

# Some interesting sequences.

| $a_1 = 2.0$<br>$a_{n+1} = a_n/2 + 1/a_n$ | $b_1 = 0.3$<br>$b_{n+1} = b_n (1 - b_n)$ | $c_1 = 0.3$<br>$c_{n+1} = 3.5 c_n (1 - c_n)$ | $d_1 = 27$<br>$d_{n+1} = \begin{cases} d_n/2 & \text{if } d_n \text{ even,} \\ 3 d_n + 1 & \text{if } d_n \text{ odd.} \end{cases}$ |
|--|--|--|---|
| $a_1 = 2.000000000000$                   | $b_1 = 0.300000000000$                   | $c_1 = 0.300000000000$                       | $d_1 = 27$  |
| $a_2 = 1.500000000000$                   | $b_2 = 0.210000000000$                   | $c_2 = 0.735000000000$                       | $d_2 = 82$  |
| $a_3 = 1.416666666667$                   | $b_3 = 0.165900000000$                   | $c_3 = 0.681712500000$                       | $d_3 = 41$  |
| $a_4 = 1.414215686275$                   | $b_4 = 0.138377190000$                   | $c_4 = 0.759431985703$                       | $d_4 = 124$   |
| $a_5 = 1.414213562375$                   | $b_5 = 0.119228943288$                   | $c_5 = 0.639432656779$                       | $d_5 = 62$  |
| $a_6 = 1.414213562373$                   | $b_6 = 0.105013402370$                   | $c_6 = 0.806954869782$                       | $d_6 = 31$  |
| $a_7 = 1.414213562373$                   | $b_7 = 0.093985587693$                   | $c_7 = 0.545225477710$                       | $d_7 = 94$  |
| $a_8 = 1.414213562373$                   | $b_8 = 0.085152296999$                   | $c_8 = 0.867841296581$                       | $d_8 = 47$  |
| $a_9 = 1.414213562373$                   | $b_9 = 0.077901383315$                   | $c_9 = 0.401424731854$                       | $d_9 = 142$   |
| $a_{10} = 1.414213562373$                | $b_{10} = 0.071832757792$                | $c_{10} = 0.840990207785$                    | $d_{10} = 71$   |
| $a_{11} = 1.414213562373$                | $b_{11} = 0.066672812700$                | $c_{11} = 0.468039873681$                    | $d_{11} = 214$  |
| $a_{12} = 1.414213562373$                | $b_{12} = 0.062227548747$                | $c_{12} = 0.871424926140$                    | $d_{12} = 107$  |
| $a_{13} = 1.414213562373$                | $b_{13} = 0.058355280924$                | $c_{13} = 0.392152334847$                    | $d_{13} = 322$  |
| $a_{14} = 1.414213562373$                | $b_{14} = 0.054949942112$                | $c_{14} = 0.834291083924$                    | $d_{14} = 161$  |
| $a_{15} = 1.414213562373$                | $b_{15} = 0.051930445974$                | $c_{15} = 0.483873149232$                    | $d_{15} = 484$  |
| $a_{16} = 1.414213562373$                | $b_{16} = 0.049233674755$                | $c_{16} = 0.874089736395$                    | $d_{16} = 242$  |
| $a_{17} = 1.414213562373$                | $b_{17} = 0.046809720025$                | $c_{17} = 0.385199041933$                    | $d_{17} = 121$  |
| $a_{18} = 1.414213562373$                | $b_{18} = 0.044618570136$                | $c_{18} = 0.828872590095$                    | $d_{18} = 364$  |
| $a_{19} = 1.414213562373$                | $b_{19} = 0.042627753335$                | $c_{19} = 0.496449868196$                    | $d_{19} = 182$  |
| $a_{20} = 1.414213562373$                | $b_{20} = 0.040810627981$                | $c_{20} = 0.874955887975$                    | $d_{20} = 91$   |
| $a_{21} = 1.414213562373$                | $b_{21} = 0.039145120625$                | $c_{21} = 0.382928287256$                    | $d_{21} = 274$  |
| $a_{22} = 1.414213562373$                | $b_{22} = 0.037612780156$                | $c_{22} = 0.827029749263$                    | $d_{22} = 137$  |
| $a_{23} = 1.414213562373$                | $b_{23} = 0.036198058925$                | $c_{23} = 0.500680400839$                    | $d_{23} = 412$  |
| $a_{24} = 1.414213562373$                | $b_{24} = 0.034887759455$                | $c_{24} = 0.874998379691$                    | $d_{24} = 206$  |
| $a_{25} = 1.414213562373$                | $b_{25} = 0.033670603695$                | $c_{25} = 0.382816753301$                    | $d_{25} = 103$  |
| $a_{26} = 1.414213562373$                | $b_{26} = 0.032536894142$                | $c_{26} = 0.826938303426$                    | $\vdots$  |
| $a_{27} = 1.414213562373$                | $b_{27} = 0.031478244662$                | $c_{27} = 0.500889710136$                    | $d_{65} = 1619$   |
| $a_{28} = 1.414213562373$                | $b_{28} = 0.030487364775$                | $c_{28} = 0.874997229456$                    | $d_{66} = 4858$   |
| $a_{29} = 1.414213562373$                | $b_{29} = 0.029557885364$                | $c_{29} = 0.382819772652$                    | $d_{67} = 2429$   |
| $a_{30} = 1.414213562373$                | $b_{30} = 0.028684216777$                | $c_{30} = 0.826940780116$                    | $d_{68} = 7288$   |
| $a_{31} = 1.414213562373$                | $b_{31} = 0.027861432484$                | $c_{31} = 0.500884042041$                    | $d_{69} = 3644$   |
| $a_{32} = 1.414213562373$                | $b_{32} = 0.027085173064$                | $c_{32} = 0.874997264644$                    | $d_{70} = 1822$   |
| $a_{33} = 1.414213562373$                | $b_{33} = 0.026351566464$                | $c_{33} = 0.382819680284$                    | $\vdots$  |
| $a_{34} = 1.414213562373$                | $b_{34} = 0.025657161409$                | $c_{34} = 0.826940704349$                    | $d_{106} = 10$  |
| $a_{35} = 1.414213562373$                | $b_{35} = 0.024998871478$                | $c_{35} = 0.500884215439$                    | $d_{107} = 5$   |
| $a_{36} = 1.414213562373$                | $b_{36} = 0.024373927903$                | $c_{36} = 0.874997263571$                    | $d_{108} = 16$  |
| $a_{37} = 1.414213562373$                | $b_{37} = 0.023779839541$                | $c_{37} = 0.382819683101$                    | $d_{109} = 8$   |
| $a_{38} = 1.414213562373$                | $b_{38} = 0.023214358773$                | $c_{38} = 0.826940706660$                    | $d_{110} = 4$   |
| $a_{39} = 1.414213562373$                | $b_{39} = 0.022675452319$                | $c_{39} = 0.500884210151$                    | $d_{111} = 2$   |
| $a_{40} = 1.414213562373$                | $b_{40} = 0.022161276181$                | $c_{40} = 0.874997263603$                    | $d_{112} = 1$   |