

# Investigating the inequality of phase change coefficients using ISS experimental data

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## Abstract

Kinetic theory is a popular approach to model liquid-vapor phase change but accurate determination of evaporation and condensation coefficients remains a challenge. Reported values of coefficients vary by several orders of magnitude. For simplicity and convenience evaporation and condensation coefficients are assumed to be equal though there is little physical evidence to support this. This study presents a novel methodology to test this assumption using data from Constrained Vapor Bubble (CVB) experiments conducted on the International Space Station (ISS). The experiments consist of a quartz cuvette that is partially filled with n-pentane; heated and cooled at opposite ends to induce simultaneous evaporation and condensation around a central bubble. Data obtained from the NASA Physical Sciences Informatics (PSI) database enabled a three-dimensional reconstruction of the liquid-vapor interface. The net mass flux over the vapor bubble surface is zero at steady operation, providing a closure relationship for simultaneous and independent calculation of both evaporation and condensation coefficients. The resulting coefficient values are within 1% of each other, but are not equal. The two coefficients are also within 2% of those predicted using transition state theory. When the evaporation and condensation coefficients are forced to be equal, the deviation from transition state theory is approximately 60%. This deviation monotonically increases with increasing rates of evaporation/condensation due to a systemic under-prediction of the bubble surface area. The agreement between derived coefficients and those predicted by transition state theory is maintained when the bubble surface area is corrected to account for Marangoni-induced interfacial instabilities.

**Keywords:** evaporation, condensation, phase change, kinetic theory, accommodation coefficients, CVB, ISS

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## Nomenclature

Symbol	Description	Units
<b>List of Symbols</b>		
$A$	Dispersion constant	J
$A_c$	Cross-sectional area of cuvette	$\text{m}^2$
$h_{fg}$	Latent heat of vaporization	$\text{J/kg}$
$k_s$	Thermal conductivity of quartz	$\text{W/m K}$
$k_l$	Thermal conductivity of pentane	$\text{W/m K}$
$k_B$	Boltzmann constant	$\text{J}\cdot\text{s}\cdot\text{m}^2\cdot\text{K}^3$
$m$	Mass of a single molecule	kg
$M$	Molar mass	$\text{kg/mol}$
$\dot{m}''$	Interfacial mass flux	$\text{kg}/\text{m}^2\text{s}$
$P$	Pressure	Pa
$\rho$	Density	$\text{kg}/\text{m}^3$
$p_o$	Outside perimeter of cuvette	m
$R$	Universal gas constant	$\text{J/kg}\cdot\text{K}$
$T$	Temperature	K
$V_l$	Molar volume	$\text{m}^3/\text{mol}$
$l_T$	translational length ratio	-
<b>Greek Symbols</b>		
$\delta$	Film thickness	m
$\epsilon$	Emissivity	-
$\kappa$	Film curvature	$\text{m}^{-1}$
$\lambda$	Wavelength of light	
$\Pi$	Disjoining pressure	Pa
$\sigma$	Surface tension	$\text{N}/\text{m}$
$\sigma_B$	Stefan-Boltzmann constant	$\text{W}/\text{m}^2\cdot\text{K}^4$
$\alpha_c$	Condensation coefficient	-
$\alpha_e$	Evaporation coefficient	-
$\beta$	Ratio of evaporation and condensation coefficients	-
$\alpha_{\text{TST}}$	Average condensation coefficient (Transition State Theory)	-
<b>Subscripts</b>		
$i$	$i^{\text{th}}$ point along the interface	
max	Maximum value	
min	Minimum value	
$sat$	Saturation	
$w$	Wall	
$\infty$	Surrounding	
<b>Superscripts</b>		
$l$	Liquid	
$v$	Vapor	

**1 1. Introduction**

Liquid vapor phase change is widespread in various scientific and industrial applications including space technologies [1–5], atmospheric science [6, 7], biology [8–10] and agriculture [11–14]. Modeling phase change during evaporation/condensation is a complex multiscale problem and kinetic theory is a widely used modeling strategy. Hertz [15] treated the vapor as an ideal gas with molecular velocities described by a Maxwell-Boltzmann distribution and developed an expression for mass flux of vapor molecules passing through an imaginary plane referred to as the Kinetic Theory Plane, KTP:

$$\dot{m}'' = \sqrt{\frac{m}{2\pi k_B}} \left( \frac{P^v}{\sqrt{T^v}} \right) \quad (1)$$

where  $\dot{m}''$  is the mass flux,  $m$  is the mass of a single vapor molecule,  $k_B$  is the Boltzmann constant,  $T^v$  is the vapor temperature,  $P^v$  is vapor pressure. It is common to assume a sharp interface separates the liquid and vapor phases and the KTP is “just inside the vapor” [16]. The position of KTP ( $S_{KTP}$ ) relative to the location of the interface ( $S$ ) is not universally established [17]. An alternative is a diffuse interface model that locates  $S$  and  $S_{KTP}$  at either end of the interfacial region where the properties are equal to the bulk phase as shown in Figure 1 [18]. Net phase change is an algebraic sum of simultaneous condensation and evaporation fluxes emanating from the bulk vapor and liquid, respectively. The vapor flux  $\dot{m}_v''$  is calculated using equation 1 for the vapor temperature  $T_i^v$  at location  $S_{KTP}$ . The evaporation flux from the liquid  $\dot{m}_l''$  is not as straightforward. Many studies approximate this flux by envisioning a hypothetical equilibrium state where the temperature is  $T_i^l$  which is the liquid-side interface temperature at saturation pressure  $P_s$ . In this hypothetical equilibrium state, the flux from the bulk liquid is by definition equal to the flux from the bulk vapor thereby enabling an approximation of  $\dot{m}_l''$ . This approximation is common to most kinetic theory models and is discussed in detail in prior publications [17, 18]. Evaporation and condensation occur simultaneously and the algebraic difference between the two is the net phase change flux [19–22]. The first term, shown in red, represents evaporation ( $\dot{m}_l''$ ) and the second term, shown in blue, represents condensation ( $\dot{m}_v''$ ):

$$\dot{m}'' = \sqrt{\frac{m}{2\pi k_B}} \left[ \frac{P_s(T_i^l)}{\sqrt{T_i^l}} - \frac{P_i^v}{\sqrt{T_i^v}} \right] \quad (2)$$

where  $P_i^v$  is the vapor pressure, and  $P_s(T_i^l)$  is the equilibrium saturation pressure at  $T_i^l$ . This approach to computing a net evaporation or condensation has two shortcomings. First, reflection of vapor molecules at the interface is neglected. Second, evaporation and condensation fluxes are based on the superposition of two different equilibrium states. The current study revisits these long-standing simplifications and analyzes their impact on heat and mass transfer during phase change.

When a vapor molecule is incident on the liquid-vapor interface, it may interact with the condensed phase in three ways. The molecule may be (1) accommodated into the liquid phase (condensation), (2) reflected back into the

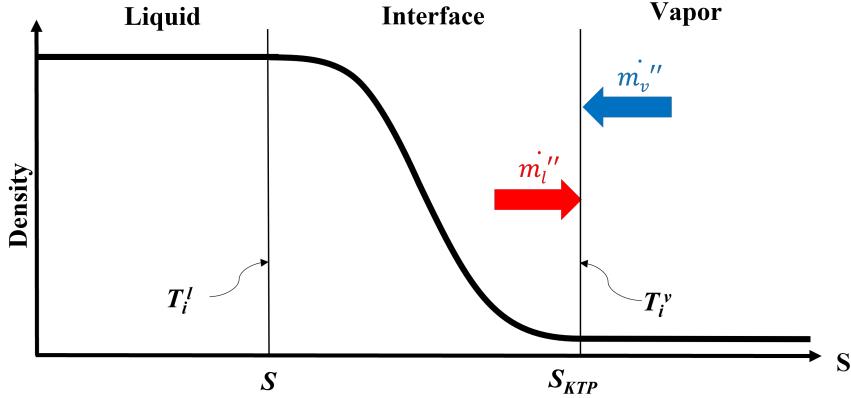


Figure 1: Schematic showing liquid, vapor, and diffuse interface during liquid-vapor phase change.  $S$  and  $S_{KTP}$  are located in the diffuse region where the local densities change from liquid to vapor. The evaporation ( $\dot{m}_l''$ ) and condensation ( $\dot{m}_v''$ ) fluxes are computed at  $S_{KTP}$

29 vapor phase, or (3) displace another molecule from the liquid phase. These three scenarios are illustrated in figure 2.  
 30 Reflection of vapor molecules results in the mass flux at surface  $S$  to deviate from equation 2. The discrepancy  
 31 between the theoretical flux and measured rates of evaporation and condensation led to the introduction of coefficients  
 32 for evaporation and condensation,  $\alpha_e$  and  $\alpha_c$ , respectively [23–25]:

$$\dot{m}'' = \sqrt{\frac{m}{2\pi k_B}} \left[ \alpha_e \frac{P_s(T_i^l)}{\sqrt{T_i^l}} - \alpha_c \frac{P_i^v}{\sqrt{T_i^v}} \right] \quad (3)$$

33  $\alpha_e$  and  $\alpha_c$  have theoretical limits of 0 and 1. A value of 1 denotes total accommodation into the new phase and a value  
 34 of 0 denotes total reflection.

