

Funktionale Programmierung in F# (2)

Grundlagen & Railway Oriented Programming

Göran Kirchner¹

2024-03-15

¹e_kirchnerg@doz.hwr-berlin.de

Programm

- Hausaufgaben
- Algorithmen
 - Operationen auf einer Liste
 - Wiederholung (Pattern Matching, Rekursion)
- ROP (Railway Oriented Programming)
 - Umgang mit fehlende Daten (Option)
 - Umgang mit Fehlern (Result)

Two-Fer

```
let twoFer (input: string option): string =  
    input  
    |> Option.defaultValue "you"  
    |> sprintf "One for %s, one for me."  
  
let test1 = [twoFer None; twoFer (Some "Alice"); twoFer (Some "Bob")]  
val twoFer: input: string option -> string  
val test1: string list =  
    ["One for you, one for me."; "One for Alice, one for me.";  
     "One for Bob, one for me."]
```

Leap

```
let divisible_by n d = n % d = 0
let leapYear year =
    let year_divisible_by = divisible_by year
    year_divisible_by 4
    && not(year_divisible_by 100)
    || year_divisible_by 400

let test1 = [leapYear 1900; leapYear 1996]
let test2 = [leapYear 2000; leapYear 2019; leapYear 2020]

val divisible_by: n: int -> d: int -> bool
val leapYear: year: int -> bool
val test1: bool list = [false; true]
val test2: bool list = [true; false; true]
```

Isogram

```
let isIsogram (str: string) =  
    let letters =  
        str.ToLowerInvariant()  
        |> Seq.filter System.Char.IsLetter  
        |> Seq.toList  
    letters  
    |> Seq.distinct  
    |> Seq.length  
    |> (=) letters.Length  
let test1 = [isIsogram ""; isIsogram "isogram"]  
let test2 = [isIsogram "eleven"; isIsogram "subdermatoglyphic"]  
val isIsogram: str: string -> bool  
val test1: bool list = [true; true]  
val test2: bool list = [false; true]
```

Sum Of Multiples

```
let multiplesOf max n =  
    if n = 0 then [0] else [n .. n .. (max - 1)]  
let sum (numbers: int list) (upperBound: int): int =  
    numbers  
    |> List.collect (multiplesOf upperBound)  
    |> List.distinct  
    |> List.sum  
#time "on"  
let test = [sum [3; 5] 1000; sum [2; 3; 5; 7; 11] 10000]  
#time "off"  
val multiplesOf: max: int -> n: int -> int list  
val sum: numbers: int list -> upperBound: int -> int
```

--> Timing now on

Real: 00:00:00.001, CPU: 00:00:00.001, GC gen0: 0, gen1: 0, gen2: 0
val test: int list = [233168; 39614537]

--> Timing now off

length

```
let rec length' list =  
    match list with  
    | [] -> 0  
    | _::xs -> 1 + length' xs  
let length list =  
    let rec _length list acc =  
        match list with  
        | [] -> acc  
        | _::xs -> _length xs (acc + 1)  
    _length list 0  
  
let test1 = [length' []; length' [1; 2; 3; 4]]  
let test2 = [length []; length [1; 2; 3; 4]]  
  
val length': list: 'a list -> int  
val length: list: 'a list -> int  
val test1: int list = [0; 4]  
val test2: int list = [0; 4]
```

reverse

```
let reverse list =  
  let rec _reverse list acc =  
    match list with  
    | [] -> acc  
    | x::xs -> _reverse xs (x::acc)  
  _reverse list []  
  
let test1 = reverse [1; 3; 5; 7]  
let test2 = reverse [[1; 2]; [3]; []; [4..8]]  
  
val reverse: list: 'a list -> 'a list  
val test1: int list = [7; 5; 3; 1]  
val test2: int list list = [[4; 5; 6; 7; 8]; []; [3]; [1; 2]]
```


map

```
let map f list =  
  let rec _map f list acc =  
    match list with  
    | [] -> acc |> reverse  
    | x::xs -> _map f xs ((f x)::acc)  
  _map f list []  
  
let test = map (fun x -> x + 1) [1; 3; 5; 7]  
val map: f: ('a -> 'b) -> list: 'a list -> 'b list  
val test: int list = [2; 4; 6; 8]
```

