

**LMN**

No.: 150666748

This booklet contains 24 printed pages.

**PAPER - 1 : PHYSICS, MATHEMATICS & CHEMISTRY**

Test Booklet Code

**D**

Do not open this Test Booklet until you are asked to do so.

Read carefully the Instructions on the Back Cover of this Test Booklet.

**Important Instructions :**

1. Immediately fill in the particulars on this page of the Test Booklet with *Blue/Black Ball Point Pen*. *Use of pencil is strictly prohibited.*
2. The Answer Sheet is kept inside this Test Booklet. When you are directed to open the Test Booklet, take out the Answer Sheet and fill in the particulars carefully.
3. The test is of 3 hours duration.
4. The Test Booklet consists of 90 questions. The maximum marks are 360.
5. There are three parts in the question paper A, B, C consisting of Physics, Mathematics and Chemistry having 30 questions in each part of equal weightage. Each question is allotted 4 (four) marks for each correct response.
6. Candidates will be awarded marks as stated above in instruction No. 5 for correct response of each question.  $\frac{1}{4}$  (one fourth) marks will be deducted for indicating incorrect response of each question. No deduction from the total score will be made if no response is indicated for an item in the answer sheet.
7. There is only one correct response for each question. Filling up more than one response in each question will be treated as wrong response and marks for wrong response will be deducted accordingly as per instruction 6 above.
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Name of the Candidate (in Capital letters): SUYASHA SINGHRoll Number : in figures 35809988  
: in words \_\_\_\_\_Examination Centre Number: 358019Name of Examination Centre (in Capital letters): PRABHA SENIOR SECONDARY PUBLIC SCHOOL  
K Block, Sarvodaya NagarCandidate's Signature: Suyasha Singh1. Invigilator's Signature: [Signature]2. Invigilator's Signature: [Signature]

SEAL

# PART A – PHYSICS

1. Distance of the centre of mass of a solid uniform cone from its vertex is  $z_0$ . If the radius of its base is  $R$  and its height is  $h$  then  $z_0$  is equal to :

(1)  $\frac{5h}{8}$

(2)  $\frac{3h^2}{8R}$

(3)  $\frac{h^2}{4R}$

(4)  $\frac{3h}{4}$

2. A red LED emits light at 0.1 watt uniformly around it. The amplitude of the electric field of the light at a distance of 1 m from the diode is :

(1) 5.48 V/m

(2) 7.75 V/m

(3) 1.73 V/m

(4) 2.45 V/m

3. A pendulum made of a uniform wire of cross sectional area  $A$  has time period  $T$ . When an additional mass  $M$  is added to its bob, the time period changes to  $T_M$ . If the Young's modulus of the material of the wire is  $Y$  then  $\frac{1}{Y}$  is equal to :  
( $g$  = gravitational acceleration)

(1)  $\left[ 1 - \left( \frac{T_M}{T} \right)^2 \right] \frac{A}{Mg}$

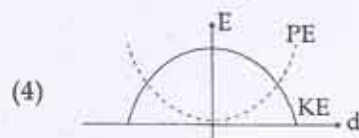
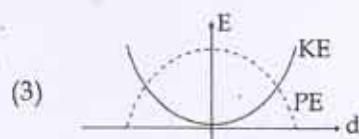
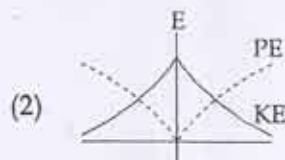
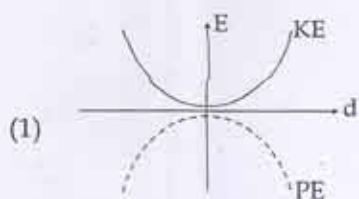
(2)  $\left[ 1 - \left( \frac{T}{T_M} \right)^2 \right] \frac{A}{Mg}$

(3)  $\left[ \left( \frac{T_M}{T} \right)^2 - 1 \right] \frac{A}{Mg}$

(4)  $\left[ \left( \frac{T_M}{T} \right)^2 - 1 \right] \frac{Mg}{A}$



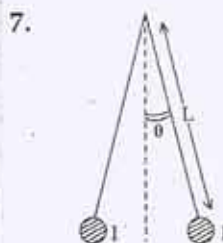
4. For a simple pendulum, a graph is plotted between its kinetic energy (KE) and potential energy (PE) against its displacement  $d$ . Which one of the following represents these correctly? (graphs are schematic and not drawn to scale)



5. A train is moving on a straight track with speed  $20 \text{ ms}^{-1}$ . It is blowing its whistle at the frequency of  $1000 \text{ Hz}$ . The percentage change in the frequency heard by a person standing near the track as the train passes him is (speed of sound  $= 320 \text{ ms}^{-1}$ ) close to:
- 18%
  - 24%
  - 6%
  - 12%

6. When  $5 \text{ V}$  potential difference is applied across a wire of length  $0.1 \text{ m}$ , the drift speed of electrons is  $2.5 \times 10^{-4} \text{ ms}^{-1}$ . If the electron density in the wire is  $8 \times 10^{28} \text{ m}^{-3}$ , the resistivity of the material is close to:

- $1.6 \times 10^{-6} \Omega \text{ m}$
- $1.6 \times 10^{-5} \Omega \text{ m}$
- $1.6 \times 10^{-8} \Omega \text{ m}$
- $1.6 \times 10^{-7} \Omega \text{ m}$



Two long current carrying thin wires, both with current  $I$ , are held by insulating threads of length  $L$  and are in equilibrium as shown in the figure, with threads making an angle ' $\theta$ ' with the vertical. If wires have mass  $\lambda$  per unit length then the value of  $I$  is:

( $g$  = gravitational acceleration)

- $2 \sqrt{\frac{\pi g L}{\mu_0} \tan \theta}$
- $\sqrt{\frac{\pi \lambda g L}{\mu_0} \tan \theta}$
- $\sin \theta \sqrt{\frac{\pi \lambda g L}{\mu_0 \cos \theta}}$
- $2 \sin \theta \sqrt{\frac{\pi \lambda g L}{\mu_0 \cos \theta}}$

