BAN 673-03 Time Series Analytics

Forecasting CVS Health Stock Price

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Summary

This is a project on Time Series Analysis and Forecasting to predict CVS Health^[1] stock^[3] using R Studio^[2]. All the steps of the Time series forecasting methods were followed starting from data selection and exploring, visualizing the series, evaluating predictability, pre-processing of data which was not required, partitioning of time series, followed by generating some forecasting model, comparing the results of these models and then implementing the best model to forecast the future data, and then the conclusions.

The methods used for forecasting / model generation were:

- 1. Naive and Seasonal Naive
- 2. Moving Average Trailing (with 6 different window widths as follows: 2, 4, 6, 8, 12)
- 3. Advanced Exponential Smoothing using Holt-Winters method
- 4. Regression models with (a) Linear Trend, (b) Quadratic Trend, (c) Seasonality, (d) Linear Trend and Seasonality, and (e) Quadratic Trend and Seasonality
- 5. Auto ARIMA.

From all the models that we developed, the best model we can use for prediction is the Regression model with Linear Trend and seasonality which has 10.261 as RMSE (Root Mean Square Error) and 11.134 as MAPE (Mean Absolute Percentage Error).

Introduction

The CVS Health stock data for four years was taken. CVS Health Corporation provides health services and plans in the United States. The company was formerly known as CVS Caremark Corporation and changed its name to CVS Health Corporation in September 2014. The company was founded in 1963 and is headquartered in Woonsocket, Rhode Island.

The stock price was \$1.59 in February of 1973. On December 1st of 2020, the stock price is \$67.54.

Everyday's closing price of CVS Health stock from January of 2016 through December of 2019 is taken from the website here: https://finance.yahoo.com/quote/CVS/history

In this project, I used the R Studio, a programming language to perform a time series analysis for CVS Health stock analysis. The aim is to find a good model that could be used to forecast the future values. I have used many modeling techniques for this project which will be discussed further in the paper.

Main Chapter

This is a project on time series analysis and forecasting. The steps followed were: data selection & exploring, visualizing the series, evaluating predictability, pre-processing of data, partitioning of time series, followed by generating numerous forecasting model, comparing the results of these models and then implementing the best model(s) for forecasting of data for future, and then the conclusions.

Step 1: Define goal

The goal of this project is to predict the CVS stock price. The resulting forecasts will be used to monitor CVS stock price. The forecasting models developed for this project were done via the R language.

Step 2: Get data

Everyday's closing price of CVS Health stock from January of 2016 through December of 2019 is taken from the website here: https://finance.yahoo.com/quote/CVS/history

The data had other factors too, but the relevant column was taken, saved as a csv file (CVS.csv) used as input for this analysis and forecasting.

Here is how the data looks:

```
> CVS.ts
       Jan
             Feb
                                May
                                      Jun
                                            Jul
                                                   Aug
                                                         Sep
                                                               0ct
                                                                      Nov
                   Mar
                          Apr
2016 96.59 97.17 103.73 100.50 96.45 95.74 92.72 93.40 88.99 84.10 76.89 78.91
2017 78.81 80.58 78.50 82.44 76.83 80.46 79.93 77.34 81.32 68.53 76.60 72.50
2018 78.69 67.73 62.21 69.83 63.39 64.35 64.86 75.24 78.72 72.39 80.20 65.52
2019 65.55 57.83 53.93 54.38 52.37 54.49 55.87 60.92 63.07 66.39 75.27 74.29
```

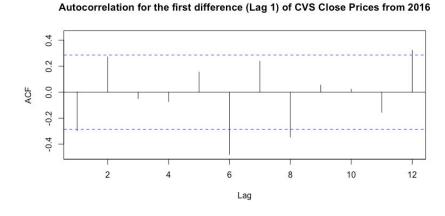
Step 3: Explore & visualize series

Firstly, let us see if the data is predictable or not. From the summary, it is seen that the ar1 value is 0.91 that is kind of close to 1. Which basically means that it might not be a random walk and the future is predictable. But, the data we are taking is stock data. So, this is common for data like this.

```
Series: CVS.ts
ARIMA(1,0,0) with non-zero mean
Coefficients:
         ar1
                mean
      0.9145
             78.4552
     0.0544
              7.7661
sigma^2 estimated as 30.76: log likelihood=-150.22
AIC=306.45 AICc=306.99
                         BIC=312.06
                    ME
                           RMSE
                                     MAE
                                               MPE
                                                       MAPE
                                                                 MASE
Training set -0.5703872 5.429707 4.230032 -1.272559 5.841641 0.3775972 -0.2549232
```