filter (Übung)

```
// filter : f:('a -> bool) -> list:'a list -> 'a list
let filter f list =
    ...
    match list with
    | [] -> ...
    | x::xs -> ...

let test = filter (fun x -> x % 2 = 1) [1..1000]

val filter : f:('a -> bool) -> list:'a list -> 'a list
val test : int list =
    [1; 3; 5; 7; 9; 11; 13; 15; 17; 19; 21; 23; 25; 27; 29; 31; 33; 35; 37; 39;
    41; 43; 45; 47; 49; 51; 53; 55; 57; 59; 61; 63; 65; 67; 69; 71; 73; 75; 77;
    79; 81; 83; 85; 87; 89; 91; 93; 95; 97; 99; 101; 103; 105; 107; 109; 111;
    113; 115; 117; 119; 121; 123; 125; 127; 129; 131; 133; 135; 137; 139; 141;
    143; 145; 147; 149; 151; 153; 155; 157; 159; 161; 163; 165; 167; 169; 171;
    173; 175; 177; 179; 181; 183; 185; 187; 189; 191; 193; 195; 197; 199; ...]
```

filter (Lösung 1)

```
let rec filter f list =  
    match list with  
    | [] -> []  
    | x::xs -> match f x with  
        | true -> x :: filter f xs  
        | false -> filter f xs  
let test = filter (fun x -> x % 2 = 1) [1..10_000]  
val filter: f: ('a -> bool) -> list: 'a list -> 'a list  
val test: int list =  
    [1; 3; 5; 7; 9; 11; 13; 15; 17; 19; 21; 23; 25; 27; 29; 31; 33; 35; 37; 39;  
    41; 43; 45; 47; 49; 51; 53; 55; 57; 59; 61; 63; 65; 67; 69; 71; 73; 75; 77;  
    79; 81; 83; 85; 87; 89; 91; 93; 95; 97; 99; 101; 103; 105; 107; 109; 111;  
    113; 115; 117; 119; 121; 123; 125; 127; 129; 131; 133; 135; 137; 139; 141;  
    143; 145; 147; 149; 151; 153; 155; 157; 159; 161; 163; 165; 167; 169; 171;  
    173; 175; 177; 179; 181; 183; 185; 187; 189; 191; 193; 195; 197; 199; ...]
```

filter (Lösung 2)

```
let filter f list =  
  let rec _filter f list acc =  
    match list with  
    | [] -> acc |> reverse  
    | x::xs -> match f x with  
                 | true -> _filter f xs (x::acc)  
                 | false -> _filter f xs acc  
  _filter f list []  
let test = filter (fun x -> x % 2 = 1) [1..10_000]  
test
```

Große Zahlen (Übung)

- Berechne $5^{4^{3^2}}$
- Wie lang ist die Zahl?
- Gib die ersten und letzten 20 Ziffern an!

Große Zahlen (Lösung)

```
#time "on"
let answer = 5I ** (int (4I ** (int (3I ** 2))));;
let sans = answer.ToString()
let l = sans.Length
let prefix = sans.Substring(0,20)
let suffix = sans.Substring(l-20)
#time "off"
printfn "Length = %d, digits %s ... %s" l prefix suffix
let sans = answer.ToString()
let l = sans.Length
let prefix = sans.Substring(0,20)
let suffix = sans.Substring(l-20)
#time "off"
printfn "Length = %d, digits %s ... %s" l prefix suffix;;
Real: 00:00:00.497, CPU: 00:00:00.802, GC gen0: 0, gen1: 0, gen2: 0
val sans: string =
    "6206069878660874470748320557284679309194219265199117173177383"+[183170 chars
val l: int = 183231
val prefix: string = "62060698786608744707"
val suffix: string = "92256259918212890625"
```

foldl

```
let rec foldl folder state list =  
    match list with  
    | [] -> state  
    | x::xs -> foldl folder (folder state x) xs  
  
let test1 = foldl (+) 0 [1..1_000]  
let test2 = foldl (*) 1I [1I..42I]  
  
val foldl: folder: ('a -> 'b -> 'a) -> state: 'a -> list: 'b list -> 'a  
val test1: int = 500500  
val test2: System.Numerics.BigInteger =  
    1405006117752879898543142606244511569936384000000000
```

foldr

```
let flip f b a = f a b
let rec foldr folder state list =
    foldl (flip folder) state (reverse list)

let test = foldr (+) 5 [1; 2; 3; 4]
val flip: f: ('a -> 'b -> 'c) -> b: 'b -> a: 'a -> 'c
val foldr: folder: ('a -> 'b -> 'b) -> state: 'b -> list: 'a list -> 'b
val test: int = 15
```


append

```
let append xs ys = foldr (fun x acc -> x :: acc) ys xs
```

```
let test = append [1..5] [6..10]
```

```
let append xs ys = foldr (fun x acc -> x :: acc) ys xs
```

```
let test = append [1..5] [6..10];;
```

```
val append: xs: 'a list -> ys: 'a list -> 'a list
```

```
val test: int list = [1; 2; 3; 4; 5; 6; 7; 8; 9; 10]
```

