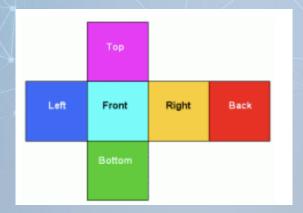
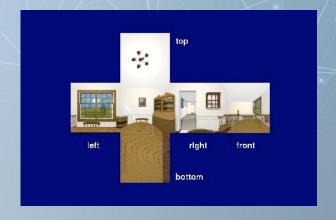


#### **Cubic Environment Mapping (Cubemap)**

- Introduced by Nate Green 1986
- Place the camera in the center of the environment and project it to 6 sides of a cube
- Cube map consists of six 2D images





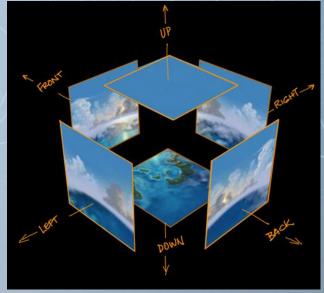
#### Cubic Environment Mapping (Cubemap)

- Applications
  - Skybox
  - Environment refraction
  - Environment reflection
  - Dynamic reflection

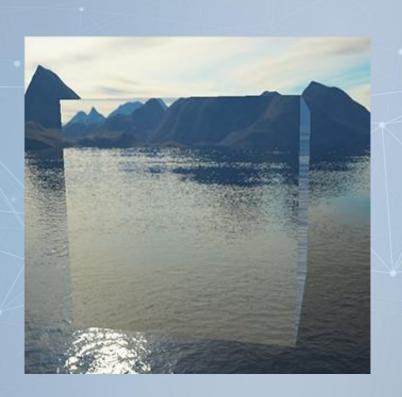
# Skybox

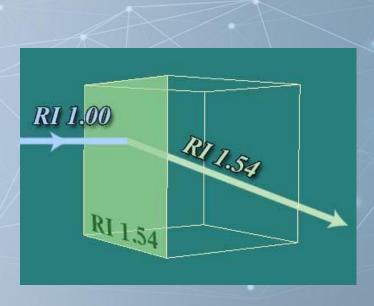
 The background comes from cube map images



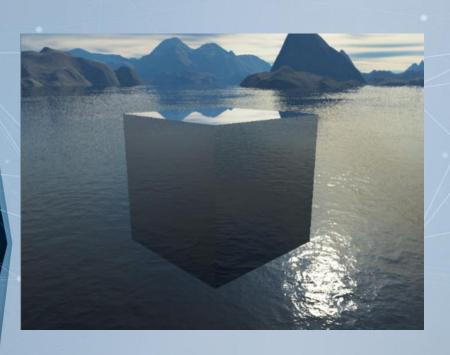


#### **Environment Refraction**



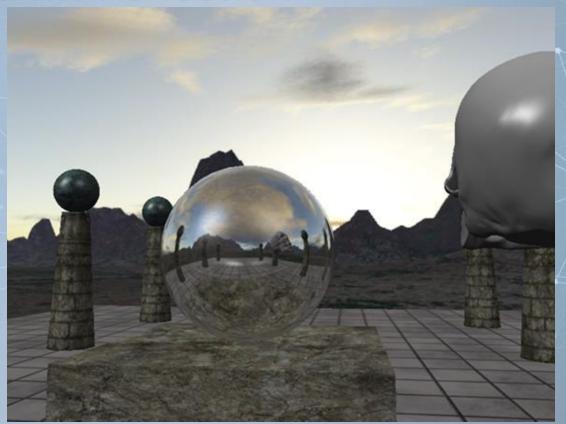


#### **Environment Reflection**





# **Dynamic Reflection**



### Skybox

- A large cube that encompass the entire scene
- Contains 6 images of a surrounding environment
- Let users/players the illusion that the environment he is in is much larger than it is
- Examples of skybox in video games: mountains, clouds or sky



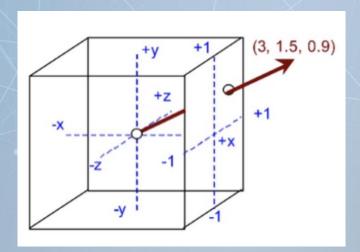
## Cubemap

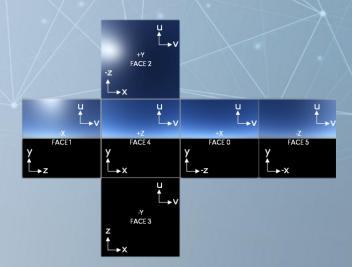
- The skypbox comes from a cubemap
- Cubemap consists of 6 images
- Load the images and use them to render the background



### Cubemap

- Cubemap is supported by WebGL
- After the 6 images (cubemap) is loaded, WebGL has a special texture, cubemap texture, to handle it
- You can use a vec3 to indicate a location and access a color on the cubemap
  - Between (+1, +1, +1) and (-1, -1, -1)





