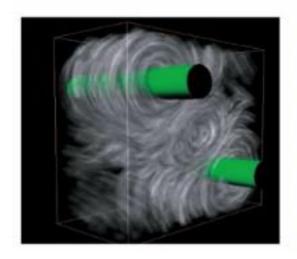
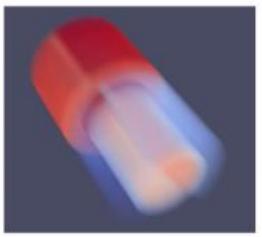
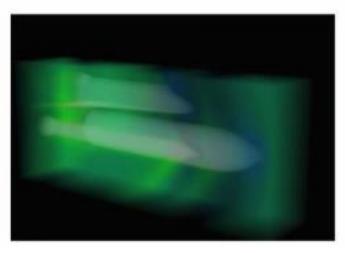
# Direct Volume Rendering Optical Model

# **Volume Rendering**

- A method to visualize the entire 3D data set by simulating light transport across the volume
- A 2D projection of 3D discrete samples

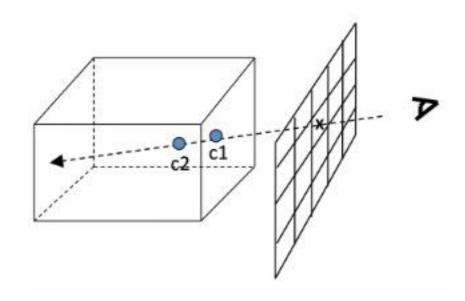






# Direct Volume Rendering

- Simulate light transport through a continuous volume
- Data are interpolated from the samples at the grid points
- Optical properties such as colors and opacities are assigned to the interpolated data
- Optical properties must be integrated along each viewing ray

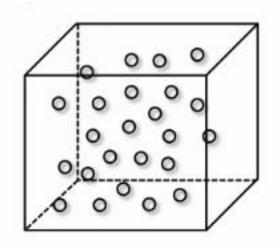


# **Optical Model**

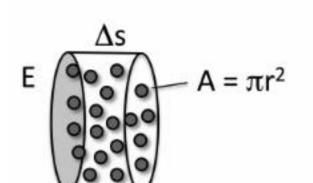
Participating medium (the voxels) can absorb, emit, or both absorb and emit light

How much light will reach the eye?

- Absorption Model
- Emission Model
- Absorption + Emission

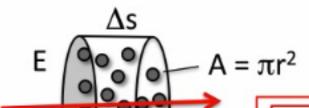


- The simplest participating medium
- Consists of perfectly black particles that absorb all the light that they intercept
- Assume
  - Each particle has an area of  $A = \pi r^2$
  - Number of particles per unit volume =  $\rho$
  - A small cylindrical slab with a base area E and thickness  $\Delta s$



- Total number of particles =  $E \Delta s \rho$
- Total area occluded by particles = A E  $\Delta$ s  $\rho$
- The fraction of occluded area =  $AE\Delta s\rho$  /  $E = A \Delta s \rho$

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$$\frac{d \, \mathbf{I(s)}}{ds} = - \, \mathbf{I(s)} \, \frac{\mathbf{x} \, \mathbf{A} \, \Delta \mathbf{s} \, \rho(\mathbf{s})}{\Delta \mathbf{s}} = - \, \mathbf{A} \, \rho \, (\mathbf{s}) \, \mathbf{I(s)}$$

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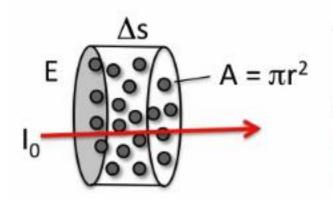
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Solve this ODE

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$$\frac{\Delta s}{ds} = - A \rho (s) I(s)$$
 Solve this ODE 
$$I(s) = I_0 \times e^{-\int_0^s \rho(t) A dt} = I_0 \times e^{-\int_0^s \tau(t) dt}$$



$$I(s) = I_0 \times e^{-\int_0^s \rho(t)Adt} = I_0 \times e^{-\int_0^s \tau(t)dt}$$

$$ho(t)A= au(t)$$
 : extinction coefficient

I<sub>0</sub> = Initial light intensity

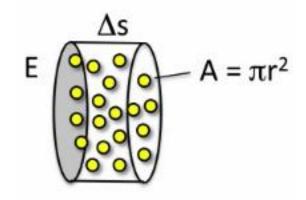
$$e^{-\int_0^s \tau(t)dt}$$

Can be seen as the transparency, or 1 – opacity of the medium from 0 to s

## **Emission Only**

- Each particle will glow diffusively with an intensity C
- In a small cylindrical slab, the total area occupied by the particle is  $AE\Delta s\rho$
- So the glow flux will be  $CAE\Delta s\rho$
- Then the glow per unit area is  $CAE\Delta s\rho/E = CA\Delta s\rho$