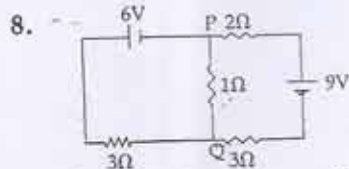
D/Page 3

SPACE FOR ROUGH WORK

$S = 20 \text{ ms}^{-1}$   
 $f = 1000 \text{ Hz}$   
 $\lambda = \frac{v}{f}$   
 $\lambda = \frac{320}{1000}$   
 $\lambda = 0.32 \text{ m}$

$R = \frac{20 \times 1}{1000}$   
 $R = \frac{20}{1000}$   
 $R = 0.02 \text{ m}$

$R = \frac{1}{4 \pi \epsilon_0} \times \frac{q_1 q_2}{r^2}$   
 $R = \frac{1}{4 \pi \epsilon_0} \times \frac{(8 \times 10^{-6})^2}{(2.5 \times 10^{-4})^2}$   
 $R = \frac{1}{4 \pi \epsilon_0} \times \frac{64 \times 10^{-12}}{6.25 \times 10^{-8}}$   
 $R = \frac{1}{4 \pi \epsilon_0} \times 1024 \times 10^{-4}$   
 $R = \frac{1}{4 \pi \epsilon_0} \times 0.1024$



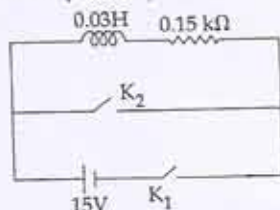
In the circuit shown, the current in the  $1\Omega$  resistor is :

- (1)  $0.13\text{ A}$ , from Q to P
- (2)  $0.13\text{ A}$ , from P to Q
- (3)  $1.3\text{ A}$ , from P to Q
- (4)  $0\text{ A}$

9. Assuming human pupil to have a radius of  $0.25\text{ cm}$  and a comfortable viewing distance of  $25\text{ cm}$ , the minimum separation between two objects that human eye can resolve at  $500\text{ nm}$  wavelength is :

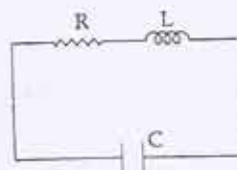
- (1)  $100\text{ }\mu\text{m}$
- (2)  $300\text{ }\mu\text{m}$
- (3)  $1\text{ }\mu\text{m}$
- (4)  $30\text{ }\mu\text{m}$

10. An inductor ( $L=0.03\text{ H}$ ) and a resistor ( $R=0.15\text{ k}\Omega$ ) are connected in series to a battery of  $15\text{ V}$  EMF in a circuit shown below. The key  $K_1$  has been kept closed for a long time. Then at  $t=0$ ,  $K_1$  is opened and key  $K_2$  is closed simultaneously. At  $t=1\text{ ms}$ , the current in the circuit will be : ( $e^5 \approx 150$ )

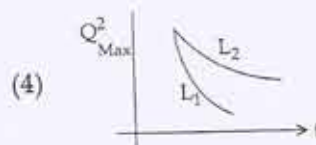
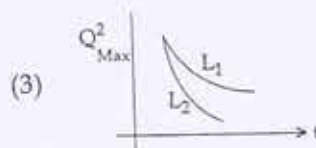
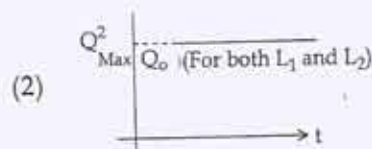
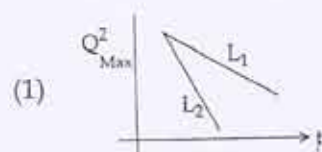


- (1)  $6.7\text{ mA}$
- (2)  $0.67\text{ mA}$
- (3)  $100\text{ mA}$
- (4)  $67\text{ mA}$

11. An LCR circuit is equivalent to a damped pendulum. In an LCR circuit the capacitor is charged to  $Q_0$  and then connected to the L and R as shown below :



If a student plots graphs of the square of maximum charge ( $Q_{\text{Max}}^2$ ) on the capacitor with time ( $t$ ) for two different values  $L_1$  and  $L_2$  ( $L_1 > L_2$ ) of L then which of the following represents this graph correctly ? (plots are schematic and not drawn to scale)

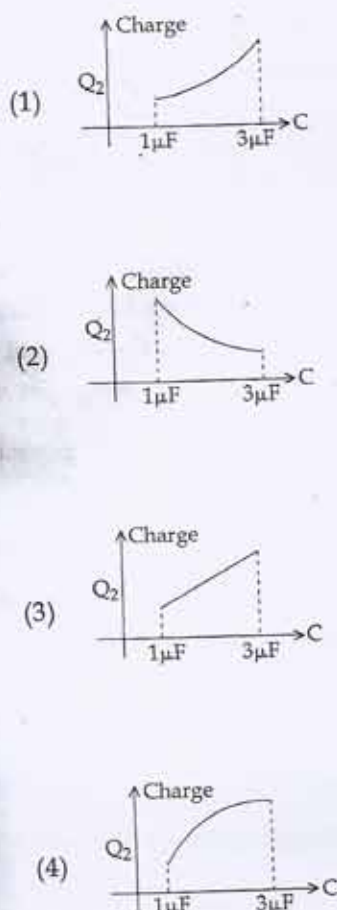
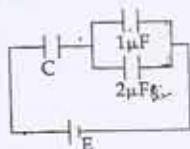


*Handwritten notes:*  
 $20-25\text{ cm}$   
 $\approx 25\text{ cm}$   
 $= \frac{0.25}{2500}$   
 $= 10^{-5}$

*Handwritten note:*  
 $30\text{ each}$



12. In the given circuit, charge  $Q_2$  on the  $2\mu\text{F}$  capacitor changes as  $C$  is varied from  $1\mu\text{F}$  to  $3\mu\text{F}$ .  $Q_2$  as a function of ' $C$ ' is given properly by: (figures are drawn schematically and are not to scale)

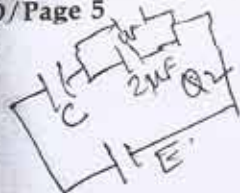


13. From a solid sphere of mass  $M$  and radius  $R$  a cube of maximum possible volume is cut. Moment of inertia of cube about an axis passing through its center and perpendicular to one of its faces is:

