

TransformationsofFunctions

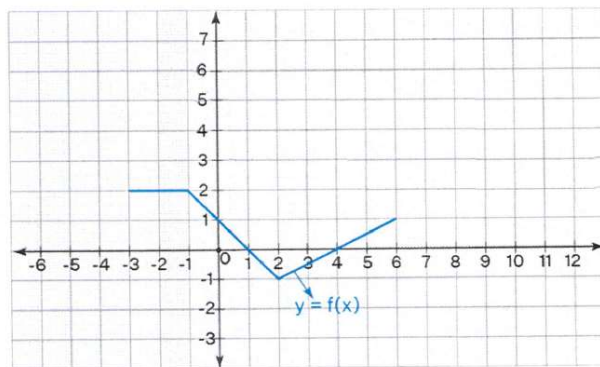
<https://www.cuemath.com/calculus/transformation-of-functions/>

Making **graphing transformations** easier: transform the function $y = f(x)$ to $y = af(b(x + c)) + d$.

- **Step1:** Note down some coordinates on the original curve that define its shape, i.e., we now know the old x and y coordinates.
- **Step2:** To find the new x —coordinate of each point just set " $b(x + c) = \text{old } x\text{-coordinate}$ " and solve this for x .
- **Step3:** To find the new y —coordinate of each point, apply all outside operations (of brackets) on the old y —coordinate. i.e., find $ay + d$ to find each new y -coordinate where 'y' is the old y —coordinate.

Q1: The following graph represents $f(x)$. Graph the function transformation

$$y = 2f\left(\frac{x}{2}\right) + 3$$

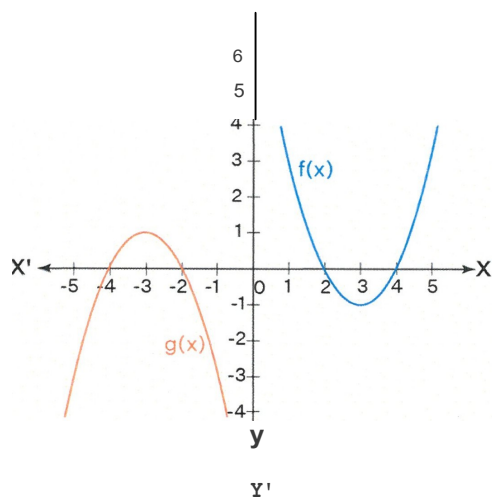


Q 2: Describe the transformations of quadratic function $g(x) = x^2 + 4x + 5$ by comparing it to its parent function $f(x) = x^2$.

Q3: State the combination of transformations applied on the function

$f(x)$ to obtain $g(x)$: $f(x) = -3x - 6$ and $g(x) = x + 2$.

Q4: Write the function corresponding to the graph of $g(x)$ that transformed from the graph $f(x)$ by using the function transformation rules.



Q5: Match the following function transformations.

$f(4x)$	⌘ Horizontal translation by 4 units left
$4f(x)$	⌘ Horizontal dilation by a scale factor of $1/4$
$f(x+4)$	⌘ Vertical translation by 4 units up
$f(x) + 4$	⌘ Vertical dilation by a scale factor of 4