

Real-Time Piano Accompaniment Using Kuramoto Model for Human-Like Synchronization

Kit Armstrong, Ji-Xuan Huang, Tzu-Ching Hung,
Jing-Heng Huang & Yi-Wen Liu

Context

(“Western classical music”)

Composer – Performer – Listener

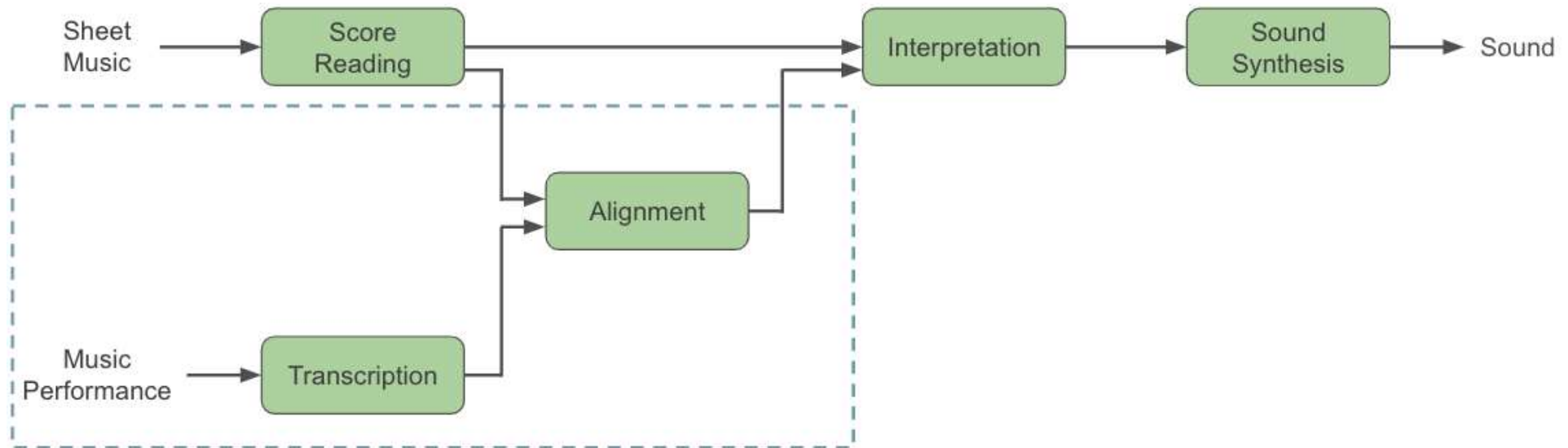
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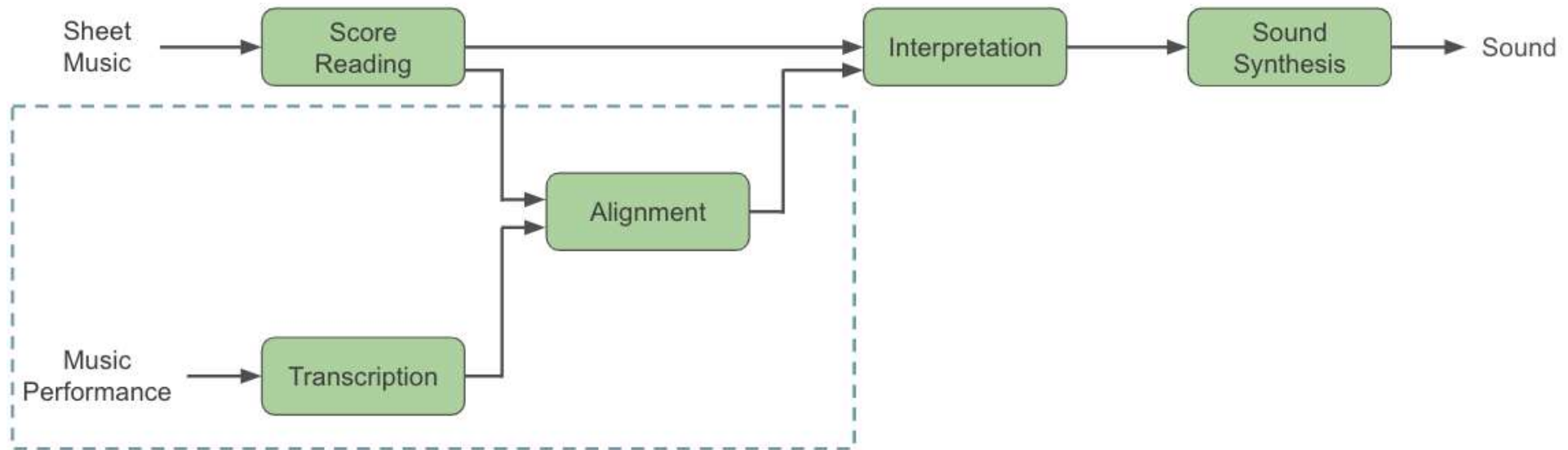
Composer – Performer – Listener