- (1)  $\frac{4MR^2}{9\sqrt{3}\pi}$
- (2)  $\frac{4MR^2}{3\sqrt{3}\pi}$
- (3)  $\frac{MR^2}{32\sqrt{2}\pi}$
- (4)  $\frac{MR^2}{16\sqrt{2}\pi}$

14. The period of oscillation of a simple pendulum is  $T = 2\pi\sqrt{\frac{L}{g}}$ . Measured value of  $L$  is  $20.0\text{ cm}$  known to  $1\text{ mm}$  accuracy and time for 100 oscillations of the pendulum is found to be  $90\text{ s}$  using a wrist watch of  $1\text{ s}$  resolution. The accuracy in the determination of  $g$  is:

- (1) 1%
- (2) 5%
- (3) 2%
- (4) 3%



$M = \text{mass (given)}$   
 $R = \text{radius}$

$2/3 \cdot 14$   
 $2/3 \cdot 21$   
 $10$   
 $30$

$T = 2\pi\sqrt{\frac{L}{g}}$   
 $L = 200$   
 $t = 100$   
 $100 \text{ oscillations}$   
 $\frac{t}{n} = \frac{90}{100}$   
 $\frac{90}{100} = 0.9$

$2\pi\sqrt{\frac{200}{9.8}}$   
 $2\pi\sqrt{20.4}$   
 $2\pi \cdot 4.5$   
 $28.2$

15. On a hot summer night, the refractive index of air is smallest near the ground and increases with height from the ground. When a light beam is directed horizontally, the Huygens' principle leads us to conclude that as it travels, the light beam :

- (1) bends downwards
- (2) bends upwards
- (3) becomes narrower
- (4) goes horizontally without any deflection

16. A signal of 5 kHz frequency is amplitude modulated on a carrier wave of frequency 2 MHz. The frequencies of the resultant signal is/are :

- (1) 2005 kHz, 2000 kHz and 1995 kHz
- (2) 2000 kHz and 1995 kHz
- (3) 2 MHz only
- (4) 2005 kHz, and 1995 kHz

17. A solid body of constant heat capacity  $1 \text{ J/}^\circ\text{C}$  is being heated by keeping it in contact with reservoirs in two ways :

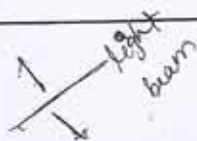
- (i) Sequentially keeping in contact with 2 reservoirs such that each reservoir supplies same amount of heat.
- (ii) Sequentially keeping in contact with 8 reservoirs such that each reservoir supplies same amount of heat.

In both the cases body is brought from initial temperature  $100^\circ\text{C}$  to final temperature  $200^\circ\text{C}$ . Entropy change of the body in the two cases respectively is :

- (1)  $\ln 2, 2\ln 2$
- (2)  $2\ln 2, 8\ln 2$
- (3)  $\ln 2, 4\ln 2$
- (4)  $\ln 2, \ln 2$

18. Consider a spherical shell of radius  $R$  at temperature  $T$ . The black body radiation inside it can be considered as an ideal gas of photons with internal energy per unit volume  $u = \frac{U}{V} \propto T^4$  and pressure  $P = \frac{1}{3} \left( \frac{U}{V} \right)$ . If the shell now undergoes an adiabatic expansion the relation between  $T$  and  $R$  is :

- (1)  $T \propto \frac{1}{R}$
- (2)  $T \propto \frac{1}{R^3}$
- (3)  $T \propto e^{-R}$
- (4)  $T \propto e^{-3R}$

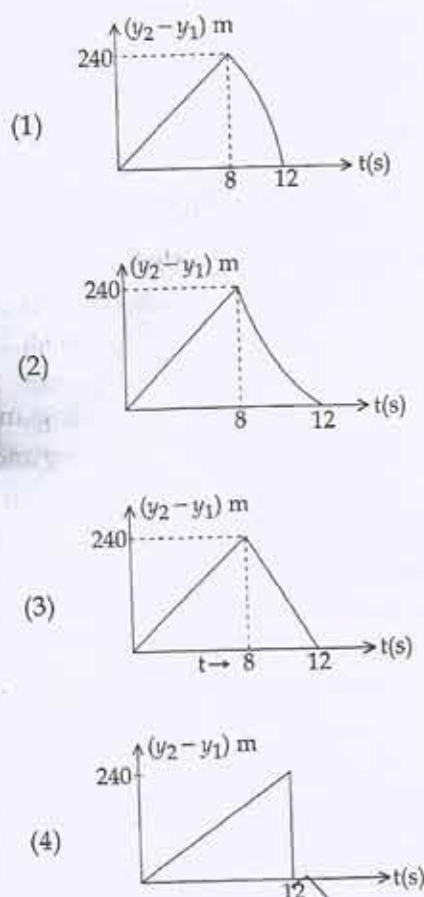




19. Two stones are thrown up simultaneously from the edge of a cliff 240 m high with initial speed of 10 m/s and 40 m/s respectively. Which of the following graph best represents the time variation of relative position of the second stone with respect to the first ?

(Assume stones do not rebound after hitting the ground and neglect air resistance, take  $g = 10 \text{ m/s}^2$ )

(The figures are schematic and not drawn to scale)



20. A uniformly charged solid sphere of radius  $R$  has potential  $V_0$  (measured with respect to  $\infty$ ) on its surface. For this sphere the equipotential surfaces with potentials  $\frac{3V_0}{2}$ ,  $\frac{5V_0}{4}$ ,  $\frac{3V_0}{4}$  and  $\frac{V_0}{4}$  have radius  $R_1$ ,  $R_2$ ,  $R_3$  and  $R_4$  respectively. Then

- (1)  $R_1 = 0$  and  $R_2 < (R_4 - R_3)$
- (2)  $2R < R_4$
- (3)  $R_1 = 0$  and  $R_2 > (R_4 - R_3)$
- (4)  $R_1 \neq 0$  and  $(R_2 - R_1) > (R_4 - R_3)$

