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 **jesusmlb** First draft of PriceO

52061aa · yesterday 🕒 History 🗨

52061aa

price\_optimization / price\_optimization\_project.ipynb

↑ Top

PreviewCodeBlame4228 lines (4228 loc) · 1000 KB

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```
import pandas as pd
import numpy as np
import matplotlib.pyplot as plt
import datetime
import seaborn as sns
import random
from sklearn.preprocessing import StandardScaler

# To Split our data into train and test sets
from sklearn.model_selection import train_test_split

# To build our model
import tqdm as notebook_tqdm
from prophet import Prophet
from prophet.plot import plot_plotly, plot_components_plotly
from sklearn.ensemble import GradientBoostingRegressor
from xgboost import XGBRegressor
from sklearn.ensemble import RandomForestRegressor

# Metrics to evaluate our model
from sklearn.metrics import mean_squared_error, mean_absolute_error, r2_score

# To optimize our model
from scipy.optimize import minimize_scalar

import warnings
warnings.filterwarnings('ignore')
```

Let's upload our datasets for this analysis

In [612..

```
# Let's see our items in transactions
items = pd.read_csv("../files/olist_order_items_dataset.csv")
orders = pd.read_csv("../files/olist_orders_dataset.csv")
items.head()
```

Out[612..

	order_id	order_item_id	product_id	seller_id	shipping_li
0	00010242fe8c5a6d1ba2dd792cb16214	1	4244733e06e7ecb4970a6e2683c13e61	48436dade18ac8b2bce089ec2a041202	2017-09-15
1	00018f77f2f0320c557190d7a144bdd3	1	e5f2d52b802189ee658865ca93d83a8f	dd7ddc04e1b6c2c614352b383efe2d36	2017-05-03
2	000229ec398224ef6ca0657da4fc703e	1	c777355d18b72b67abbef9df44fd0fd	5b51032eddd242adc84c38acab88f23d	2018-01-16
3	00024acbcd0a6daa1e931b038114c75	1	7634da152a4610f1595efa32f14722fc	9d7a1d34a5052409006425275ba1c2b4	2018-08-15
4	00042b26cf59d7ce69dfabb4e55b4fd9	1	ac6c3623068f30de03045865e4e10089	df560393f3a51e74553ab94004ba5c87	2017-02-13

In [613..

```
# Let's evaluate the datatypes and null values
items.info()
```

```
<class 'pandas.core.frame.DataFrame'>
RangeIndex: 112650 entries, 0 to 112649
Data columns (total 7 columns):
#   Column                Non-Null Count  Dtype
---  ---
0   order_id              112650 non-null object
1   order_item_id        112650 non-null int64
2   product_id           112650 non-null object
3   seller_id            112650 non-null object
4   shipping_limit_date   112650 non-null object
5   price                112650 non-null float64
6   freight_value        112650 non-null float64
dtypes: float64(2), int64(1), object(4)
memory usage: 6.0+ MB
```

We don't have any null values, but some column has a datatype as an object when it is supposed to be datetime. Let's change it.

In [614..

```
# Change column shipping_limit_date to a DateTime Dtype
items['shipping_limit_date'] = pd.to_datetime(items['shipping_limit_date'])
items.info()
```

```
<class 'pandas.core.frame.DataFrame'>
RangeIndex: 112650 entries, 0 to 112649
Data columns (total 7 columns):
#   Column                Non-Null Count  Dtype
---  ---
0   order_id              112650 non-null object
1   order_item_id        112650 non-null int64
2   product_id           112650 non-null object
3   seller_id            112650 non-null object
4   shipping_limit_date   112650 non-null datetime64[ns]
5   price                112650 non-null float64
6   freight_value        112650 non-null float64
dtypes: datetime64[ns](1), float64(2), int64(1), object(3)
memory usage: 6.0+ MB
```

Great! Now let's evaluate another dataset

In [615..

```
# Let's check our order data
orders.head()
```

Out[615..

	order_id	customer_id	order_status	order_purchase_timestamp	order_approved_at	o
0	e481f51cbdc54678b7cc49136f2d6af7	9ef432eb6251297304e76186b10a928d	delivered	2017-10-02 10:56:33	2017-10-02 11:07:15	
1	53cdb2fc8bc7dce0b6741e2150273451	b0830fb4747a6c6d20dea0b8c802d7ef	delivered	2018-07-24 20:41:37	2018-07-26 03:24:27	
2	47770eb9100c2d0c44946d9cf07ec65d	41ce2a54c0b03bf3443c3d931a367089	delivered	2018-08-08 08:38:49	2018-08-08 08:55:23	
3	949d5b44dbf5de918fe9c16f97b45f8a	f88197465ea7920adcdbec7375364d82	delivered	2017-11-18 19:28:06	2017-11-18 19:45:59	
4	ad21c59c0840e6cb83a9ceb5573f8159	8ab97904e6dae8866dbdbc4fb7aad2c	delivered	2018-02-13 21:18:39	2018-02-13 22:20:29	

In [616..

```
# Let's see the null values and datatypes
orders.info()
```

```
<class 'pandas.core.frame.DataFrame'>
RangeIndex: 99441 entries, 0 to 99440
Data columns (total 8 columns):
#   Column                Non-Null Count  Dtype
---  ---
0   order_id              99441 non-null object
1   customer_id           99441 non-null object
2   order_status          99441 non-null object
3   order_purchase_timestamp 99441 non-null object
4   order_approved_at     99281 non-null object
5   order_delivered_carrier_date 97658 non-null object
6   order_delivered_customer_date 96476 non-null object
7   order_estimated_delivery_date 99441 non-null object
dtypes: object(8)
memory usage: 6.1+ MB
```

We can see that some columns don't have the right datatype. Let's change them.

In [617..

```
# Change object to datetime Dtype
date_columns = [
    'order_purchase_timestamp',
    'order_approved_at',
    'order_delivered_carrier_date',
    'order_delivered_customer_date',
    'order_estimated_delivery_date'
]
orders[date_columns] = orders[date_columns].apply(pd.to_datetime)
orders.info()
```

```
<class 'pandas.core.frame.DataFrame'>
RangeIndex: 99441 entries, 0 to 99440
Data columns (total 8 columns):
#   Column                Non-Null Count  Dtype
---  ---
0   order_id              99441 non-null object
1   customer_id           99441 non-null object
2   order_status          99441 non-null object
3   order_purchase_timestamp 99441 non-null datetime64[ns]
```

```
4 order_approved_at          99281 non-null  datetime64[ns]
5 order_delivered_carrier_date 97658 non-null  datetime64[ns]
6 order_delivered_customer_date 96476 non-null  datetime64[ns]
7 order_estimated_delivery_date 99441 non-null  datetime64[ns]
dtypes: datetime64[ns](5), object(3)
memory usage: 6.1+ MB
```

Perfect! Now that we have the right data types, let's evaluate our null values.

```
In [618... # Let's see our first column with null values that is oder_approved_at
orders[orders['order_approved_at'].isnull()].value_counts('order_status')
```

```
Out[618... order_status
canceled      141
delivered      14
created         5
dtype: int64
```

As we can see most of them are canceled and created orders, so we can drop them. Created orders as well because don't have the dates yet.

