

Lecture 4: Lines and planes

Math 195 Section 91

Monday June 29, 2009

Section 13.5, and 14.1 and 14.2.

parametric equation for line: $v = tw + u$. parametric equation for line segment.

1 Lines

find line through two points

check if two lines intersect

skew lines versus parallel lines.

2 Planes

point on plane, and vector normal to the plane

equation: $n \cdot (v - w) = 0$ for w on the plane and n normal.

write as scalar equation by substituting in coordinates

find normal vector by taking cross product

two planes are parallel if their normals are parallel

find angle between two planes

find distance from point to a plane

3 Calculus

vector-valued function—in coordinates, a parametric equation!

take limits componentwise

sketch curve: $(\cos t, \sin t, t)$.

4 Derivatives

define derivative

take derivatives componentwise

find unit tangent vector

second derivative (on circle!)

how to differentiate: dot products, cross products. it is the leibniz rule again!

5 Integrating vectors

Indeed we can do it.