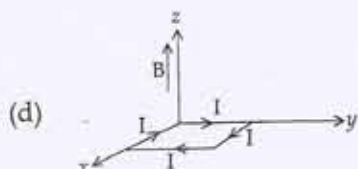
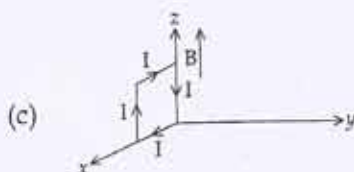
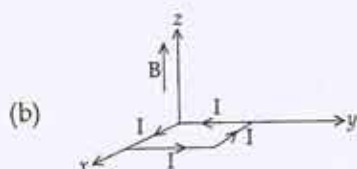
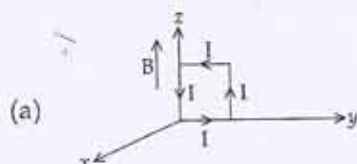
21. Monochromatic light is incident on a glass prism of angle  $A$ . If the refractive index of the material of the prism is  $\mu$ , a ray, incident at an angle  $\theta$ , on the face  $AB$  would get transmitted through the face  $AC$  of the prism provided :



- (1)  $\theta > \cos^{-1} \left[ \mu \sin \left( A + \sin^{-1} \left( \frac{1}{\mu} \right) \right) \right]$
- (2)  $\theta < \cos^{-1} \left[ \mu \sin \left( A + \sin^{-1} \left( \frac{1}{\mu} \right) \right) \right]$
- (3)  $\theta > \sin^{-1} \left[ \mu \sin \left( A - \sin^{-1} \left( \frac{1}{\mu} \right) \right) \right]$
- (4)  $\theta < \sin^{-1} \left[ \mu \sin \left( A - \sin^{-1} \left( \frac{1}{\mu} \right) \right) \right]$

$\theta > \cos^{-1} \left[ \mu \sin \left( A + \sin^{-1} \left( \frac{1}{\mu} \right) \right) \right]$

22. A rectangular loop of sides 10 cm and 5 cm carrying a current  $I$  of 12 A is placed in different orientations as shown in the figures below :



If there is a uniform magnetic field of 0.3 T in the positive  $z$  direction, in which orientations the loop would be in (i) stable equilibrium and (ii) unstable equilibrium ?

- (1) (b) and (d), respectively
- (2) (b) and (c), respectively
- (3) (a) and (b), respectively
- (4) (a) and (c), respectively

23. Two coaxial solenoids of different radii carry current  $I$  in the same direction. Let

$\vec{F}_1$  be the magnetic force on the inner solenoid due to the outer one and  $\vec{F}_2$  be the magnetic force on the outer solenoid due to the inner one. Then :

- (1)  $\vec{F}_1$  is radially inwards and  $\vec{F}_2 = 0$
- (2)  $\vec{F}_1$  is radially outwards and  $\vec{F}_2 = 0$
- (3)  $\vec{F}_1 = \vec{F}_2 = 0$
- (4)  $\vec{F}_1$  is radially inwards and  $\vec{F}_2$  is radially outwards

24. A particle of mass  $m$  moving in the  $x$  direction with speed  $2v$  is hit by another particle of mass  $2m$  moving in the  $y$  direction with speed  $v$ . If the collision is perfectly inelastic, the percentage loss in the energy during the collision is close to :

- (1) 56%
- (2) 62%
- (3) 44%
- (4) 50%



25. Consider an ideal gas confined in an isolated closed chamber. As the gas undergoes an adiabatic expansion, the average time of collision between molecules increases as  $V^q$ , where  $V$  is the volume of the gas. The value of  $q$  is :

$$\left( \gamma = \frac{C_p}{C_v} \right)$$

(1)  $\frac{\gamma + 1}{2}$

(2)  $\frac{\gamma - 1}{2}$

(3)  $\frac{3\gamma + 5}{6}$

(4)  $\frac{3\gamma - 5}{6}$

26. From a solid sphere of mass  $M$  and radius  $R$ , a spherical portion of radius  $\frac{R}{2}$  is removed, as shown in the figure. Taking gravitational potential  $V=0$  at  $r=\infty$ , the potential at the centre of the cavity thus formed is :

( $G$  = gravitational constant)



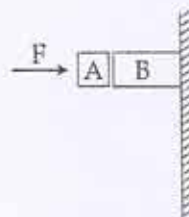
(1)  $-\frac{2GM}{3R}$

(2)  $-\frac{2GM}{R}$

(3)  $-\frac{GM}{2R}$

(4)  $-\frac{GM}{R}$

27.



Given in the figure are two blocks A and B of weight 20 N and 100 N, respectively. These are being pressed against a wall by a force  $F$  as shown. If the coefficient of friction between the blocks is 0.1 and between block B and the wall is 0.15, the frictional force applied by the wall on block B is :

(1) 120 N

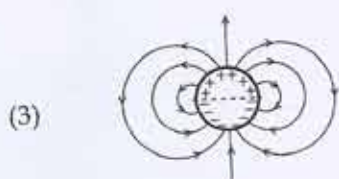
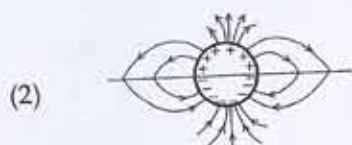
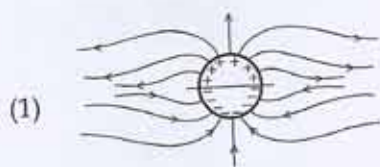
(2) 150 N

(3) 100 N

(4) 80 N



28. A long cylindrical shell carries positive surface charge  $\sigma$  in the upper half and negative surface charge  $-\sigma$  in the lower half. The electric field lines around the cylinder will look like figure given in :  
(figures are schematic and not drawn to scale)



29. As an electron makes a transition from an excited state to the ground state of a hydrogen-like atom/ion :

- (1) kinetic energy decreases, potential energy increases but total energy remains same
- (2) kinetic energy and total energy decrease but potential energy increases
- (3) its kinetic energy increases but potential energy and total energy decrease
- (4) kinetic energy, potential energy and total energy decrease

30. Match List - I (Fundamental Experiment) with List - II (its conclusion) and select the correct option from the choices given below the list :

