Use the given pair of functions to find the following values if they exist. If the value is not defined, write "undefined".

**Exercise 1**  $f(x) = x^2$ , g(x) = 2x + 1

- $(g \circ f)(0) = \boxed{1}$
- $(f \circ g)(-1) = \boxed{1}$
- $\bullet \ (f \circ f)(2) = \boxed{16}$
- $(g \circ f)(-3) = \boxed{19}$
- $(f \circ g) \left(\frac{1}{2}\right) = \boxed{4}$
- $(f \circ f)(-2) = \boxed{16}$

**Exercise** 2  $f(x) = |x - 1|, g(x) = x^2 - 5$ 

- $(g \circ f)(0) = \boxed{-4}$
- $\bullet \ (f \circ g)(-1) = \boxed{5}$
- $\bullet \ (f \circ f)(2) = \boxed{0}$
- $(g \circ f)(-3) = \boxed{11}$
- $(f \circ g) \left(\frac{1}{2}\right) = \boxed{\frac{23}{4}}$
- $\bullet \ (f \circ f)(-2) = \boxed{2}$

**Exercise** 3  $f(x) = \sqrt{3-x}, g(x) = x^2 + 1$ 

- $(g \circ f)(0) = \boxed{4}$
- $\bullet \ (f \circ g)(-1) = \boxed{1}$
- $(f \circ f)(2) = \boxed{\sqrt{2}}$
- $(g \circ f)(-3) = \boxed{7}$
- Acknowledgements: Stitz Zeager Open Source Mathematics (https://www.stitz-zeager.com/)

$$\bullet \ (f \circ g) \left(\frac{1}{2}\right) = \boxed{\frac{\sqrt{7}}{2}}$$

$$\bullet \ (f \circ f)(-2) = \boxed{\sqrt{3 - \sqrt{5}}}$$

**Exercise** 4  $f(x) = \sqrt[3]{x+1}, g(x) = 4x^2 - x$ 

• 
$$(g \circ f)(0) = \boxed{3}$$

• 
$$(f \circ g)(-1) = 6^{1/3}$$

• 
$$(f \circ f)(2) = (3^{1/3} + 1)^{1/3}$$

• 
$$(g \circ f)(-3) = \boxed{4(4^{1/3}) + 2^{1/3}}$$

$$\bullet \ (f \circ g) \left(\frac{1}{2}\right) = \boxed{\frac{12^{1/3}}{2}}$$

• 
$$(f \circ f)(-2) = \boxed{0}$$

**Exercise** 5  $f(x) = \frac{3}{1-x}, g(x) = \frac{4x}{x^2+1}$ 

• 
$$(g \circ f)(0) = \boxed{\frac{6}{5}}$$

• 
$$(f \circ g)(-1) = \boxed{1}$$

• 
$$(f \circ f)(2) = \boxed{\frac{3}{4}}$$

$$\bullet \ (g \circ f)(-3) = \boxed{\frac{48}{25}}$$

• 
$$(f \circ g) \left(\frac{1}{2}\right) = \boxed{-5}$$

2

• 
$$(f \circ f)(-2) = \boxed{undefined}$$