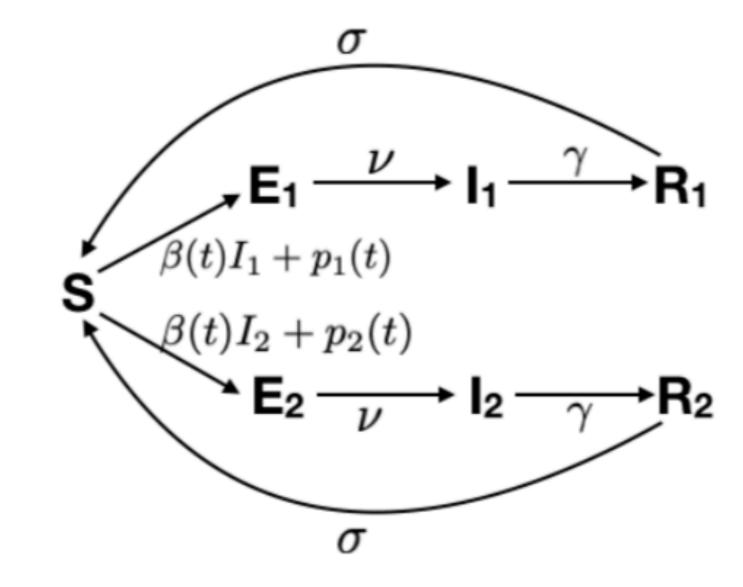
## **Early models**

Two strains with waning immunity



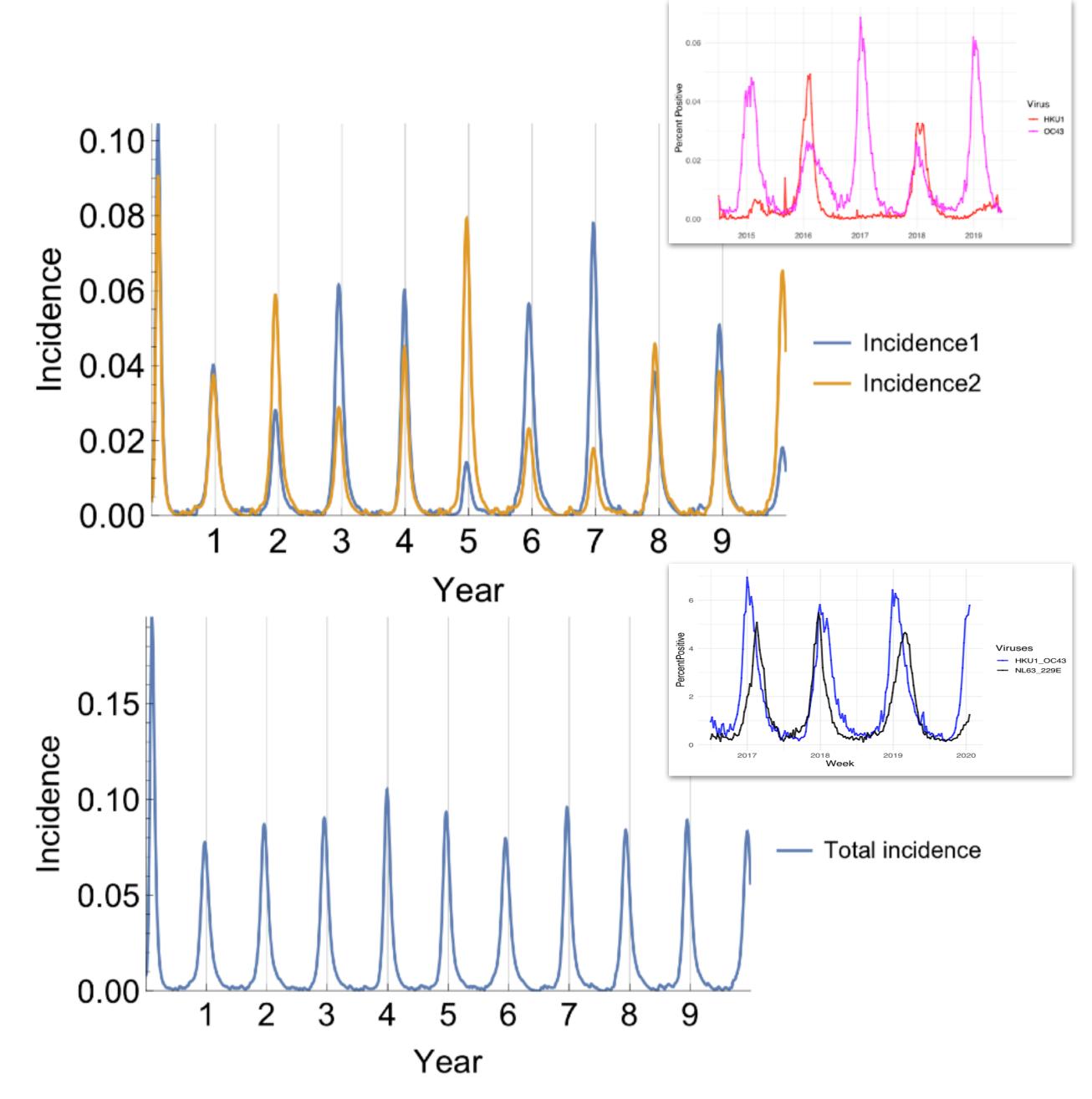
 $\beta(t)$ : seasonal (cosine with 1-year period) forcing