	List - I		List - II
(A)	Franck-Hertz Experiment.	(i)	Particle nature of light
(B)	Photo-electric experiment.	(ii)	Discrete energy levels of atom
(C)	Davison - Germer Experiment.	(iii)	Wave nature of electron
		(iv)	Structure of atom

- (1) (A) - (ii) (B) - (i) (C) - (iii)
- (2) (A) - (iv) (B) - (iii) (C) - (ii)
- (3) (A) - (i) (B) - (iv) (C) - (iii)
- (4) (A) - (ii) (B) - (iv) (C) - (iii)



# PART B – MATHEMATICS

31. Let  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  be three non-zero vectors such that no two of them are collinear and

$$(\vec{a} \times \vec{b}) \times \vec{c} = \frac{1}{3} |\vec{b}| |\vec{c}| \vec{a}. \text{ If } \theta \text{ is the}$$

angle between vectors  $\vec{b}$  and  $\vec{c}$ , then a value of  $\sin \theta$  is :

(1)  $\frac{2}{3}$

(2)  $\frac{-2\sqrt{3}}{3}$

(3)  $\frac{2\sqrt{2}}{3}$

(4)  $\frac{-\sqrt{2}}{3}$

32. Let O be the vertex and Q be any point on the parabola,  $x^2 = 8y$ . If the point P divides the line segment OQ internally in the ratio 1 : 3, then the locus of P is :

(1)  $y^2 = 2x$

(2)  $x^2 = 2y$

(3)  $x^2 = y$

(4)  $y^2 = x$

33. If the angles of elevation of the top of a tower from three collinear points A, B and C, on a line leading to the foot of the tower, are  $30^\circ$ ,  $45^\circ$  and  $60^\circ$  respectively, then the ratio, AB : BC, is :

(1)  $1 : \sqrt{3}$

(2)  $2 : 3$

(3)  $\sqrt{3} : 1$

(4)  $\sqrt{3} : \sqrt{2}$

34. The number of points, having both co-ordinates as integers, that lie in the interior of the triangle with vertices (0, 0), (0, 41) and (41, 0), is :

(1) 820

(2) 780

(3) 901

(4) 861

35. The equation of the plane containing the line  $2x - 5y + z = 3$ ;  $x + y + 4z = 5$ , and parallel to the plane,  $x + 3y + 6z = 1$ , is :

(1)  $x + 3y + 6z = 7$

(2)  $2x + 6y + 12z = -13$

(3)  $2x + 6y + 12z = 13$

(4)  $x + 3y + 6z = -7$

36. Let A and B be two sets containing four and two elements respectively. Then the number of subsets of the set  $A \times B$ , each having at least three elements is :

(1) 275

(2) 510

(3) 219

(4) 256



37. Locus of the image of the point  $(2, 3)$  in the line  $(2x - 3y + 4) + k(x - 2y + 3) = 0$ ,  $k \in \mathbb{R}$ , is a :

- (1) circle of radius  $\sqrt{2}$ .
- (2) circle of radius  $\sqrt{3}$ .
- (3) straight line parallel to x-axis.
- (4) straight line parallel to y-axis.

38.  $\lim_{x \rightarrow 0} \frac{(1 - \cos 2x)(3 + \cos x)}{x \tan 4x}$  is equal to :

- (1) 2
- (2)  $\frac{1}{2}$
- (3) 4
- (4) 3

39. The distance of the point  $(1, 0, 2)$  from the point of intersection of the line  $\frac{x-2}{3} = \frac{y+1}{4} = \frac{z-2}{12}$  and the plane  $x - y + z = 16$ , is :

- (1)  $3\sqrt{21}$
- (2) 13
- (3)  $2\sqrt{14}$
- (4) 8

40. The sum of coefficients of integral powers of  $x$  in the binomial expansion of  $(1 - 2\sqrt{x})^{50}$  is :

- (1)  $\frac{1}{2}(3^{50} - 1)$
- (2)  $\frac{1}{2}(2^{50} + 1)$
- (3)  $\frac{1}{2}(3^{50} + 1)$
- (4)  $\frac{1}{2}(3^{50})$

41. The sum of first 9 terms of the series  $\frac{1^3}{1} + \frac{1^3 + 2^3}{1+3} + \frac{1^3 + 2^3 + 3^3}{1+3+5} + \dots$  is :

- (1) 142
- (2) 192
- (3) 71
- (4) 96

42. The area (in sq. units) of the region described by

$\{(x, y) : y^2 \leq 2x \text{ and } y \geq 4x - 1\}$  is :

- (1)  $\frac{15}{64}$
- (2)  $\frac{9}{32}$
- (3)  $\frac{7}{32}$
- (4)  $\frac{5}{64}$



43. The set of all values of  $\lambda$  for which the system of linear equations :

$$2x_1 - 2x_2 + x_3 = \lambda x_1$$

$$2x_1 - 3x_2 + 2x_3 = \lambda x_2$$

$$-x_1 + 2x_2 = \lambda x_3$$

has a non-trivial solution,

- (1) contains two elements.
- (2) contains more than two elements.
- (3) is an empty set.
- (4) is a singleton.

44. A complex number  $z$  is said to be unimodular if  $|z|=1$ . Suppose  $z_1$  and  $z_2$

are complex numbers such that  $\frac{z_1 - 2z_2}{2 - z_1 z_2}$

is unimodular and  $z_2$  is not unimodular. Then the point  $z_1$  lies on a :

- (1) circle of radius 2.
- (2) circle of radius  $\sqrt{2}$ .
- (3) straight line parallel to x-axis.
- (4) straight line parallel to y-axis.

