

# COM 530500 Network Science Final Project

DUE: Thursday, January 21, 2021

*No late homework will be accepted.*

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**Problem 1. (40%)** Consider the **ego-Facebook** [1] dataset. A node in this dataset represents a user on Facebook, and an edge between two nodes represents the relationship between two users.

- (a) (10%) List some statistical information of this dataset, such as the number of nodes, number of edges, average clustering coefficient, diameter, average degree, maximum degree, etc.
- (b) (10%) Visualize the dataset by plotting it.
- (c) (10%) Plot the degree distribution with log-log scale.
- (d) (10%) List the top 10 nodes ranked by the following centrality measures.
  - Degree centrality
  - Katz centrality
  - Eigenvector centrality
  - Betweenness centrality
  - Closeness centrality

*Solution:* Type your answer here.

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**Problem 2. (60%+bonus 10%)** In this problem, we want to investigate the disease propagation by the independent cascade (IC) model in **ego-Facebook** [1] dataset. Assume the propagation probability is  $\phi$ , and the set of seeds nodes  $S$  are randomly selected. Collect the set of infected nodes within the distance  $D$  of the seed nodes, and calculate the prevalence rate  $r_1$  (which is defined by the ratio of the number of infected nodes to the total number of nodes). Set  $\phi = 0.1$ ,  $|S| = 5$ , and  $D$  the diameter of the graph.

- (a) (40%) Simulate the disease propagation by IC model after removing the top 0%, 10%, 20%, ..., 50% of nodes from the following centrality measures respectively, and calculate the corresponding prevalence rate  $r_1$ . Please plot the curves of  $r_1$  vs. the percentage of nodes removed. (*Note: Please run the simulation 100 times and average the results.*)
  - Degree centrality
  - Katz centrality
  - Eigenvector centrality

- Betweenness centrality
- Closeness centrality

- (b) (bonus 10%) Could you find a centrality measure that achieves a better performance?
- (c) (20%) Write a report to compare and discuss the results of different centrality measures.

*Solution:* Type your answer here.

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## References

- [1] J. Leskovec and J. J. Mcauley, “Learning to discover social circles in ego networks,” in *Advances in neural information processing systems*, 2012, pp. 539–547.