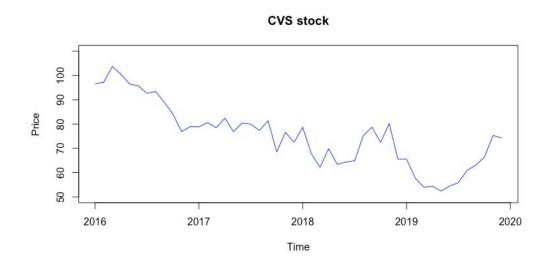
The model's equation is: $e_t = 78.45 + 0.91 e_{t-1}$

The coefficient of the ar1 (Y_{t-1}) variable, 0.91, is below 1. Therefore, the data time series might be likely to be predictable and might not be a random walk. Let's analyse further.

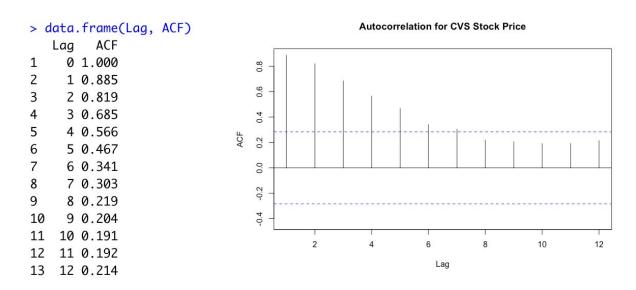


By the above chart, we can say that the data is not a random walk and the future is predictable. We see a strong negative autocorrelation at lag 6 saying that it has a half yearly seasonality.

The time series data plotted below is the CVS stock data from 2016 to 2019 which appear to have a downward trend.

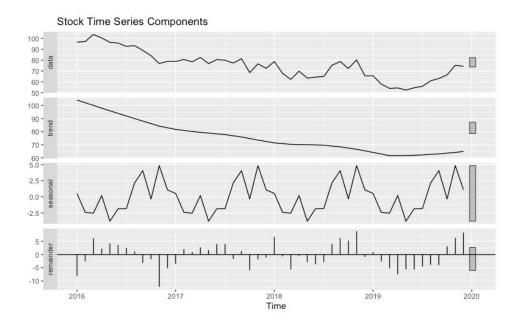


From the below auto-correlation chart and table, we see that the data is highly correlated, as the autocorrelation coefficients in all the lags are substantially higher than the horizontal threshold (significantly greater than zero).



We can also say that the auto-correlation is very high with a lag of 1 and it decreases respectively for the further lags. From this, we can visualize, it has a strong trend relationship.

Here is a plot of the time-series components which shows the trend, seasonality and noise.



The above plot shows the data has a downward trend.

Step 4: Data pre-processing

We need not do any pre-processing for this data.

Step 5: Partition series

The data was partitioned to train data and validation data.

Train data has 3 years of the data. From 2016 to 2018. It is shown as below.

```
> train.ts
        Jan
                                                   Jul
                                                                  Sep
                                                                                Nov
                                                                                        Dec
               Feb
                      Mar
                              Apr
                                     May
                                            Jun
                                                          Aug
                                                                         0ct
2016
     96.59
             97.17 103.73 100.50
                                   96.45
                                          95.74
                                                 92.72
                                                        93.40
                                                                88.99
                                                                       84.10
                                                                              76.89
                                                                                     78.91
2017
                                   76.83
      78.81
                   78.50
                           82.44
                                          80.46
                                                 79.93
                                                         77.34
                                                                81.32
                                                                       68.53
                                                                              76.60 72.50
             80.58
2018
      78.69
             67.73
                    62.21
                           69.83
                                   63.39
                                          64.35
                                                 64.86
                                                        75.24
                                                                78.72
                                                                       72.39
                                                                              80.20 65.52
```

Validation data has the year 2019. It is shown as below.