```
In [619... # Remove cancel and created orders from our dataset
orders = orders[(orders['order_status'] != 'canceled') & (orders['order_status'] != 'created')]
orders.info()
```

```
<class 'pandas.core.frame.DataFrame'>
Int64Index: 98811 entries, 0 to 99440
Data columns (total 8 columns):
#   Column                                Non-Null Count  Dtype
---  -
0   order_id                             98811 non-null  object
1   customer_id                         98811 non-null  object
2   order_status                        98811 non-null  object
3   order_purchase_timestamp            98811 non-null  datetime64[ns]
4   order_approved_at                  98797 non-null  datetime64[ns]
5   order_delivered_carrier_date        97583 non-null  datetime64[ns]
6   order_delivered_customer_date       96470 non-null  datetime64[ns]
7   order_estimated_delivery_date       98811 non-null  datetime64[ns]
dtypes: datetime64[ns](5), object(3)
memory usage: 6.8+ MB
```

What about our delivered orders? Let's filter our data to evaluate this datapoint.

```
In [620... # Null rows with order_status delivered
orders[orders['order_approved_at'].isnull()]
```

```
Out[620...      order_id      customer_id  order_status  order_purchase_timestamp  order_approved
5323  e04abd8149ef81b95221e88f6ed9ab6a  2127dc6603ac33544953ef05ec155771      delivered      2017-02-18 14:40:00      1
16567  8a9adc69528e1001fc68dd0aaebbb54a  4c1ccc74e00993733742a3c786dc3c1f      delivered      2017-02-18 12:45:31      1
19031  7013bfc1c97fe719a7b5e05e61c12db  2941af76d38100e0f8740a374f1a5dc3      delivered      2017-02-18 13:29:47      1
22663  5cf925b116421afa85ee25e99b4c34fb  29c35fc91fc13fb5073c8f30505d860d      delivered      2017-02-18 16:48:35      1
23156  12a95a3c06dbaec84bcfb0e2da5d228a  1e101e0daffadce8159d25a8e53f2b2      delivered      2017-02-17 13:05:55      1
26800  c1d4211b3dae76144deccd6c74144a88  684cb238dc5b5d6366244e0e0776b450      delivered      2017-01-19 12:48:08      1
38290  d69e5d356402adc8cf17e08b5033acfb  68d081753ad4fe22fc4d410a9eb1ca01      delivered      2017-02-19 01:28:47      1
39334  d77031d6a3c8a52f019764e68f211c69  0bf35cac6cc7327065da879e2d90fae8      delivered      2017-02-18 11:04:19      1
48401  7002a78c79c519ac54022d4f8a65e6e8  d5de688c321096d15508faae67a27051      delivered      2017-01-19 22:26:59      1
61743  2eecb0d85f281280f79fa00f9cec1a95  a3d3c38e58b9d2dfb9207cab690b6310      delivered      2017-02-17 17:21:55      1
63052  51eb2eebd5d76a24625b31c33dd41449  07a2a7e0f63fd8cb757ed77d4245623c      delivered      2017-02-18 15:52:27      1
67697  88083e8f64d95b932164187484d90212  f67cd1a215aae2a1074638bbd35a223a      delivered      2017-02-18 22:49:19      1
72407  3c0b8706b065f9919d0505d3b3343881  d85919cb3c0529589c6fa617f5f43281      delivered      2017-02-17 15:53:27      1
84999  2babbb4b15e6d2dfe95e2de765c97bce  74beba46603f9340e3b50c6b086f992      delivered      2017-02-18 17:15:03      1
```

We can observe that it is just missing our approved date. We can take the average of other orders and fill it.

```
In [621... # Let's calculate the average of the delivered orders when the customer purchased the product and when the order when approved
average_difference = (orders['order_approved_at'] - orders['order_purchase_timestamp']).mean()
average_difference
```

```
Out[621... Timedelta('0 days 10:23:53.854246586')
```

Our mean is around 10 hours, so let's fill this row with this value.

```
In [622... # Fill null values in 'order_approved_at' with the calculated average difference
orders['order_approved_at'].fillna(orders['order_purchase_timestamp'] + average_difference, inplace=True)
orders.info()
```

```
<class 'pandas.core.frame.DataFrame'>
Int64Index: 98811 entries, 0 to 99440
Data columns (total 8 columns):
#   Column                                Non-Null Count  Dtype
---  -
0   order_id                             98811 non-null  object
1   customer_id                         98811 non-null  object
2   order_status                        98811 non-null  object
3   order_purchase_timestamp            98811 non-null  datetime64[ns]
4   order_approved_at                  98811 non-null  datetime64[ns]
5   order_delivered_carrier_date        97583 non-null  datetime64[ns]
6   order_delivered_customer_date       96470 non-null  datetime64[ns]
7   order_estimated_delivery_date       98811 non-null  datetime64[ns]
dtypes: datetime64[ns](5), object(3)
memory usage: 6.8+ MB
```

Great! Now we can see the other null values, let's start with order\_delivered\_customer\_date

```
In [623... # Let's see null values from order_delivered_carrier_date
orders[orders['order_delivered_carrier_date'].isnull()].value_counts('order_status')
```

```
Out[623... order_status
unavailable      609
invoiced         314
processing       301
approved          2
delivered         2
dtype: int64
```

```
In [624... # Let's see those who say unavailable
orders[orders['order_status'] == 'unavailable'].isnull().sum()
```

```
Out[624... order_id      0
customer_id  0
order_status 0
order_purchase_timestamp 0
order_approved_at 0
order_delivered_carrier_date 609
order_delivered_customer_date 609
order_estimated_delivery_date 0
dtype: int64
```

After checking the null values, we see that the two columns don't have the information we need. Let's drop these rows because it's complicated to calculate both columns.

```
In [625... # Remove rows with null values of order_delivered_carrier_date and order_delivered_customer_date
orders = orders[(orders['order_delivered_carrier_date'].notna()) & (orders['order_delivered_customer_date'].notna())]
orders.info()
```

```
<class 'pandas.core.frame.DataFrame'>
Int64Index: 96469 entries, 0 to 99440
Data columns (total 8 columns):
#   Column                                Non-Null Count  Dtype
---  -
0   order_id                             96469 non-null  object
1   customer_id                         96469 non-null  object
2   order_status                        96469 non-null  object
3   order_purchase_timestamp            96469 non-null  datetime64[ns]
4   order_approved_at                  96469 non-null  datetime64[ns]
5   order_delivered_carrier_date        96469 non-null  datetime64[ns]
6   order_delivered_customer_date       96469 non-null  datetime64[ns]
7   order_estimated_delivery_date       96469 non-null  datetime64[ns]
dtypes: datetime64[ns](5), object(3)
memory usage: 6.6+ MB
```

Great! Our three datasets are ready to be analyzed

Great! Our three datasets are ready to be analyzed.

## Exploratory Data Analysis

In [626...  

```
# Let's look out for the top 10 products that have been sold
items['product_id'].value_counts().head(10)
```

Out[626...  
aca2eb7d00ea1a7b8ebd4e68314663af 527  
99a4788cb24856965c36a24e339b6058 488  
422879e10f46682990de24d770e7f83d 484  
389d119b48cf3043d311335e499d9c6b 392  
368c6c730842d78016ad823897a372db 388  
53759a2ecddad2bb87a079a1f1519f73 373  
d1c427060a0f73f6b889a5c7c61f2ac4 343  
53b36df67ebb7c41585e8d54d6772e08 323  
154e7e31ebfa092203795c972e5804a6 281  
3dd2a17168ec895c781a9191c1e95ad7 274  
Name: product\_id, dtype: int64

Let's see the prices over time of our most sold product but first, we need to merge the dataset items and orders to have the purchased date.

In [627...  

