


Chapter 8. Classification: Basic Concepts

- ❑ Classification: Basic Concepts
- ❑ Decision Tree Induction
- ❑ Bayes Classification Methods 
- ❑ Linear Classifier
- ❑ Model Evaluation and Selection
- ❑ Techniques to Improve Classification Accuracy: Ensemble Methods
- ❑ Additional Concepts on Classification
- ❑ Summary

What Is Bayesian Classification?

เป็นการใช้สถิติทำนาย

- ❑ A statistical classifier
 - ❑ Perform *probabilistic prediction* (i.e., predict class membership probabilities)
- ❑ Foundation—Based on Bayes' Theorem
- ❑ Performance
 - ❑ A simple Bayesian classifier, ^{ง่าย}*naïve Bayesian classifier*, has comparable performance with decision tree and selected neural network classifiers
- ❑ Incremental
 - ❑ Each training example can incrementally increase/decrease the probability that a hypothesis is correct—prior knowledge can be combined with observed data
- ❑ Theoretical Standard
 - ❑ Even when Bayesian methods are computationally intractable, they can provide a standard of optimal decision making against which other methods can be measured

Bayes' Theorem: Basics

- Total probability Theorem:

$$p(B) = \sum_i p(B|A_i)p(A_i)$$

p (red arrow pointing to p(B))
test data (red arrow pointing to B)
A? (red arrow pointing to A_i)
B? (red arrow pointing to B)

- Bayes' Theorem:

$$p(H|X) = \frac{p(X|H)P(H)}{p(X)} \propto p(X|H)P(H)$$

training data (red arrow pointing to p(X|H) and P(H))

posteriori probability likelihood prior probability

What we should choose What we just see What we knew previously

- **X**: a data sample (“evidence”)

Prediction can be done based on Bayes' Theorem:

- **H**: X belongs to class C

x ကို ကြည့်ကာ H-ကို ရှာဖွေခြင်း၊ အကယ်၍ မရှိပါက အခြားတစ်ခုကို ရှာဖွေခြင်း

Classification is to derive the maximum posteriori

Naïve Bayes Classifier: Making a Naïve Assumption

- ❑ Practical difficulty of Naïve Bayes inference: It requires initial knowledge of many probabilities, which may not be available or involving significant computational cost
- ❑ A Naïve Special Case
 - ❑ Make an additional assumption to simplify the model, but achieve comparable performance.

attributes are conditionally independent
(i.e., no dependence relation between attributes)

$$p(X|C_i) = \prod_k p(x_k|C_i) = p(x_1|C_i) \cdot p(x_2|C_i) \cdots p(x_n|C_i)$$

- ❑ Only need to count the class distribution w.r.t. features

Naïve Bayes Classifier: Categorical vs. Continuous Valued Features

- If feature x_k is categorical, $p(x_k = v_k | C_i)$ is the # of tuples in C_i with $x_k = v_k$, divided by $|C_{i,D}|$ (# of tuples of C_i in D)

$$p(X|C_i) = \prod_k p(x_k|C_i) = p(x_1|C_i) \cdot p(x_2|C_i) \cdots p(x_n|C_i)$$

- If feature x_k is continuous-valued, $p(x_k = v_k | C_i)$ is usually computed based on Gaussian distribution with a mean μ and standard deviation σ

$$p(x_k = v_k | C_i) = N(x_k | \mu_{C_i}, \sigma_{C_i}) = \frac{1}{\sqrt{2\pi}\sigma_{C_i}} e^{-\frac{(x - \mu_{C_i})^2}{2\sigma^2}}$$

Naïve Bayes Classifier: Training Dataset

Class:

C1:buys_computer = 'yes'

C2:buys_computer = 'no'

Data to be classified:

example

X = (age <=30, Income = medium,

Student = yes, Credit_rating = Fair)

age	income	student	credit_rating	buys_computer
<=30	high	no	fair	no
<=30	high	no	excellent	no
31...40	high	no	fair	yes
>40	medium	no	fair	yes
>40	low	yes	fair	yes
>40	low	yes	excellent	no
31...40	low	yes	excellent	yes
<=30	medium	no	fair	no
<=30	low	yes	fair	yes
>40	medium	yes	fair	yes
<=30	medium	yes	excellent	yes
31...40	medium	no	excellent	yes
31...40	high	yes	fair	yes
>40	medium	no	excellent	no

training data

$$P(H^{-N} | X) = ?$$

$$P(H^{-y} | X) = ?$$

$$= P(X | H^{-y}) P(H^{-y}) \rightarrow \frac{9}{14}$$

training data

Naïve Bayes Classifier: An Example

□ $P(C_i): P(\text{buys_computer} = \text{"yes"}) = 9/14 = 0.643$

$P(\text{buys_computer} = \text{"no"}) = 5/14 = 0.357$

□ Compute $P(X|C_i)$ for each class

$P(\text{age} = \text{"<=30"} | \text{buys_computer} = \text{"yes"}) = 2/9 = 0.222$

$P(\text{age} = \text{"<= 30"} | \text{buys_computer} = \text{"no"}) = 3/5 = 0.6$