concat (1)

```
let concat xs = foldr append [] xs
let rec concat' xs =
  match xs with
  | [] -> []
  | []::ys -> concat' ys
  | (x::xs)::ys -> x::(concat' (xs::ys))
let concat'' xs =
  let rec _concat xs acc =
    match xs with
    | [] -> acc |> reverse
    | []::ys -> _concat ys acc
    | (x::xs)::ys -> _concat (xs::ys) (x::acc)
  _concat xs []

val concat: xs: 'a list list -> 'a list
val concat': xs: 'a list list -> 'a list
val concat'': xs: 'a list list -> 'a list
```

concat (2)

```
let test1 = concat [[1; 2]; [3]; []; [4; 5; 6]]
let test2 = concat' [[1; 2]; [3]; []; [4; 5; 6]]
let test3 = concat'' [[1; 2]; [3]; []; [4; 5; 6]]
```

```
let test1b = concat [[[1]; [2]]; [[3]]; [[]]; [[4; 5; 6]]]
let test2b = concat' [[[1]; [2]]; [[3]]; [[]]; [[4; 5; 6]]]
let test3b = concat'' [[[1]; [2]]; [[3]]; [[]]; [[4; 5; 6]]]
```

```
let test1 = concat [[1; 2]; [3]; []; [4; 5; 6]]
let test2 = concat' [[1; 2]; [3]; []; [4; 5; 6]]
let test3 = concat'' [[1; 2]; [3]; []; [4; 5; 6]]
```

```
let test1b = concat [[[1]; [2]]; [[3]]; [[]]; [[4; 5; 6]]]
let test2b = concat' [[[1]; [2]]; [[3]]; [[]]; [[4; 5; 6]]]
let test3b = concat'' [[[1]; [2]]; [[3]]; [[]]; [[4; 5; 6]]];;
val test1: int list = [1; 2; 3; 4; 5; 6]
val test2: int list = [1; 2; 3; 4; 5; 6]
val test3: int list = [1; 2; 3; 4; 5; 6]
val test1b: int list list = [[1]; [2]; [3]; []; [4; 5; 6]]
val test2b: int list list = [[1]; [2]; [3]; []; [4; 5; 6]]
val test3b: int list list = [[1]; [2]; [3]; []; [4; 5; 6]]
```

Pause

There is no programming language, no matter how structured, that will prevent programmers from making bad programs.

–Larry Flon (1975)

ROP

⇒ Railway Oriented Programming

–Scott Wlashin: F# for Fun and Profit

Option

```
type BillingDetails = {  
    name : string  
    billing : string  
    delivery : string option }  
  
let order1 = {  
    name = "Adam Smith"  
    billing = "112 Fibonacci Street\n35813"  
    delivery = None }  
  
let order2 = {  
    name = "John Doe"  
    billing = "314 Pi Avenue\n35999"  
    delivery = Some "16 Planck Parkway\n62291" }
```

Option

```
let addressForPackage (details : BillingDetails) =  
    let address =  
        match details.delivery with  
        | Some s -> s  
        | None -> details.billing  
    sprintf "%s\n%s" details.name address  
printfn "%s" (addressForPackage order1)  
printfn "%s" (addressForPackage order2)
```

```
let addressForPackage (details : BillingDetails) =  
    _____~~~~~~
```

/Users/kirchner/Desktop/courses/course.2024.hwr.fun/slides/stdin(123,34): error

Option bind and map

```
open System

let tryLastLine (address : string) =
    let parts = address.Split(['\n'], StringSplitOptions.RemoveEmptyEntries)
    parts |> Array.tryLast

let tryPostalCode (codeString : string) =
    match Int32.TryParse(codeString) with
    | true, i -> i |> Some
    | false, _ -> None

let postalCodeHub (code : int) =
    if code = 62291 then "Hub 1" else "Hub 2"

let tryHub (details : BillingDetails) =
    details.delivery
    |> Option.bind tryLastLine
    |> Option.bind tryPostalCode
    |> Option.map postalCodeHub
```


Option

```
let test1 = order1 |> tryHub  
let test2 = order2 |> tryHub
```

```
    let test1 = order1 |> tryHub  
    -----^^^^^^
```

/Users/kirchner/Desktop/courses/course.2024.hwr.fun/slides/stdin(132,13): erro

Result (Imperativ)

```
open System
let checkString (s : string) =
    if isNull(s) then
        raise <| ArgumentException("Must not be null")
    elif String.IsNullOrEmpty(s) then
        raise <| ArgumentException("Must not be empty")
    elif String.IsNullOrWhiteSpace(s) then
        raise <| ArgumentException("Must not be white space")
    else
        s
//checkString null
//checkString ""
checkString " "
```

