

Consider the functions $f(x)$ and $g(x)$

$$f(x) = \sqrt{x-3}$$

$$g(x) = x^3$$

Answer the following questions about the functions $f(x)$ and $g(x)$.

Exercise 1 What are domain and range of $f(x)$?

Domain: $\boxed{3}, \boxed{\infty}$

Range: $\boxed{0}, \boxed{\infty}$

Exercise 1.1 What are domain and range of $g(x)$?

Domain: $\boxed{-\infty}, \boxed{\infty}$

Range: $\boxed{-\infty}, \boxed{\infty}$

Exercise 1.1.1 Find the following compositions of functions:

$$f(g(x)) = \boxed{\sqrt{x^3-3}}$$

$$g(f(x)) = \boxed{(\sqrt{x-3})^3}$$

$$f(f(x)) = \boxed{\sqrt{\sqrt{x-3}-3}}$$

$$g(g(x)) = \boxed{x^9}$$

Exercise 1.1.1.1 What are domain and range of $f(g(x))$?

Domain: $\boxed{3^{\frac{1}{3}}}, \boxed{\infty}$

Range: $\boxed{0}, \boxed{\infty}$

Exercise 1.1.1.1.1 What are domain and range of $g(f(x))$?

Domain: $\boxed{3}, \boxed{\infty}$

Range: $\boxed{0}, \boxed{\infty}$