```
# Let's merge our datasets
orders_items = pd.merge(orders, items, on='order_id')
# Let's see how many items were sold by the year
orders_items['order_purchase_year'] = orders_items['order_purchase_timestamp'].dt.year
orders_items['order_purchase_year'].value_counts()
```

Out[627...  
2018 60318  
2017 49553  
2016 317  
Name: order\_purchase\_year, dtype: int64

We can see that 2016 doesn't have enough data compared to other years, let's remove it and keep just the years that have more data.

In [628...  

```
# Remove 2016 from our dataset
orders_items = orders_items[orders_items['order_purchase_year'] != 2016]
```

In [629...  

```
# Group data by day and calculate the sum of quantity sold and mean price
daily_sales = orders_items.groupby(orders_items['order_purchase_timestamp'].dt.date).agg({'price': 'mean', 'freight_value':  
# Let's change the name of the columns order_item_id to quantity_sold and order_purchase_timestamp to date
daily_sales.rename(columns={'order_item_id': 'quantity_sold', 'order_purchase_timestamp': 'date'}, inplace=True)
```

In [630...  

```
# Let's create a function to plot our data
# Specify the figure size (width, height) in inches
def plot_2axis(df, column_name_1, column_name_2):
    plt.figure(figsize=(20, 10)) # Adjust the size as needed

    # Create two subplots with the shared x-axis
    ax1, ax2, ax3 = plt.axes(), plt.subplot(), plt.subplot()

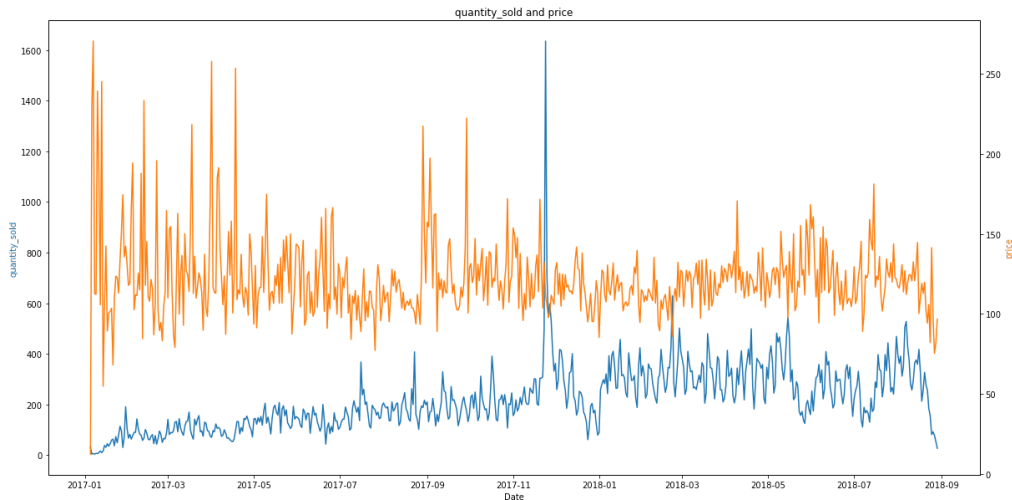
    # Plot quantity sold (quantity_sold) using the first y-axis (ax1)
    ax1.set_xlabel('Date')
    ax1.set_ylabel(column_name_1, color='tab:blue')
    ax1.plot(df['date'], df[column_name_1], color='tab:blue')
    #ax1.tick_params(axis='y', labelcolor='tab:blue')

    # Create a second y-axis (ax2) and plot price using it
    ax2 = ax1.twinx() # share the same x-axis
    ax2.set_ylabel(column_name_2, color='tab:orange')
    ax2.plot(df['date'], df[column_name_2], color='tab:orange')
    #ax2.tick_params(axis='y', labelcolor='tab:orange')

    # Customize the appearance of the plot
    plt.title(f'{column_name_1} and {column_name_2}')
    plt.xticks(rotation=45)

    # Show the plot
    plt.show()

plot_2axis(daily_sales, 'quantity_sold', 'price')
```



We can observe that there is a correlation between the price and the quantity of orders. Seems that a considerable quantity of products are elastic. Also, we can observe that we have an outlier in 2017, let's look at the date and check if it has something to do with any holiday or event in Brazil.

In [631...  

```
# Date of the outlier
daily_sales[daily_sales['quantity_sold'] == daily_sales['quantity_sold'].max()]
```

Out[631...  

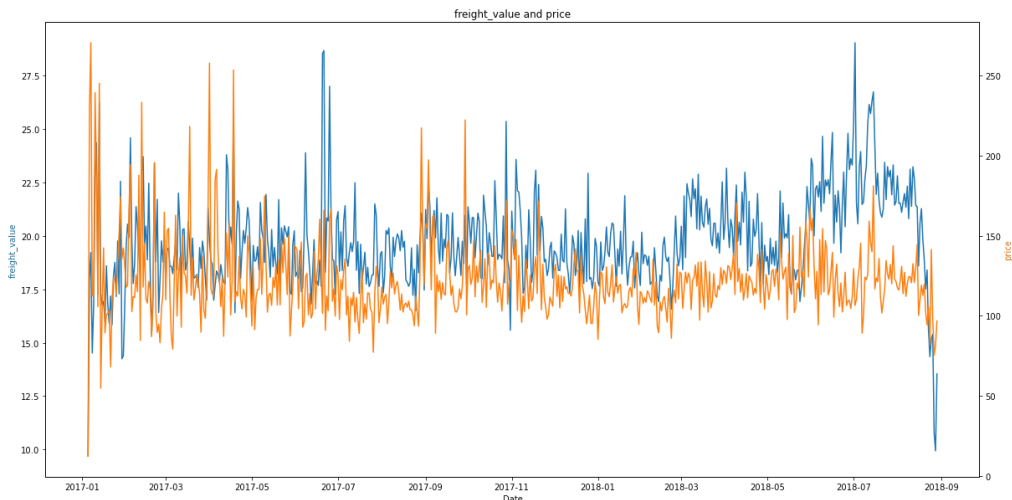
	date	price	freight_value	quantity_sold
323	2017-11-24	111.462141	18.782067	1636

This date matches with Black Friday so it's ok that we have a higher volume of sales in this period.

How about price and freight value over time? Do they have any correlation?

In [632...  

```
plot_2axis(daily_sales, 'freight_value', 'price')
```



We can see that the freight feature has had a bigger gap in the last few months. Why is that notorious now? Does it have something to do with some macroeconomic event?

In [633...  

```
# Let's upload our datasets, Let's start with the Consumer Confidex Index, Inflation rate and unemployment rate
cci = pd.read_csv("../files/cci_brazil.csv")
```

```
inflation = pd.read_csv("../files/inflation_brazil.csv")
unemployment = pd.read_csv("../files/unem_br.csv")
```

```
In [634... # Let's change the date format of our datasets
daily_sales['date'] = pd.to_datetime(daily_sales['date'], format='%Y-%m-%d')
cci['date'] = pd.to_datetime(cci['date'], format='%Y-%m-%d')
inflation['date'] = pd.to_datetime(inflation['date'], format='%Y-%m-%d')
#unemployment['date'] = pd.to_datetime(unemployment['date'], format='%d/%m/%y').dt.strftime('%Y-%m-%d')
unemployment['date'] = pd.to_datetime(unemployment['date'], format='%Y-%m-%d')
```

Let's merge our datasets to have a better understanding of the data. If our new data has an impact on sales, freight value, or price.