Step 6: Apply forecasting Methods

1. Naive Forecasting

This shows the RMSE value of 8.685 and MAPE of 12.95

2. Seasonal Naive Forecasting

This shows the RMSE value of 11.048 and MAPE of 17.656.

3. Moving Average

```
> round(accuracy(ma.trail_2, CVS.ts), 3) #Best
            ME RMSE
                     MAE
                              MPE MAPE
                                         ACF1 Theil's U
Test set -0.236 2.775 2.185 -0.427 3.021 -0.298
> round(accuracy(ma.trail_4, CVS.ts), 3)
            ME RMSE
                       MAE
                             MPE MAPE ACF1 Theil's U
Test set -0.901 4.648 3.695 -1.431 5.264 0.446
                                                 0.853
> round(accuracy(ma.trail_5, CVS.ts), 3)
            ME RMSE
                       MAE
                              MPE MAPE ACF1 Theil's U
Test set -1.297 5.567 4.485 -2.059 6.446 0.553
                                                 1.027
> round(accuracy(ma.trail_6, CVS.ts), 3)
            ME RMSE
                      MAE
                             MPE MAPE ACF1 Theil's U
Test set -1.658 6.34 5.282 -2.667 7.646 0.638
                                                1.172
> round(accuracy(ma.trail_8, CVS.ts), 3)
            ME RMSE
                       MAE
                             MPE MAPE ACF1 Theil's U
Test set -2.454 7.626 6.448 -4.013 9.464 0.678
                                                 1.396
> round(accuracy(ma.trail_12, CVS.ts), 3)
                       MAE MPE MAPE ACF1 Theil's U
            ME RMSE
Test set -3.829 8.322 7.187 -6.29 10.766 0.602
                                                 1.483
```

Trailing Moving Averages were generated using rollmean() function with window widths of 2, 4, 5, 6, 8, and 12. The lowest values of MAPE and RMSE are for the window width of 2. The RMSE is 2.775 and MAPE is 3.021. This is the best till now.

4. Advanced Exponential Smoothing (Holt-Winters Model)

Holt-Winters Model was used with ets() function and model = "ZZZ" to get the optimum model selected by the system for error trend and seasonality. The model is as shown below with Additive error, no trend and no seasonality (A,N,N).

The alpha value is 0.62. It indicates the level component of the model.

Here is the accuracy measure for the Holt-Winters Model.

This is the accuracy of this model. It has RMSE of 11.713 and MAPE of 18.358.

5. Regression based models

Below are the summaries for the regression models developed later we will compare and get the better results.

i. Regression model with linear trend

```
Call:
tslm(formula = train.ts ~ trend)
Residuals:
              1Q Median
                                30
                                       Max
    Min
-10.2645 -4.5973 0.2326
                            4.0628 14.8648
Coefficients:
           Estimate Std. Error t value Pr(>|t|)
                       2.08042 46.418 < 2e-16 ***
(Intercept) 96.56967
trend
           -0.89241
                       0.09805 -9.101 1.23e-10 ***
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Residual standard error: 6.112 on 34 degrees of freedom
Multiple R-squared: 0.709,
                               Adjusted R-squared: 0.7004
F-statistic: 82.83 on 1 and 34 DF, p-value: 1.229e-10
```

The Regression model with linear trend has an Adjusted R-squared value of 0.7 which says that the model accounts for 70% of the variations.

Also, the p-value is less than 0.01. So, it is statistically significant.

This regression model with linear trend has only one variable, period index (t).

$$Y_t = 95.57 - 0.89 (t)$$

ii. Regression model with quadratic trend

Call:

tslm(formula = train.ts ~ trend + I(trend^2))

Residuals:

Min 1Q Median 3Q Max -8.9846 -3.9857 0.6107 3.8200 8.9677

Coefficients:

Residual standard error: 5.042 on 33 degrees of freedom Multiple R-squared: 0.8077, Adjusted R-squared: 0.7961 F-statistic: 69.32 on 2 and 33 DF, p-value: 1.529e-12

The Regression model with linear trend has an Adjusted R-squared value of approximately 0.796 which says that the model accounts for 79.6% of the variations.