35 Schrage [26] modified this kinetic model by considering a drift velocity in the bulk vapor superimposed on the  
 36 Maxwell-Boltzmann distribution. A drift velocity correction factor,  $D(\xi)$ , was added to the condensation term:

$$\dot{m}'' = \sqrt{\frac{m}{2\pi k_B}} \left[ \alpha_e \frac{P_s(T_i^l)}{\sqrt{T_i^l}} - D(\xi) \alpha_c \frac{P_i^v}{\sqrt{T_i^v}} \right] \quad (4)$$

37  $D(\xi) = \exp(\xi^2) - \sqrt{\pi}\xi [1 + \text{erf}(\xi)] \quad (5)$

38 where  $\xi$  is the ratio of macroscopic drift velocity ( $w_o$ ) to the most probable velocity of the vapor molecule ( $v_{mp}$ ). Drift  
 39 velocity can be expressed as  $w_o = \dot{m}''/\rho_v$ . For  $\xi < 10^{-3}$ , equation 4 reduces to the simplified Schrage model:

$$\dot{m}'' = \frac{2}{2 - \alpha_c} \sqrt{\frac{m}{2\pi k_B}} \left[ \alpha_e \frac{P_s(T_i^l)}{\sqrt{T_i^l}} - \alpha_c \frac{P_i^v}{\sqrt{T_i^v}} \right] \quad (6)$$

40 The Schrage model is applicable to flat liquid-vapor interfaces far from solid substrates. Phase change can be  
 41 affected by the presence of a solid substrate through mechanical forces arising from disjoining (intermolecular effects)

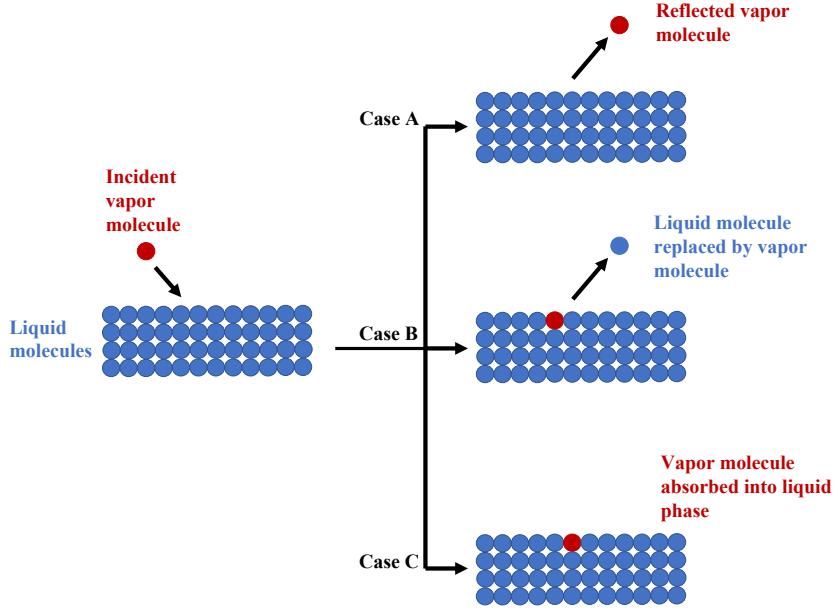


Figure 2: Different ways in which an incident vapor molecule can interact with liquid molecules: (A) Vapor molecule gets reflected off the interface. (B) Vapor molecule displaces a liquid molecule undergoing simultaneous evaporation and condensation, (C) Vapor molecule is absorbed into the liquid phase and undergoes condensation.

and capillary pressure (interfacial curvature) [27]. Wayner [28] incorporated these effects using Clausius-Clapeyron equation and integrating the Gibbs-Duhem equation over small intervals where fugacity change and vapor pressure changes are equal. The work of Wayner [28] has been reformulated by Bellur et al. [18] as:

$$\dot{m}'' = \left( \frac{2\alpha_c}{2 - \alpha_c} \right) \frac{P_i^v}{\sqrt{\pi} v_{mp}} \left[ \beta W \sqrt{\frac{T_i^v}{T_i^l}} - 1 \right] \quad (7)$$

where,  $\beta = \alpha_e/\alpha_c$  and  $W$  is a ratio of the pressures,  $P_s(T_i^l)/P_i^v$ , that incorporates curvature-induced pressure and disjoining pressure.

$$W = \frac{P_s(T_i^l)}{P_i^v} = \frac{P_{\text{sat}}^v}{P_i^v} + \frac{\rho_{\text{sat}}^v h_{fg}}{P_i^v} \left( 1 - \frac{T_i^v}{T_i^l} \right) + \left( \frac{T_i^v}{T_i^l} \right) \left( \frac{\rho_{\text{sat}}^v}{\rho^l} \right) \left( \frac{\Pi + P_c}{P_i^v} \right) \quad (8)$$

$\Pi$  is disjoining pressure and  $P_c$  is the capillary pressure of the liquid given by the product of surface tension ( $\sigma$ ) and curvature ( $\kappa$ ). Equation 7 is equivalent to that derived by Wayner [28], but is presented in a form where each term is non-dimensional and  $\alpha_e$  and  $\alpha_c$  are not assumed to be equal. There are three unknowns in equation 7, the liquid side temperature ( $T_i^l$ ) and coefficients  $\alpha_e$  and  $\alpha_c$ . To bring closure, it is commonly assumed that  $T_i^l = T_i^v$ ; that is, the saturation conditions at the liquid interface is the same as the far field vapor equilibrium temperature. The ramifications of this assumption are discussed in Bellur et al. [18] and Chakrabarti et al. [5]. An additional assumption is that  $\alpha_e = \alpha_c$ . There is no physical evidence to suggest this latter assumption is appropriate [5, 25, 29–33]. These two assumptions leaves  $\alpha_c$  as the only unknown variable in the kinetic formulation, which often becomes a tuning parameter used to match the computed rate of phase-change to experimental data. As a result, there are significant

discrepancies in reported values of the condensation coefficient, also known as an accommodation coefficient. The reported values of the coefficients for water range from 0.01 to 1 [25, 34–36]. Badam et al. [37] showed that assuming equality of evaporation and condensation coefficients required an order of magnitude adjustment to match experimental and theoretical values. Kryukov and Levashov [38] reinforced this argument by demonstrating that the uncertainty in calculating these coefficient values is significantly greater when the coefficients are assumed to be equal than when they are considered distinct. Montazeri et al. [39] reported a 50% variation between evaporation and condensation coefficients using molecular dynamics simulations of phase change in adsorbed water films on top of nanostructures. Meland et al. [40] also reported inequality of evaporation and condensation coefficients for an LJ-spline fluid near equilibrium. The potential inequality of coefficients is also impacted by parameters on a molecular level such as the structure of the interface [41, 42], polarity of molecules undergoing phase change [34], and presence of contaminants on non-renewing interfaces [20, 33, 43–46]. In summary, forcing  $\alpha_c = \alpha_e$  is a convenient simplifying assumption to attain closure of the kinetic model, but is not based on a mechanistic understanding. The present study provides a new methodology to test the equality of the two coefficients using high-quality data from the Constrained Vapor Bubble experiments [47, 48] conducted on the International Space Station.

## 2. Constrained Vapor Bubble experiments

The Constrained Vapor Bubble (CVB) experiment [2, 47, 49–52] was envisioned as an ideal wickless grooved heat pipe to investigate microscale heat transfer and interfacial phenomena. The setup consisted of a quartz cuvette with an internal dimension of 3 mm x 3 mm. An overview of the experiment setup can be seen in figure 3(a). The cuvette was evacuated and partially filled with n-pentane. The liquid fully wets the interior surface of the cuvette and forms a central bubble. During the experiments, one end of the cuvette was heated while the other was cooled. Liquid evaporated at the heated end into vapor, which was transported through the central bubble to the cooler end where it condensed. The condensed liquid wicked up the corners and was then transported back to the heated end through capillarity. Temperatures along the axis of the cuvette were measured by thermocouples that were embedded in one wall of the cuvette. Two types of imaging data were obtained. The first was a macro view of the cuvette. The second were high magnification (50x) interferograms that were used to determine the curvature of the liquid-vapor interface. The interferograms were ‘stitched’ together to obtain an end-to-end perspective of the liquid film curvature. The CVB tests were conducted in a microgravity environment on board the International Space Station (ISS) and are described at length in prior publications [2, 47, 49–52]. Temperature, heater power, and imaging data from these experiments are available from the NASA Physical Sciences Informatics (PSI) data base [53].