 $p_i(t)$ : pulses of imported infectiousness from strain i

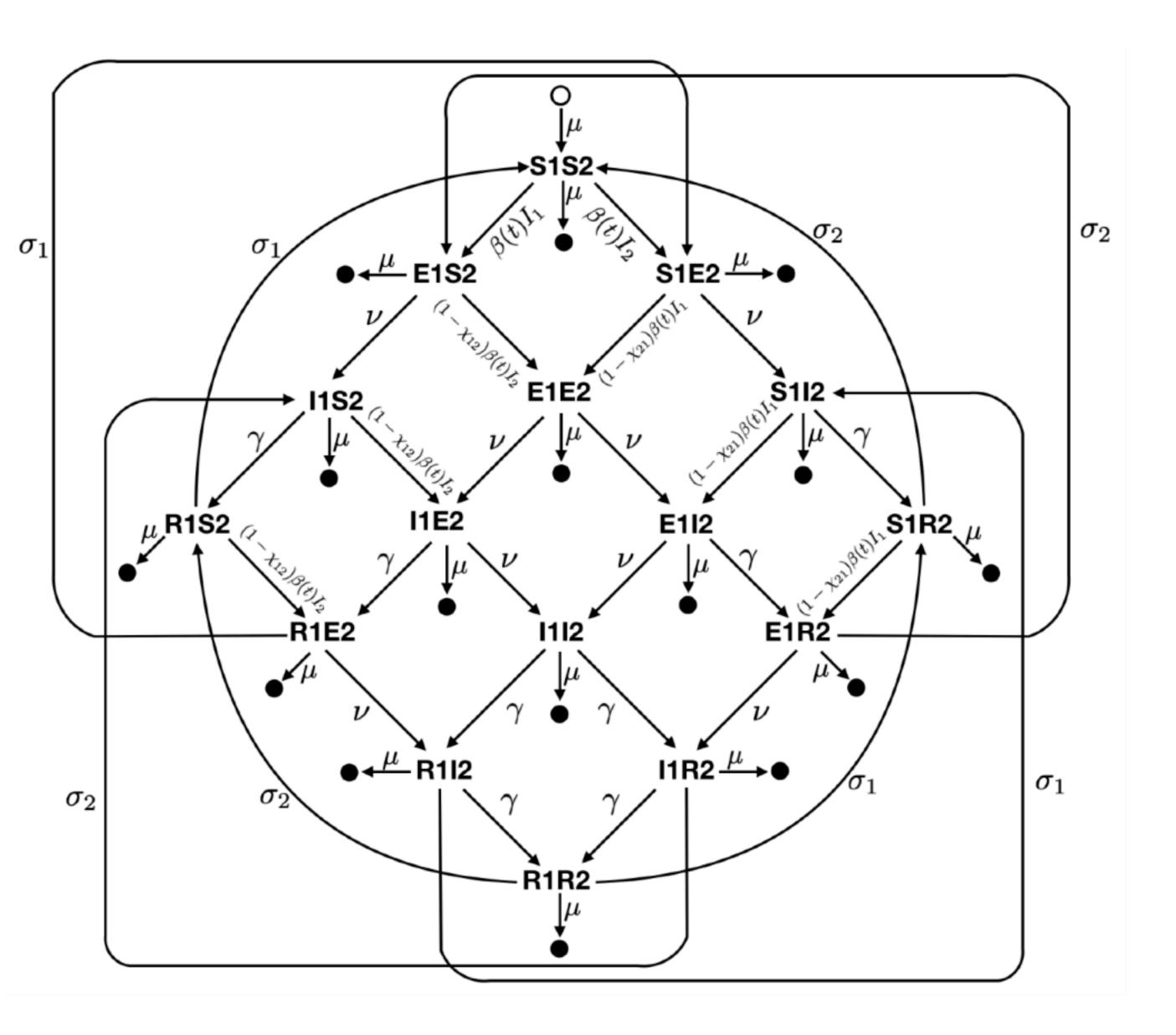
 $\nu$ : Rate of progression to infectiousness ( $\frac{1}{\nu} = 1$  week)

 $\gamma$ : Rate of recovery ( $\frac{1}{\gamma} = 1$  week)

 $\sigma$ : Rate of waning immunity ( $\frac{1}{\sigma} = 35$  weeks)



## The full model



## Includes:

- Waning immunity ( $\sigma$ )
- Partial cross-immunity (χ)
- Seasonality  $(\beta(t))$