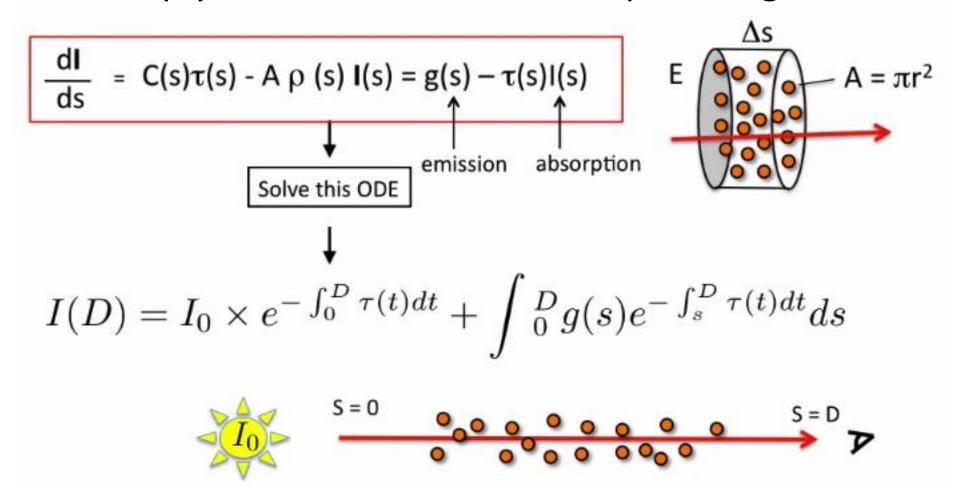
$$\frac{dI}{ds} = C(s) A \rho(s) = C(s)\tau(s) = g(s)$$
 Solve this ODE