```
In [635... # Let's merge our three datasets with daily_sales
daily_sales = pd.merge(daily_sales, cci[['date', 'cci_value']], on='date')
daily_sales = pd.merge(daily_sales, inflation[['date', 'inflation_value']], on='date')
daily_sales = pd.merge(daily_sales, unemployment[['date', 'unemr_value']], on='date')
```

```
In [636... daily_sales.head()
```

	date	price	freight_value	quantity_sold	cci_value	inflation_value	unemr_value
0	2017-02-01	117.793281	19.530156	67	98.91882	4.758907	13.2
1	2017-03-01	109.940631	17.906036	141	99.22443	4.571105	13.7
2	2017-04-01	257.624559	19.763235	70	99.36663	4.082517	13.6
3	2017-05-01	93.546746	16.954762	143	99.42970	3.597256	13.3
4	2017-06-01	142.869259	18.096148	148	99.39207	2.998557	13.0

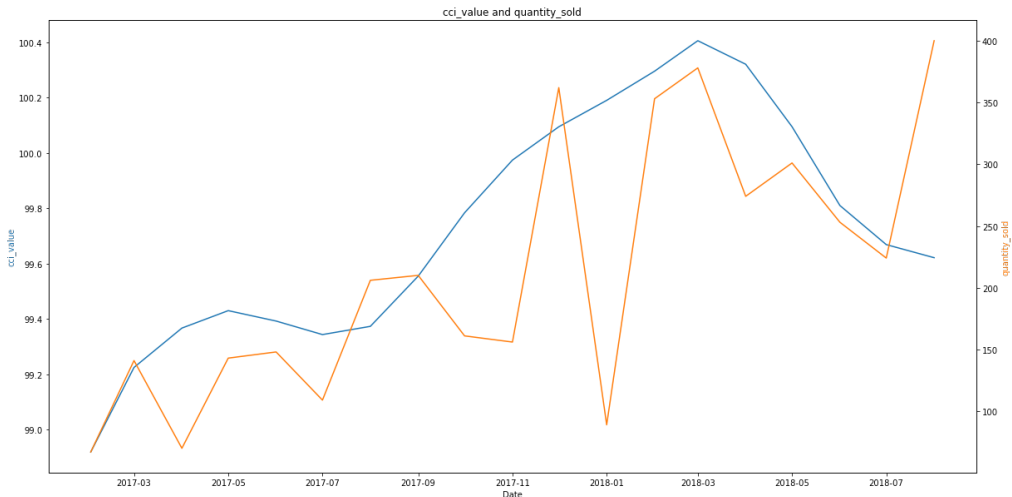
Great! Now that we have our data merged, let's check the correlation between our features

```
In [637... # Let's plot a correlation matrix with our features
corr = daily_sales.iloc[:, 1:-1].corr()
corr.style.background_gradient(cmap='rocket_r')
```

	price	freight_value	quantity_sold	cci_value	inflation_value
price	1.000000	0.228232	-0.211767	-0.179760	0.140919
freight_value	0.228232	1.000000	0.319191	0.116893	0.242310
quantity_sold	-0.211767	0.319191	1.000000	0.630159	-0.194877
cci_value	-0.179760	0.116893	0.630159	1.000000	-0.515951
inflation_value	0.140919	0.242310	-0.194877	-0.515951	1.000000

Okay, we can observe here that these macroeconomic features don't have a big impact on our prices but for our sales it does, for example, our CCI has a positive correlation with our quantity sold. To understand more the correlation, let's plot a chart and see how this positive correlation is.

```
In [638... plot_2axis(daily_sales, 'cci_value', 'quantity_sold')
```



Now we observe when Consumer Index increases people tend to buy more in this e-commerce. Great, we have a feature that would help us to forecast our sales. After checking the features that we are going to use. We can think of the products that we would like to optimize.

## Products to optimize

We have so many products in the dataset but to optimize our prices, we need to select the products that have enough data. We propose those items that have been sold at least 1 product and their price points are diverse. Let's find out.

```
In [639... # Let's add the week number plus the year to our dataset so we can check the variance of the quantity sold
orders_items['week_number'] = orders_items['order_purchase_timestamp'].dt.strftime('%Y-%U')
```

Let's going to filter those products and count how many products we have with the conditions that we propose.

```
In [640... # Let's group the products by unique prices and sales
grouped = orders_items.groupby('product_id').agg({
    'price': pd.Series.nunique, # Count unique prices
    'order_id': 'count' # Count total sales (orders)
}).reset_index()

# Filter products with multiple unique prices and consistent sales
filtered_products = grouped[(grouped['price'] > 10) & (grouped['order_id'] > 0)]

# Get the List of 'product_id' for the filtered products
filtered_product_ids = filtered_products['product_id'].tolist()

# Let's count the number of filtered products
print(f"The numbers of products to optimize: {len(filtered_product_ids)}")
```

The numbers of products to optimize: 35

How about if we plot some charts to evaluate the performance of the filtered products over time?

```
In [641... # Let's create a function that will take a List of product, select 4 random products and plot the weekly sales
def plot_weekly_sales(product_ids_list):
    # Randomly select 4 product IDs from the List
    selected_product_ids = random.sample(product_ids_list, 4)

    # Create a subplot with 2 rows and 2 columns to plot 4 charts side by side
    fig, axes = plt.subplots(2, 2, figsize=(20, 12))
    fig.suptitle('Quantity sold and Price by Week for Randomly Selected Products', fontsize=16)

    # Loop through the selected product IDs and plot each one on a separate subplot
    for i, product_id in enumerate(selected_product_ids):
        row = i // 2
        col = i % 2
        ax = axes[row, col]

        # Filter the data for the current product ID
        weekly_sales = orders_items.loc[orders_items['product_id'] == product_id].groupby(['week_number', 'product_id']).agg('sum')
        weekly_sales = weekly_sales.rename(columns={'order_id': 'quantity_sold'})

        # Plot quantity sold using the first y-axis (ax1)
        ax.set_xlabel('Week Number')
        ax.set_ylabel('quantity_sold', color='tab:green')
        ax.plot(weekly_sales['week_number'], weekly_sales['quantity_sold'], color='tab:green', label='Quantity Sold')

        # Create a second y-axis (ax2) and plot price using it
        ax2 = ax.twinx() # share the same x-axis
        ax2.set_ylabel('Price', color='tab:orange')
        ax2.plot(weekly_sales['week_number'], weekly_sales['price'], color='tab:orange', label='Price')

        # Customize the appearance of the subplot
        ax.set_title(f'Product ID: {product_id}')
        #ax.grid()
```

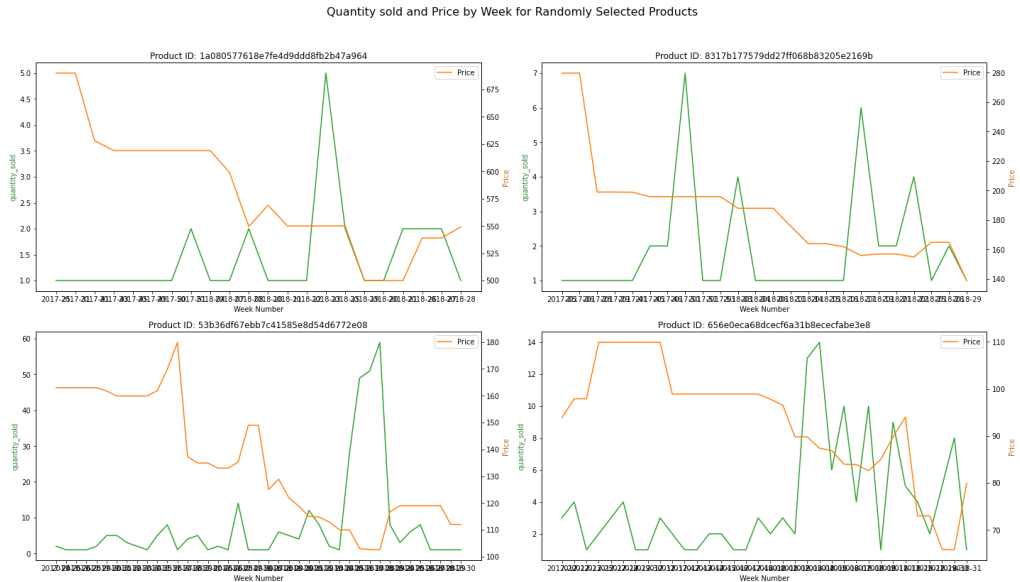
```
ax2.legend(loc='upper right')

