

# XOR FROM LEFT TO RIGHT

★ In this problem, we are given 2 numbers  $L$  and  $R$ , and our job is to find the XOR of all numbers from  $L \rightarrow R$ .

Brute force solution is to obviously iterate through  $L \rightarrow R$  and calculate entire XOR.

In case  $L = 1$ , Optimal Solution comes from a pattern. Every fourth XOR is 1.

$N = 1$	XOR = 1
2	3
3	0
4	4
5	1
6	7
7	0
8	8
9	1

```
∴ if (N % 4 == 0) return N
   if (N % 4 == 1) return 1
   if (N % 4 == 2) return N + 1
   if (N % 4 == 3) return 0
```

But if  $L \neq 1$ , then we use the above algorithm for  $1 \rightarrow L$  and then for  $L \rightarrow R$ . Then we just XOR both of these.

Eg :  $L = 4$

$R = 7$

$$(\cancel{1} \wedge \cancel{2} \wedge \cancel{3}) \wedge (\cancel{1} \wedge \cancel{2} \wedge \cancel{3} \wedge 4 \wedge 5 \wedge 6 \wedge 7) \\ = (4 \wedge 5 \wedge 6 \wedge 7)$$

```
xorRange(N) {  
    if (N % 4 == 0) return N  
    if (N % 4 == 1) return 1  
    if (N % 4 == 2) return N + 1  
    if (N % 4 == 3) return 0  
}
```

```
xorRangeLeftToRight(L, R) {  
    return xorRange(L - 1) ^ xorRange(R)  
}
```