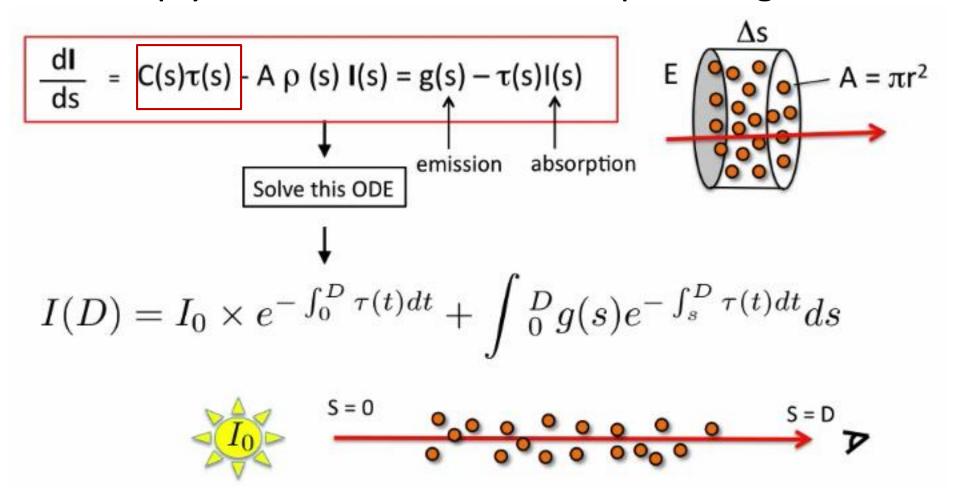


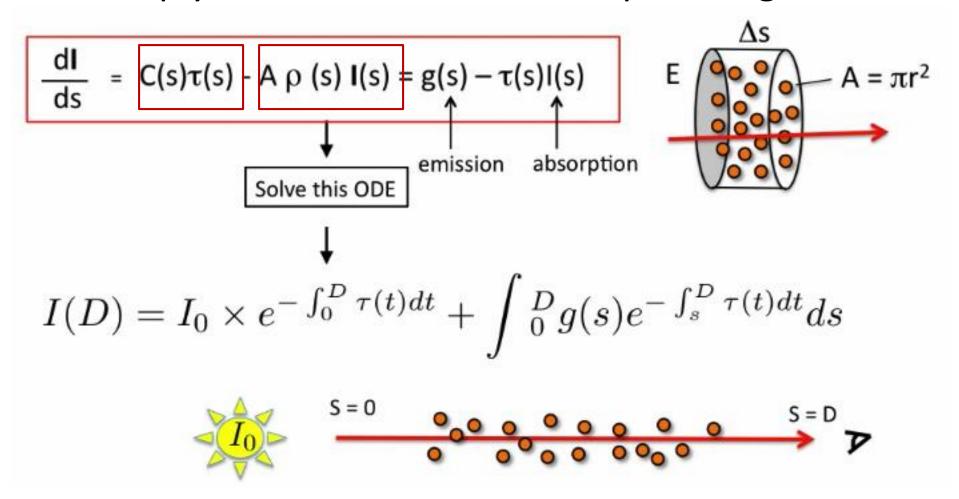
#### **Emission Only**

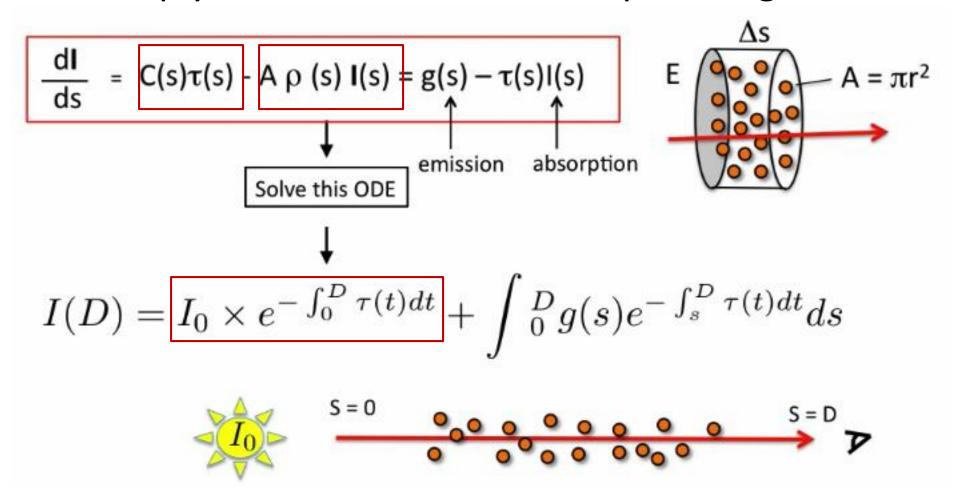
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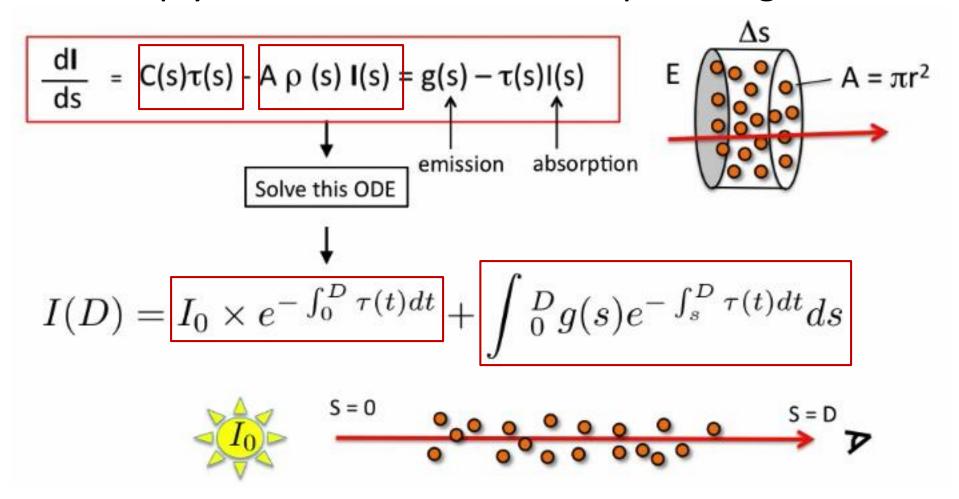
$$\frac{\mathrm{d}\mathbf{I}}{\mathrm{d}\mathbf{s}} = \mathbf{C}(\mathbf{s}) \ \mathbf{A} \ \rho(\mathbf{s}) = \mathbf{C}(\mathbf{s}) \tau(\mathbf{s}) = \mathbf{g}(\mathbf{s})$$
 Solve this ODE 
$$I(s) = I_0 + \int_0^s g(t) dt = I_0 + \int_0^s C(t) \tau(t) dt$$











## Put It All Together



Absorption only:

$$I(s) = I_0 \times e^{-\int_0^s \rho(t)Adt} = I_0 \times e^{-\int_0^s \tau(t)dt}$$

Emission only:

$$I(s) = I_0 + \int_0^s g(t)dt = I_0 + \int_0^s C(t)\tau(t)dt$$

Emission plus absorption:

$$I(D) = I_0 \times e^{-\int_0^D \tau(t)dt} + \int_0^D g(s)e^{-\int_s^D \tau(t)dt}ds$$

# Look More Closely

$$I(D) = I_0 \times e^{-\int_0^D \tau(t)dt} + \int_0^D g(s)e^{-\int_s^D \tau(t)dt}ds$$

 $I_0$  : background light

au(t) : extinction coefficient at t , related to the rate that light is occluded

D: total distance light will travel

 $e^{-\int_0^D au(t)dt}$  : transparency of medium between 0 and D

$$1-e^{-\int_0^D au(t)dt}=lpha$$
 : opacity of medium between 0 and D