# Adjust layout and spacing
plt.tight_layout(rect=[0, 0.03, 1, 0.95])

# Show the plots
plt.show()
```

In [642...

```
plot_weekly_sales(filtered_product_ids)
```



Now that we have the products, let's forecast demand for the next week and see if we can optimize our prices.

Now that we have the potential products to optimize, let's find out more data about them. Let's bring the category name.

In [643...

```
# Let's upload details of the products
products = pd.read_csv('./files/olist_products_dataset.csv')
# Let's merge with product_category_name_translation to have the translation from Brazil to English
en_cat = pd.read_csv('./files/product_category_name_translation.csv')
products_items = pd.merge(products, en_cat, on='product_category_name')
products_items.head()
```

Out[643...

	product_id	product_category_name	product_name_lenght	product_description_lenght	product_photos_qty	pr
0	1e9e8ef04dbcff4541ed26657ea517e5	perfumaria	40.0	287.0	1.0	
1	6a2fb4dd53d2cdb88e0432f1284a004c	perfumaria	39.0	346.0	2.0	
2	0d009643171aee696f4733340bc2fdd0	perfumaria	52.0	150.0	1.0	
3	b1eae565a61935e0011ee7682fef9dc9	perfumaria	49.0	460.0	2.0	
4	8da90b37f0fb171b4877c124f965b1f6	perfumaria	56.0	733.0	3.0	

Our data is in Portuguese, let's translate it into English with another data dataset that has a relation

In [644...

```
df = pd.merge(orders_items, products_items[['product_id', 'product_category_name_english']], on='product_id')
df.head()
```

Out[644...

	order_id	customer_id	order_status	order_purchase_timestamp	order_approved_at	c
0	e481f51cbdc54678b7cc49136f2d6af7	9ef432eb6251297304e76186b10a928d	delivered	2017-10-02 10:56:33	2017-10-02 11:07:15	
1	128e10d95713541c87cd1a2e48201934	a20e8105f23924cd00833fd87daa0831	delivered	2017-08-15 18:29:31	2017-08-15 20:05:16	
2	0e7e841ddf8f8f2de2bad69267ecfbcf	26c7ac168e1433912a51b924fbd34d34	delivered	2017-08-02 18:24:47	2017-08-02 18:43:15	
3	bfc39df4f36c3693ff3b63fcbcea9e90a	53904ddbea91e1e92b2b3f1d09a7af86	delivered	2017-10-23 23:26:46	2017-10-25 02:14:11	
4	53cdb2fc8bc7dce0b6741e2150273451	b0830fb4747a6c6d20dea0b8c802d7ef	delivered	2018-07-24 20:41:37	2018-07-26 03:24:27	

The id of the product that we are going to optimize is: 7a10781637204d8d10485c71a6108a2e. Let's see the category

In [645...

```
# Let's see the category of the product mentioned before
df[df['product_id'] == '7a10781637204d8d10485c71a6108a2e'].head().value_counts('product_category_name_english')
```

Out[645...

```
product_category_name_english
watches_gifts      5
dtype: int64
```

Now that we know that are watched. Let's find more information that can help us with the analysis

To complement our numbers we bring the trend of people looking those on internet (Google Trend) of watches in Brazil during this period, also the exchange rate between USD and BRL.

In [646...

```
# Let's upload our trend dataset
trend = pd.read_csv('./files/trend.csv')
exchange_rate = pd.read_csv('./files/exchange_rate.csv')
# Let's format the date
trend['date'] = pd.to_datetime(trend['date'], format='%Y-%m-%d')
exchange_rate['date'] = pd.to_datetime(exchange_rate['date'], format='%Y-%m-%d')
```

In [647...

```
id = orders_items.loc[orders_items['product_id'] == '7a10781637204d8d10485c71a6108a2e'].groupby(['order_purchase_timestamp',
# Now Let's change the name of the columns as date and quantity sold
id = id.rename(columns={'order_purchase_timestamp': 'date', 'order_id': 'quantity_sold'})
# Let's add the year and moth to the dataset so we can match with our cct_values dataset
id['month'] = id['date'].dt.strftime('%Y-%m')
# Let's remove the time fo the date
id['date'] = id['date'].dt.strftime('%Y-%m-%d')
# Let's change it to datetime
id['date'] = pd.to_datetime(id['date'])
```

Now that we have our data formatted, let's merge them

In [648...

```
# Let's merge the data with exchange rate
id = pd.merge(id, exchange_rate, how='left', on='date')
# Let's merge the data with trend
id = pd.merge(id, trend, how='left', on='date')
id.head()
```

Out[648...

	date	price	freight_value	quantity_sold	month	Ex_rate	trends
0	2017-08-06	229.9	16.36	1	2017-08	NaN	NaN
1	2017-08-08	229.9	16.36	1	2017-08	3.1269	NaN
2	2017-08-10	229.9	13.11	1	2017-08	3.1757	81.0
3	2017-08-12	229.9	13.11	1	2017-08	NaN	NaN
4	2017-08-13	229.9	16.36	1	2017-08	NaN	82.0

In [649...

```
# Fill NaN values using ffill and then bfill
id['Ex_rate'].fillna(method='ffill', inplace=True)
id['trends'].fillna(method='ffill', inplace=True)
id['Ex_rate'].fillna(method='bfill', inplace=True)
id['trends'].fillna(method='bfill', inplace=True)
```

```
In [650... # Let's add the cci_value to our id dataset but our cci dates is in monthly format so we need to identify the month and year
cci['month'] = cci['date'].dt.strftime('%Y-%m')
unemployment['month'] = unemployment['date'].dt.strftime('%Y-%m')
inflation['month'] = inflation['date'].dt.strftime('%Y-%m')
```

```
In [651... # Let's merge our datasets
id = pd.merge(id, cci[['month', 'cci_value']], on='month')
id = pd.merge(id, unemployment[['month', 'unemr_value']], on='month')
id = pd.merge(id, inflation[['month', 'inflation_value']], on='month')
# Let's drop the month column
id = id.drop(columns=['month'])
# The last weeks of freight_value are 0, let's fill them with the last value
id['freight_value'] = id['freight_value'].replace(0, 15.550)
id.tail()
```

Out[651...

	date	price	freight_value	quantity_sold	Ex_rate	trends	cci_value	unemr_value	inflation_value
135	2018-05-08	199.0	15.55	1	3.5636	72.0	100.0945	12.7	2.855013
136	2018-05-09	199.0	15.55	1	3.5924	72.0	100.0945	12.7	2.855013
137	2018-05-09	199.0	15.55	1	3.5924	72.0	100.0945	12.7	2.855013
138	2018-05-09	199.0	15.55	1	3.5924	72.0	100.0945	12.7	2.855013
139	2018-05-12	199.0	15.55	1	3.5924	72.0	100.0945	12.7	2.855013