Load a cubemap and use it to color a cube

Files





- initCubeTexture() in WebGL.js
- Very similar to initalize a 2D texture
- Steps
  - Create a texture buffer
  - Bind the buffer to "gl.TEXTURE CUBE MAP"
  - Assign a loaded image to the appropriate target (ex: gl.TEXTURE\_CUBE\_MAP\_POSITIVE\_Y)
  - Configurate the cubemap
    - gl.texParameteri()

```
function initCubeTexture(posXName, negXName, posYName, negYName,
                        posZName, negZName, imgWidth, imgHeight)
 var texture = ql.createTexture();
 const faceInfos = [
     target: gl.TEXTURE_CUBE_MAP_POSITIVE_X,
     fName: posXName,
     target: gl.TEXTURE_CUBE_MAP_NEGATIVE_X,
     fName: negXName,
     target: gl.TEXTURE_CUBE_MAP_POSITIVE_Y,
     fName: posYName,
     target: gl.TEXTURE_CUBE_MAP_NEGATIVE_Y,
     fName: negYName.
     target: gl.TEXTURE_CUBE_MAP_POSITIVE_Z,
     fName: posZName,
     target: gl.TEXTURE_CUBE_MAP_NEGATIVE_Z,
     fName: negZName,
 faceInfos.forEach((faceInfo) => {
   const {target, fName} = faceInfo;
   // setup each face so it's immediately renderable (avoid error message)
   gl.bindTexture(gl.TEXTURE CUBE MAP, texture);
   gl.texImage2D(target, 0, gl.RGBA, imgWidth, imgHeight, 0,
                 gl.RGBA, gl.UNSIGNED_BYTE, null);
   var image = new Image();
   image.onload = function(){
     gl.bindTexture(gl.TEXTURE_CUBE_MAP, texture);
     gl.texImage2D(target, 0, gl.RGBA, gl.UNSIGNED_BYTE, image);
     gl.texParameteri(gl.TEXTURE_CUBE_MAP, gl.TEXTURE_MIN_FILTER, gl.LINEAR);
   image.src = fName;
 return texture;
```

- initCubeTexture() in WebGL.js
- Very similar to initalize a 2D texture
- Steps
  - Create a texture buffer
  - Bind the buffer to "gl.TEXTURE CUBE MAP"
  - Assign a loaded image to the appropriate target (ex: gl.TEXTURE\_CUBE\_MAP\_POSITIVE\_Y)
  - Configurate the cubemap
    - gl.texParameteri()

```
function initCubeTexture(posXName, negXName, posYName, negYName,
                        posZName, negZName, imgWidth, imgHeight)
 var texture = ql.createTexture();
 const faceInfos = [
     target: gl.TEXTURE_CUBE_MAP_POSITIVE_X,
     fName: posXName,
     target: gl.TEXTURE_CUBE_MAP_NEGATIVE_X,
     fName: negXName,
     target: gl.TEXTURE_CUBE_MAP_POSITIVE_Y,
     fName: posYName,
     target: gl.TEXTURE_CUBE_MAP_NEGATIVE_Y,
     fName: negYName.
     target: gl.TEXTURE_CUBE_MAP_POSITIVE_Z,
     fName: posZName,
     target: gl.TEXTURE_CUBE_MAP_NEGATIVE_Z,
     fName: negZName,
 faceInfos.forEach((faceInfo) => {
   const {target, fName} = faceInfo;
   // setup each face so it's immediately renderable (avoid error message)
   gl.bindTexture(gl.TEXTURE CUBE MAP, texture);
   gl.texImage2D(target, 0, gl.RGBA, imgWidth, imgHeight, 0,
                 gl.RGBA, gl.UNSIGNED_BYTE, null);
   var image = new Image();
   image.onload = function(){
     gl.bindTexture(gl.TEXTURE_CUBE_MAP, texture);
     gl.texImage2D(target, 0, gl.RGBA, gl.UNSIGNED_BYTE, image);
     gl.texParameteri(gl.TEXTURE_CUBE_MAP, gl.TEXTURE_MIN_FILTER, gl.LINEAR);
   image.src = fName;
 return texture;
```