45. The number of common tangents to the circles  $x^2 + y^2 - 4x - 6y - 12 = 0$  and  $x^2 + y^2 + 6x + 18y + 26 = 0$ , is :

- (1) 3
- (2) 4
- (3) 1
- (4) 2

46. The number of integers greater than 6,000 that can be formed, using the digits 3, 5, 6, 7 and 8, without repetition, is :

- (1) 120
- (2) 72
- (3) 216
- (4) 192

47. Let  $y(x)$  be the solution of the differential equation

$$(x \log x) \frac{dy}{dx} + y = 2x \log x, (x \geq 1).$$

Then  $y(e)$  is equal to :

- (1) 2
- (2)  $2e$
- (3)  $e$
- (4) 0

48. If  $A = \begin{bmatrix} 1 & 2 & 2 \\ 2 & 1 & -2 \\ a & 2 & b \end{bmatrix}$  is a matrix satisfying

the equation  $AA^T = 9I$ , where  $I$  is  $3 \times 3$  identity matrix, then the ordered pair  $(a, b)$  is equal to :

- (1) (2, 1)
- (2) (-2, -1)
- (3) (2, -1)
- (4) (-2, 1)

D/ Page 13

$(x \log x) \frac{dy}{dx} + y = 2x \log x$

$\frac{d}{dx} (x \log x) \frac{dy}{dx} + \frac{dy}{dx} = \frac{dy}{dx} 2x \log x$

SPACE FOR ROUGH WORK

49. If  $m$  is the A.M. of two distinct real numbers  $l$  and  $n$  ( $l, n > 1$ ) and  $G_1, G_2$  and  $G_3$  are three geometric means between  $l$  and  $n$ , then  $G_1^4 + 2G_2^4 + G_3^4$  equals.

- (1)  $4lmn^2$
- (2)  $4l^2m^2n^2$
- (3)  $4l^2mn$
- (4)  $4lm^2n$

50. The negation of  $\sim s \vee (\sim r \wedge s)$  is equivalent to :

- (1)  $s \vee (r \vee \sim s)$
- (2)  $s \wedge r$
- (3)  $s \wedge \sim r$
- (4)  $s \wedge (r \wedge \sim s)$

51. The integral  $\int \frac{dx}{x^2(x^4 + 1)^{3/4}}$  equals :

- (1)  $-(x^4 + 1)^{1/4} + c$
- (2)  $-\left(\frac{x^4 + 1}{x^4}\right)^{1/4} + c$
- (3)  $\left(\frac{x^4 + 1}{x^4}\right)^{1/4} + c$
- (4)  $(x^4 + 1)^{1/4} + c$

52. The normal to the curve,  $x^2 + 2xy - 3y^2 = 0$ , at  $(1, 1)$  :

- (1) meets the curve again in the third quadrant.
- (2) meets the curve again in the fourth quadrant.
- (3) does not meet the curve again.
- (4) meets the curve again in the second quadrant.

53. Let

$$\tan^{-1} y = \tan^{-1} x + \tan^{-1} \left( \frac{2x}{1 - x^2} \right),$$

where  $|x| < \frac{1}{\sqrt{3}}$ . Then a value of  $y$  is :

- (1)  $\frac{3x - x^3}{1 + 3x^2}$
- (2)  $\frac{3x + x^3}{1 + 3x^2}$
- (3)  $\frac{3x - x^3}{1 - 3x^2}$
- (4)  $\frac{3x + x^3}{1 - 3x^2}$

54. If the function.

$$g(x) = \begin{cases} k\sqrt{x+1}, & 0 \leq x \leq 3 \\ mx+2, & 3 < x \leq 5 \end{cases}$$

is differentiable, then the value of  $k+m$  is :

- (1)  $\frac{10}{3}$
- (2) 4
- (3) 2
- (4)  $\frac{16}{5}$

Handwritten notes:

$$\lim_{x \rightarrow 0} \frac{k\sqrt{x+1}}{k\sqrt{0+1}} = \frac{k\sqrt{1}}{k\sqrt{1}} = 1$$

$$\lim_{x \rightarrow 3} \frac{k\sqrt{x+1}}{mx+2} = \frac{k\sqrt{3+1}}{3m+2} = \frac{k\sqrt{4}}{3m+2} = \frac{2k}{3m+2}$$

For differentiability at  $x=3$ , the limits must be equal:

$$1 = \frac{2k}{3m+2} \Rightarrow 3m+2 = 2k \Rightarrow k = \frac{3m+2}{2}$$

Then  $k+m = \frac{3m+2}{2} + m = \frac{3m+2+2m}{2} = \frac{5m+2}{2}$

From the options, if  $k+m = \frac{10}{3}$ , then  $\frac{5m+2}{2} = \frac{10}{3} \Rightarrow 5m+2 = \frac{20}{3} \Rightarrow 5m = \frac{14}{3} \Rightarrow m = \frac{14}{15}$

Then  $k = \frac{3(\frac{14}{15})+2}{2} = \frac{\frac{14}{5}+2}{2} = \frac{\frac{14+10}{5}}{2} = \frac{\frac{24}{5}}{2} = \frac{12}{5}$

Check:  $k+m = \frac{12}{5} + \frac{14}{15} = \frac{36+14}{15} = \frac{50}{15} = \frac{10}{3}$



55. The mean of the data set comprising of 16 observations is 16. If one of the observation valued 16 is deleted and three new observations valued 3, 4 and 5 are added to the data, then the mean of the resultant data, is :

- (1) 15.8  
(2) 14.0  
(3) 16.8  
(4) 16.0

56. The integral

$$\int_2^4 \frac{\log x^2}{\log x^2 + \log (36 - 12x + x^2)} dx$$

is equal to :

- (1) 1  
(2) 6  
(3) 2  
(4) 4

57. Let  $\alpha$  and  $\beta$  be the roots of equation  $x^2 - 6x - 2 = 0$ . If  $a_n = \alpha^n - \beta^n$ , for  $n \geq 1$ , then the value of  $\frac{a_{10} - 2a_8}{2a_9}$  is equal to :

- (1) 3  
(2) -3  
(3) 6  
(4) -6

58. Let  $f(x)$  be a polynomial of degree four having extreme values at  $x=1$  and  $x=2$ .

If  $\lim_{x \rightarrow 0} \left[ 1 + \frac{f(x)}{x^2} \right] = 3$ , then  $f(2)$  is equal

to :

- (1) 0  
(2) 4  
(3) -8  
(4) -4

59. The area (in sq. units) of the quadrilateral formed by the tangents at the end points of the latera recta to the ellipse

$$\frac{x^2}{9} + \frac{y^2}{5} = 1, \text{ is :}$$

- (1)  $\frac{27}{2}$   
(2) 27  
(3)  $\frac{27}{4}$   
(4) 18

60. If 12 identical balls are to be placed in 3 identical boxes, then the probability that one of the boxes contains exactly 3 balls is :