The p-value of this regression model indicates that it is statistically insignificant because it is <0.01 This regression model with linear trend has two independent variables, period index (t), and squared period index squared (t^2).

$$Y_t = 104.98 - 2.22 (t) - 0.03 (t^2)$$

iii. Regression model with seasonality

Call:

tslm(formula = train.ts ~ season)

Residuals:

Coefficients:

	Estimate	Std. Error	t value	Pr(>ltl)	
(Intercept)	84.697	7.375	11.484	3.09e-11	***
season2	-2.870	10.430	-0.275	0.786	
season3	-3.217	10.430	-0.308	0.760	
season4	-0.440	10.430	-0.042	0.967	
season5	-5.807	10.430	-0.557	0.583	
season6	-4.513	10.430	-0.433	0.669	
season7	-5.527	10.430	-0.530	0.601	
season8	-2.703	10.430	-0.259	0.798	
season9	-1.687	10.430	-0.162	0.873	
season10	-9.690	10.430	-0.929	0.362	
season11	-6.800	10.430	-0.652	0.521	
season12	-12.387	10.430	-1.188	0.247	

Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' '1

Residual standard error: 12.77 on 24 degrees of freedom Multiple R-squared: 0.1025, Adjusted R-squared: -0.3088 F-statistic: 0.2493 on 11 and 24 DF, p-value: 0.9899

The Regression model with seasonality has an Adjusted R-squared value of -0.3. And the p-value is 0.98 (greater than 0.05) which states the model is statistically insignificant.

This regression model with seasonality contains 11 seasonal variables season2 (D_2), season3 (D_3), and so on upto season12 (D_{12})

$$Yt = 84.697 - 2.87 (D_2) - 3.217 (D_3) - 0.44 (D_4) + \dots - 6.8 (D_{11}) - 12.387 (D_{12})$$

iv. Regression model with linear trend and seasonality

```
Call:
tslm(formula = train.ts ~ trend + season)
Residuals:
   Min
             1Q Median
                             3Q
                                    Max
-11.926 -3.710 -1.272
                          4.230 13.223
Coefficients:
            Estimate Std. Error t value Pr(>|t|)
(Intercept) 96.52576
                        4.18744 23.051 < 2e-16 ***
trend
            -0.90993
                        0.11521 -7.898 5.34e-08 ***
                        5.53137 -0.354
season2
            -1.96007
                                           0.726
season3
            -1.39680
                        5.53497 -0.252
                                           0.803
             2.28979
                        5.54096
                                  0.413
                                           0.683
season4
            -2.16694
                        5.54934 -0.390
                                           0.700
season5
                        5.56010
season6
            0.03632
                                  0.007
                                           0.995
            -0.06708
                        5.57321 -0.012
                                           0.991
season7
season8
             3.66618
                        5.58867
                                  0.656
                                           0.518
            5.59278
                        5.60646
                                  0.998
                                           0.329
season9
            -1.50063
                        5.62654 -0.267
season10
                                           0.792
             2.29930
                        5.64891
                                  0.407
season11
                                           0.688
            -2.37743
season12
                        5.67353 -0.419
                                           0.679
                0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Signif. codes:
Residual standard error: 6.773 on 23 degrees of freedom
Multiple R-squared: 0.7582,
                                Adjusted R-squared: 0.6321
F-statistic: 6.011 on 12 and 23 DF, p-value: 0.0001209
```

The Regression model with seasonality has an Adjusted R-squared value of 0.63. And the p-value is 0.00012, which states the model is statistically significant.

This regression model with seasonality contains 11 seasonal variables season2 (D_2), season3 (D_3), and so on upto season12 (D_{12})

