

**Exercise 1** For each of the following functions, find two simpler functions  $f$  and  $g$  such that the given function can be written as a composite function  $g \circ f$ . The functions  $f$  and  $g$  should each be a famous function or a polynomial.

- If  $g(f(x)) = \sin(x^2)$ , then we could decompose this function into  $g(x) = \boxed{\sin(x)}$  and  $f(x) = \boxed{x^2}$ .
  - If  $g(f(x)) = \sqrt{2x^5 - 7}$ , then we could decompose this function into  $g(x) = \boxed{\sqrt{x}}$  and  $f(x) = \boxed{2x^5 - 7}$ .
  - If  $g(f(x)) = e^{3x-x^2}$ , then we could decompose this function into  $g(x) = \boxed{e^x}$  and  $f(x) = \boxed{3x - x^2}$ .
  - If  $g(f(x)) = |\ln(x)|$ , then we could decompose this function into  $g(x) = \boxed{|x|}$  and  $f(x) = \boxed{\ln(x)}$ .
  - If  $g(f(x)) = 5e^{4x} + 7e^{3x} - 11e^x + 4$ , then we could decompose this function into  $g(x) = \boxed{5x^4 + 7x^3 - 11x + 4}$  and  $f(x) = \boxed{e^x}$ .
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