- initCubeTexture() in WebGL.js
- Very similar to initalize a 2D texture
- Steps
  - Create a texture buffer
  - Bind the buffer to "gl.TEXTURE\_CUBE\_MAP"
  - Assign a loaded image to the appropriate target (ex: gl.TEXTURE CUBE MAP POSITIVE Y)
  - Configurate the cubemap
    - gl.texParameteri()

```
function initCubeTexture(posXName, negXName, posYName, negYName,
                        posZName, negZName, imgWidth, imgHeight)
 var texture = ql.createTexture();
 const faceInfos = [
     target: gl.TEXTURE_CUBE_MAP_POSITIVE_X,
     fName: posXName,
     target: gl.TEXTURE_CUBE_MAP_NEGATIVE_X,
     fName: negXName,
     target: gl.TEXTURE_CUBE_MAP_POSITIVE_Y,
     fName: posYName,
     target: gl.TEXTURE_CUBE_MAP_NEGATIVE_Y,
     fName: negYName.
     target: gl.TEXTURE_CUBE_MAP_POSITIVE_Z,
     fName: posZName,
     target: gl.TEXTURE_CUBE_MAP_NEGATIVE_Z,
     fName: negZName,
 faceInfos.forEach((faceInfo) => {
   const {target, fName} = faceInfo;
   // setup each face so it's immediately renderable (avoid error message)
   gl.bindTexture(gl.TEXTURE CUBE MAP, texture);
   gl.texImage2D(target, 0, gl.RGBA, imgWidth, imgHeight, 0,
                 gl.RGBA, gl.UNSIGNED_BYTE, null);
   var image = new Image();
    image.onload = function(){
     gl.bindTexture(gl.TEXTURE_CUBE_MAP, texture);
     gl.texImage2D(target, 0, gl.RGBA, gl.UNSIGNED_BYTE, image);
     gl.texParameteri(gl.TEXTURE_CUBE_MAP, gl.TEXTURE_MIN_FILTER, gl.LINEAR);
   image.src = fName;
 return texture;
```

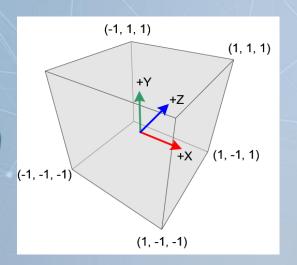
- initCubeTexture() in WebGL.js
- Very similar to initalize a 2D texture
- Steps
  - Create a texture buffer
  - Bind the buffer to "gl.TEXTURE CUBE MAP"
  - Assign a loaded image to the appropriate target (ex: gl.TEXTURE\_CUBE\_MAP\_POSITIVE\_Y)
  - Configurate the cubemap
    - gl.texParameteri()

```
function initCubeTexture(posXName, negXName, posYName, negYName,
                        posZName, negZName, imgWidth, imgHeight)
 var texture = gl.createTexture();
 const faceInfos = [
     target: gl.TEXTURE_CUBE_MAP_POSITIVE_X,
     fName: posXName,
     target: gl.TEXTURE_CUBE_MAP_NEGATIVE_X,
     fName: negXName,
      target: gl.TEXTURE_CUBE_MAP_POSITIVE_Y,
     fName: posYName,
     target: gl.TEXTURE_CUBE_MAP_NEGATIVE_Y,
     fName: negYName,
     target: gl.TEXTURE_CUBE_MAP_POSITIVE_Z,
     fName: posZName,
     target: gl.TEXTURE_CUBE_MAP_NEGATIVE_Z,
     fName: negZName,
 faceInfos.forEach((faceInfo) => {
   const {target, fName} = faceInfo;
   // setup each face so it's immediately renderable (avoid error message)
   gl.bindTexture(gl.TEXTURE CUBE MAP, texture);
   gl.texImage2D(target, 0, gl.RGBA, imgWidth, imgHeight, 0,
                 gl.RGBA, gl.UNSIGNED_BYTE, null);
   var image = new Image();
   image.onload = function(){
     gl.bindTexture(gl.TEXTURE_CUBE_MAP, texture);
     gl.texImage2D(target, 0, gl.RGBA, gl.RGBA, gl.UNSIGNED_BYTE, image);
     gl.texParameteri(gl.TEXTURE_CUBE_MAP, gl.TEXTURE_MIN_FILTER, gl.LINEAR);
   image.src = fName;
 return texture;
```

- initCubeTexture() in WebGL.js
- Very similar to initalize a 2D texture
- Steps
  - Create a texture buffer
  - Bind the buffer to "gl.TEXTURE\_CUBE\_MAP"
  - Assign a loaded image to the appropriate target (ex: gl.TEXTURE\_CUBE\_MAP\_POSITIVE\_Y)
  - Configurate the cubemap
    - gl.texParameteri()

```
function initCubeTexture(posXName, negXName, posYName, negYName,
                        posZName, negZName, imgWidth, imgHeight)
 var texture = ql.createTexture();
 const faceInfos = [
     target: gl.TEXTURE_CUBE_MAP_POSITIVE_X,
     fName: posXName,
     target: gl.TEXTURE_CUBE_MAP_NEGATIVE_X,
     fName: negXName,
     target: gl.TEXTURE_CUBE_MAP_POSITIVE_Y,
     fName: posYName,
     target: gl.TEXTURE_CUBE_MAP_NEGATIVE_Y,
     fName: negYName.
     target: gl.TEXTURE_CUBE_MAP_POSITIVE_Z,
     fName: posZName,
     target: gl.TEXTURE_CUBE_MAP_NEGATIVE_Z,
     fName: negZName,
 faceInfos.forEach((faceInfo) => {
   const {target, fName} = faceInfo;
   // setup each face so it's immediately renderable (avoid error message)
   gl.bindTexture(gl.TEXTURE CUBE MAP, texture);
   gl.texImage2D(target, 0, gl.RGBA, imgWidth, imgHeight, 0,
                 gl.RGBA, gl.UNSIGNED_BYTE, null);
   var image = new Image();
   image.onload = function(){
     gl.bindTexture(gl.TEXTURE_CUBE_MAP, texture);
     gl.texImage2D(target, 0, gl.RGBA, gl.UNSIGNED_BYTE, image);
     gl.texParameteri(gl.TEXTURE_CUBE_MAP, gl.TEXTURE_MIN_FILTER, gl.LINEAR);
   image.src = fName;
 return texture;
```

