

Lecture 13: Integrals and coordinate systems

Math 195 Section 91

Monday July 20, 2009

1 spherical coordinates (16.8)

$$x = \rho \sin \varphi \cos \theta, \ y = \rho \sin \varphi \sin \theta, \ z = \rho \cos \varphi.$$
$$dV = \rho^2 \sin \varphi d\rho d\varphi d\theta.$$

2 chain of variables (16.9)

examples: cylindrical, spherical, polar coordinates

“transformations” and images, injective (1 to 1), bijective, etc.

assume the “transformations” to be C^1 .

inverse transformations

Jacobian matrix

triple integrals (three-by-three determinants)