$P(\text{income} = \text{"medium"} | \text{buys_computer} = \text{"yes"}) = 4/9 = 0.444$

$P(\text{income} = \text{"medium"} | \text{buys_computer} = \text{"no"}) = 2/5 = 0.4$

$P(\text{student} = \text{"yes"} | \text{buys_computer} = \text{"yes"}) = 6/9 = 0.667$

$P(\text{student} = \text{"yes"} | \text{buys_computer} = \text{"no"}) = 1/5 = 0.2$

$P(\text{credit_rating} = \text{"fair"} | \text{buys_computer} = \text{"yes"}) = 6/9 = 0.667$

$P(\text{credit_rating} = \text{"fair"} | \text{buys_computer} = \text{"no"}) = 2/5 = 0.4$

□ $X = (\text{age} \leq 30, \text{income} = \text{medium}, \text{student} = \text{yes}, \text{credit_rating} = \text{fair})$

$P(X|C_i): P(X | \text{buys_computer} = \text{"yes"}) = 0.222 \times 0.444 \times 0.667 \times 0.667 = 0.044$

$P(X | \text{buys_computer} = \text{"no"}) = 0.6 \times 0.4 \times 0.2 \times 0.4 = 0.019$

$P(X|C_i) * P(C_i): P(X | \text{buys_computer} = \text{"yes"}) * P(\text{buys_computer} = \text{"yes"}) = 0.028$

$P(X | \text{buys_computer} = \text{"no"}) * P(\text{buys_computer} = \text{"no"}) = 0.007$

Therefore, X belongs to class ("buys_computer = yes")

age	income	student	credit_rating	buys_computer
<=30	high	no	fair	no
<=30	high	no	excellent	no
31...40	high	no	fair	yes
>40	medium	no	fair	yes
>40	low	yes	fair	yes
>40	low	yes	excellent	no
31...40	low	yes	excellent	yes
<=30	medium	no	fair	no
<=30	low	yes	fair	yes
>40	medium	yes	fair	yes
<=30	medium	yes	excellent	yes
31...40	medium	no	excellent	yes
31...40	high	yes	fair	yes
>40	medium	no	excellent	no

$\hat{X} = \text{age} = 42, \text{student} = \text{yes?}$

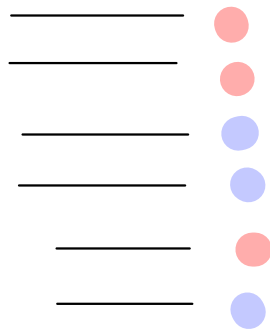
$$P(H|\hat{X}) = ?$$

$$P(H=y | (\text{age} = 42, \text{students} = \text{yes})) = P(\text{age} = 42 |_{byy}) P(\text{stu} = \text{yes} |_{byy}) P(byy)$$

$\downarrow \quad \quad \quad \downarrow \quad \quad \downarrow$
 $\frac{3}{9} \quad \quad \quad \times \quad \quad \frac{6}{9} \quad \quad \times \quad \quad \frac{9}{14}$

$$P(H_{byy} = N | (\text{age} = 42, \text{stu} = \text{yes}))$$

k -NN



test data

หาค่า $k=5$ ใกล้เคียง

(, ,)
Ans (, ,)
โดยหาสมาชิก
ที่ใกล้ที่สุด

1 plot ลงใน space

2. หาเพื่อนบ้าน

และ $CU=3$ โดยหาเพื่อนบ้าน
ที่ใกล้ที่สุด

Avoiding the Zero-Probability Problem

- ❑ Naïve Bayesian prediction requires each conditional probability be **non-zero**

- ❑ Otherwise, the predicted probability will be zero

$$p(X|C_i) = \prod_k p(x_k|C_i) = p(x_1|C_i) \cdot p(x_2|C_i) \cdots p(x_n|C_i)$$

- ❑ Example. Suppose a dataset with 1000 tuples:

income = low (0), income = medium (990), and income = high (10)

- ❑ Use **Laplacian correction** (or Laplacian estimator)

- ❑ *Adding 1 to each case*

$$\text{Prob}(\text{income} = \text{low}) = 1/(1000 + 3)$$

$$\text{Prob}(\text{income} = \text{medium}) = (990 + 1)/(1000 + 3)$$

$$\text{Prob}(\text{income} = \text{high}) = (10 + 1)/(1000 + 3)$$

- ❑ The “corrected” probability estimates are close to their “uncorrected” counterparts

Naïve Bayes Classifier: Strength vs. Weakness

- ❑ Strength
 - ❑ Easy to implement
 - ❑ Good results obtained in most of the cases
- ❑ Weakness
 - ❑ Assumption: attributes conditional independence, therefore loss of accuracy
 - ❑ Practically, dependencies exist among variables
 - ❑ E.g., Patients: Profile: age, family history, etc.
Symptoms: fever, cough etc.
Disease: lung cancer, diabetes, etc.
 - ❑ Dependencies among these cannot be modeled by Naïve Bayes Classifier
- ❑ How to deal with these dependencies?
 - ❑ Use Bayesian Belief Networks (to be covered in the next chapter)