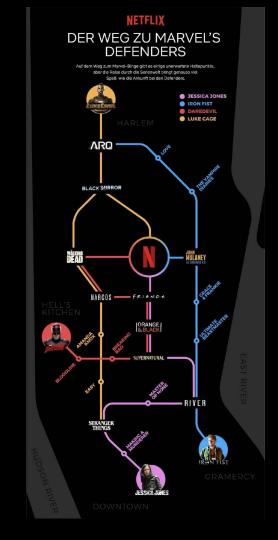


Clustering Introduction to Clustering

Prof. Dr. Jan Kirenz HdM Stuttgart









Kinder







NETFLIX





























Weil Ihnen "Unser Kosmos: Die Reise geht weiter" gefallen hat























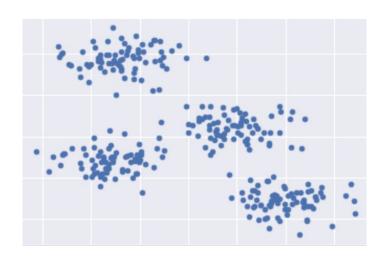




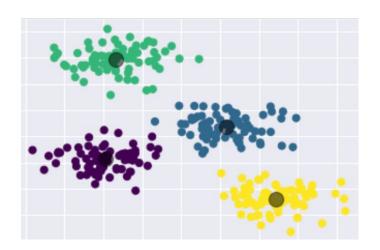


Discover unknown subgroups in data.

Unlabeled examples (observations)



Grouping unlabeled examples is called clustering.



Clustering is unsupervised learning

The goal is to discover interesting things about the observations:

- is there an informative way to visualize the data?
- Can we discover subgroups among the variables or among the observations?

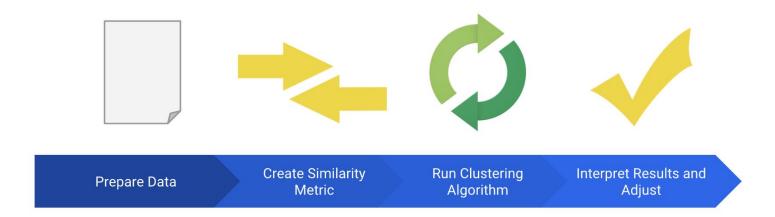
- Customer segmentation (understanding different customer segments to devise marketing strategies)
- Recommender systems (grouping togethe users with similar viewing patterns on Netflix, in order to recommend similar content)
- Anomaly detection (fraud detection, detecting defective mechanical parts)

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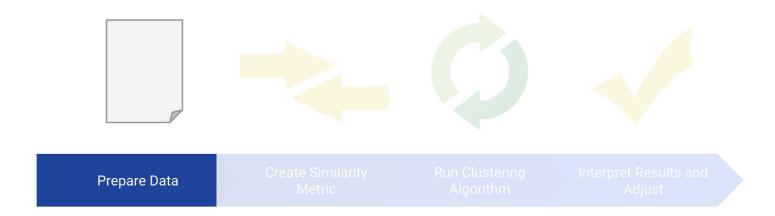
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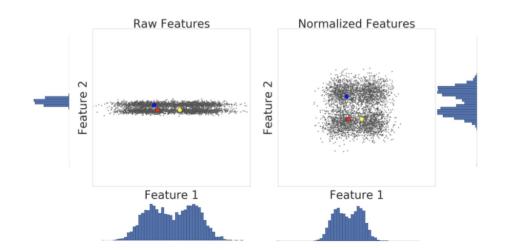
Exclude all missing values and outliers

Normalizing Data

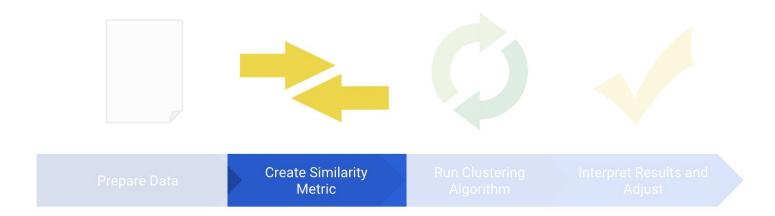
$$x'=(x-\mu)/\sigma$$

where: $\mu = \text{mean}$

 $\sigma = \text{standard deviation}$



To cluster your data, you'll follow these steps:



How to create a similarity measure for a numeric feature?

