

Finding Zeros of Polynomials

Introduction

This section covers a technique for factoring polynomials like $x^3 + 3x^2 + 2x + 6$, which factors as $(x^2 + 2)(x + 3)$. If there are four terms, the technique in this section might help you to factor the polynomial.

Recall that to factor $3x+6$, we factor out the common factor 3: $3x + 6 = \overset{\downarrow}{3}x + \overset{\downarrow}{3} \cdot 2 = 3(x + 2)$

The “3” here could have been something more abstract, and it still would be

valid to factor it out: $x(a + b) + 2(a + b) = \overset{\downarrow}{x(a + b)} + \overset{\downarrow}{2(a + b)}$ In this last example, we factored out the binomial factor $(a + b)$. Factoring out binomials is the essence of this section, so let’s see that a few more times:

$$\begin{aligned} x(x + 2) + 3(x + 2) &= \overset{\downarrow}{x(x + 2)} + \overset{\downarrow}{3(x + 2)} \\ &= (x + 2)(x + 3) \end{aligned}$$

$$\begin{aligned} z^2(2y + 5) + 3(2y + 5) &= \overset{\downarrow}{z^2(2y + 5)} + \overset{\downarrow}{3(2y + 5)} \\ &= (2y + 5)(z^2 + 3) \end{aligned}$$

And even with an expression like $Q^2(Q - 3) + Q - 3$, if we re-write it in the right way using a 1 and some parentheses, then it too can be factored:

$$\begin{aligned} Q^2(Q - 3) + Q - 3 &= Q^2(Q - 3) + 1(Q - 3) \\ &= \overset{\downarrow}{Q^2(Q - 3)} + \overset{\downarrow}{1(Q - 3)} \\ &= (Q - 3)(Q^2 + 1) \end{aligned}$$

The truth is you are unlikely to come upon an expression like $x(x+2)+3(x+2)$, as in these examples. Why wouldn’t someone have multiplied that out already? Or factored it all the way? So far in this section, we have only been looking at a stepping stone to a real factoring technique called **factoring by grouping**.

Learning outcomes:
Author(s):

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