Of particular interest here is the fact that the CVB is a closed system and the net mass flux across the liquid-vapor surface must be zero at steady state. In other words, whatever amount of liquid evaporated at the heated end must

87 condense at the cold end. This provides a unique closure condition that enables independent calculation of  $\alpha_e$  and  $\alpha_c$ .  
 88 The high quality data from the ISS experiments conducted in the absence of gravity provides the perfect sandbox to  
 89 test the equivalence of  $\alpha_e$  and  $\alpha_c$ . The following sections describe analysis of the experimental data, multiscale model  
 90 and the of the heat and mass balances to calculate the coefficients.

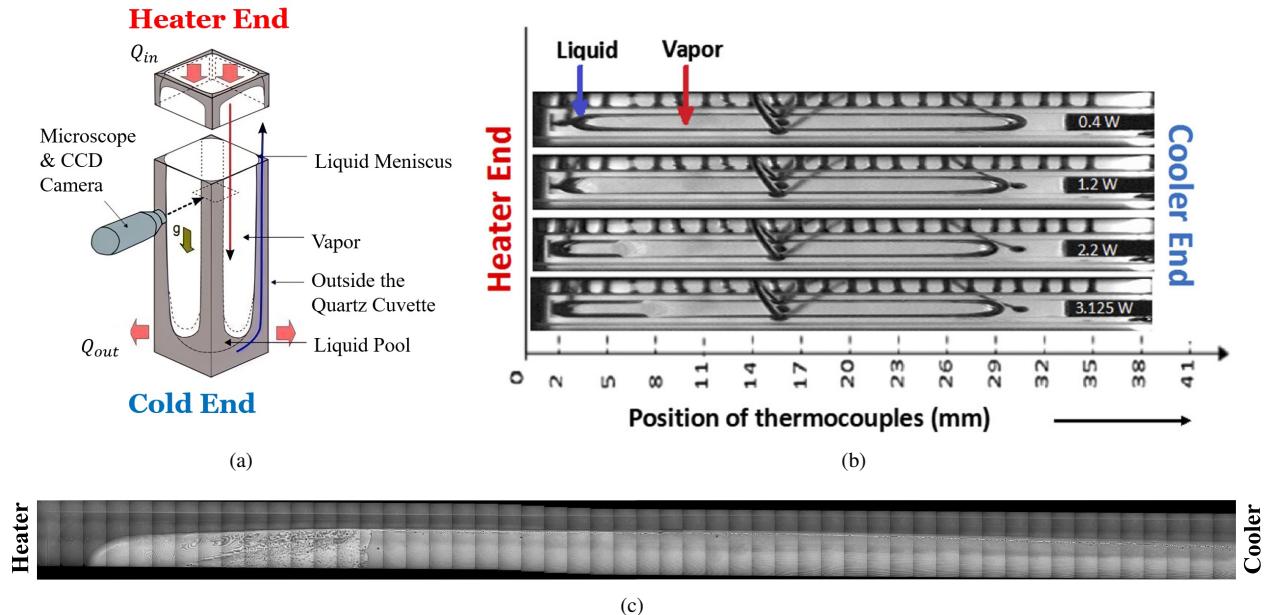


Figure 3: (a) Schematic of the CVB experimental setup. (b) Sample low magnification(10X) images showing steady, equilibrium bubble shapes for different heater inputs. (c) High magnification (50X) “stitched” images that are used the present study for reconstruction of the bubble as explained in section 3.1. Images were obtained from the NASA PSI database [53].

### 91 3. Image Analysis and Liquid Surface Reconstruction

92 Monochromatic light ( $\lambda = 546 \text{ nm}$ ) is incident on the closed cuvette during the CVB experiment which is partly  
 93 reflected at both solid-liquid and liquid-vapor interfaces. A phase shift is created between the two reflecting light  
 94 rays leading to interference. A fringe pattern with constructive and destructive interference is produced for a curved  
 95 surface, where the film thickness is gradually changing (figure 4). These fringe patterns are observed in the 50x images  
 96 (figure 3(c)). A 3-dimensional geometry of the liquid domain is reconstructed using a custom image processing routine  
 97 where the pixel intensities along a line scan (blue arrow in figures 4, 5) in the fringe pattern images are converted to  
 98 a film thickness profile. The authors have discussed the specifics of the image processing in a previous publication  
 99 [5]. The film thickness profiles are obtained for the entire surface of the bubble when there is no input (0 W) from the  
 100 heater end. The current study is limited to the shape obtained from the 0W setting due to a lack of high-resolution data  
 101 for cases with higher heat settings. The final outcome of this step is a computational liquid-solid domain representing  
 102 1/8th of the CVB cross-section symmetric about 3 axes as shown in figure 4. The next step involves the implementation  
 103 of appropriate thermal boundary conditions to calculate the two coefficients.

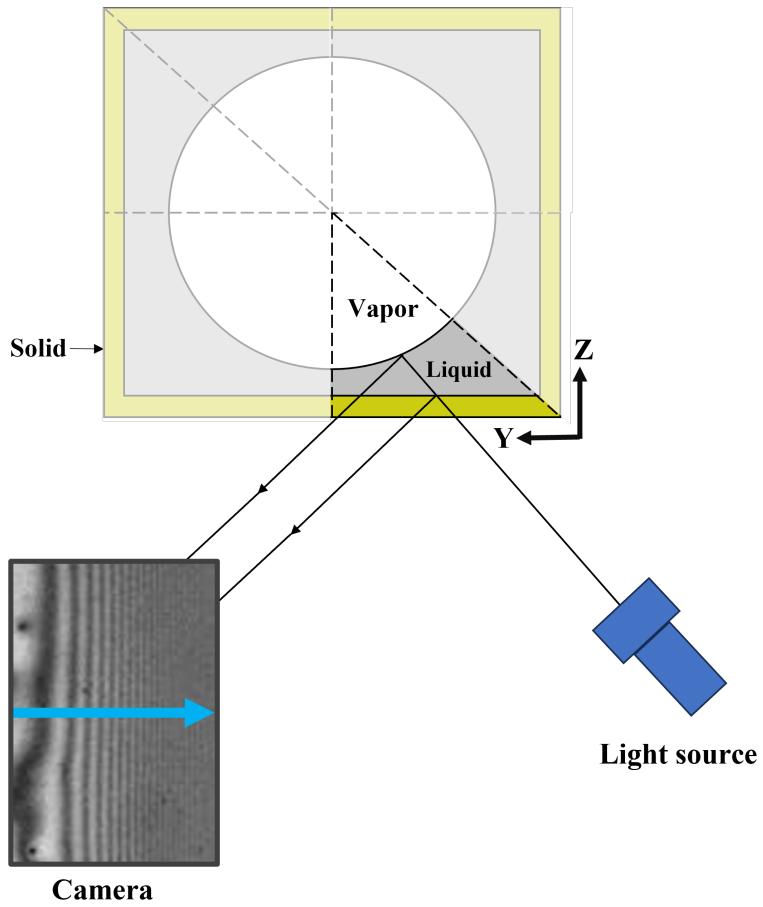


Figure 4: The diagram above is a schematic description of the reflection of a monochromatic light ray from an incident source at the solid-liquid and liquid-vapor interfaces of the 2D cross section of CVB experimental setup. Interaction of the two reflected waves for incident rays at different points along the curved liquid-vapor interface of the bubble forms interference patterns captured by the camera in the experimental setup

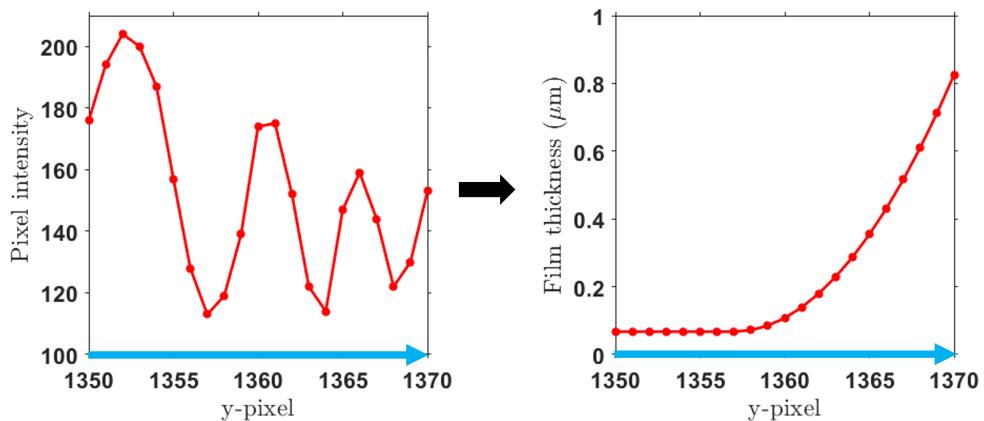


Figure 5: Line scans in the positive y direction (blue arrow in Figure 4), provides a 2D pixel intensity plot along the same direction. The pixel intensity is converted to a film thickness plot along the y-direction using the methodology established in [5].