• Feature X₁: shoe size





size: 8

Shoe B



size: 11

Picture source: Allbirds Prof. Dr. Jan Kirenz

How to create a similarity measure for a numeric feature?

Feature X₁: shoe size



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- Feature X_1 : shoe size (numeric)
- Feature X₂: price (numeric)



size: 8 price: 120



size: 11 price: 150



Picture source: Allbirds Prof. Dr. Jan Kirenz

Action	Method
Scale the size.	Assume a maximum possible shoe size of 20. Divide 8 and 11 by the maximum size 20 to get 0.4 and 0.55.
Scale the price.	Divide 120 and 150 by the maximum price 150 to get 0.8 and 1.
Find the difference in size.	0.55-0.4=0.15
Find the difference in price.	1 - 0.8 = 0.2
Find the RMSE.	$\sqrt{rac{0.2^2+0.15^2}{2}}=0.17$

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Feature X₃: color (categorical)





color: black color: blue

Picture source: Allbirds Prof. Dr. Jan Kirenz

Feature X_o: color (categorical)



color: black







color: blue

Feature with multiple levels (multivalent)

- Movie genres: comedy, action, drama, non-fiction, biographical
- Can be "action" and "comedy" simultaneously, or just "action"

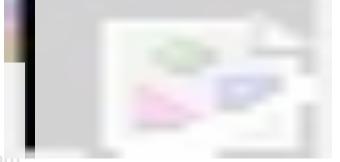
- A: ["comedy","action"] and B: ["comedy","action"] = 1
- A: ["comedy","action"] and B: ["action"] = ½
- A: ["comedy","action"] and B: ["action", "drama"] = 1/3
- A: ["comedy","action"] and B: ["non-fiction","biographical"] = 0

Calculate similarity using the ratio of common values, called **Jaccard** similarity.



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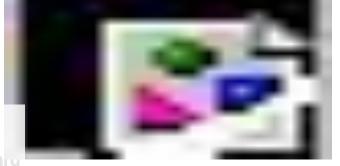
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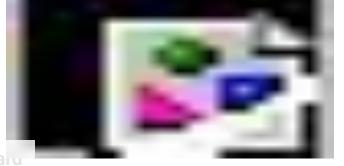
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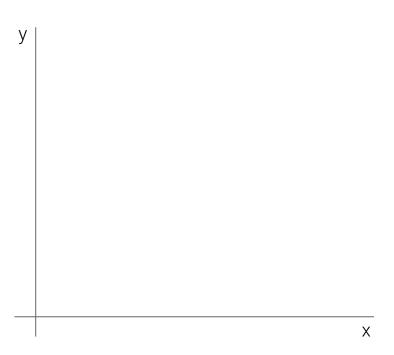
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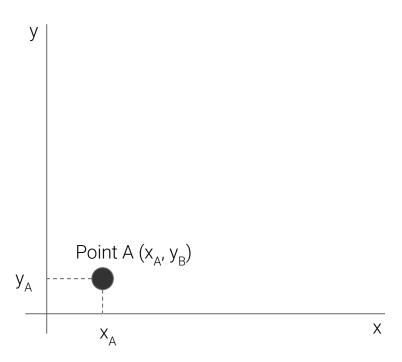


Popular distance metrics for numerical features

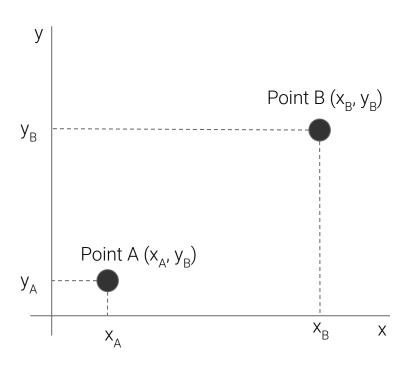
Let's start with a simple coordinate system (CS)



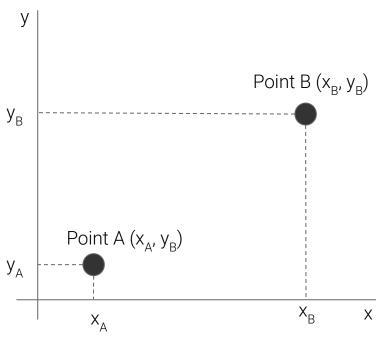
We include one observation "A"



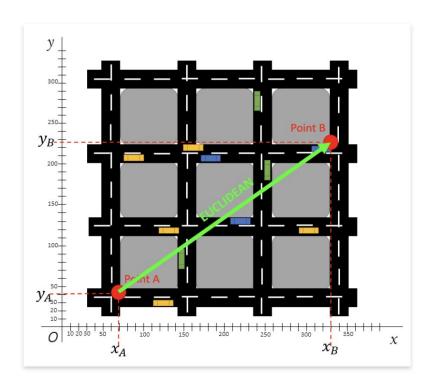
And another observation "B"



How can we measure the distance between A and B?



