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DATA STRUCTURE MINI PROJECT

AIM

To implement a C++ program that assigns colors to the vertices of a graph such that no two adjacent vertices have the same color, using a backtracking algorithm.

ALGORITHM

Step 1:

Start the program.

Step 2:

Represent the graph using an adjacency matrix, where $\text{graph}[i][j] = 1$ means there is an edge between vertex i and vertex j , and 0 means no edge.

Step 3:

Decide how many colors (m) you want to use for coloring the graph.

Step 4:

Start coloring from the first vertex (vertex 0).

Step 5:

For each vertex:

- Try assigning each color (from 1 to m).
- Before assigning, check if it's safe (i.e., none of its adjacent vertices have the same color).

Step 6:

If it's safe, assign that color to the vertex and move to the next vertex.

Step 7:

If the next vertex cannot be colored (no color fits), then backtrack —remove the color from the current vertex and try a different color.

Step 8:

If all vertices are successfully colored, print the color of each vertex.

Step 9:

If no color combination works, print “No solution exists.”

Step 10:

Stop the program.

CODE

```
#include <iostream>
#include <vector>
using namespace std;
```

```

bool isSafe(int v, const vector<vector<int>>& graph, const
vector<int>& color, int c) {
    for (int i = 0; i < graph.size(); i++) {
        if (graph[v][i] && color[i] == c)
            return false;
    }
    return true;
}

```

```

bool graphColoringUtil(const vector<vector<int>>& graph, int m,
vector<int>& color, int v) {
    int n = graph.size();
    if (v == n)
        return true;
    for (int c = 1; c <= m; c++) {
        if (isSafe(v, graph, color, c)) {
            color[v] = c;
            if (graphColoringUtil(graph, m, color, v + 1))
                return true;
            color[v] = 0;
        }
    }
    return false;
}

```

```

bool graphColoring(const vector<vector<int>>& graph, int m) {

```

```

int n = graph.size();
vector<int> color(n, 0);
if (!graphColoringUtil(graph, m, color, 0)) {
    cout << "No solution exists.\n";
    return false;
}

cout << "Solution exists: Following are the assigned
colors:\n";
for (int i = 0; i < n; i++)
    cout << "Vertex " << i << " ---> Color " << color[i] << endl;

return true;
}

```

```

int main() {
    vector<vector<int>> graph = {
        {0, 1, 1, 1},
        {1, 0, 1, 0},
        {1, 1, 0, 1},
        {1, 0, 1, 0}
    };

```

```

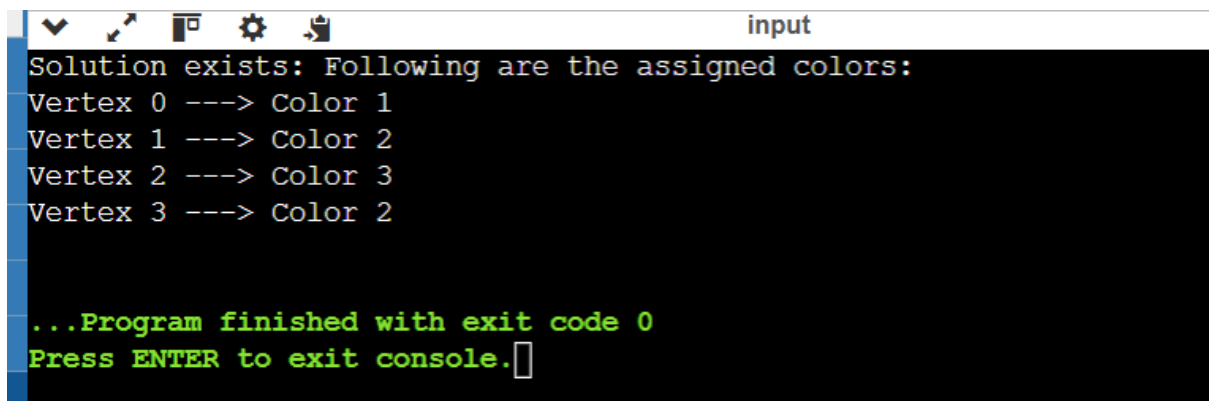
int m = 3;

```

```
graphColoring(graph, m);

return 0;
}
```

OUTPUT:

A screenshot of a terminal window with a dark background. The title bar at the top shows standard window controls and the text 'input'. The terminal output is as follows:

```
Solution exists: Following are the assigned colors:
Vertex 0 ---> Color 1
Vertex 1 ---> Color 2
Vertex 2 ---> Color 3
Vertex 3 ---> Color 2

...Program finished with exit code 0
Press ENTER to exit console.
```

CONCLUSION

The program successfully assigns colors to all vertices of a graph so that no two adjacent vertices have the same color. It demonstrates how **backtracking** can be used to solve combinatorial optimization problems efficiently.