## Strong magnetic fields and contact interactions in few-fermion systems

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Technical manual detailing the implementation of a variational solution of the non-relativistic few-body problem in an external, i.e., static magnetic field.

a. The symmetric Gauge

$$\mathbf{A}_{i} = \frac{B_{0}}{2}(-y_{i}, x_{i}, 0) \tag{1}$$

b. The Hamiltonian

$$\hat{H} = -\frac{\hbar^2}{2m} \sum_{i=1}^{N} \left\{ \nabla_i^2 + i \left( \frac{\hbar^2}{2m} \right) \left( \frac{q_i B_0}{\hbar} \right) L_i^z + \left( \frac{\hbar^2}{2m} \right) \left( \frac{q_i B_0}{\hbar} \right)^2 \frac{1}{4} \left( x_i^2 + y_i^2 \right) - g_i \left( \frac{\hbar^2}{2m} \right) \left( \frac{q_i B_0}{\hbar} \right) \sigma_{z_i} \right\}$$

$$+ \sum_{i < j}^{N} \left[ C_a + C_b (\sigma_i^+ \sigma_j^- + \sigma_i^- \sigma_j^+ - \sigma_i^z \sigma_j^z) \right] e^{-\frac{\Lambda^2}{4} (\mathbf{r}_i - \mathbf{r}_j)^2} + \sum_{\text{cyc. } i < j < k} D \cdot e^{-\frac{\Lambda^2}{4} \left( (\mathbf{r}_i - \mathbf{r}_j)^2 + (\mathbf{r}_i - \mathbf{r}_k)^2 \right)}$$
(3)

c. The variational basis

$$|A, \lambda, \theta\rangle := e^{-\frac{1}{2}\boldsymbol{x}^T A_x \boldsymbol{x}} e^{-\frac{1}{2}\boldsymbol{y}^T A_y \boldsymbol{y}} e^{-\frac{1}{2}\boldsymbol{z}^T A_z \boldsymbol{z}} \cdot \sum_{i=1}^{N} \lambda_i |s_1^i, \dots, s_N^i\rangle \cdot \sum_{i=1}^{N} \theta_i |t_1^i, \dots, t_N^i\rangle$$

$$(4)$$

d. The generic matrix element

$$I_{\mathbb{O}}(A', \lambda', \theta', A, \lambda, \theta; P) := \langle A', \lambda', \theta' \mid \hat{\mathbb{O}} \hat{P} \mid A, \lambda, \theta \rangle$$
 (5)

with  $\hat{P} \in \mathcal{A}$  and

$$\hat{\mathcal{O}} \in \left\{ \mathbb{1} \; ; \; \boldsymbol{p}^{\mathsf{T}} \mathbb{1}_{(3N \times 3N)} \boldsymbol{p} \; ; \; \sum_{i=1}^{N} q_{i} L_{i}^{z} \; ; \; \sum_{i=1}^{N} q_{i} (x_{i}^{2} + y_{i}^{2} + z_{i}^{2}) \; ; \; \sum_{i=1}^{N} q_{i} \sigma_{i}^{z} \; ; \; \sum_{i < j}^{N} e^{-\frac{\Lambda^{2}}{4} (\boldsymbol{r}_{i} - \boldsymbol{r}_{j})^{2}} \right\}$$

$$(6)$$

e. The matrix elements

$$\frac{\hat{\mathbb{Q}}}{\mathbb{I}_{\mathbb{Q}}(A', \lambda', \boldsymbol{\theta}', A, \lambda, \boldsymbol{\theta}; P)}$$

$$\mathbf{p}^{\mathsf{T}}\mathbb{1}_{(3N\times3N)}\mathbf{p}$$

$$\sum_{i=1}^{N} q_{i}L_{i}^{z}$$

$$\sum_{i=1}^{N} q_{i}(x_{i}^{2} + y_{i}^{2} + z_{i}^{2})$$

$$\sum_{i=1}^{N} q_{i}\sigma_{i}^{z}$$

$$\sum_{i < j}^{N} e^{-\frac{\Lambda^{2}}{4}(\boldsymbol{r}_{i} - \boldsymbol{r}_{j})^{2}}$$

$$i < j$$

$$(7)$$