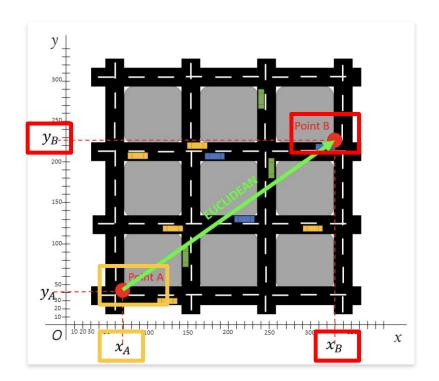
Imagine there are streets on the CS



This would be the shortest distance

$$d(A,B) = \sqrt{\sum_{i=1}^n (A_i - B_i)^2}$$

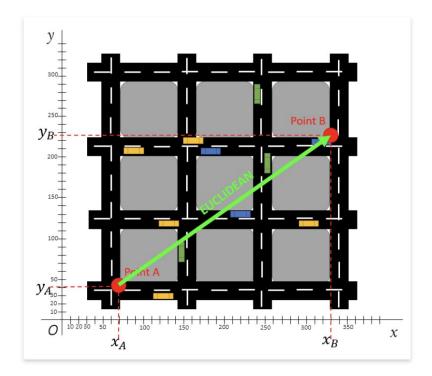
- $x_A = 70$
- $x_B = 330$
- $y_A = 40$
- y_B = 228



Euclidean distance (L₂ distance)

$$d(A,B) = \sqrt{\sum_{i=1}^n (A_i - B_i)^2}$$

- $x_A = 70$
- x_B = 330
- y_A = 40
- y_B = 228

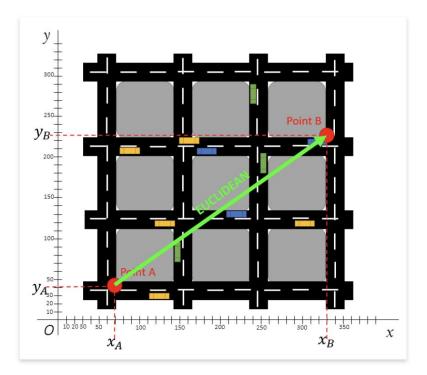


$$egin{align} d(A,B) &= \sqrt{(x_A-x_B)^2+(y_A-y_B)^2} \ d(A,B) &= \sqrt{(70-330)^2+(40-228)^2} \ d(A,B) &= \sqrt{(-260)^2+(-188)^2} \ d(A,B) &= \sqrt{(76600+35344)} \ d(A,B) &= \sqrt{(112225)} \ d(A,B) &= 335 \ \end{pmatrix}$$

Squared Euclidean distance (L₂)

$$d^2(A,B) = \sum_{i=1}^n (A_i - B_i)^2$$

- $x_A = 70$
- $x_B = 330$
- y_A = 40
- y_B = 228

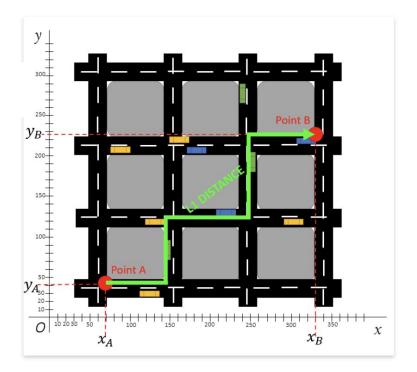


$$d^2(A,B) = (x_A - x_B)^2 + (y_A - y_B)^2$$
 $d^2(A,B) = (70 - 330)^2 + (40 - 228)^2$ $d^2(A,B) = 112225$