- main() in WebGL.js
- Load a cube from obj



```
async function main(){
   canvas = document.getElementById('webgl');
   gl = canvas.getContext('webgl2');
   if(!ql){
       console.log('Failed to get the rendering context for WebGL');
       return:
   response = await fetch('cube.obj');
   text = await response.text();
   obj = parseOBJ(text);
   for( let i=0; i < obj.geometries.length; i ++ ){</pre>
     let o = initVertexBufferForLaterUse(gl,
                                          obj.geometries[i].data.position,
                                          obj.geometries[i].data.normal,
                                          obj.geometries[i].data.texcoord);
     cubeObj.push(o);
   program = compileShader(gl, VSHADER_SOURCE, FSHADER_SOURCE);
   program.a_Position = gl.getAttribLocation(program, 'a_Position');
   program.u_MvpMatrix = gl.getUniformLocation(program, 'u_MvpMatrix');
   program.u_envCubeMap = gl.getUniformLocation(program, 'u_envCubeMap');
   gl.useProgram(program);
   cubeMapTex = initCubeTexture("pos-x.jpg", "neg-x.jpg", "pos-y.jpg", "neg-y.jpg",
                                      "pos-z.jpg", "neg-z.jpg", 512, 512)
   canvas.onmousedown = function(ev){mouseDown(ev)};
   canvas.onmousemove = function(ev){mouseMove(ev)};
   canvas.onmouseup = function(ev){mouseUp(ev)};
```

- Pass the cube map texture to shader
- Similar to passing 2D texture
  - But the target is "gl.TEXTURE\_CUBE\_MAP"

```
function draw(){
 gl.useProgram(program);
 gl.viewport(0, 0, canvas.width, canvas.height);
 gl.clearColor(0.4,0.4,0.4,1);
 gl.clear(gl.COLOR_BUFFER_BIT | gl.DEPTH_BUFFER_BIT);
 gl.enable(gl.DEPTH_TEST);
 var mvpFromCamera = new Matrix4();
 // //model Matrix (part of the mvp matrix)
 let modelMatrix = new Matrix4();
 modelMatrix.setRotate(angleY, 1, 0, 0);//for mouse rotation
 modelMatrix.rotate(angleX, 0, 1, 0);//for mouse rotation
 let cubeMdlMatrix = new Matrix4();
 cubeMdlMatrix.setScale(2.0, 2.0, 2.0);
 modelMatrix.multiply(cubeMdlMatrix);
 // //mvp: projection * view * model matrix
 mvpFromCamera.setPerspective(60, 1, 1, 15);
 mvpFromCamera.lookAt(cameraX, cameraY, cameraZ, 0, 0, 0, 0, 1, 0);
 mvpFromCamera.multiply(modelMatrix);
 ql.uniformMatrix4fv(program.u_MvpMatrix, false, mvpFromCamera.elements);
 gl.activeTexture(gl.TEXTURE0);
 gl.bindTexture(gl.TEXTURE_CUBE_MAP, cubeMapTex)
 gl.uniform1i(program.u_envCubeMap, 0);
 gl.useProgram(program);
 gl.uniformMatrix4fv(program.u_MvpMatrix, false, mvpFromCamera.elements);
 for( let i=0; i < cubeObj.length; i ++ ){</pre>
   initAttributeVariable(ql, program.a_Position, cubeObj[i].vertexBuffer);
   gl.drawArrays(gl.TRIANGLES, 0, cubeObj[i].numVertices);
```

- Shader in WebGL.js
- Variable type to represent the cubemap texture: "samplerCube"

 Access color from the cube map: textureCube()

```
var VSHADER_SOURCE = `
 attribute vec4 a_Position;
 varying vec4 v TexCoord;
 uniform mat4 u_MvpMatrix;
 void main() {
   gl_Position = u_MvpMatrix * a_Position;
   v TexCoord = a Position;
var FSHADER SOURCE = `
 precision mediump float;
 varying vec4 v_TexCoord;
 uniform samplerCube u_envCubeMap;
 void main() {
  _gl_FragColor = textureCube(u_envCubeMap, v_TexCoord.stp);
```

