

Exercise 1 (a) The average rate of change of the sine function on the interval $\left[0, \frac{\pi}{2}\right]$ is $AV_{\left[0, \frac{\pi}{2}\right]} = \boxed{\frac{2}{\pi}}$.

(b) The average rate of change of the sine function on the interval $\left[0, \frac{5\pi}{2}\right]$ is

$$AV_{\left[0, \frac{5\pi}{2}\right]} = \boxed{\frac{2}{5\pi}}.$$

(c) The average rate of change of the sine function on the interval $\left[\frac{\pi}{2}, \pi\right]$ is

$$AV_{\left[\frac{\pi}{2}, \pi\right]} = \boxed{-\frac{2}{\pi}}.$$

(d) The average rate of change of the sine function on the interval $\left[\frac{\pi}{2}, \frac{5\pi}{2}\right]$ is

$$AV_{\left[\frac{\pi}{2}, \frac{5\pi}{2}\right]} = \boxed{0}.$$

(e) Select all intervals on which the sine function is increasing.

Select All Correct Answers:

(i) $\left(\frac{\pi}{2}, \pi\right)$

(ii) $\left(0, \frac{\pi}{2}\right)$ ✓

(iii) $(0, \pi)$

(iv) $\left(-\frac{\pi}{2}, \frac{\pi}{2}\right)$ ✓

(v) $\left(0, \frac{5\pi}{2}\right)$