

# 9. Multi Layer Perceptron

Course: Introduction to AI

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Teaching Assistant(s): Raghav Awasty & Subhrajit Roy

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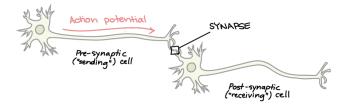


#### Genesis of neural networks

- Mathematical model of a Neuron
  - Understanding the mechanics of a single neuron
- Building of a perceptron
- Single to Multi-layer perceptrons



#### Neuron - A physical model<sup>1</sup>



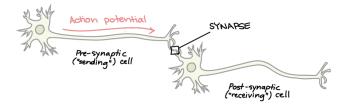
The simplest functional unit in the human brain that,

- Fires at a certain pattern of values at its input
- Passes this information to its neighbours

Image courtesy of Khan Academy



#### Neuron - A physical model<sup>1</sup>



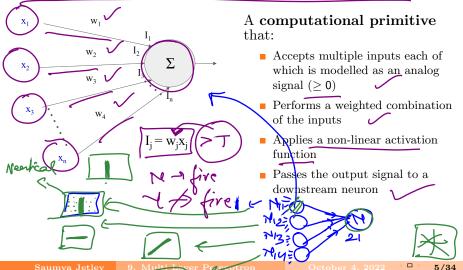
#### Hubel and Weisel (1962)

- Early neurons in the visual cortex fire at simpler patterns
- Later neurons in the visual cortex fire at more complex patterns

Image courtesy of Khan Academy

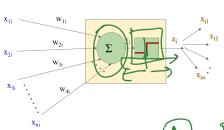


#### Neuron - A mathematical model (McCulloch-Pitts Neuron)









#### Parameters of this model?

$$\mathbf{x}_{i}^{\mathsf{T}} = [x_{1i}, x_{2i}, x_{3i}, \dots x_{ni}]$$
 $\mathbf{w}_{i}^{\mathsf{T}} = [w_{1i}, w_{2i}, w_{3i}, \dots W_{ni}]^{\mathsf{T}}$ 

- $y_i = \mathbf{w}_i^T \mathbf{x}_i$
- $z_i = max(y_i, 0)$







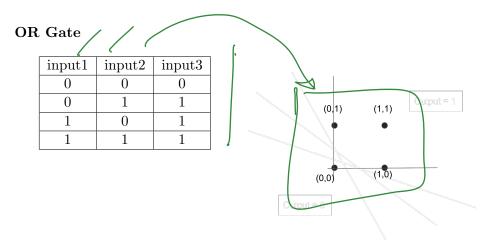
#### Genesis of neural networks

- Mathematical model of a Neuron
- Building of a perceptron
  - Building a network of neurons one input layer and one output layer
- Single to Multi-layer perceptrons

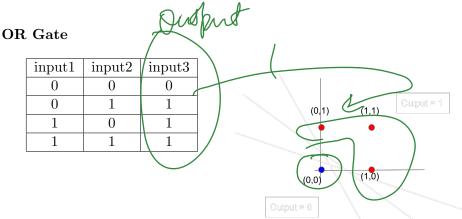


- **Aim**: To use the network of neurons to perform mathematical operations
- Context:
  - Early computers (and modern too) are based on binary logic
  - Are neural networks able to implement logical operations?
- Todo:
  - Implement elementary logic gates AND, OR and NOT
  - Any gate can be implemented using the 3 gates above





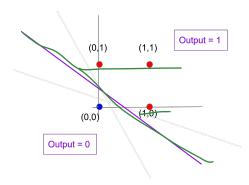






#### **OR** Gate

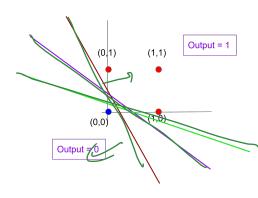
input1	input2	input3
0	0	0
0	1	1
1	0	1
1	1	1