```
In [652... # Let's set the date as the index
id = id.set_index('date')
# Let's resample our data id by week but sum the quantity sold and the median of the different features
w_data = id.resample('W').agg({'quantity_sold': 'sum', 'price': 'median', 'cci_value': 'median', 'freight_value': 'median',
# Let's fill the null values with the previous price
w_data['price'] = w_data['price'].fillna(method='ffill')
w_data['cci_value'] = w_data['cci_value'].fillna(method='ffill')
w_data['freight_value'] = w_data['freight_value'].fillna(method='ffill')
w_data['unemr_value'] = w_data['unemr_value'].fillna(method='ffill')
w_data['inflation_value'] = w_data['inflation_value'].fillna(method='ffill')
w_data['trends'] = w_data['trends'].fillna(method='ffill')
w_data['Ex_rate'] = w_data['Ex_rate'].fillna(method='ffill')
# Let's set the date as the index
w_data.head()
```

Out[652...

	date	quantity_sold	price	cci_value	freight_value	unemr_value	inflation_value	trends	Ex_rate
0	2017-08-06	1	229.9	99.37289	16.360	12.6	2.455909	81.0	3.1269
1	2017-08-13	4	229.9	99.37289	14.735	12.6	2.455909	81.0	3.1757
2	2017-08-20	0	229.9	99.37289	14.735	12.6	2.455909	81.0	3.1757
3	2017-08-27	3	229.9	99.37289	16.360	12.6	2.455909	82.0	3.1611
4	2017-09-03	2	229.9	99.55448	16.545	12.4	2.537691	82.0	3.1416

```
In [653... # Let's save our data already processed
w_data.to_csv('./files/w_data.csv')
```

Excellent! Now that we have our data merged, let's start with our demand forecast. For this analysis, we are going to use the time series model called Prophet from Facebook.

### Time series (Facbook Prophet)

```
In [654... # Let's create a copy of our weekly dataset
df = w_data.copy()

# Rename trend because the name 'tren' is already taken for the model
df = df.rename(columns={'trend': 'trends'})
df.head()
```

Out[654...

	date	quantity_sold	price	cci_value	freight_value	unemr_value	inflation_value	trends	Ex_rate
0	2017-08-06	1	229.9	99.37289	16.360	12.6	2.455909	81.0	3.1269
1	2017-08-13	4	229.9	99.37289	14.735	12.6	2.455909	81.0	3.1757
2	2017-08-20	0	229.9	99.37289	14.735	12.6	2.455909	81.0	3.1757
3	2017-08-27	3	229.9	99.37289	16.360	12.6	2.455909	82.0	3.1611
4	2017-09-03	2	229.9	99.55448	16.545	12.4	2.537691	82.0	3.1416

```
In [655... # Create a copy of the original DataFrame 'df' and store it in 'train'
train = df.copy()

# Convert the 'date' column in the 'train' DataFrame to datetime format
train['date'] = pd.to_datetime(train['date'])

# Create a new DataFrame 'fd' by selecting specific columns from 'train'
fd = train[['date', 'cci_value', 'freight_value', 'unemr_value', 'Ex_rate', 'trends', 'inflation_value']]

# Display the last few rows of the 'fd' DataFrame
fd.tail()

# Rename the columns in the 'train' DataFrame
train = train.rename(columns={'quantity_sold': 'y', 'date': 'ds'})
```

```
In [656... # Instantiate Prophet
model_new = Prophet()

# Add monthly seasonality
model_new.add_seasonality(name='monthly', period=30.5, fourier_order=5)

# Add our regressors
model_new.add_regressor('cci_value')
model_new.add_regressor('freight_value')
model_new.add_regressor('unemr_value')
model_new.add_regressor('Ex_rate')
model_new.add_regressor('trends')
model_new.add_regressor('inflation_value')

# Add our holidays from Brazil
model_new.add_country_holidays(country_name='BR')
```

Out[656... <prophet.forecaster.Prophet at 0x7fd458d4ddf0>

```
In [657... # Fit the model to the training data
model_new.fit(train)

# Create a future DataFrame for 4 weeks
future_data = model_new.make_future_dataframe(periods=4, freq = 'W')
```

15:52:34 - cmdstanpy - INFO - Chain [1] start processing  
15:52:34 - cmdstanpy - INFO - Chain [1] done processing

```
In [658... # Let's see our future data
future_data['ds'] = future_data['ds'].dt.strftime('%Y-%m-%d')
future_data.tail()
```

Out[658...

	ds
40	2018-05-13
41	2018-05-20
42	2018-05-27
43	2018-06-03
44	2018-06-10

```
In [659... # Let's merge our future data with our features
combined_df = pd.concat([fd, future_data], axis=1)
combined_df = combined_df[['ds', 'cci_value', 'freight_value', 'unemr_value', 'Ex_rate', 'trends', 'inflation_value']]

# Fill NaN values in the 'Value' column with the last valid value
combined_df['cci_value'].fillna(method='ffill', inplace=True)
combined_df['freight_value'].fillna(method='ffill', inplace=True)
combined_df['unemr_value'].fillna(method='ffill', inplace=True)
combined_df['Ex_rate'].fillna(method='ffill', inplace=True)
```



```
combined_df['ex_rate'].fillna(method='ffill', inplace=True)
combined_df['trends'].fillna(method='ffill', inplace=True)
combined_df['inflation_value'].fillna(method='ffill', inplace=True)

# Let's see our combined data
combined_df.tail()
```

Out[659...	ds	cci_value	freight_value	unemr_value	Ex_rate	trends	inflation_value
40	2018-05-13	100.0945	15.55	12.7	3.5636	72.0	2.855013
41	2018-05-20	100.0945	15.55	12.7	3.5636	72.0	2.855013
42	2018-05-27	100.0945	15.55	12.7	3.5636	72.0	2.855013
43	2018-06-03	100.0945	15.55	12.7	3.5636	72.0	2.855013
44	2018-06-10	100.0945	15.55	12.7	3.5636	72.0	2.855013

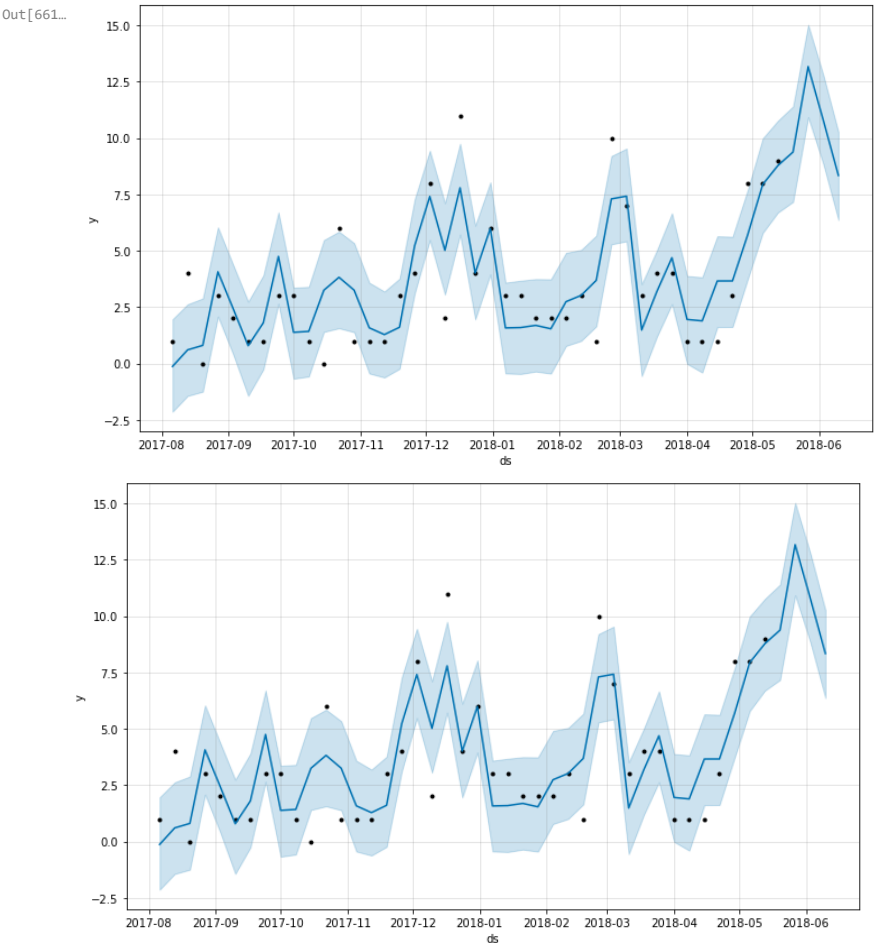
```
In [660...
# Predict on the 'future' dataset
forecast_data = model_new.predict(combined_df)