$$Yt = 96.525 - 0.909 (t) - 1.96 (D_2) - 1.396 (D_3) - \dots - 2.377 (D_{12})$$

v. Regression model with quadratic trend and seasonality.

```
Call:
tslm(formula = train.ts \sim trend + I(trend^2) + season)
Residuals:
   Min
            10 Median
                            3Q
                                   Max
-9.6919 -2.6551 0.8163 2.4547 8.0400
Coefficients:
             Estimate Std. Error t value Pr(>|t|)
(Intercept) 104.567904
                        3.767849 27.753 < 2e-16 ***
trend
            -2.287520
                        0.346657 -6.599 1.23e-06 ***
I(trend^2)
             0.037232
                        0.009058
                                 4.110 0.000461 ***
                        4.254464 -0.373 0.712575
season2
            -1.587746
                        4.259389 -0.171 0.866102
            -0.726625
season3
                        4.266417 0.746 0.463479
             3.183366
season4
                        4.274848 -0.263 0.794970
season5
            -1.124444
             1.153283
                        4.284213 0.269 0.790289
season6
                        4.294278
season7
             1.049883
                                  0.244 0.809122
             4.708680
                        4.305037
                                  1.094 0.285892
season8
             6.486350
                        4.316714
                                  1.503 0.147158
season9
season10
            -0.830447
                        4.329755 -0.192 0.849658
             2.671626
                        4.344828 0.615 0.544930
season11
season12
            -2.377429
                        4.362816 -0.545 0.591284
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
Residual standard error: 5.208 on 22 degrees of freedom
Multiple R-squared: 0.8632,
                               Adjusted R-squared:
F-statistic: 10.68 on 13 and 22 DF, p-value: 1.118e-06
```

The Regression model with seasonality has an Adjusted R-squared value of 0.78. And the p-value is less than 0.01, which states the model is statistically significant.

This regression model with seasonality contains 11 seasonal variables season2 (D_2), season3 (D_3), and so on upto season12 (D_{12})

$$Yt = 104.56 - 2.287 (t) - 0.037 (t^2) - 1.587 (D_2) - 0.726 (D_3) - \dots - 2.377 (D_{12})$$

Comparing all these regression models

```
> round(accuracy(train.lin.pred, CVS.ts), 3) #best2
                     RMSE
                                  MPE
                                        MAPE MASE ACF1 Theil's U
               ME
                           MAE
Training set 0.000 5.939 4.789 -0.557 6.178 0.415 0.521
                                                                NA
Test set
             2.555 10.164 8.170 2.422 12.747 0.708 0.761
                                                             2.331
> round(accuracy(train.quad.pred, CVS.ts), 3)
                ME
                      RMSE
                              MAE
                                     MPE
                                           MAPE MASE ACF1 Theil's U
Training set
               0.00 4.828 4.151 -0.416 5.404 0.360 0.224
                                                                   NA
             -14.67 15.746 14.670 -25.352 25.352 1.271 0.598
Test set
                                                                4.204
> round(accuracy(train.season.pred, CVS.ts), 3)
                 ME
                       RMSE
                              MAE
                                      MPE
                                            MAPE MASE ACF1 Theil's U
Training set
               0.000 10.430 8.278 -1.681 10.421 0.717 0.859
Test set
             -18.863 21.266 19.193 -33.020 33.464 1.663 0.704
                                                                 5.526
> round(accuracy(train.linear.trend.season.pred, CVS.ts),3) #Best1
               ME
                     RMSE
                           MAE
                                  MPE
                                        MAPE MASE ACF1 Theil's U
Training set 0.000 5.414 4.391 -0.444 5.604 0.380 0.637
                                                                NA
Test set
             2.975 10.261 7.293 3.178 11.134 0.632 0.704
                                                             2.294
> round(accuracy(train.trend.season.pred, CVS.ts),3)
                       RMSE
                                      MPE
                                            MAPE MASE ACF1 Theil's U
                 ME
                              MAE
Training set
               0.000 4.072 3.320 -0.295 4.314 0.288 0.337
                                                                    NA
            -14.896 16.224 14.896 -25.690 25.690 1.291 0.574
Test set
                                                                 4.351
```

From the above table, we can see that the RMSE and MAPE values of the regression model with linear trend and seasonality have the lowest values as 10.261 and 11.134.

The next best is the regression model with linear trend with RMSE value of 10.164 and MAPE of 12.747.

6. Auto - ARIMA

Auto-ARIMA model is the model which is used to identify optimal ARIMA model and its perspective p, d, q parameters which indicate level, trend and seasonality.

Here is the summary for the Auto-Arima model

Series: train.ts ARIMA(1,1,0)

Coefficients:

ar1

-0.4604 s.e. 0.1633

sigma^2 estimated as 29.67: log likelihood=-108.6 AIC=221.21 AICc=221.58 BIC=224.32

Training set error measures:

ME RMSE MAE MPE MAPE MASE ACF1
Training set -1.071767 5.293736 4.084865 -1.63162 5.406063 0.3539489 -0.01388919

The equation for this can be given as below:

$$Y_{t} - Y_{t-1} = -0.46 (Y_{t-1} - Y_{t-2})$$

> round(accuracy(train.auto.arima.pred, valid.ts), 3)

ME RMSE MAE MPE MAPE MASE ACF1 Theil's U Training set -1.072 5.294 4.085 -1.632 5.406 0.354 -0.014 NA Test set -9.073 11.740 10.617 -16.450 18.513 0.920 0.727 3.136

This the accuracy values of the auto - ARIMA. The RMSE is 11.740 and MAPE value is 18.513.