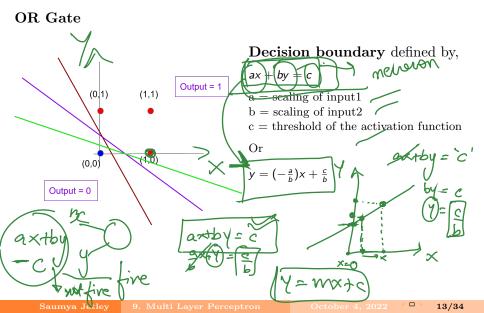


#### **OR** Gate

input1	input2	input3
0	0	0
0	1	1
1	0	1
1	1	1

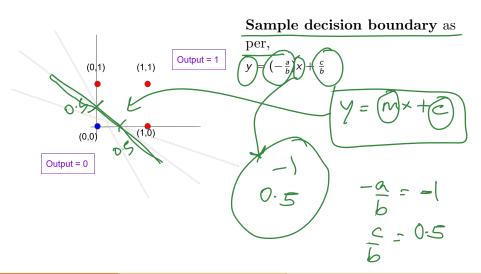






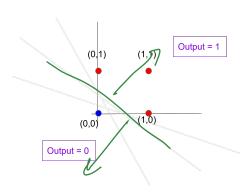


#### **OR** Gate





#### OR Gate



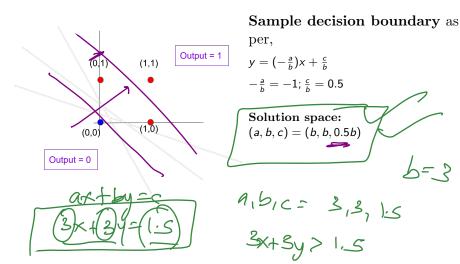
# Sample decision boundary as per,

$$y = \left(-\frac{a}{b}\right)x + \frac{c}{b}$$
$$-\frac{a}{b} = -1; \frac{c}{b} = 0.5$$

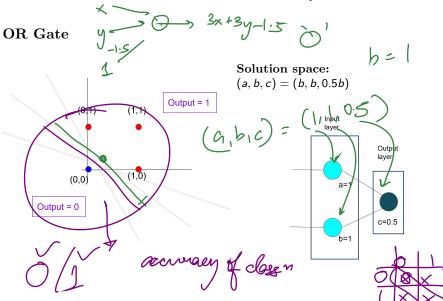




#### **OR** Gate

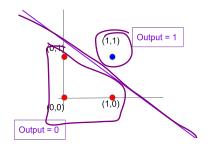




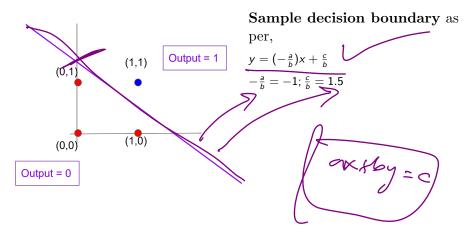




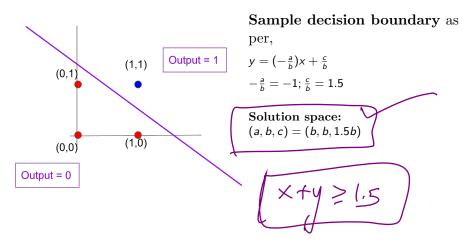
input1	input2	input3
0	0	0
0	1	0
1	0	0
1	1	1



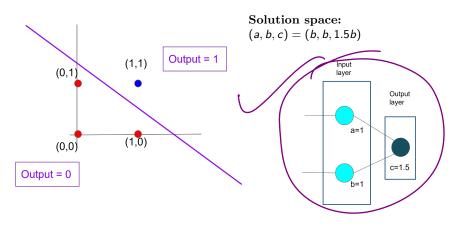










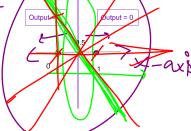




#### NOT Gate

input1	input2
0	1
1	0





Sample decision boundary as per,

$$y = \left(-\frac{a}{b}\right)x + \frac{c}{b}$$

$$-\frac{a}{b} = -1; \frac{c}{b} = 0.5$$



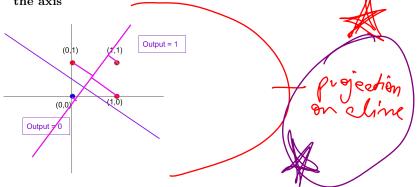
$$(a, b, c) \neq (b, b, 0.5b)$$





Task of learning the model is equivalent to:

