

# Matter of Parentheses (parentheses)

Antonio loves brackets (or parentheses). He calls a sequence of ‘(’ and ‘)’ characters a “valid bracket sequence” if either:

- It's an empty sequence, or
- For each open bracket we can find a closed bracket on its right such that the substring between these two brackets forms a valid bracket sequence, and such that after removing that substring the remaining brackets also form a valid bracket sequence.



Figure 1: Brackets. Why not?

For example  $(( ))$  and  $( ) ( )$  are both valid, while  $) ($  and  $( ) ( ( )$  are not.

Furthermore, he calls a string of parentheses “ $K$ -valid” if, after adding  $K$  open brackets to its left and  $K$  closed brackets to its right, it is valid (either because it was valid before, or because it became valid).

For example  $()()$  and  $(())()$  are both 1-valid, while  $))(($  is 2-valid.

Antonio is curious to find for any given  $N$  and  $K$  how many bracket sequences there are with length  $2N$  that are  $K$ -valid. Because the result may be very large, Antonio is only interested in its remainder after dividing it by 1 000 000 007.

Help Antonio by writing a program that quickly calculates this number for  $Q$  different queries.

## Input

The first line contains one integer  $Q$ , the number of queries Antonio is interested in.

The next  $N$  lines contain each a pair of integers:  $N_i$  and  $K_i$ .

## Output

You need to write  $Q$  lines containing each the result of the  $i$ -th query: for each query, print the number of strings of length  $2N_i$  that are  $K_i$ -valid, modulo 1 000 000 007.

## Constraints

- $1 \leq Q \leq 100\,000$ .
- $1 \leq N_i \leq 1\,000\,000$ .
- $0 \leq K_i \leq 1\,000\,000$ .

## Examples

input	output
3	5
2 1	62
4 2	242
5 3	

## Explanation

In the first query there are 5 strings of length 4 that are 1-valid. They are highlighted below:

- In `( (()) )` the sequence `(( ))` is valid, but also 1-valid.
- In `( ()() )` the sequence `()()` is valid, but also 1-valid.
- In `( ()) ( )` the sequence `()))` is invalid, but 1-valid.
- In `( )(( )` the sequence `))((` is invalid, but 1-valid.
- In `( )() ( )` the sequence `))() (` is invalid, but 1-valid.