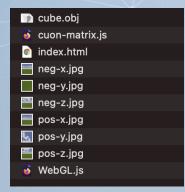
## Try and Think (5mins)

Download the code and run

- Make sure you know how to load cube map image, pass the cube map texture to shader and access color from the cube map texture
- If you move the camera into the cube, what you see?
  - Set cameraX, cameraY, cameraZ to 0, 0 and 0.001, respectively

- Instead of using model matrix to rotate a object, we want move the camera (player) and rotate the view of the camera in the scene
  - Move the camera position if users press 'w' or 's' (move forward or backward)
  - change the view direction if users use mouse to drag and move

• / Files





I have one more variable set for view direction

```
var mouseLastX, mouseLastY;
var mouseDragging = false;
var angleX = 0, angleY = 0;
var gl, canvas;
var modelMatrix;
var nVertex;

var cameraX = 0, cameraY = 0, cameraZ = 0;
var cameraDirX = 0, cameraDirY = 0, cameraDirZ = 1;
var cubeObj = [];
var cubeMapTex;
```

- draw() in WebGL.js
- Now, we rotate the view direction by the information / stored in "angleX" and "angleY"
- Then, use the camera position and the look-at point (camera position + view direction) to set the view matrix

```
function draw(){
 gl.useProgram(program);
 gl.viewport(0, 0, canvas.width, canvas.height);
 gl.clearColor(0.4,0.4,0.4,1);
 gl.clear(gl.COLOR_BUFFER_BIT | gl.DEPTH_BUFFER_BIT);
 ql.enable(ql.DEPTH TEST);
 var mvpFromCamera = new Matrix4();
 // //model Matrix (part of the mvp matrix)
 let modelMatrix = new Matrix4();
 modelMatrix.setScale(2.0, 2.0, 2.0);
 // //mvp: projection * view * model matrix
 mvpFromCamera.setPerspective(60, 1, 1, 15);
 let rotateMatrix = new Matrix4();
 rotateMatrix.setRotate(angleY, 1, 0, 0);//for mouse rotation
 rotateMatrix.rotate(angleX, 0, 1, 0);//for mouse rotation
 var viewDir= new Vector3([cameraDirX, cameraDirY, cameraDirZ]);
 var newViewDir = rotateMatrix.multiplyVector3(viewDir);
 mvpFromCamera.lookAt(cameraX, cameraY, cameraZ,
                      cameraX + newViewDir.elements[0],
                      cameraY + newViewDir.elements[1],
                      cameraZ + newViewDir.elements[2],
                      0, 1, 0);
 mvpFromCamera.multiply(modelMatrix);
 ql.uniformMatrix4fv(program.u_MvpMatrix, false, mvpFromCamera.elements);
 gl.activeTexture(gl.TEXTURE0);
 gl.bindTexture(gl.TEXTURE_CUBE_MAP, cubeMapTex);
 gl.uniform1i(program.u_envCubeMap, 0);
 gl.useProgram(program);
 gl.uniformMatrix4fv(program.u_MvpMatrix, false, mvpFromCamera.elements);
 for( let i=0; i < cubeObj.length; i ++ ){</pre>
   initAttributeVariable(gl, program.a_Position, cubeObj[i].vertexBuffer);
   gl.drawArrays(gl.TRIANGLES, 0, cubeObj[i].numVertices);
```

- draw() in WebGL.js
- Now, we rotate the view direction by the information stored in "angleX" and "angleY"
- Then, use the camera position and the look-at point (camera position + view direction) to set the view matrix

```
function draw(){
 gl.useProgram(program);
 gl.viewport(0, 0, canvas.width, canvas.height);
 gl.clearColor(0.4,0.4,0.4,1);
 gl.clear(gl.COLOR_BUFFER_BIT | gl.DEPTH_BUFFER_BIT);
 ql.enable(ql.DEPTH TEST);
 var mvpFromCamera = new Matrix4();
 // //model Matrix (part of the mvp matrix)
 let modelMatrix = new Matrix4();
 modelMatrix.setScale(2.0, 2.0, 2.0);
 // //mvp: projection * view * model matrix
 mvpFromCamera.setPerspective(60, 1, 1, 15);
 let rotateMatrix = new Matrix4();
 rotateMatrix.setRotate(angleY, 1, 0, 0);//for mouse rotation
 rotateMatrix.rotate(angleX, 0, 1, 0);//for mouse rotation
 var viewDir= new Vector3([cameraDirX, cameraDirY, cameraDirZ]);
 var newViewDir = rotateMatrix.multiplyVector3(viewDir);
 mvpFromCamera.lookAt(cameraX, cameraY, cameraZ,
                      cameraX + newViewDir.elements[0],
                      cameraY + newViewDir.elements[1],
                      cameraZ + newViewDir.elements[2],
                      0, 1, 0);
 mvpFromCamera.multiply(modelMatrix);
 ql.uniformMatrix4fv(program.u_MvpMatrix, false, mvpFromCamera.elements);
 gl.activeTexture(gl.TEXTURE0);
 gl.bindTexture(gl.TEXTURE_CUBE_MAP, cubeMapTex);
 gl.uniform1i(program.u_envCubeMap, 0);
 gl.useProgram(program);
 gl.uniformMatrix4fv(program.u_MvpMatrix, false, mvpFromCamera.elements);
 for( let i=0; i < cubeObj.length; i ++ ){</pre>
   initAttributeVariable(gl, program.a_Position, cubeObj[i].vertexBuffer);
   gl.drawArrays(gl.TRIANGLES, 0, cubeObj[i].numVertices);
```