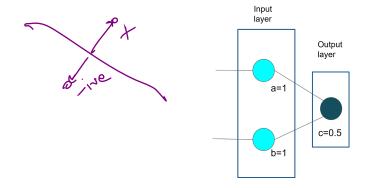
- (a) Finding the weights on the incoming lines Axis of projection
- (b) Finding the appropriate threshold for a linear separation Threshold along the axis





Task of learning the model is equivalent to:

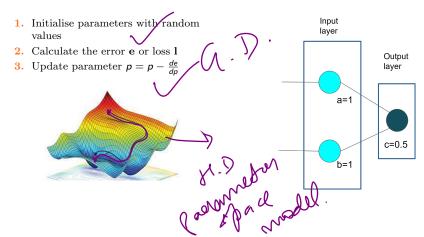
- (a) Finding the weights on the incoming lines
- (b) Finding the appropriate threshold for a linear separation





Task of learning the model is equivalent to:

- (a) Finding the weights on the incoming lines
- (b) Finding the appropriate threshold for a linear separation



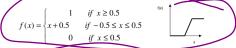


 ${\it Loss function description:} \ {\bf Map \ to \ Categorical \ distribution} + {\it Measure \ loss}$ 

1. Step function - Non-continuous and Non-differentiable

		f(x)
$f(x) = \begin{cases} 1 \\ 0 \end{cases}$	if $x \ge 0$	<u></u>
$\int f(x) = \int 0$	if $x < 0$	L, )

2. Piecewise linear - Continuous and Non-differentiable



3. Signoid - Continuous and differentiable



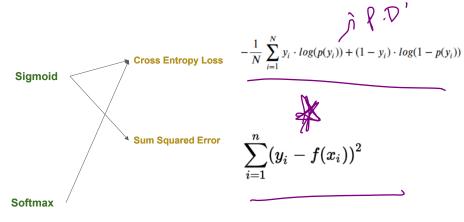




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Loss function description: Map to Categorical distribution + Measure loss

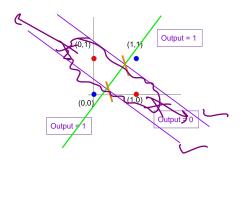




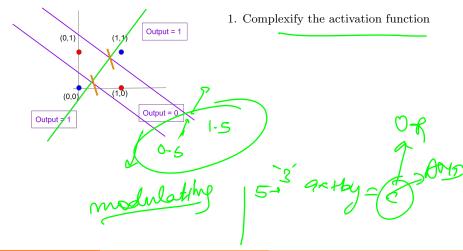
#### **XOR** Gate

i	nput1	input2	input3
	0	0	0
	0	1	1
	1	0	1
	1	1	0

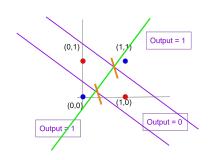




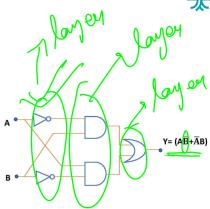








1. Complexify the activation function



2. Complexify the mapping/projection

### Single to Multi-layer perceptrons

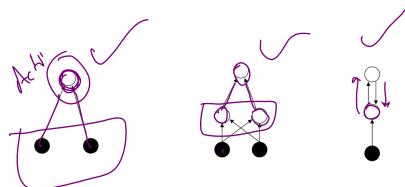


#### Genesis of neural networks

- Mathematical model of a Neuron
- Building of a perceptron
- Single to Multi-layer perceptrons
  - Limitations of single layer network and introduction of hidden layers
  - Complexify the mapping/projection
  - More general than adapting number of threshold to unknown settings

# Single to Multi-layer perceptrons





**Figure:** Left: Single layer perceptron; Middle: Multi layer perceptron; Right: Recurrent/ feedback perceptron

#### Overview



- 1 Genesis of neural networks
  - Mathematical model of a Neuron
  - Building of a perceptron
  - Single to Multi-layer perceptrons

motivated from

#### Attendance