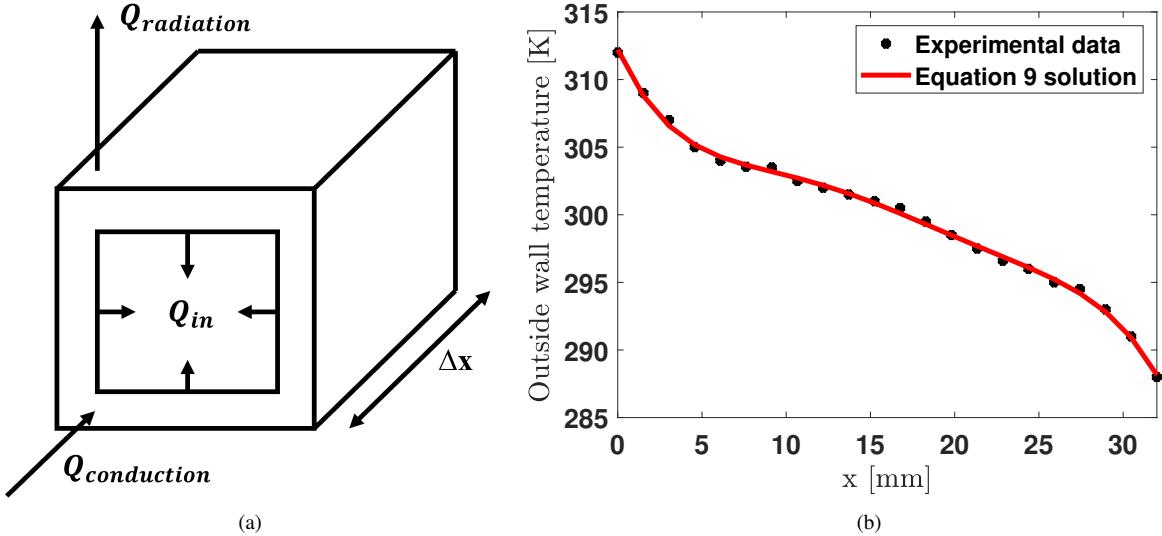


Figure 6: (a) Sectional schematic of heat balance along the wall where for every unit length  $\Delta x$  heat conducted axially ( $Q_{conduction}$ ) balanced by heat loss due to radiation ( $Q_{radiation}$ ) and heat lost into the fluid ( $Q_{in}$ ). (b) Experimental temperature measurements at the outside wall are used to obtain optimized emissivity and surrounding temperature values. Equation 9 is solved and compared to the experimental data. The emissivity and surrounding temperatures are then used as boundary condition parameters in the computational analysis.

#### 104 4. Thermal boundary conditions in the CVB

##### 105 4.1. Outer wall boundary conditions from evacuated “dry” tests

106 During the CVB experiments a fully evacuated cuvette was heated in order to determine the outer wall heat transfer  
 107 to the ISS environment. In the absence of natural convection in microgravity, the dominant mechanism is radiation  
 108 [47, 54]. Heat conducted axially was balanced by radiative heat transfer to the environment and heat transferred into  
 109 the fluid (when present) as shown in figure 6(a). The resultant heat balance is given by:

$$\underbrace{-k_s A_c \frac{d^2 T(x)}{dx^2}}_{\text{conduction}} = \underbrace{\sigma_B \epsilon p_o (T(x)^4 - T_\infty^4)}_{\text{radiation}} + Q_{in} \quad (9)$$

110 Here,  $Q_{in}$  is the heat input to the liquid. For an evacuated cell,  $Q_{in}$  is assumed to be negligible. Emissivity  $\epsilon$  and the  
 111 ambient temperature  $T_\infty$  were determined by fitting equation 9 to the experimentally recorded temperatures as shown  
 112 in figure 6(b). A 4th order Runge-Kutta method (ODE45 in Matlab™) was used to solve equation 9 subject to an  
 113 experimentally known heater setting and cooler side temperature. The radiation view factor was taken to be unity. The  
 114 resulting values for  $\epsilon$  and  $T_\infty$  were found to be 0.773 and 293 K, respectively. This correlates well with the average  
 115 ambient temperature on board the ISS during the CVB testing; also reported to be 293 K [54].

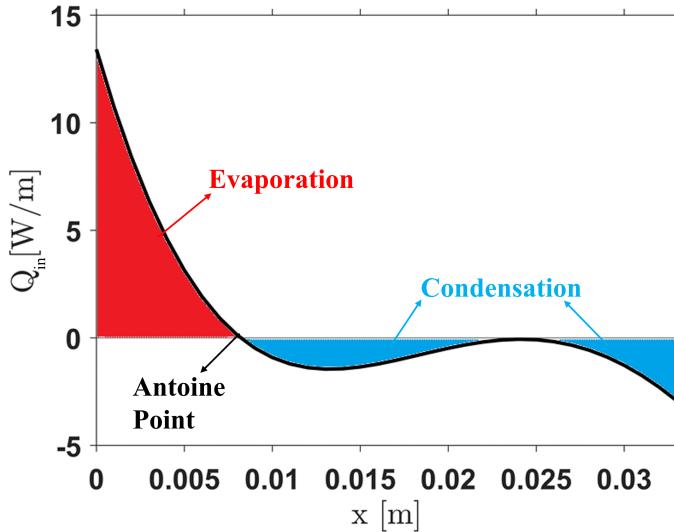


Figure 7: The profile of heat flow rate per unit length ( $Q_{in}$ ) along the outer wall with  $Q_{in}^+$  represented by the red shaded area representing evaporation. The plot obtained is for a heater setting of 0.2W.  $Q_{in}$  becomes zero at the Antoine point.

<sup>116</sup> 4.2. Inner wall conditions from “wet” tests

<sup>117</sup> Using the values for  $\epsilon$  and  $T_\infty$  determined in section 4.1, the discrete (i.e., local) heat transferred into the fluid ( $Q_{in}$ )  
<sup>118</sup> during the pentane-filled cuvette test was computed. Figure 7 illustrates  $Q_{in}(x)$  for the 30 mm long cuvette at 0.2 W  
<sup>119</sup> heater power as computed from equation 9. The net heat transfer to the fluid is zero when operating at steady state  
<sup>120</sup> conditions. However, this is split into two separate integrals that are equal and opposite: heat addition (evaporation)  
<sup>121</sup> and heat rejection (condensation). By considering just the positive values of  $Q_{in}(x)$ , the net heat addition to the cuvette  
<sup>122</sup> ( $Q_{in}^+$ ) is calculated. This is effectively just the area of the red colored evaporation section in figure 7. This particular  
<sup>123</sup> feature is critical to obtaining a non-zero integral value to calculate  $\alpha_c$  as discussed in section 5.

$$Q_{in}^+ = \int Q_{in}(x) \cdot dx \quad (10)$$

<sup>124</sup> 5. Multiscale Model

<sup>125</sup> The liquid film thickness in the curved interfacial domain reconstructed in Section 3 has length scales ranging  
<sup>126</sup> from millimeters to nanometers. For computational efficiency, the domain is divided into macroscale and microscale  
<sup>127</sup> submodels. The heat and mass transfer calculations are performed separately for the submodels and are coupled  
<sup>128</sup> together using the methodology explained in the upcoming subsections.

