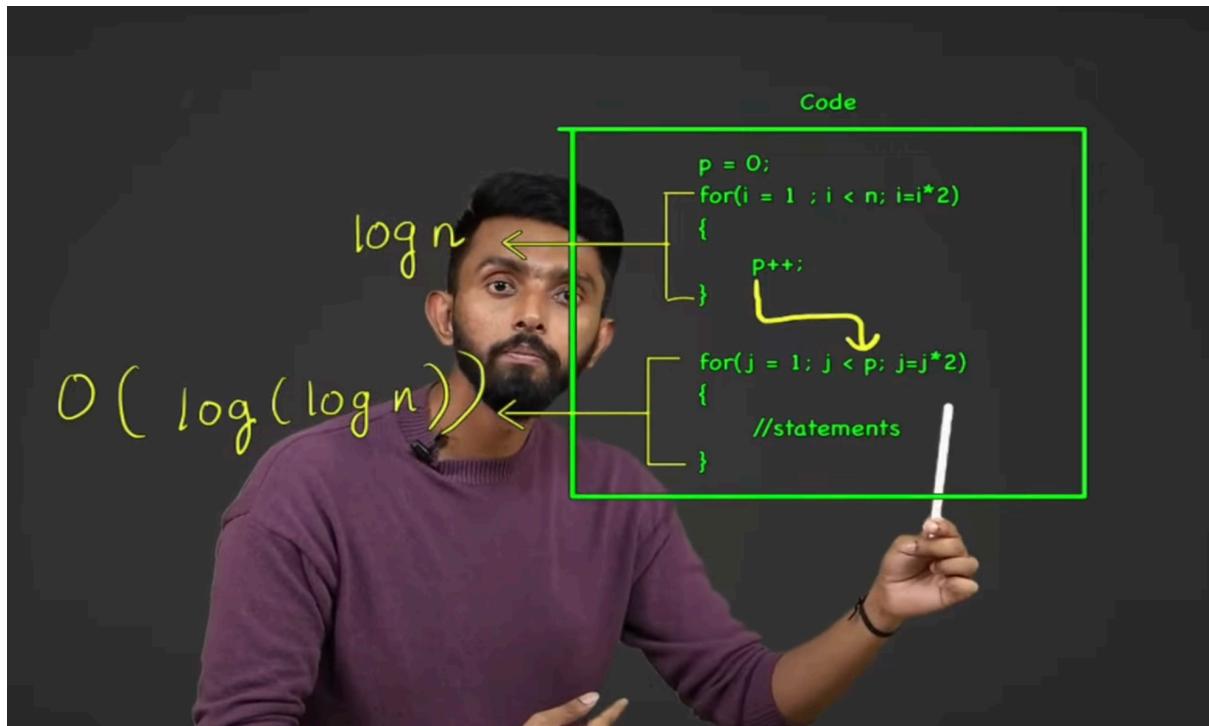
Code

```
for(i = 0; i < n; i++)  
{  
    //statements  
}  
  
for(j = 0; j < n; j++)  
{  
    //statements  
}
```

10) Ans $O(\log(\log n))$. First for loop $\log n$. and second for loop can be represented as $\log p$. Since p itself take $\log n$ we are coming to conclusion of $\log(\log n)$

$$P = \log n$$

$$\log p = \log(\log n)$$



11)

A man with a beard, wearing a maroon long-sleeved shirt, is standing and gesturing with his hands while speaking. He is positioned in front of a chalkboard or screen displaying code and its time complexity analysis.

Code	Frequency
<pre>for(i = 0; i < n; i++) { for(j = 1; j < n; j=j*2) { //statements } }</pre>	$n + l$ $n * \log n$ $n * \log n - 1$

Handwritten calculations and the final result are written below the board:

$$n + 2 * (n * \log n)$$
$$n + n \log n$$
$$\mathcal{O}(n \log n)$$

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