System.ArgumentException: Must not be white space
at FSI_0034.checkString(String s) in /Users/kirchner/Desktop/courses/course
at <StartupCode\$FSI_0034>.\$FSI_0034.main@() in /Users/kirchner/Desktop/cour
at System.RuntimeMethodHandle.InvokeMethod(Object target, Void** arguments,
at System.Reflection.MethodBaseInvoker.InvokeWithNoArgs(Object obj, BindingF
Stopped due to error

Result (Result<'Success,'Failure>)

```
open System

let notEmpty (s : string) =
    if isNull(s) then Error "Must not be null"
    elif String.IsNullOrEmpty(s) then Error "Must not be empty"
    elif String.IsNullOrWhiteSpace(s) then Error "Must not be white space"
    else Ok s

let t1 = notEmpty null;;
let t2 = notEmpty "";;
let t3 = notEmpty " ";;
t1, t2, t3

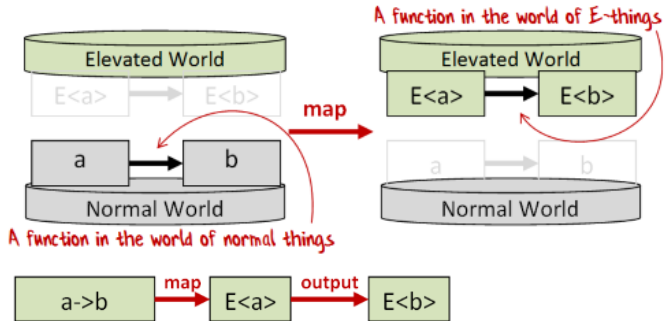
t1, t2, t3;;
val it: Result<string,string> * Result<string,string> * Result<string,string>
= (Error "Must not be null", Error "Must not be empty",
    Error "Must not be white space")
```

Result (Error-Types DU)

```
open System
type ValidationError =
    | MustNotBeNull
    | MustNotBeEmpty
    | MustNotBeWhiteSpace
let notEmpty (s : string) =
    if isNull(s) then Error MustNotBeNull
    elif String.IsNullOrEmpty(s) then Error MustNotBeEmpty
    elif String.IsNullOrWhiteSpace(s) then Error MustNotBeWhiteSpace
    else Ok s
let t1 = notEmpty null;;
let t2 = notEmpty "";;
let t3 = notEmpty " ";;
notEmpty, t1, t2, t3
notEmpty, t1, t2, t3;;
val it:
    (string -> Result<string,ValidationError>) * Result<string,ValidationError> *
    Result<string,ValidationError> * Result<string,ValidationError> =
    (<fun:it@173-3>, Error MustNotBeNull, Error MustNotBeEmpty,
    Error MustNotBeWhiteSpace)
```

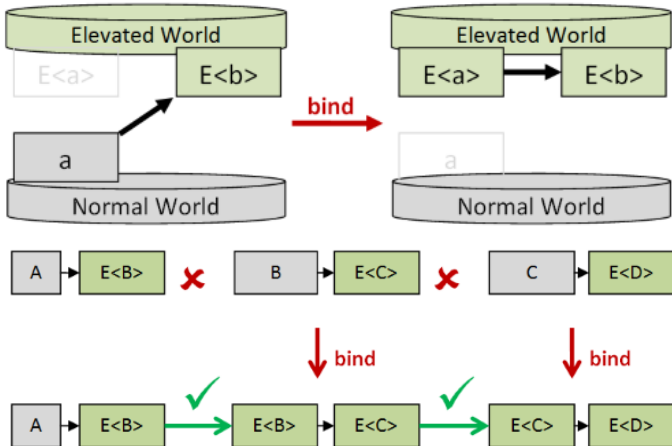
Map

- $E.map (<\$>): (a \rightarrow b) \rightarrow E<a> \rightarrow E$



Bind

- $E.\text{bind } (>>=): (a \rightarrow E\langle b \rangle) \rightarrow E\langle a \rangle \rightarrow E\langle b \rangle$



Pause

Applications programming is a race between software engineers, who strive to produce idiot-proof programs, and the universe which strives to produce bigger idiots. So far the Universe is winning.

– Rick Cook (1989)

Zusammenfassung

- funktionale Operationen auf Listen (Tail-Rekursion)
- funktionaler Umgang mit fehlenden Daten (Option)
- funktionaler Umgang mit Fehlern (Result)

Links

- fsharp.org
- docs.microsoft.com/../../dotnet/fsharp
- [F# weekly](#)
- fsharpforfunandprofit.com
- github.com/../../awesome-fsharp

Hausaufgabe

- exercism.io (E-Mail bis 02.04)
 - ☐ Queen Attack
 - ☐ Raindrops
 - ☐ Gigasecond
- exercism.io (E-Mail bis 15.04)
 - ☐ Bank Account
 - ☐ Accumulate
 - ☐ Space Age
- exercism.io (E-Mail bis 29.04)
 - ☐ Poker (Programmieraufgabe)