129 *5.1. Macroscale submodel*

130 The liquid-solid domain, reconstructed and comprising of 5.7 million mesh cells, is implemented in Ansys Fluent.  
131 In figure 8, the liquid domain is depicted in gray, while the solid wall is represented in yellow, with the hot and cold  
132 end apex tips at  $x = 5$  mm and 29.7 mm respectively. Assuming laminar flow within the liquid, a no-slip boundary  
133 condition is applied to the entire inner solid wall. Experimentally known heater setting of 0.2 W used as the thermal  
134 boundary condition at the hot end. The cold end is maintained at a constant temperature of 288 K, consistent with  
135 the experimental setup with an anticipated error of less than 0.5 K [3]. Symmetry boundary conditions are employed  
136 as appropriate. A radiative heat flux boundary condition is implemented at the outer wall, utilizing  $\epsilon$  and  $T_\infty$  derived  
137 from the dry heat balance (section 4). Thermophysical properties for pentane are obtained from the NIST website [55],  
138 while the density and thermal conductivity of quartz are set at 2719 kg/m<sup>3</sup> and 1.4 W/mK respectively. Considering a  
139 steady-state near-equilibrium bubble, constant vapor properties are assumed and only the liquid domain is modeled. To  
140 model phase change at the curved interface, a single-cell thick layer of mesh cells in the liquid domain, adjacent to the  
141 interfacial surface is marked and designated as the “active region”. User Defined Functions (UDFs) are utilized within  
142 this region to calculate local mass flux based on a phase change model for curved liquid-vapor interfaces (equation 7)  
143 with locally queried liquid properties and constant vapor properties. Latent heat flux is then determined by multiplying  
144 the mass flux with the enthalpy of evaporation of pentane. These computed fluxes act as volumetric source or sink  
145 terms in the active region to account for evaporation and condensation. Equation 7 needs an input for  $\alpha_e$  and  $\alpha_c$ . So,  
146 as a starting point, the value of  $\alpha_c$  is initially set to be equal to  $\alpha_e$  with a value of 0.5, making  $\beta = 1$ . The temperature  
147 and pressure for vapor are determined using a similar methodology to that of Chatterjee et al. [47]. Wall temperature  
148 is extracted at the x-location where the  $Q_{in}$  crosses zero; i.e. the Antoine point. The temperature at this point is  
149 considered to be the vapor temperature. The vapor pressure at the Antoine point is:

$$\log_{10}(P_i^v) = C_1 + \frac{C_2}{T_i^v + C_3} \quad (11)$$

150  $C_1$ ,  $C_2$  and  $C_3$  are constants equal to 7.00877, 1134.15 and 238.678 respectively for pentane [47]. Surface tension is  
151 modeled as a linear function of liquid temperature at the interface ( $T_i^l$ ),

$$\sigma = \sigma_0 + \gamma(T_i^l - T_0) \quad (12)$$

152 where  $\sigma_0$  is 0.0476 N/m at  $T_0 = 300$  K and  $\gamma = -10^{-4}$  N/m-K [55].

153 The macroscale domain is truncated at a liquid film thickness of 10  $\mu\text{m}$  resulting in a cutoff plane (figure 8).  
154 Initially, a zero heat and mass flux boundary condition is applied at the cut-off plane. Steady-state mass, momentum,  
155 and energy equations are solved using the SIMPLEC pressure-velocity coupling in Ansys Fluent. The temperatures

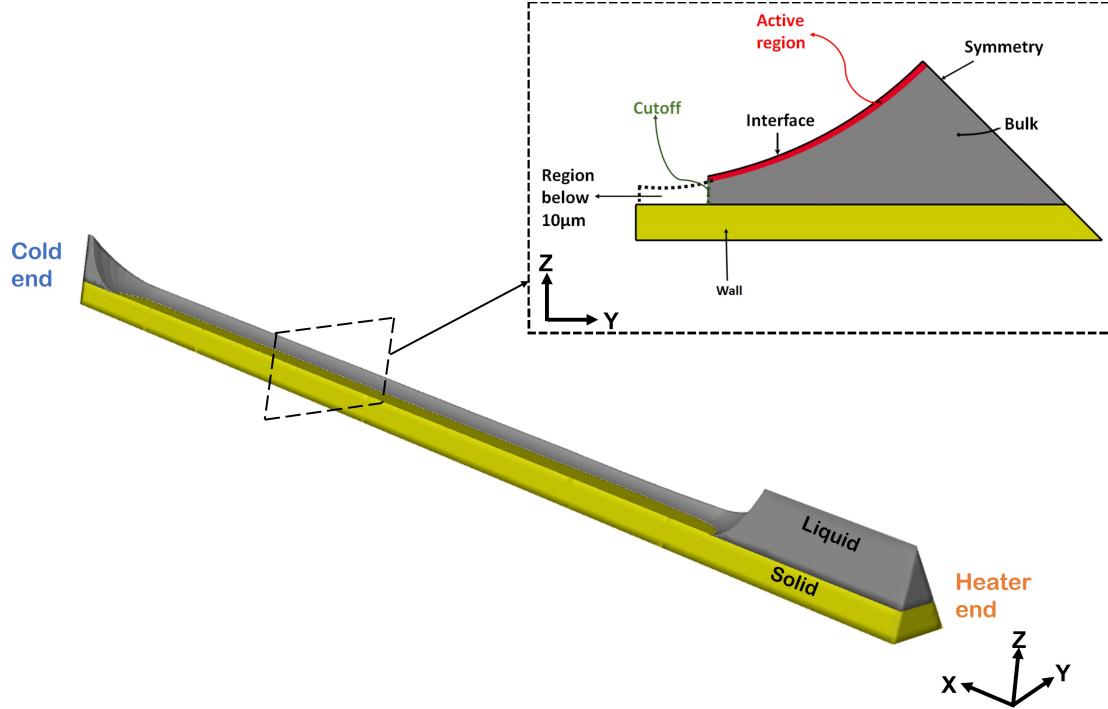


Figure 8: The reconstructed 1/8<sup>th</sup> section of the CVB experiment showing the liquid pentane and quartz solid with the location of the heater and the constant cold temperature [5]

156 extracted from the inner wall are used to determine heat and mass flux contributions from the cut-off thin film below  
157 10  $\mu\text{m}$ , as detailed in the following section.

158 *5.2. Microscale submodel*

159 A microscale thin film submodel is used to solve for net mass and heat transfer in the truncated region and is  
160 coupled with the macroscale submodel. The thin film submodel is centered around a heat balance, wherein the con-  
161 duction heat flux from the solid wall is equal to the phase change heat flux. The temperature gradient through the film  
162 (z-direction) is significantly larger than that in the x and y directions due to orders of magnitude difference in length  
163 scales. Hence, a 1D heat transfer approximation is applied in the microscale thin film [5]:

$$h_{fg}\dot{m}'' = -\frac{k_l}{\delta}(T_w - T_i^l) \quad (13)$$

164 Equation 13 is a balance of latent heat flux at the curved interface and 1D conduction through the pentane liquid  
165 using Fourier's law. Employing the film thickness ( $\delta$ ) obtained from image processing for the profile below the 10  
166  $\mu\text{m}$  cutoff and results from the macroscale submodel, a new local interfacial mass flux ( $\dot{m}''$ ) and  $T_i^l$  and is calculated  
167 at each point on the microscale thin film. The process starts at the cutoff and proceeds in a direction of reducing  
168 film thickness. The interfacial temperature at the cutoff ( $T_i^l$ ) and the wall temperature profile ( $T_w$ ) is readily available

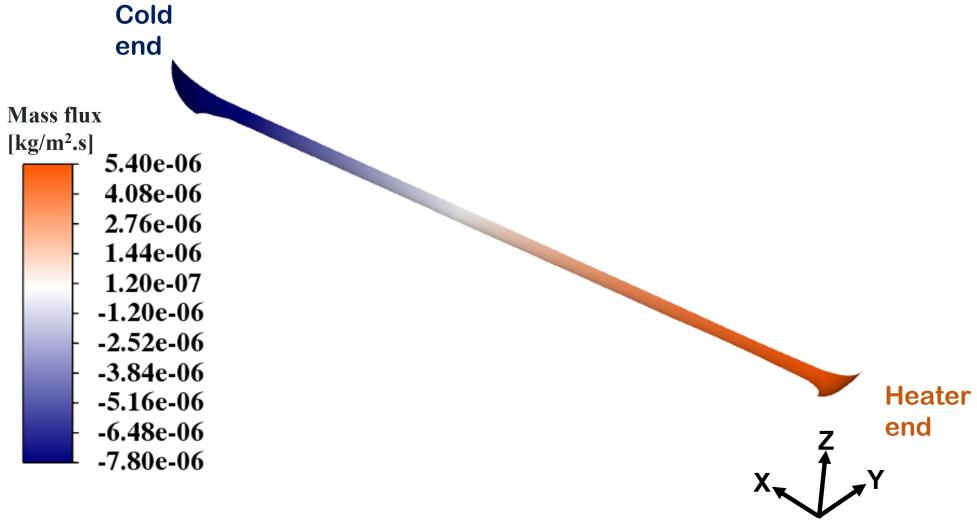


Figure 9: Mass flux profile of the interfacial region of the CVB domain obtained by coupling the thin film model with the macroscale model.

from the macroscale submodel. This is used to calculate a new value of  $T_i^l$  and  $\dot{m}''$  at an adjacent  $y$  location based on equation 13. This process is repeated until the symmetry plane ( $y = 0$  mm) is reached or the  $\dot{m}''$  becomes negligible. This process is repeated for multiple axial locations along the CVB. The mass flux profiles in the microscale regions ( $<10 \mu\text{m}$ ) are then extracted and integrated over the corresponding film length to obtain the mass and heat flow rate per unit length along the axis. This can now be fed back into the macroscale submodel as a mass flow boundary condition, effectively relaxing the previously made no-mass flux at the cutoff assumption and establishing a robust 2-way coupling between the submodels.