- keydown() in WebGL.js
- Add a keyboard event to move the camera position
- 'w': move forward along the view direction
- 's': move backward along the view direction

```
function keydown(ev){
 //implment keydown event here
 let rotateMatrix = new Matrix4():
 rotateMatrix.setRotate(angleY, 1, 0, 0);//for mouse rotation
 rotateMatrix.rotate(angleX, 0, 1, 0);//for mouse rotation
 var viewDir= new Vector3([cameraDirX, cameraDirY, cameraDirZ]);
 var newViewDir = rotateMatrix.multiplyVector3(viewDir);
 if(ev.key == 'w'){
     cameraX += (newViewDir.elements[0] * 0.1):
     cameraY += (newViewDir.elements[1] * 0.1);
     cameraZ += (newViewDir.elements[2] * 0.1);
 else if(ev.key == 's'){
   cameraX -= (newViewDir.elements[0] * 0.1);
   cameraY -= (newViewDir.elements[1] * 0.1);
   cameraZ -= (newViewDir.elements[2] * 0.1);
 draw();
```

## Try and Think (5mins)

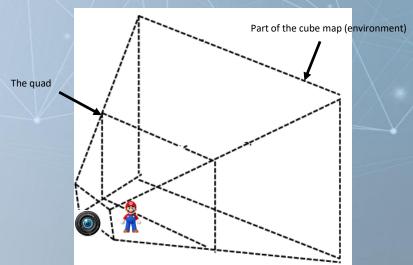
- Download and run the code
- Keep moving, do you go out the skybox?
- We usually want to keep staying in the skybox, how to solve this problem?



- We should never go out of the skybox
  - The environment cube supposes to stay at infinite distance
- Instead of coloring an "real cube", draw a quad which covers the whole camera view
  - Put the quad behind all the objects you want to render
  - Project the cube map to the quad
    - Only the rotation of the view has impact on this projection (do not consider translation)

Files





- In main() WebGL.js
- We define a quad and the coordinate here is in "clip space"
  - We will NOT transform it in vertex shader
  - Z of this quad is 1:
    - we want the quad always behind all objects
    - Any object with z grater than 1 will be clipped out

```
async function main(){
   canvas = document.getElementById('webgl');
   gl = canvas.getContext('webgl2');
   if(!al){
       console.log('Failed to get the rendering context for WebGL');
   var quad = new Float32Array(
       -1, -1, 1,
        1. -1. 1.
       -1, 1, 1,
        1, -1, 1,
        1, 1, 1
     ]); //just a quad
   programEnvCube = compileShader(ql, VSHADER SOURCE ENVCUBE, FSHADER SOURCE ENVCUBE);
   programEnvCube.a Position = ql.getAttribLocation(programEnvCube, 'a Position');
   programEnvCube.u_envCubeMap = gl.getUniformLocation(programEnvCube, 'u_envCubeMap');
   programEnvCube.u viewDirectionProjectionInverse =
              ql.qetUniformLocation(programEnvCube, 'u viewDirectionProjectionInverse');
   quadObj = initVertexBufferForLaterUse(ql, quad);
   cubeMapTex = initCubeTexture("pos-x.jpg", "neg-x.jpg", "pos-y.jpg", "neg-y.jpg",
                                      "pos-z.jpg", "neg-z.jpg", 512, 512)
   canvas.onmousedown = function(ev){mouseDown(ev)};
   canvas.onmousemove = function(ev){mouseMove(ev)};
   canvas.onmouseup = function(ev){mouseUp(ev)};
   document.onkeydown = function(ev){keydown(ev)};
```