Step 7: Evaluate & compare performance

Below are the accuracy measures of the two best models. Regression model with linear trend, and Regression model with linear trend and seasonality

```
> round(accuracy(train.lin.pred$mean, CVS.ts), 3)
            ME
                 RMSE
                       MAE
                             MPE
                                   MAPE
                                         ACF1 Theil's U
Test set 2.555 10.164 8.17 2.422 12.747 0.761
                                                   2.331
> round(accuracy(train.linear.trend.season.pred$mean, CVS.ts),3)
                                    MAPE ACF1 Theil's U
            ME
                 RMSE
                        MAE
                              MPE
Test set 2.975 10.261 7.293 3.178 11.134 0.704
                                                    2.294
```

From these compared accuracies, we can say that both are really close in values. But, we can see that the Regression model with linear trend and seasonality has slightly lower values of the ME, MAE, ACF1 and Theil's U. So, we choose the next best one as a regression model with linear trend and seasonality. It has the RMSE value of 10.261 and MAPE of 11.134.

Step 8: Implement forecast system

We have used a Regression model with linear trend and seasonality to implement the forecast.

```
Point Forecast
                            Lo 0
                                     Hi 0
                                             Lo 95
                                                      Hi 95
Jan 2020
               54.84333 54.84333 54.84333 37.18766 72.49901
Feb 2020
               50.76084 50.76084 50.76084 33.10516 68.41651
               49.52583 49.52583 49.52583 31.87016 67.18151
Mar 2020
Apr 2020
               51.72084 51.72084 51.72084 34.06516 69.37651
               47.19333 47.19333 47.19333 29.53766 64.84901
May 2020
               48.69333 48.69333 48.69333 31.03766 66.34901
Jun 2020
Jul 2020
               48.27833 48.27833 48.27833 30.62266 65.93401
Aug 2020
               51.65833 51.65833 51.65833 34.00266 69.31401
               52.95833 52.95833 52.95833 35.30266 70.61401
Sep 2020
               47.78583 47.78583 47.78583 30.13016 65.44151
Oct 2020
Nov 2020
               52.17333 52.17333 52.17333 34.51765 69.82901
               47.73833 47.73833 47.73833 30.08266 65.39401
Dec 2020
```

From the result above, we can see the prediction for the CVS Health of the year 2020.

Conclusion

This project on time series analysis and forecasting on CVS Health stocks can be predicted best using the regression model with linear trend and seasonality. The model has the RMSE value of 10.261 and MAPE of 11.134.

Although the moving average and naive models have better RMSE and MAPE values, we do not get the right prediction values for this data. Not everything can be forecast reliably, if the factors that relate to what is being forecast are known and well understood and there is a significant amount of data that can be used, very reliable forecasts can often be obtained. If this is not the case or if the actual outcome is affected by the forecasts, the reliability of the forecasts can be significantly lower. And so, we had to choose the regression model with the linear trend model.

This project was a great learning opportunity to me because I have learnt a lot by the challenges I have faced in accomplishing the goals and overcoming the challenges and understanding the subject.

Bibliography

[1] CVS Health is the name of the company that was referred in this document.

More details can be seen here: https://en.wikipedia.org/wiki/CVS Health

[2] R Studio is the programming language mainly used for statistical analysis.

More details are here: https://en.wikipedia.org/wiki/RStudio

[3] Stock is the price of a share.

More can be known here: https://en.wikipedia.org/wiki/Stock

Appendices

PPT's and other study material provided in the Time Series course by **Dr. Zinovy Radivosky** at California State University, East Bay.

2. Data from the wikipedia website to know about CVS.

Link given here: https://en.wikipedia.org/wiki/CVS_Health

3. Data used from Yahoo website to do the analysis.

Link provided here: https://finance.yahoo.com/quote/CVS/