Create an AI performer

Context



Context



Score reading: sheet music → a machine-friendly representation

Transcription: musical performance → a machine-friendly representation

Score following: musical performance + score → score-aligned performance

Interpretation: score + score-aligned performance → MIDI or similar

Sound synthesis: interpretation → sound

Focus: Interpretation

Prevalence:

- Music-notation programs like Finale, Sibelius, MuseScore, etc.
- Useful tool for composers
- Not suitable for performance

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Levels of advancement:

- Basic, in essence MusicXML to MIDI
- Algorithmic expressiveness
- Ongoing attempts with machine learning

Focus: Interpretation

Challenges:

- Deformation for natural performance

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Focus: Interpretation

Challenges:

- Deformation for natural performance
- Understanding score indications
- Synchronization in an ensemble

Model

Scope:

- Digital piano
- 1 person (“input”) + AI “accompaniment”
- Precisely defined score

Goal:

- Human-like time synchronization

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Collaboration more than synchronization

Model

Human-like time synchronization

Intuition:

“I'm early” → Slow down

“I'm late” → Speed up

Model

Human-like time synchronization

Introduce the concept of **score position**



Model

Human-like time synchronization

A performance is a function: time \rightarrow score position

$$f(t) = 2\pi * (\text{beat number reached at time } t)$$

Model

Human-like time synchronization

A performance is a function: time \rightarrow score position

$$f(t) = 2\pi * (\text{beat number reached at time } t)$$

{input timings}, {input score positions} determine f

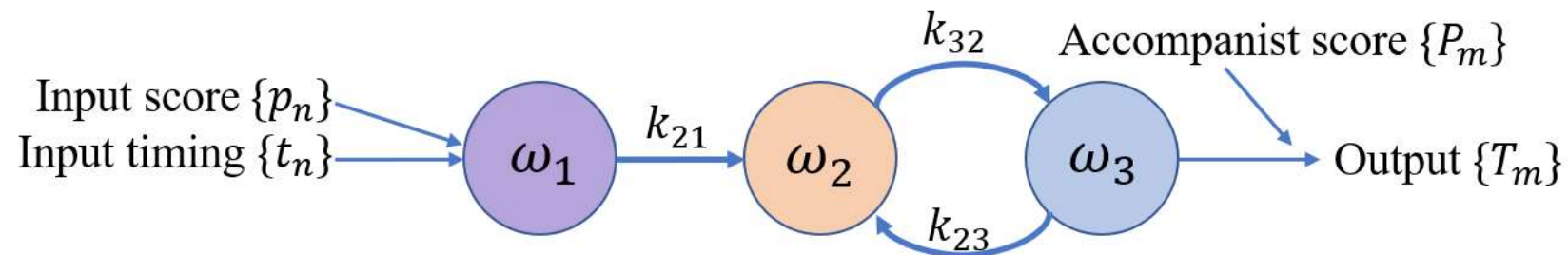
Input is one such function,
accompaniment is another function

Model

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$$\frac{d\theta_i(t)}{dt} = \sum_{j \neq i} k_{ij} \sin(\theta_j(t) - \theta_i(t)) + \Omega_i(t)$$