- Shaders in WebGL.js
- The quad vertices is already in clip space, so we direct assign it to gl Position
- We also pass the quad vertices coordinates to fragment shader

```
var VSHADER SOURCE ENVCUBE =
 attribute vec4 a_Position;
 varying vec4 v_Position;
 void main() {
   v_Position = a_Position;
   gl_Position = a_Position;
var FSHADER_SOURCE_ENVCUBE = `
 precision mediump float;
 uniform samplerCube u_envCubeMap;
 uniform mat4 u viewDirectionProjectionInverse;
 varying vec4 v_Position;
 void main() {
   vec4 t = u_viewDirectionProjectionInverse * v_Position;
   gl_FragColor = textureCube(u_envCubeMap, normalize(t.xyz / t.w));
```

- Shaders in WebGL.js
- To project the environment cube map to the quad, we should look up the color from the cube map to color the quad
- This look-up behavior depends on which direction the user is looking at (about the view matrix)
- We only know the coordinates on the quad (v\_Position) and the coordinate is defined in the clip space
- To look up the color from the cube map, we need the direction vector defined in world space (of course, environment is in the world space)
- We know:
  - $C_{clip} = M_{proj} * M_{view} * C_{world}$
  - $\left(M_{proj} * M_{view}\right)^{-1} * C_{clip} = C_{world}$

```
var VSHADER SOURCE ENVCUBE =
 attribute vec4 a_Position;
 varying vec4 v_Position;
 void main() {
   v_Position = a_Position;
   gl_Position = a_Position;
var FSHADER_SOURCE_ENVCUBE = `
 precision mediump float;
 uniform samplerCube u_envCubeMap;
 uniform mat4 u viewDirectionProjectionInverse;
 varying vec4 v_Position;
 void main() {
   vec4 t = u_viewDirectionProjectionInverse * v_Position;
   gl_FragColor = textureCube(u_envCubeMap, normalize(t.xyz / t.w));
```

- draw() in WebGL.js
- Prepare  $(M_{proj} * M_{view})^{-1}$  and pass it into the shader

```
function draw(){
 gl.viewport(0, 0, canvas.width, canvas.height);
 gl.clearColor(0.4, 0.4, 0.4, 1);
 gl.clear(gl.COLOR_BUFFER_BIT | gl.DEPTH_BUFFER_BIT);
 gl.enable(gl.DEPTH_TEST);
 let rotateMatrix = new Matrix4();
 rotateMatrix.setRotate(angleY, 1, 0, 0);//for mouse rotation
 rotateMatrix.rotate(angleX, 0, 1, 0);//for mouse rotation
 var viewDir= new Vector3([cameraDirX, cameraDirY, cameraDirZ]);
 var newViewDir = rotateMatrix.multiplyVector3(viewDir);
 var vpFromCamera = new Matrix4();
 vpFromCamera.setPerspective 60, 1, 1, 15);
 var viewMatrixRotationUnity = new Matrix4();
 viewMatrixRotationOnly.lookAt cameraX, cameraY, cameraZ,
                               cameraX + newViewDir.elements[0],
                               cameraY + newViewDir.elements[1],
                               cameraZ + newViewDir.elements[2],
                               0, 1, 0);
 viewMatrixRotationOnly.elements[12] = 0; //ignore translation
 viewMatrixRotationOnly.elements[13] = 0;
 viewMatrixRotationOnly.elements[14] = 0;
 vpFromCamera.multiply(viewMatrixRotationOnly);
 var vpFromCameraInverse = vpFromCamera.invert();
 gl.useProgram(programEnvCube);
 gl.depthFunc(gl.LEQUAL);
 ql.uniformMatrix4fv(programEnvCube.u viewDirectionProjectionInverse,
        false, vpFromCameraInverse.elements);
 gl.activeTexture(gl.TEXTURE0);
 gl.bindTexture(gl.TEXTURE_CUBE_MAP, cubeMapTex);
 gl.uniform1i(programEnvCube.u_envCubeMap, 0);
 initAttributeVariable(gl, programEnvCube.a_Position, quadObj.vertexBuffer);
 gl.drawArrays(gl.TRIANGLES, 0, quadObj.numVertices);
```

