

1 Gaussian integrals

Real

$$\int d\boldsymbol{v} \, e^{-\frac{1}{2}\boldsymbol{v}^T \boldsymbol{A} \boldsymbol{v}} = (2\pi)^{N/2} \, \det \boldsymbol{A}^{-1/2} \tag{1}$$

$$\int d\boldsymbol{v} \, e^{-\frac{1}{2}\boldsymbol{v}^T \boldsymbol{A} \boldsymbol{v} + \boldsymbol{j}^T \cdot \boldsymbol{v}} = (2\pi)^{N/2} \, \det \boldsymbol{A}^{-1/2} \, e^{\frac{1}{2}\boldsymbol{j}^T \boldsymbol{A}^{-1} \boldsymbol{j}} \tag{2}$$

$$\int d\boldsymbol{v} \, e^{-\frac{1}{2}\boldsymbol{v}^T \boldsymbol{A} \boldsymbol{v}} (\dots) = (2\pi)^{N/2} \, \det \boldsymbol{A}^{-1/2} \sum_{\substack{\text{pairings of} \\ \{i_1, \dots, i_{2n}\}}} A_{i_{k_1} i_{k_2}}^{-1} \dots A_{i_{k_1} i_{k_2}}^{-1} \tag{3}$$