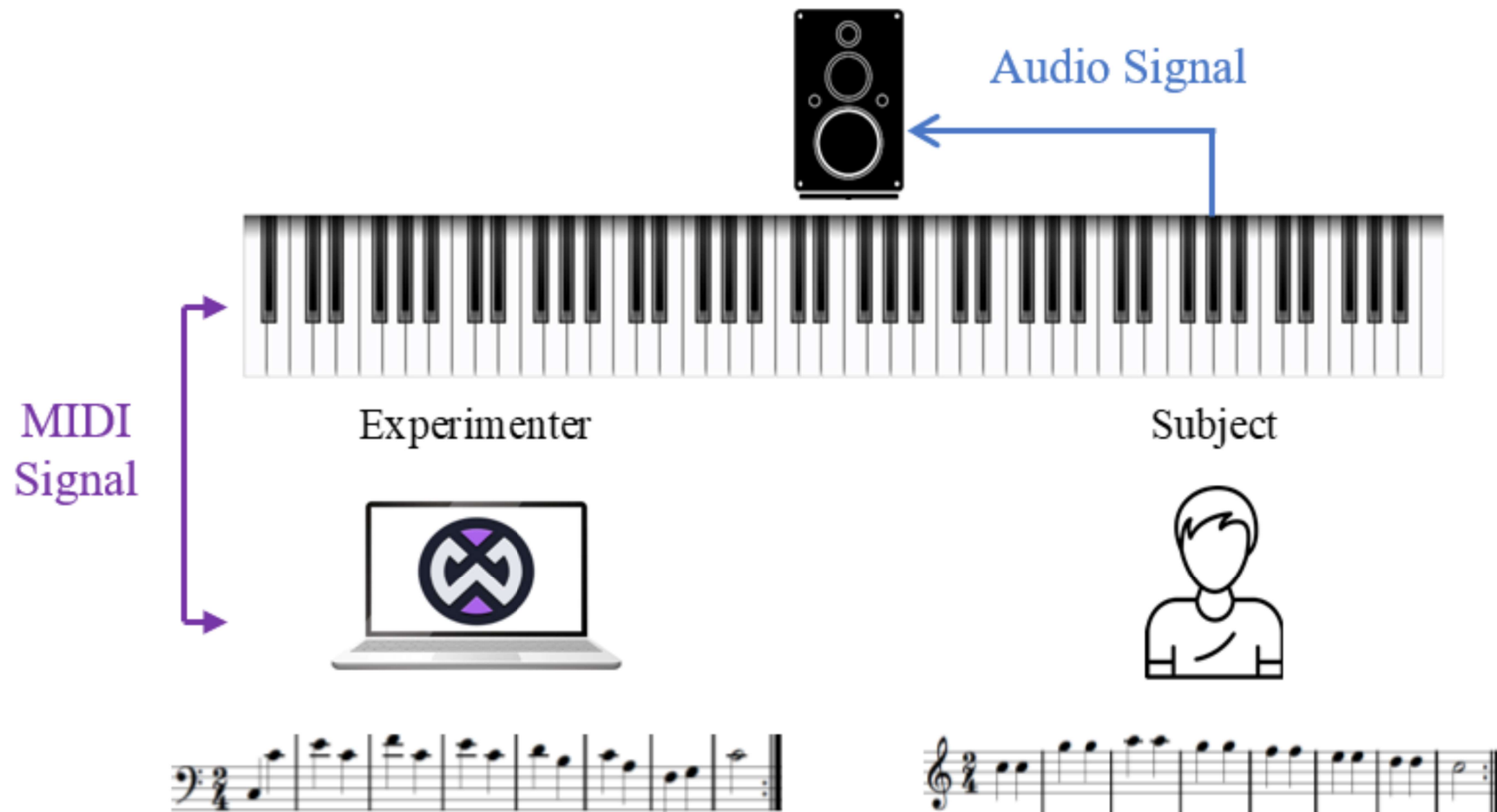
Model

Predictive nature:

- extrapolate ω_3 to predict next outputs
- additional learned parameter: “reaction time”
- each new input rewrites all future predictions

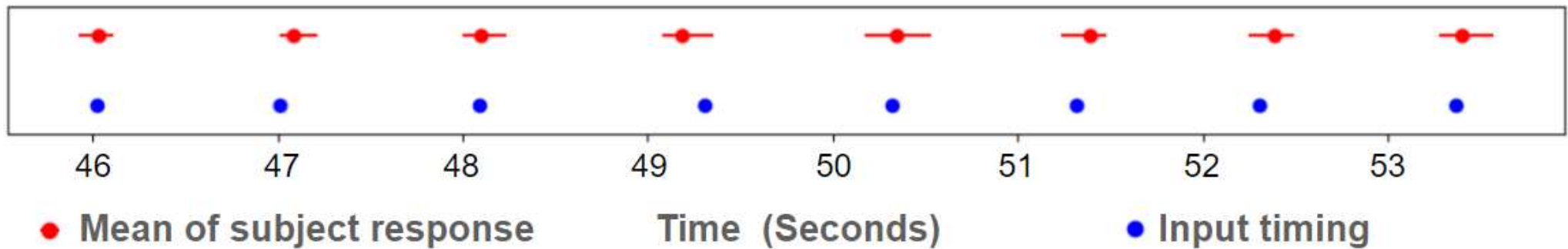
Model training

Capturing human behavior



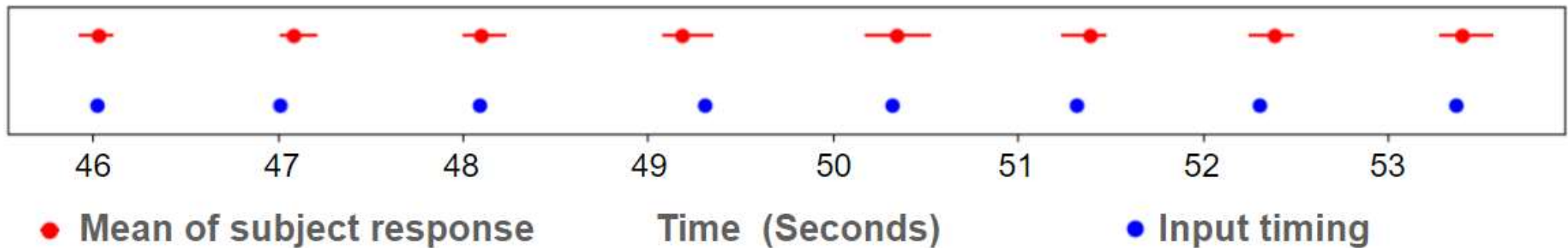
Model training

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Model training

Capturing human behavior



Choose parameters such that
the model performs most similarly

Architecture

- input reading thread

writes all MIDI messages to *Input Queue*

- calculation thread

listens to *Input Queue*,
determines outputs of form (note, velocity, time),
and writes them to *Output Queue*

- output thread

listens to *Output Queue*,
sends MIDI messages at corresponding time

Demonstration

Additional elements:

- Simple velocity matching (running average)
- Basic error-correction

Testing

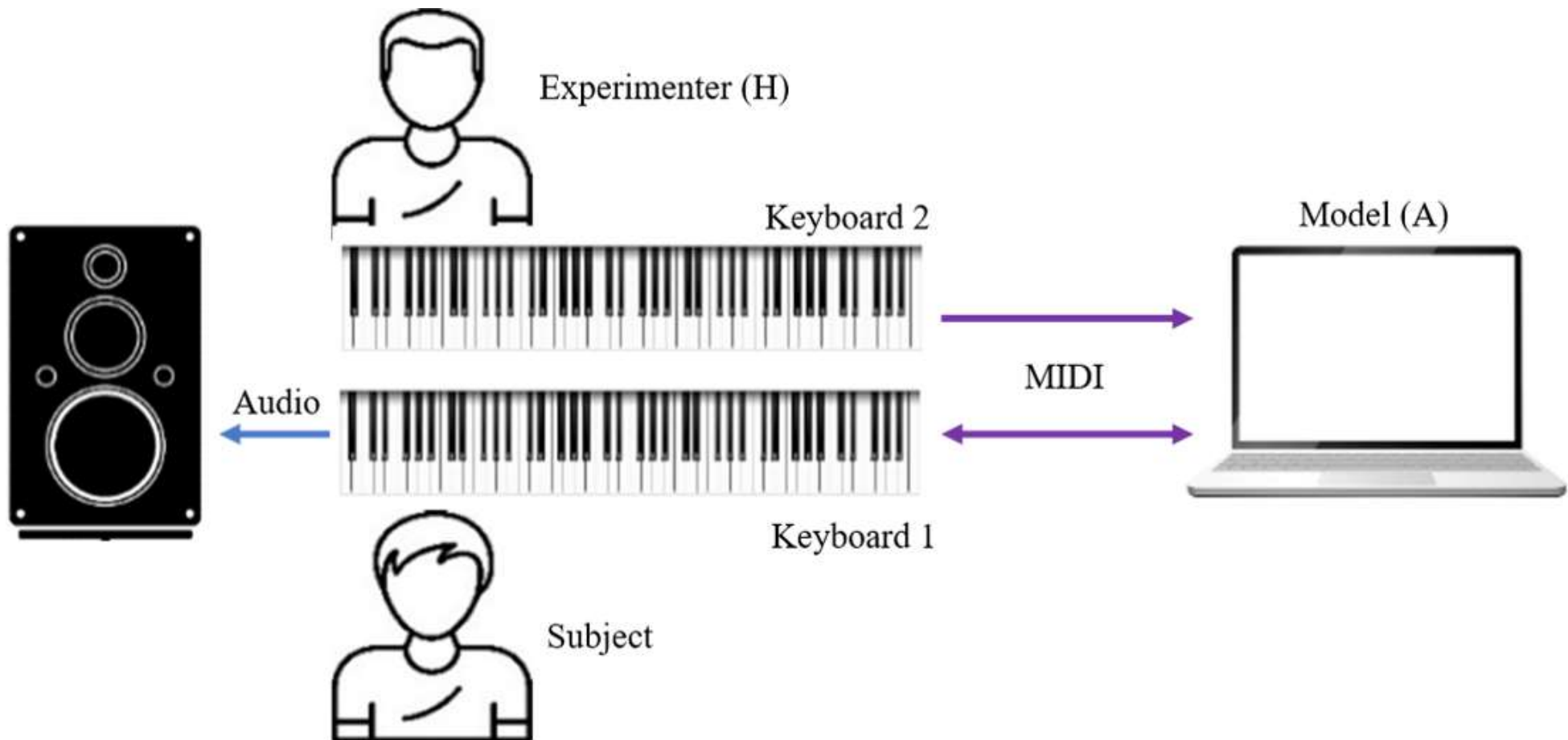
“Turing test”

Can people tell the difference between Human (H) and AI (A)?

Environment:

Create identical setup for H and A

Testing



Testing

- **1.**
W. A. Mozart: *“Twinkle, Twinkle, Little Star”*
K. 265, Theme
- **2.**
W. A. Mozart: *“Twinkle, Twinkle, Little Star”*
K. 265, Variation II
- **3.**
J. S. Bach/C. Gounod:
“Ave Maria, Méditation sur le Prélude de Bach”

Testing

Results:

12 participants, 80 trials

Total: 59% correct guesses

Problems & Limitations

Problem: Output delay

Getting the OS to reliably send a MIDI message at a pre-determined future time

- Misrepresents the model
- Bumpy effect
- Cascading slow-down
- Worse when the output has many notes

Problems & Limitations

Limitations:

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General limitations:

- No intrinsic musicality
- Primitive score reading

Taking stock

- This model is conceptually simple, and its scope is very limited.
- Playing with it is surprisingly satisfying, especially compared to “perfect accompaniment”.
- New trial suggests this may not be thanks to the Kuramoto model, but rather the predictive nature.
- We are devising a new model with larger scope and different internal workings.