L₁ distance (Manhattan distance)

$$d(A,B) = \sum_i |A_i - B_i|$$

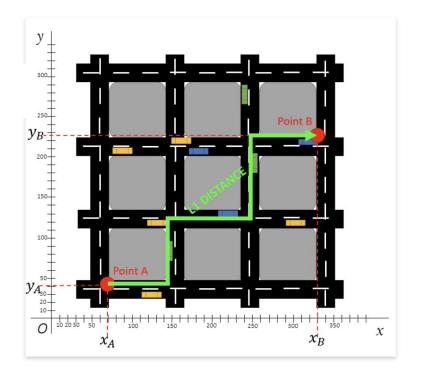
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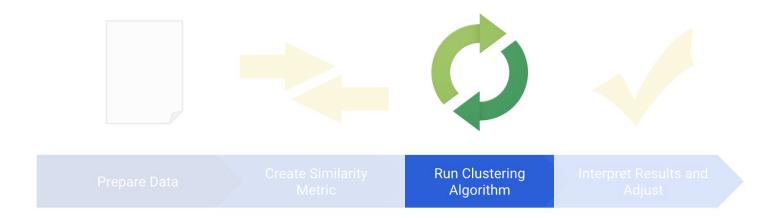
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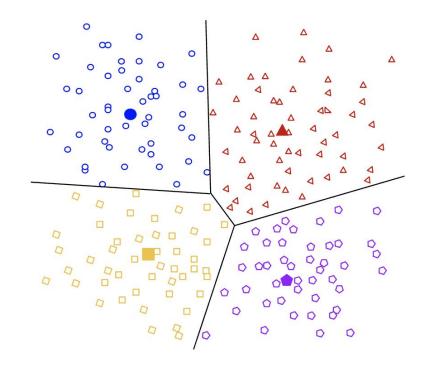
$$d(A,B) = |x_A - x_B| + |y_A - y_B|$$
 $d(A,B) = |70 - 330| + |40 - 228|$
 $d(A,B) = |-260| + |-188|$
 $d(A,B) = 260 + 188$
 $d(A,B) = 448$

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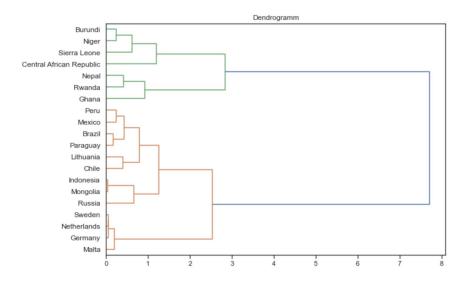
Centroid-based Clustering

- Centroid-based algorithms are efficient
- But sensitive to initial conditions and outliers.
- k-means is the most widely-used centroid-based clustering algorithm.



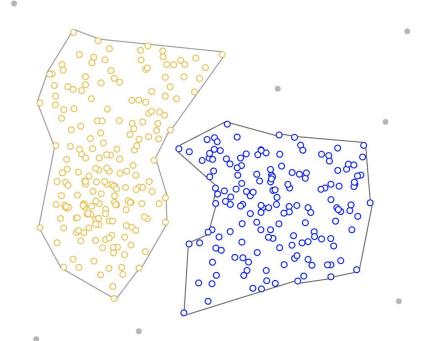
Hierarchical Clustering

- Hierarchical clustering creates a tree of clusters.
- One advantage is that any number of clusters can be chosen by cutting the tree at the right level.

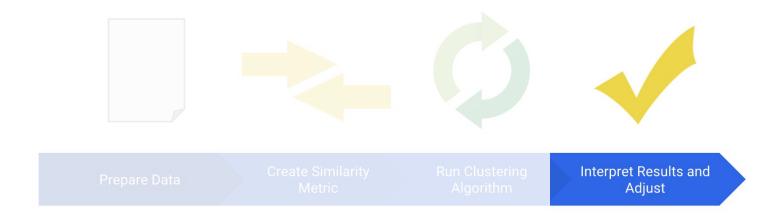


Density-based Clustering

- Density-based clustering connects areas of high example **density** into clusters
- Advantage: they do not assign outliers to clusters.
- Disadvantage: have difficulty with data of varying densities and high dimensions.



To cluster your data, you'll follow these steps:



Because clustering is unsupervised, no "truth" is available to verify results

- It mainly depends on the subjective interpretability
- We have some kind of quality measures for some algorithms (like k-Means)

