

Problem A: Calculator Messages

Given the mappings between some digits and letters, you have to find which words Alex typed on his calculator. You can solve this problem using a dictionary (`std::map` in C++, `Map` in Java and `dict` in Python), a `switch` instruction or a several `if` instructions. Note that since one needs to rotate the calculator in order to read the words, we must process the input digits in reverse order.

Problem B: Winner

Given a sequence of numbers consisting solely of 1s and 2s, you have to find the number which occurs the most.

Problem C: Easy Contest

This problem can be solved with a greedy algorithm. First, we will generate all possible problems, i.e. all combinations of ideas and statements with associated difficulty and store them in an array. Then we will sort the problems in increasing order of difficulty. Finally we will loop over the sorted array and select the N easiest problems. We will need to keep track of already selected ideas and statements since an idea or a statement can be used only once.

Problem D: Largest Number

To get the largest number that can be formed with the given digits, sort the digits in decreasing order.

Problem E: Matrix

Given a square grid G , you have to find k , which is the number of square sub-grids of length x which remains the same after been rotated 90° clockwise. We use matrix notation in the following paragraphs. $g_{r,c}$ represents the element at row r and column c in the grid. And $s_{r,c}$ represents the element at row r and column c in a sub-grid s .

To find k , we need to consider each sub-grid and compare it to its rotation. We can do this in place using a simple trick. Let $g_{i,j}$ be the top-left element of a sub-grid s . $g_{i,j}$ is mapped to $s_{0,0}$ and any other element $g_{p,q}$ that belongs to the sub-grid is mapped to $s_{p-i,q-j}$. Note that it is always possible to get the original coordinates of a sub-grid element $s_{c,d}$ in G since $(p,q) = (c+i, d+i)$.

When a sub-grid is rotated, $s_{i,j}$ moves to the position of $s_{j,x-i-1}$. So for each element $s_{i,j}$ of the sub-grid, we have to find the element $s_{a,b}$ that will be moved to the position of $s_{i,j}$ after the rotation and check if they are equal. It is easy to find a and b since $(i,j) = (b, x-a-1)$. Once the values of a and b are computed, we just have to find the original coordinates of $s_{a,b}$ and $s_{i,j}$ in G and compare them.

Problem F: Sequence

Given a sequence of integers, you have to find which of the following categories it belongs to: **increasing**, **decreasing**, **increasing then decreasing** or **decreasing then increasing**. The simplest way to find the answer is to loop over the sequence and check the relative order of consecutive elements.

Note: This problem can be solved easily in C++ by using STL functions `is_sorted` and `is_sorted_until`.

Problem G: Painting

The judges were very kind and gave the formula to get the neighbors of a cell. The only task left was how to flip the value v of cell when needed. This can be done in several ways.

1. Increase v by 1 each time the cell state changes, and output v modulo 2 at the end.
2. Each time the state of a cell has to change, compute $(v + 1)$ modulo 2.
3. Flip the value of a cell by computing $v \text{ xor } 1$.

Problem H: Conferences Day

This problem can be modeled as a graph theory problem and solved using Kahn's algorithm for topological sort. The challenge left is how to select the next speech so that it will always be the longest that can start. This can be achieved by using a heap instead of a simple FIFO queue to get the next available speech.

Problem I: Bridges and Trees

Another graph theory problem. We have to find all the bridges in a graph and then compute for each bridge the minimum and maximal spanning trees of the connected components created after removing the bridge from the graph. Since bridges are always part of the spanning tree, once we find the min and max spanning trees of the graph, we will have to remove each bridge from the spanning trees and compute the cost of spanning trees of the associated connected components.

Problem J: Minimize Me

The minimum value of S is reached when K is the arithmetic mean of the collection $T_i - i$. In order words,

$$K = \sum_{i=1}^n T_i - i$$

Problem K: Mango

Given a sequence of letters, compute the number of occurrence of each letter and finally sort the sequence.

Problem L: A Little Trick

Given two numbers X and Y , find the maximum of $X + Y$, $X - Y$, $X * Y$ and $Y - X$.

Problem M: New Year and Problems Robbers

We have a grid consisting of several type of cells. Each type of cell has an associated blocking cost. Some cells can't be blocked. We have to find the cheapest set of cells to block so that given a starting cell, it will be impossible to reach an edge of the grid.

To find a solution, we can simulate the strategy of a robber and try to find a way to leave the grid by testing all possible paths. As soon as a cell is reached, we check if the cell can be blocked or not. If the cell can be blocked, we block it and add its cost to a total. If the cell can't be blocked, we have to explore its neighborhood. We continue this process until we reach an edge cell that can't be block or there is no more cell to explore because we find a way to block the robbers. In the first case, we report that it is not possible to stop the robbers. In the second case, we can stop them.