The macroscale and microscale submodels are solved iteratively to resolve interfacial mass fluxes in the entire multiscale domain. The solution begins in the macroscale submodel assuming no evaporation contribution from the thin film. The interface temperature at the cutoff and inner solid wall temperatures from the macroscale submodel are then used as inputs in the microscale model. The heat and mass flux contribution from the microscale model is fed back into the macroscale model in successive iterations. The coupled multiscale model is iteratively solved until the change in inner wall temperature ( $T_w$ ) is less than 0.1 % between consecutive iterations. Coupling the thin film submodel with the macroscale submodel yields a continuous, smooth mass flux distribution along the entire surface (figure 9). This coupled approach eliminates the need for guessed or arbitrary matching conditions, relying solely on experimental inputs. Additional detail on this modeling strategy can be found in the authors' prior publication [5]. The interfacial temperatures ( $T_i^l$ ), mass fluxes and other geometric properties obtained from the multiscale model are used as inputs to mass and energy conservation equations to determine the values of condensation ( $\alpha_c$ ) and evaporation coefficients ( $\alpha_e$ ) using mass and energy conservation constraints as described in the next section.

188 **6. Determining  $\alpha_c$  and  $\beta$**

189 From the multiscale model results, the values of temperatures, pressures, film thickness, and curvature are first  
 190 queried at all the data points along the interface. Using these parameters, the mass flux  $\dot{m}''$  is determined along the  
 191 interface using equation 7. Since the CVB experimental setup is a closed system, the net mass flux across the interface  
 192 is zero. This provides the first constraint for calculation of the coefficients:

$$193 \quad \dot{m} = \int_s \left[ \frac{2\alpha_c}{2 - \alpha_c} \frac{P_i^v}{\pi v_{mp}} \left[ \beta W \sqrt{\frac{T_i^v}{T_i^l}} - 1 \right] \right] dA = 0 \quad (14)$$

$\alpha_c$  and  $\sqrt{\frac{m}{2\pi k_B}}$  are uniform on the entire surface and equation 14 reduces to:

$$193 \quad \int_s \left[ \beta W \sqrt{\frac{T_i^v}{T_i^l}} - 1 \right] dA = 0 \quad (15)$$

194  $\beta$  obtained from equation 15 is a single value that applies to the entire interfacial domain.  $\alpha_c$  is obtained from an  
 195 evaporation-only energy balance. The net heat added into the CVB domain obtained from equation 10 ( $Q_{in}^+$ ) must  
 196 equal the net mass flux integrated over just the positive values of  $\dot{m}''$  multiplied by the local latent heat of evaporation  
 197 ( $h_{fg}$ ) as shown in equation 16:

$$197 \quad Q_{in}^+ = \int h_{fg} \dot{m}'' dA \quad (16)$$

198 Using the value of  $\beta$  from the first constraint (equation 15) for mass flux in equation 16, the second constraint is  
 199 derived to compute a constant  $\alpha_c$  for the entire interfacial domain:

$$200 \quad Q_{in}^+ = h_{fg} \frac{2\alpha_c}{2 - \alpha_c} \sqrt{\frac{m}{2\pi k_B}} \int \left[ \beta W \sqrt{\frac{T_i^v}{T_i^l}} - 1 \right] dA \quad (17)$$

200 The algorithm to iteratively compute  $\alpha_c$  and  $\beta$  is shown in figure 10. The process starts with initial guessed  
 201 values. The multiscale model is used to obtain local thermophysical properties and a map of mass flux along the entire  
 202 domain. The values of  $\alpha_c$  and  $\beta$  are computed from equations 15 and 17. The calculated set of  $\alpha_c$  and  $\beta$  values are fed  
 203 back into the multiscale model and iterated till the change in both  $\alpha_c$  and  $\beta$  are less than 0.001 %. The results obtained  
 204 from this iterative scheme, choice of initial guesses and the sensitivity of the value of  $\beta$  are discussed in the proceeding  
 205 section.

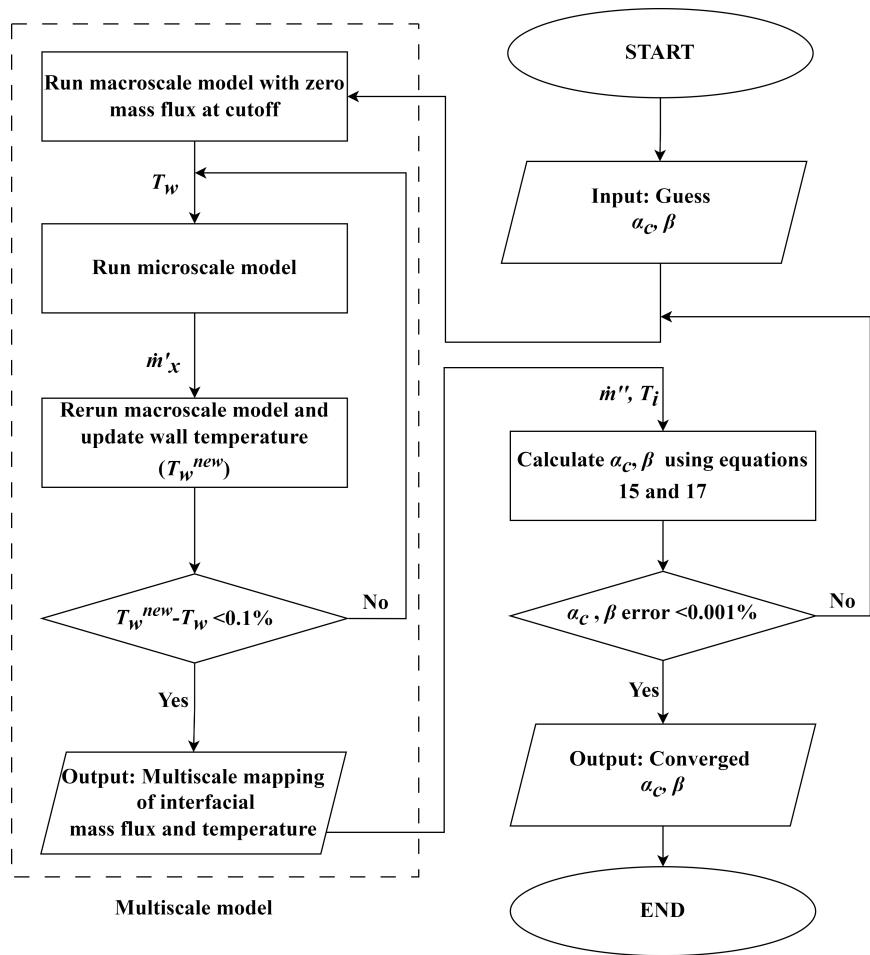


Figure 10: Flow chart explaining entire methodology used for obtaining  $\alpha_c$  and  $\beta$

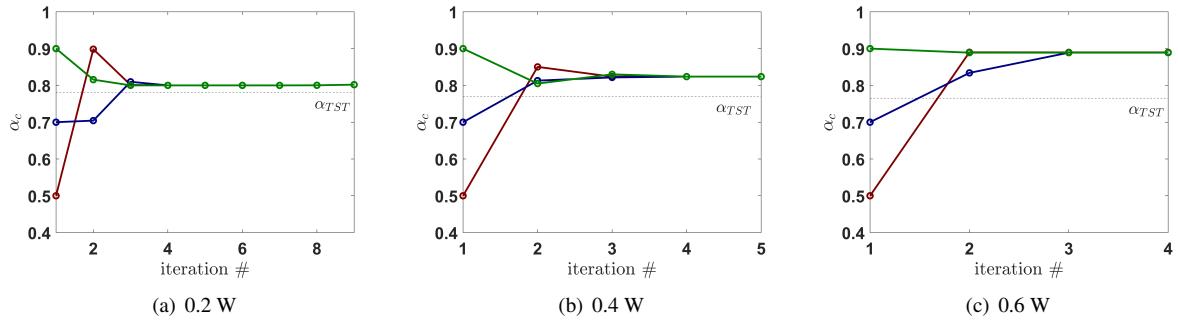


Figure 11: The computed values of  $\alpha_c$  values in each iteration as explained in section 2.6 are plotted against the iterative loop number.  $\alpha_c$  convergence for different initial guess at (a) 0.2 W, (b) 0.4 W and (c) 0.6 W heater setting are shown above. The red, blue, and green connectors are not interpolants. They are used to explain the propagation of the solution over different iterations. A horizontal line is drawn to represent expected  $\alpha_{TST}$  obtained from transition state theory(TST). Although the obtained  $\alpha_c$  and  $\alpha_{TST}$  are within 2% for the 0.2 W heater setting, the difference between the converged  $\alpha_c$  and  $\alpha_{TST}$  is seen to increase with heater settings of 0.4 W and 0.6 W.