# Display the first few rows of the resulting DataFrame 'forecast_data'
forecast_data[['ds', 'yhat', 'yhat_lower', 'yhat_upper']].tail()
```

Out[660...	ds	yhat	yhat_lower	yhat_upper
40	2018-05-13	8.777564	6.695799	10.770377
41	2018-05-20	9.379716	7.169249	11.403958
42	2018-05-27	13.170325	10.923229	15.024032
43	2018-06-03	10.794044	8.847263	12.801958
44	2018-06-10	8.341331	6.367506	10.265719

What about if we check how are model performed with a chart?

```
In [661...
# Let's plot the forecast
model_new.plot(forecast_data)
```



Great! Let's evaluate the performance of our model with the metrics.

```
In [662...
performance = pd.merge(train, forecast_data[['ds', 'yhat', 'yhat_lower', 'yhat_upper']], on='ds')
performance_MAE = mean_absolute_error(performance['y'], performance['yhat'])
print(f'Performance MAE: {performance_MAE}')
```

Performance MAE: 1.2340877773888004

```
In [663...
# Now Let's take out the Last 4 weeks of our forecast
forecast_data_4w = forecast_data.iloc[-4:, :]
forecast_data_4w = forecast_data_4w[['ds', 'yhat_lower', 'yhat_upper']]

# Let's rename to lower quantity and upper quantity
forecast_data_4w = forecast_data_4w.rename(columns={'yhat_lower': 'lower_quantity', 'yhat_upper': 'upper_quantity'})
# Let's also lower round the values
forecast_data_4w['lower_quantity'] = forecast_data_4w['lower_quantity'].apply(np.floor).astype(int)
forecast_data_4w['upper_quantity'] = forecast_data_4w['upper_quantity'].apply(np.floor).astype(int)

forecast_data_4w
```

Out[663...	ds	lower_quantity	upper_quantity
41	2018-05-20	7	11
42	2018-05-27	10	15
43	2018-06-03	8	12
44	2018-06-10	6	10

Now that we have our demand forecast for the next 4 weeks. We can work on our price optimization. Let's start to predict our prices for each point of our demand forecast. For this analysis, we are going to use the linear regression model.

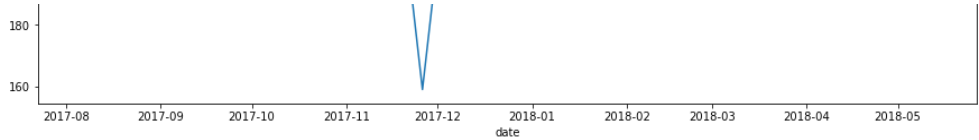
## Linear regression

```
In [664...
# Let's add the month, weekly, and year seasonality to our dataset
w_data['month'] = w_data['date'].dt.month
w_data['week'] = w_data['date'].dt.isocalendar().week
```

```
In [665...
# How about if before start the model, Let's plot a chart to see all the prices that have been recorded
fig, ax = plt.subplots(figsize=(15, 5))
sns.lineplot(data=w_data, x='date', y='price', ax=ax)
plt.title('Price of the product over time')
plt.show()
```







We have a price point very unusual, which is close to Black Friday. Let's filter if this drop has a relation with this event. Also, there are price points higher than usual. Let's check both.

```
In [666... # Outliers
w_data.loc[w_data['price'] < 180]
```

	date	quantity_sold	price	cci_value	freight_value	unemr_value	inflation_value	trends	Ex_rate	month	week
16	2017-11-26	4	159.0	99.97388	18.39	12.0	2.803785	71.0	3.2219	11	47

```
In [667... # Higher than 220
w_data.loc[w_data['price'] > 220]
```

	date	quantity_sold	price	cci_value	freight_value	unemr_value	inflation_value	trends	Ex_rate	month	week
0	2017-08-06	1	229.9	99.37289	16.360	12.6	2.455909	81.0	3.1269	8	31
1	2017-08-13	4	229.9	99.37289	14.735	12.6	2.455909	81.0	3.1757	8	32
2	2017-08-20	0	229.9	99.37289	14.735	12.6	2.455909	81.0	3.1757	8	33
3	2017-08-27	3	229.9	99.37289	16.360	12.6	2.455909	82.0	3.1611	8	34
4	2017-09-03	2	229.9	99.55448	16.545	12.4	2.537691	82.0	3.1416	9	35
5	2017-09-10	1	229.9	99.55448	13.110	12.4	2.537691	82.0	3.1174	9	36
6	2017-09-17	1	228.9	99.55448	13.100	12.4	2.537691	80.0	3.1174	9	37
9	2017-10-08	1	249.9	99.78332	19.000	12.2	2.701321	80.0	3.1544	10	40
10	2017-10-15	0	249.9	99.78332	19.000	12.2	2.701321	80.0	3.1544	10	41
24	2018-01-21	2	229.0	100.18980	22.310	12.2	2.855116	45.0	3.2243	1	3

We can observe that we just have two price points with 249.9 and one of them didn't have sales. To avoid any bias, let's remove this price point.

Yes, this drop has a relation with Black Friday. Let's remove this point so our model can't be biased.

```
In [668... # Removing the outliers
w_data = w_data.drop(w_data[w_data['price'] == 159].index)
w_data = w_data.drop(w_data[w_data['price'] > 240].index)
```

Great! Now that we have our prices okay, let's select our features and train our model.

