Lecture 3: Tautologies

Math 345

Monday, September 27, 2010

Jim Fowler

Textbook

This lecture discusses section 2 of the textbook.

Homework

The homework is due Wednesday, September 29, 2010. From Section 2 of the textbook, do exercises 14, 15, and 17.

Modus Ponens

If P holds and $P \Rightarrow Q$ holds, then Q holds.

Examples

$$\begin{split} P &\Rightarrow (P \lor Q) \\ &(P \land Q) \Rightarrow P \\ &(P \land Q) \Rightarrow Q \\ &(P \land Q) \Rightarrow (P \lor Q) \\ &((P \lor Q) \land ((P \Rightarrow R) \land (Q \to R))) \Rightarrow Q. \\ &((P \Rightarrow Q) \land (Q \Rightarrow R)) \Rightarrow (P \Rightarrow R) \end{split}$$

Reinforcement

Converse

Contrapositive

Examples

Distributive law homework

Have someone come up and write out the proof of the distributive law

$$P \wedge (Q \vee R) \equiv (P \wedge Q) \vee (P \wedge R)$$