## 206 7. Results and discussion

### 207 7.1. Converged coefficient values

208 Based on the methodology described in the previous section, the results for converged values of  $\alpha_c$  and  $\beta$  are cal-  
 209 culated to be  $0.801 \pm 0.031$  and  $0.996 \pm 0.001$  respectively for the 30 mm cuvette set to 0.2 W . The uncertainty in these  
 210 values are due to both experimental inputs and numerical modeling. The uncertainty in thermocouple measurement  
 211 was reported during the CVB experiments to be  $\pm 0.5$  K along with a thermocouple location uncertainty of  $\pm 0.1$  mm.  
 212 The propogated error in  $T_i^l$  while using the multiscale model is 0.53 K . The propagated error as a result of all the  
 213 sources mentioned above results in an uncertainty of around 0.1% in  $\beta$  and 3.9% in reported values of  $\alpha_c$ . The iterative  
 214 scheme is stable and reproducible. The values of  $\alpha$  and  $\beta$  calculated are independent of the initial guess. Figure 11(a)  
 215 shows that the same converged values are obtained even when a wide range of the initial guess for  $\alpha_c$  are used at  
 216 different heater settings.

217 For validation, the calculated condensation coefficient  $\alpha_c$  is compared with that obtained by Nagayama and Tsuruta  
 218 [56] ( $\alpha_{TST}$ ) using transition state theory (equation 18). To the best of the author's knowledge, this is the current state-of-  
 219 the-art formulation for calculating the coefficients and agrees well with several other studies [18].  $\alpha_{TST}$  was estimated  
 220 using the saturation properties of liquid and gaseous pentane using temperatures from the Antoine point as explained  
 221 in section 5.1.

$$\alpha_{TST} = (1 - l_T) \exp\left(\frac{-1}{2l_T - 1}\right) \quad (18)$$

222 where the translational length ratio ( $l_T$ ) =  $\sqrt[3]{\rho_{sat}^v / \rho_{sat}^l}$ . This results in  $\alpha_{TST} = 0.782$ , which matches the model converged  
 223  $\alpha_c$  within < 2% at the 0.2 W heater setting. Hence, a new methodology is established for the calculation of evaporation  
 224 and condensation coefficients independently using mass and energy conservation. The variation between the two  
 225 coefficients is less than 0.4 %. Although the two calculated coefficients are very close to being equal to each other,

226 the implication of assuming their equality is still not clear. In the next section, the significance of forced equality is  
227 explored.

228 *7.2. Convergence by forcing coefficients to be equal*

229 To explore the implications of forced equality,  $\alpha_e$  and  $\alpha_c$  are calculated using the same iterative method described  
230 above (figure 10) with the exception that  $\beta$  is arbitrarily fixed to be a constant value. This would require the calculation  
231 of  $\alpha_c$  using equation 17 and multiplying  $\alpha_c$  with the fixed  $\beta$  value to obtain  $\alpha_e$ . The calculated  $\alpha_c$  and  $\alpha_e$  are plotted  
232 against fixed values of  $\beta$  (figure 12). It is observed that  $\alpha_e$  and  $\alpha_c$  reduce by about 60 % when  $\beta$  is changed from the  
233 actual converged value from the previous section (0.996) to the commonly assumed value of unity. While it is certainly  
234 enticing to assume  $\beta \approx 1$ , it must be done so with caution because  $\alpha_c$  is extremely sensitive to  $\beta$ . Figure 12 suggests  
235 that a variation of almost an order of magnitude in  $\alpha_c$  is possible for < 1% variation in  $\beta$ . This finding explains one of  
236 the many reasons for the wide range in reported values of  $\alpha_c$  that have spanned many orders of magnitude [25].

237 To further assess the impact of assuming equality in coefficients, the coupled multiscale model is run using  $\beta =$   
238 1 and it was found that the mass flux values obtained at individual points along the interface vary by about 1.5 %.  
239 However, when the local interfacial mass flux is integrated over the interfacial area and multiplied by the latent heat of  
240 evaporation to obtain the net evaporative heat flow rate ( $\dot{Q}_{in}^+$ ), an underestimation of 12% in the evaporative heat flow  
241 rate is observed for cases when  $\beta$  is increased from 0.996 to 1. Hence, assuming equal evaporation and condensation  
242 coefficients (as done by many researchers) can induce significant inaccuracies in estimating phase change heat transfer  
243 over large liquid-vapor interfacial areas like those in space mission fuel tanks, nuclear power plants, large water bodies  
244 etc. This finding adds to the rising concerns regarding the assumption of equal coefficients as discussed in Section 1.

245 The results for the calculation of coefficients discussed until now are obtained for an equilibrium domain shape of  
246 the bubble at 0 W heater setting with boundary conditions at 0.2 W heater setting. The effects of increasing the heater  
247 settings for the setup on the calculation of coefficients are explored in the next section.

248 *7.3. Results for higher heater settings*

249 The iterative method described in figure 10 is repeated for a heater settings of 0.4 W and 0.6 W. The calculation  
250 procedure described in sections 4-6 are repeated with updated vapor pressure, temperatures along with  $\sigma$ ,  $\epsilon$  and  $Q_{in}$   
251 obtained from the dry and wet heat balance for the new heater setting. For 0.4 W,  $\alpha_c$  and  $\beta$  equal to 0.824 and  
252 0.996 respectively, are obtained (figure 11(b)). For 0.6 W,  $\alpha_c$  and  $\beta$  are calculated to be 0.887 and 0.994 respectively  
253 (figure 11(c)). Interestingly, these values deviate from  $\alpha_{TST}$  as the heater setting is increased. The deviation between  
254 calculated  $\alpha_c$  and  $\alpha_{TST}$  increases from about 2 % for 0.2 W setting to 6.9 % for the 0.4 W setting and 15 % for the 0.6  
255 W setting.

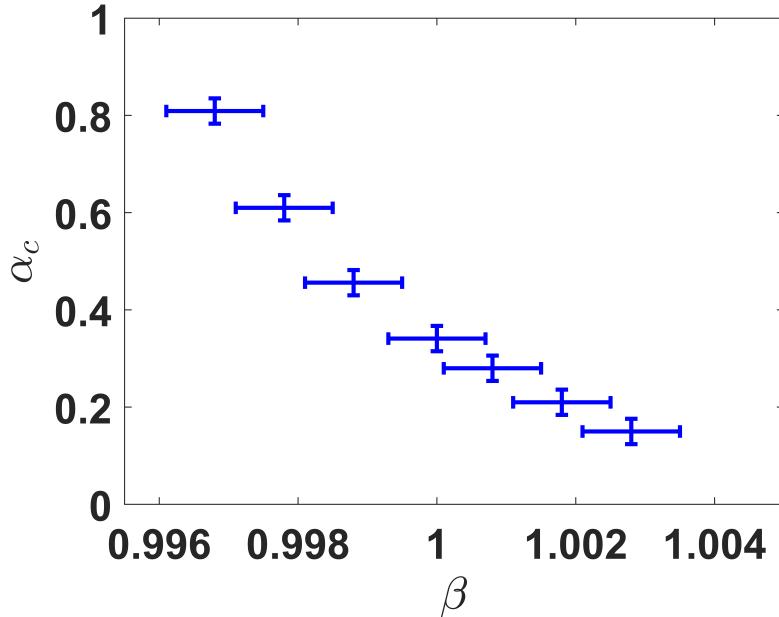


Figure 12: Obtained  $\alpha_c$  and  $\alpha_e$  values by fixing  $\beta$  as constant. The trend shows that assuming equal  $\alpha_e$  and  $\alpha_c$  ( $\beta = 1$ ) changes the obtained  $\alpha_c$  and  $\alpha_e$  by about 60% when compared to the coefficients calculated from the iterative scheme mentioned in section 4.1. All values are plotted with error bars estimated in section 4.1