```
In [669... # Select specific columns from the 'w_data' DataFrame to create the feature matrix 'X'
X = w_data[['quantity_sold', 'cci_value', 'freight_value', 'month', 'unemr_value']]

# Select the target variable 'price' and create the target vector 'y'
y = w_data[['price']]

# Create an instance of StandardScaler, which will be used to standardize (scale) the features
scaler = StandardScaler()

# Standardize the feature matrix 'X' using the StandardScaler
X = scaler.fit_transform(X)

# The 'test_size' parameter specifies that 15% of the data will be used for testing, and 'random_state' sets a seed for repr
X_train, X_test, y_train, y_test = train_test_split(X, y, test_size=0.15, random_state=42)
```

Now it is time to train our model and evaluate their performance. We are going to test: Gradient boosting, Random Forest, and XGBoost.

### Gradient boosting regressor

```
In [670... # Let's train our model
model = GradientBoostingRegressor()

# Let's train our model
model.fit(X_train,y_train)

# Let's predict the price
y_pred = model.predict(X_test)

# Let's calculate the mean squared error
mse = mean_squared_error(y_test, y_pred)
# Let's calculate the mean absolute error
mae = mean_absolute_error(y_test, y_pred)
# Let's calculate the r2 score
r2 = r2_score(y_test, y_pred)

# Let's print the results
print('MSE: ', mse)
print('MAE: ', mae)
print('R2: ', r2)
```

MSE: 11.032681934458134  
MAE: 2.3925488738259495  
R2: 0.8998414946890433

```
In [671... # Let's train our model
model_X = XGBRegressor()

# Let's train our model
model_X.fit(X_train,y_train)

# Let's predict the price
y_pred_X = model_X.predict(X_test)

# Let's calculate the mean squared error
mse_X = mean_squared_error(y_test, y_pred_X)
# Let's calculate the mean absolute error
mae_X = mean_absolute_error(y_test, y_pred_X)
# Let's calculate the r2 score
r2_X = r2_score(y_test, y_pred_X)

# Let's print the results
print('MSE: ', mse_X)
print('MAE: ', mae_X)
print('R2: ', r2_X)
```

MSE: 2.3979404600771765  
MAE: 1.1094004313151042  
R2: 0.978230666511298

```
In [672... # Let's train our model
model_R = RandomForestRegressor()

# Let's train our model
model_R.fit(X_train,y_train)

# Let's predict the price
y_pred_R = model_R.predict(X_test)

# Let's calculate the mean squared error
mse_R = mean_squared_error(y_test, y_pred_R)
# Let's calculate the mean absolute error
mae_R = mean_absolute_error(y_test, y_pred_R)
# Let's calculate the r2 score
r2_R = r2_score(y_test, y_pred_R)

# Let's print the results
print('MSE: ', mse_R)
print('MAE: ', mae_R)
print('R2: ', r2_R)
```

MSE: 17.097144499999626  
MAE: 2.942833333333278  
R2: 0.8447862044443583

```
In [673... # Let's create a dataframe with the results
results = pd.DataFrame({'Regression Model': ['Gradient Boosting', 'XGBoost', 'Random Forest'],
                        'MSE': [mse, mse_X, mse_R],
```

```
'MAE': [mae, mae_X, mae_R],
'R2': [r2, r2_X, r2_R]).sort_values(by='R2', ascending=False).reset_index(drop=True)

results
```

Out[673...

	Regression Model	MSE	MAE	R2
0	XGBoost	2.397940	1.109400	0.978231
1	Gradient Boosting	11.032682	2.392549	0.899841
2	Random Forest	17.097144	2.942833	0.844786

Now that we have the best model performance let's use the best one to predict the prices of our product.

In [674...

```
# Let's create a function to make predictions
def predict_price(quantity_sold, cci_value, freight_value, month, unemr_value):
    price = model_X.predict(scaler.transform([[quantity_sold, cci_value, freight_value, month, unemr_value]]))
    print(f'Predicted price: {price[0]}')
```

To predict the prices for the next week, we need to predict the prices for each point of our demand forecast. Let's do it.

But our regressor model has more than quantity features. We have Customer Index, Unemployment rate and Freight value. For this analysis, we are going to use the last one that the government publish. As a usual practice, we use the last data available.

In [675...

```
# Let's set our variables
cci_value = 100.0945
freight_value = 15.55
unemr_value = 12.7
# Month 5 is May
month = 5
# Let's bring the lower and upper bounds of the quantity sold of forecast_data_4w
lower_bound = forecast_data_4w['lower_quantity'].iloc[0]
upper_bound = forecast_data_4w['upper_quantity'].iloc[0]
```

In [700...

```
prices = []
quantity_sold = []

# Now Let's iterate through the List make predictions and then store them in a List
for i in range(lower_bound, upper_bound + 1):
    quantity_sold.append(i)
    price = model_X.predict(scaler.transform([[i, cci_value, freight_value, month, unemr_value]]))
    prices.append(price[0])

# Let's create a dataframe with the results
results = pd.DataFrame({'quantity_sold': quantity_sold,
                        'price': prices})

# Now that we have the prices and quantity sold, Let's calculate our profit by subtracting the freight value from our price
results['profit'] = (results['price'] - freight_value) * results['quantity_sold']

# Let's see our results for the different prices
results
```

Out[700...

	quantity_sold	price	profit
0	7	199.420792	1287.095520
1	8	199.379089	1470.632690
2	9	198.999908	1651.049149
3	10	199.472931	1839.229279
4	11	199.472931	2023.152206

Now that we have the prices for different quantities, let's evaluate what is the optimal price to maximize our profit.

## Price Optimization

For this problem, we are going to use the library Scipy the function minimize\_scalar. This function will help us to find the optimal price to maximize our profit.

In [703...

```
# Your price and profit data
prices = np.array(results['price'])
profits = np.array(results['profit'])

# Fit a polynomial regression model (in this case, let's use a polynomial of degree 2)
degree = 2
coefficients = np.polyfit(prices, profits, degree)

# Create the polynomial fit function
polyfit_func = np.poly1d(coefficients)

# Generate a range of x values for the plot
x_values = np.linspace(min(prices), max(prices), 100)

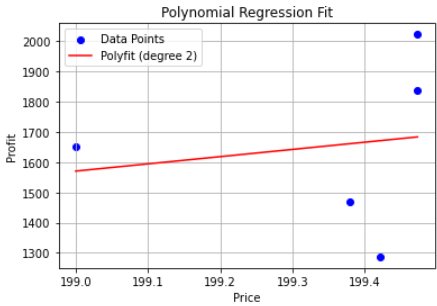
# Calculate corresponding y values using the polynomial fit function
y_values = polyfit_func(x_values)

# Create a scatterplot of the data
plt.scatter(prices, profits, label='Data Points', color='b', marker='o')

# Plot the polynomial fit curve
plt.plot(x_values, y_values, label=f'Polyfit (degree {degree})', color='r')

plt.title('Polynomial Regression Fit')
plt.xlabel('Price')
plt.ylabel('Profit')
plt.legend()
plt.grid(True)

# Show the plot
plt.show()
```



Let's plot the function

In [704...

```
# Create the polynomial fit function
polyfit_func = np.poly1d(coefficients)

# Print the polynomial function
print("Polynomial Fit Function:")
print(polyfit_func)
```

Polynomial Fit Function:  
2  
0.5927 x + 2.813 x - 2.246e+04

Let's use the function to optimize our prices

In [705...

```
# Define the profit function based on your new polynomial function
def profit(price):
    # Define your new polynomial function coefficients
    coefficients = [0.5927, 2.813, -2.246e+04]
    return -(coefficients[0] * price**2 + coefficients[1] * price + coefficients[2])

# Define the price constraints
price_bounds = (price.min(), price.max())

# Use minimize_scalar to find the maximum profit
result = minimize_scalar(profit, bounds=price_bounds, method='bounded')
```

```
# Extract the optimized price and maximized profit
optimized_price = result.x
maximized_profit = -result.fun # Convert back to positive

# Print the results
print(f"Optimal Price: ${optimized_price:.2f}")
print(f"Maximized Profit: ${maximized_profit:.2f}")
```

Optimal Price: \$199.47  
Maximized Profit: \$1684.32