- (1)  $220 \left( \frac{1}{3} \right)^{12}$   
(2)  $22 \left( \frac{1}{3} \right)^{11}$   
(3)  $\frac{55}{3} \left( \frac{2}{3} \right)^{11}$   
(4)  $55 \left( \frac{2}{3} \right)^{10}$

$\frac{1 + P(1)}{(1)^2}$

$m(1+2)$   
 $m(5)+2$   
 $5m+2$   
 $3m+2$   
 $2m0$

$2m=0$   
 $2k=0$   
 $k\sqrt{1}=0$   
 $k=0$

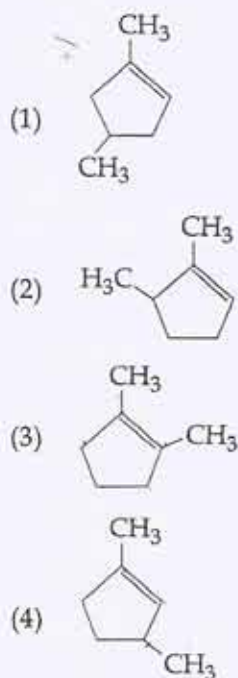
$k+m=0$   
 $2-2=0$   
 $-4$

$a_{10} - 2a_8$   
 $2a_9$   
 $a_{10} - 2a_8$   
 $2a_9$

$\frac{1-2}{2} = \frac{1}{2}$

# PART C – CHEMISTRY

61. Which compound would give 5 - keto - 2 - methyl hexanal upon ozonolysis ?



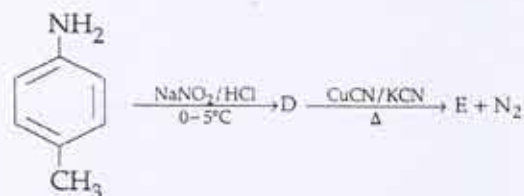
62. Which of the vitamins given below is water soluble ?

- (1) Vitamin E  
(2) Vitamin K  
(3) Vitamin C  
(4) Vitamin D

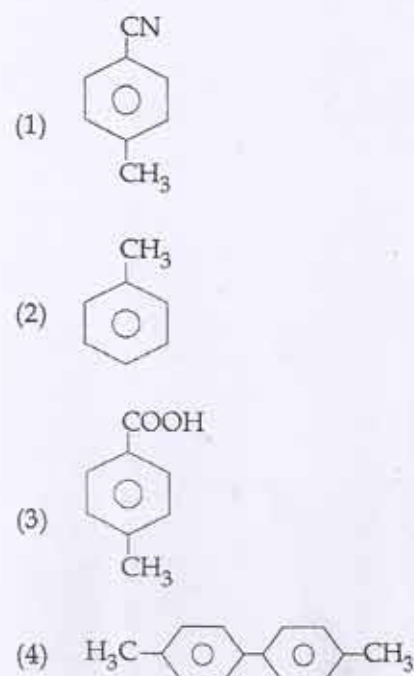
63. Which one of the following alkaline earth metal sulphates has its hydration enthalpy greater than its lattice enthalpy ?

- (1)  $\text{BaSO}_4$   
(2)  $\text{SrSO}_4$   
(3)  $\text{CaSO}_4$   
(4)  $\text{BeSO}_4$

64. In the reaction



the product E is :



65. Sodium metal crystallizes in a body centred cubic lattice with a unit cell edge of  $4.29\text{\AA}$ . The radius of sodium atom is approximately :

- (1)  $5.72\text{\AA}$   
(2)  $0.93\text{\AA}$   
(3)  $1.86\text{\AA}$   
(4)  $3.22\text{\AA}$



66. Which of the following compounds is not colored yellow ?

- (1)  $(\text{NH}_4)_3 [\text{As} (\text{Mo}_3 \text{O}_{10})_4]$
- (2)  $\text{BaCrO}_4$
- (3)  $\text{Zn}_2[\text{Fe}(\text{CN})_6]$
- (4)  $\text{K}_3[\text{Co}(\text{NO}_2)_6]$

67. Which of the following is the energy of a possible excited state of hydrogen ?

- (1)  $-3.4 \text{ eV}$
- (2)  $+6.8 \text{ eV}$
- (3)  $+13.6 \text{ eV}$
- (4)  $-6.8 \text{ eV}$

68. Which of the following compounds is not an antacid ?

- (1) Phenelzine
- (2) Ranitidine
- (3) Aluminium hydroxide
- (4) Cimetidine

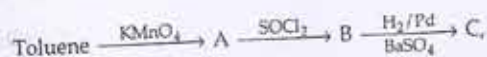
69. The ionic radii (in Å) of  $\text{N}^{3-}$ ,  $\text{O}^{2-}$  and  $\text{F}^-$  are respectively :

- (1) 1.71, 1.40 and 1.36
- (2) 1.71, 1.36 and 1.40
- (3) 1.36, 1.40 and 1.71
- (4) 1.36, 1.71 and 1.40

70. In the context of the Hall - Heroult process for the extraction of Al, which of the following statements is false ?

- (1)  $\text{Al}^{3+}$  is reduced at the cathode to form Al
- (2)  $\text{Na}_3\text{AlF}_6$  serves as the electrolyte
- (3) CO and  $\text{CO}_2$  are produced in this process
- (4)  $\text{Al}_2\text{O}_3$  is mixed with  $\text{CaF}_2$  which lowers the melting point of the mixture and brings conductivity

71. In the following sequence of reactions :



the product C is :

- (1)  $\text{C}_6\text{H}_5\text{CH}_2\text{OH}$
- (2)  $\text{C}_6\text{H}_5\text{CHO}$
- (3)  $\text{C}_6\text{H}_5\text{COOH}$
- (4)  $\text{C}_6\text{H}_5\text{CH}_3$

72. Higher order ( $>3$ ) reactions are rare due to :

- (1) shifting of equilibrium towards reactants due to elastic collisions
- (2) loss of active species on collision
- (3) low probability of simultaneous collision of all the reacting species
- (4) increase in entropy and activation energy as more molecules are involved