The systemic deviation can be attributed to uncertainties in the interface shape. Absence of high resolution image data and spontaneous oscillations in the liquid film make it difficult to reconstruct interface shapes at higher heater settings. For all cases a 0 W shape is used as standard for the multiscale model and only the boundary conditions relevant to higher heater settings are changed. However, as the heat transferred to the bubble increases, the vapor pressure of the bubble would increase causing it to expand. To account for this increase without actually reconstructing the bubble shape, an area increment factor is introduced to the elemental areas during integral calculations in equation 15 and 17. This area increment can be qualitatively estimated using CVB experimental data. The expansion of the bubble in the  $y$  direction is estimated by the change in distance (yellow arrows in figure 13) between the region where the thin film begins(fringe patterns begin to form) and the inner wall. The axial distance is estimated by examining the change in distance between the apex point of the bubble and the inner wall on the heater side (blue arrows in figure 13). An area increase of 6.8 % and 17.1 % is estimated between the 0 W & 0.4 W shapes and 0 W & 0.6 W shapes respectively. Since this area increase was not inherently captured in the multiscale model, the elemental areas are incremented during the numerical integration process when evaluating equations 15 and 17. New values of the coefficients are again calculated with the incremented elemental areas. It is observed that new calculated values of condensation coefficient ( $\alpha_c^{new}$ ) reduce for both 0.4 and 0.6W cases when the elemental areas are increased. The new values of the calculated condensation coefficient ( $\alpha_c^{new}$ ) are now closer to that from transition state theory ( $\alpha_{TST}$ ) upon taking the bubble's area expansion into account at higher heater settings (Table 1). The area increase estimation however becomes difficult

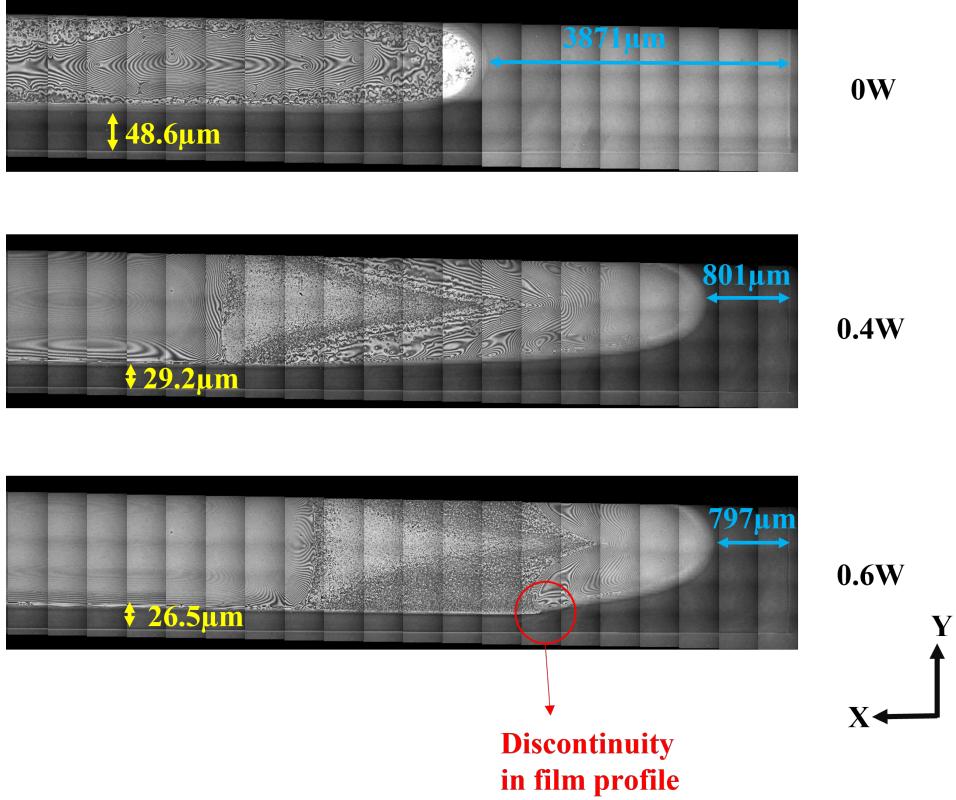


Figure 13: Expansion of the bubble at higher heater settings along the axial(blue) and transverse (yellow) direction. The expansion data is usable until 0.4W. However, at 0.6 W setting, a discontinuity is observed near the heater making it difficult to estimate the expansion.

Table 1: For heater settings of 0.4 and 0.6W,  $\alpha_c$  values calculated without adding the area increment ( $\Delta A$ ) are seen to deviate significantly from the expected  $\alpha_{TST}$  values. Upon adding  $\Delta A$  to the area integrals in equation 15,17, this overestimate is reduced and new  $\alpha_c^{new}$  is calculated which matched well with  $\alpha_{TST}$

Heater (W)	$\alpha_c$	$\alpha_{TST}$	$\Delta A$ (%)	$\alpha_c^{new}$
0.4	0.824	0.770	6.8	0.812
0.6	0.888	0.765	17.1	0.722

at heater settings beyond 0.6 W. This is because of discontinuities observed in the bubble shape (figure 13). This is likely due to instabilities arising from dominant Marangoni forces near the thin film as explained in many prior studies [5, 57]. Higher spatiotemporal mapping of the liquid-vapor interfacial area in future experiments could potentially improve the results described here.

## 8. Conclusion

Kinetic theory based models for liquid-vapor phase change are popular in literature but contain several longstanding assumptions that have not been well characterized. At the core of all kinetic models is a superposition of two independent pseudo-equilibrium states. This results in two separate terms for condensation and evaporation; each with its own independent coefficient. The net phase change is then simply the algebraic sum of the condensation and evap-

oration terms. Since the two coefficients are generally unknown, a commonly made assumption is that the evaporation coefficient ( $\alpha_e$ ) is equal to the condensation coefficient ( $\alpha_c$ ). To the best of the authors knowledge, there is no physical reasoning for this assumption other than mathematical simplification and closure of equations. This work explores this seemingly ubiquitous simplifying assumption and explores its applicability using the Constrained Vapor Bubble (CVB) experiments conducted on the International Space Station (ISS). The CVB experiment is a closed cuvette that is partially filled with pentane; heated and cooled at opposite ends to form a central bubble. Although it was originally designed for a different purpose, the CVB setup is uniquely suited for testing this fundamental assumption because it is a closed system at steady state where conservation laws dictate that: (1) net mass flux must equal zero and (2) the net heat added to the fluid must equal the total latent heat. This provides the much needed closure conditions to compute both coefficients independently and test the applicability of the simplifying assumption. The study reveals that the two coefficients are close to each other but they are not strictly equal. For the 0.2 W case,  $\beta = \alpha_e/\alpha_c = 0.996 \pm 0.001$  and  $\alpha_c = 0.801 \pm 0.031$ . The value of  $\alpha_c$  agrees well with the predicted transition state theory value,  $\alpha_{\text{TST}}$  [56]. Since  $\beta \approx 1$ , it may be tempting to force equality by setting  $\beta = 1$ . This artificially boosts evaporation and this must be compensated by a reduction in  $\alpha_c$ . If one does not care about the true value of  $\alpha_c$  and merely wishes to use it as a fitting coefficient or as input in modeling this may not matter. However, the sensitivity between  $\beta$  and  $\alpha_c$  is quite dramatic. The value of  $\alpha_c$  reduces by almost 50% when  $\beta$  is artificially increased by <0.1%. This reduction in  $\alpha_c$  is also accompanied by a similar reduction in  $\alpha_e$  and conservation laws are still applicable. More importantly, this reduction in the coefficient reduces the overall latent heat rate considerably. This has the potential to artificially reduce the model predicted throughput of heat transfer devices that rely on phase change such as heat pipes, evaporators, etc.

In conclusion, assuming  $\alpha_e = \alpha_c$  reduces the formulation to a single coefficient, called the “accommodation” coefficient. This simplification of the physics has led researchers to reduce the coefficient to a tuning parameter in modeling or empirical fit to experimental data. Assuming  $\alpha_e = \alpha_c$  forces an artificially lower value of  $\alpha_c$  which in a modeling paradigm limits heat transfer performance of latent heat based devices. This forcing equality in the coefficients is not always applicable. This assumption has the potential to under predict latent heat transfer and artificially limit device performance. This assumption could also be a reason for the discrepancy in prior reported values.

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### 313 Data Availability

314 The data that support the findings of this study are available from the corresponding author upon reasonable  
315 request.

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