- draw() in WebGL.js
- Although the player (camera) can move, we want to ignore the camera translation when draw the environment
  - We assume the environment cube is at the infinite distance.
  - The local camera move (translation) will not affect what the camera can see about the environment
- We ignore the view translation by setting  $m_{12}$ ,  $m_{13}$ ,  $m_{14}$  ( $\frac{m_0}{m_1}$ ,  $\frac{m_4}{m_5}$ ,  $\frac{m_6}{m_1}$ ,  $\frac{m_{12}}{m_2}$ ) to 0
  - Because  $m_{12}$ ,  $m_{13}$ ,  $m_{14}$  in view matrix are responsible for camera translation

```
function draw(){
 gl.viewport(0, 0, canvas.width, canvas.height);
 gl.clearColor(0.4, 0.4, 0.4, 1);
 gl.clear(gl.COLOR_BUFFER_BIT | gl.DEPTH_BUFFER_BIT);
 gl.enable(gl.DEPTH_TEST);
 let rotateMatrix = new Matrix4();
 rotateMatrix.setRotate(angleY, 1, 0, 0);//for mouse rotation
 rotateMatrix.rotate(angleX, 0, 1, 0);//for mouse rotation
 var viewDir= new Vector3([cameraDirX, cameraDirY, cameraDirZ]);
 var newViewDir = rotateMatrix.multiplyVector3(viewDir);
 var vpFromCamera = new Matrix4();
 vpFromCamera.setPerspective(60, 1, 1, 15);
 var viewMatrixRotationOnly = new Matrix4();
 viewMatrixRotationOnly.lookAt(cameraX, cameraY, cameraZ,
                               cameraX + newViewDir.elements[0],
                               cameraY + newViewDir.elements[1],
                               cameraZ + newViewDir.elements[2],
                               0, 1, 0);
 viewMatrixRotationOnly.elements[12] = 0; //ignore translation
 viewMatrixRotationOnly.elements[13] = 0;
 viewMatrixRotationOnly.elements[14] = 0;
 vpFromCamera.multiply(viewMatrixRotationOnly);
 var vpFromCameraInverse = vpFromCamera.invert();
 gl.useProgram(programEnvCube);
 gl.depthFunc(gl.LEQUAL);
 ql.uniformMatrix4fv(programEnvCube.u viewDirectionProjectionInverse,
                     false, vpFromCameraInverse.elements);
 gl.activeTexture(gl.TEXTURE0);
 gl.bindTexture(gl.TEXTURE_CUBE_MAP, cubeMapTex);
 gl.uniform1i(programEnvCube.u_envCubeMap, 0);
 initAttributeVariable(gl, programEnvCube.a_Position, quadObj.vertexBuffer);
 gl.drawArrays(gl.TRIANGLES, 0, quadObj.numVertices);
```

- draw() in WebGL.js
- gl.depthFunc()
  - Set what z value is possible to pass the depth buffer (in depth test)
  - By default, it is gl.depthFunc(gl.LESS), the value is smaller than current buffer value is possible to pass
  - We set the z of the quad at 1 and we want it is possible to pass the depth test. (the initial depth buffer value is 1)
    - gl.depthFunc(gl.LEQUAL): less ang equal
  - https://developer.mozilla.org/en-US/docs/Web/API/WebGLRenderingC ontext/depthFunc

```
function draw(){
 gl.viewport(0, 0, canvas.width, canvas.height);
 gl.clearColor(0.4, 0.4, 0.4, 1);
 gl.clear(gl.COLOR_BUFFER_BIT | gl.DEPTH_BUFFER_BIT);
 gl.enable(gl.DEPTH_TEST);
 let rotateMatrix = new Matrix4();
 rotateMatrix.setRotate(angleY, 1, 0, 0);//for mouse rotation
 rotateMatrix.rotate(angleX, 0, 1, 0);//for mouse rotation
 var viewDir= new Vector3([cameraDirX, cameraDirY, cameraDirZ]);
 var newViewDir = rotateMatrix.multiplyVector3(viewDir);
 var vpFromCamera = new Matrix4():
 vpFromCamera.setPerspective(60, 1, 1, 15);
 var viewMatrixRotationOnly = new Matrix4();
 viewMatrixRotationOnly.lookAt(cameraX, cameraY, cameraZ,
                               cameraX + newViewDir.elements[0],
                               cameraY + newViewDir.elements[1],
                               cameraZ + newViewDir.elements[2],
                               0, 1, 0);
 viewMatrixRotationOnly.elements[12] = 0; //ignore translation
 viewMatrixRotationOnly.elements[13] = 0;
 viewMatrixRotationOnly.elements[14] = 0;
 vpFromCamera.multiply(viewMatrixRotationOnly);
 var vpFromCameraInverse = vpFromCamera.invert();
 gl.useProgram(programEnvCube);
 gl.depthFunc(gl.LEQUAL);
 ql.uniformMatrix4fv(programEnvCube.u viewDirectionProjectionInverse,
                     false, vpFromCameraInverse.elements);
 gl.activeTexture(gl.TEXTURE0);
 gl.bindTexture(gl.TEXTURE_CUBE_MAP, cubeMapTex);
 gl.uniform1i(programEnvCube.u_envCubeMap, 0);
 initAttributeVariable(gl, programEnvCube.a_Position, quadObj.vertexBuffer);
 gl.drawArrays(gl.TRIANGLES, 0, quadObj.numVertices);
```

### Try and Think (5mins)

- Download and run Ex10-3
- It looks like you never move, when you press "w" and "s". However, you move.
- I use console.log() to output the camera position (x, y, z in world space) in console when you press "w" or "s". You can check.
- Think why you don't see any change even if the camera move?
- And, is this what we want?
  - The answer is YES.
  - The environment you can see should not change if you only move forward or backward (no camera rotation) because the environment background suppose to stay at infinite distance
  - If you add objects around you, you will realize you actually move