73. Which of the following compounds will exhibit geometrical isomerism ?

- (1) 2 - Phenyl - 1 - butene
- (2) 1, 1 - Diphenyl - 1 - propane
- (3) 1 - Phenyl - 2 - butene
- (4) 3 - Phenyl - 1 - butene

74. Match the catalysts to the correct processes :

Catalyst	Process
(A) $\text{TiCl}_3$	(i) Wacker process
(B) $\text{PdCl}_2$	(ii) Ziegler - Natta polymerization
(C) $\text{CuCl}_2$	(iii) Contact process
(D) $\text{V}_2\text{O}_5$	(iv) Deacon's process
(1) (A) - (ii), (B) - (iii), (C) - (iv), (D) - (i)	
(2) (A) - (iii), (B) - (i), (C) - (ii), (D) - (iv)	
(3) (A) - (iii), (B) - (ii), (C) - (iv), (D) - (i)	
(4) (A) - (ii), (B) - (i), (C) - (iv), (D) - (iii)	

75. The intermolecular interaction that is dependent on the inverse cube of distance between the molecules is :

- (1) London force
- (2) hydrogen bond
- (3) ion - ion interaction
- (4) ion - dipole interaction

76. The molecular formula of a commercial resin used for exchanging ions in water softening is  $\text{C}_8\text{H}_7\text{SO}_3\text{Na}$  (Mol. wt. 206). What would be the maximum uptake of  $\text{Ca}^{2+}$  ions by the resin when expressed in mole per gram resin ?

- (1)  $\frac{2}{309}$
- (2)  $\frac{1}{412}$
- (3)  $\frac{1}{103}$
- (4)  $\frac{1}{206}$

77. Two Faraday of electricity is passed through a solution of  $\text{CuSO}_4$ . The mass of copper deposited at the cathode is : (at. mass of  $\text{Cu} = 63.5 \text{ amu}$ )

- (1) 2 g
- (2) 127 g
- (3) 0 g
- (4) 63.5 g

78. The number of geometric isomers that can exist for square planar  $[\text{Pt}(\text{Cl})(\text{py})(\text{NH}_3)(\text{NH}_2\text{OH})]^+$  is (py = pyridine) :

- (1) 4
- (2) 6
- (3) 2
- (4) 3



79. In Carius method of estimation of halogens, 250 mg of an organic compound gave 141 mg of AgBr. The percentage of bromine in the compound is :

(at. mass Ag = 108; Br = 80)

- (1) 48
- (2) 60
- (3) 24
- (4) 36

80. The color of  $\text{KMnO}_4$  is due to :

- (1)  $L \rightarrow M$  charge transfer transition
- (2)  $\sigma - \sigma^*$  transition
- (3)  $M \rightarrow L$  charge transfer transition
- (4)  $d - d$  transition

81. The synthesis of alkyl fluorides is best accomplished by :

- (1) Finkelstein reaction
- (2) Swarts reaction
- (3) Free radical fluorination
- (4) Sandmeyer's reaction

82. 3 g of activated charcoal was added to 50 mL of acetic acid solution (0.06N) in a flask. After an hour it was filtered and the strength of the filtrate was found to be 0.042 N. The amount of acetic acid adsorbed (per gram of charcoal) is :

- (1) 42 mg
- (2) 54 mg
- (3) 18 mg
- (4) 36 mg

83. The vapour pressure of acetone at  $20^\circ\text{C}$  is 185 torr. When 1.2 g of a non-volatile substance was dissolved in 100 g of acetone at  $20^\circ\text{C}$ , its vapour pressure was 183 torr. The molar mass ( $\text{g mol}^{-1}$ ) of the substance is :

- (1) 128
- (2) 488
- (3) 32
- (4) 64

84. Which among the following is the most reactive ?

- (1)  $\text{I}_2$
- (2)  $\text{ICl}$
- (3)  $\text{Cl}_2$
- (4)  $\text{Br}_2$

85. The standard Gibbs energy change at 300 K for the reaction  $2A \rightleftharpoons B + C$  is

2494.2 J. At a given time, the composition

of the reaction mixture is  $[A] = \frac{1}{2}$ ,  $[B] = 2$

and  $[C] = \frac{1}{2}$ . The reaction proceeds in the :  $[R = 8.314 \text{ J/K/mol}, e = 2.718]$

- (1) forward direction because  $Q < K_c$
- (2) reverse direction because  $Q < K_c$
- (3) forward direction because  $Q > K_c$
- (4) reverse direction because  $Q > K_c$

86. **Assertion :** Nitrogen and Oxygen are the main components in the atmosphere but these do not react to form oxides of nitrogen.

**Reason :** The reaction between nitrogen and oxygen requires high temperature.

- (1) The assertion is incorrect, but the reason is correct
- (2) Both the assertion and reason are incorrect
- (3) Both assertion and reason are correct, and the reason is the correct explanation for the assertion
- (4) Both assertion and reason are correct, but the reason is not the correct explanation for the assertion

87. Which one has the highest boiling point ?

- (1) Kr
- (2) Xe
- (3) He
- (4) Ne

88. Which polymer is used in the manufacture of paints and lacquers ?

- (1) Polypropene
- (2) Poly vinyl chloride
- (3) Bakelite
- (4) Glyptal

89. The following reaction is performed at 298 K.



The standard free energy of formation of NO(g) is 86.6 kJ/mol at 298 K. What is the standard free energy of formation of NO<sub>2</sub>(g) at 298 K? ( $K_p = 1.6 \times 10^{12}$ )

- (1)  $86600 - \frac{\ln(1.6 \times 10^{12})}{R(298)}$
- (2)  $0.5[2 \times 86,600 - R(298) \ln(1.6 \times 10^{12})]$
- (3)  $R(298) \ln(1.6 \times 10^{12}) - 86600$
- (4)  $86600 + R(298) \ln(1.6 \times 10^{12})$

90. From the following statements regarding H<sub>2</sub>O<sub>2</sub>, choose the **incorrect** statement :

- (1) It has to be stored in plastic or wax lined glass bottles in dark
- (2) It has to be kept away from dust
- (3) It can act only as an oxidizing agent
- (4) It decomposes on exposure to light

- o o o -