Data Mining

Practical Machine Learning Tools and Techniques

Slides for Chapter 12, Ensemble learning

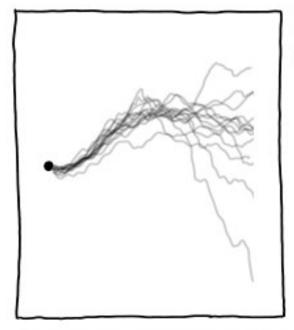
of *Data Mining* by I. H. Witten, E. Frank, M. A. Hall and C. J. Pal

Ensemble learning

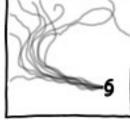
- Combining multiple models
 - The basic idea
- Bagging
 - Bias-variance decomposition, bagging with costs
- Randomization
 - Random forests, rotation forests
- Boosting
 - AdaBoost, the power of boosting
- Additive regression
 - Numeric prediction, additive logistic regression
- Interpretable ensembles
 - Option trees, alternating decision trees, logistic model trees
- Stacking

Ensemble Models

IN AN ENSEMBLE MODEL, FORECASTERS RUN MANY DIFFERENT VERSIONS OF A WEATHER MODEL WITH SUGHTLY DIFFERENT INITIAL CONDITIONS. THIS HELPS ACCOUNT FOR UNCERTAINTY AND SHOWS FORECASTERS A SPREAD OF POSSIBLE OUTCOMES.







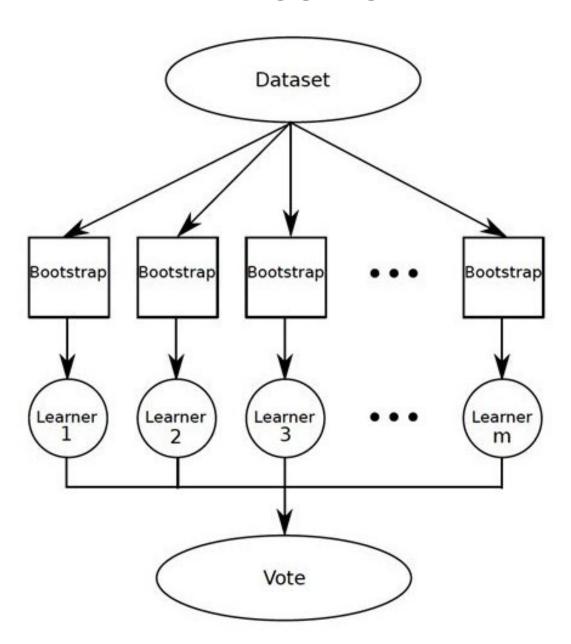
MEMBERS IN A TYPICAL ENSEMBLE: A UNIVERSE WHERE...

- ... RAIN IS 0.5% MORE LIKELY IN SOME AREAS
- ... WIND SPEEDS ARE SLIGHTLY LOWER
- ...PRESSURE LEVELS ARE RANDOMLY TWEAKED
- ...DOGS RUN SLIGHTLY FASTER
- ... THERE'S ONE EXTRA CLOUD IN THE BAHAMAS
- ...GERMANY WON WWII
- ... SNAKES ARE WIDE INSTEAD OF LONG
- ...WILL SMITH TOOK THE LEAD IN THE MATRIX
 INSTEAD OF WILD WILD WEST
- ... SWIMMING POOLS ARE CARBONATED
- ...SLICED BREAD, AFTER BEING BANNED IN JANUARY 1943, WAS NEVER RE-LEGALIZED

Combining multiple models

- Basic idea: build different "experts", let them vote
- Advantage:
 - often improves predictive performance
- Disadvantage:
 - usually produces output that is very hard to analyze
 - but: there are approaches that aim to produce a single comprehensible structure

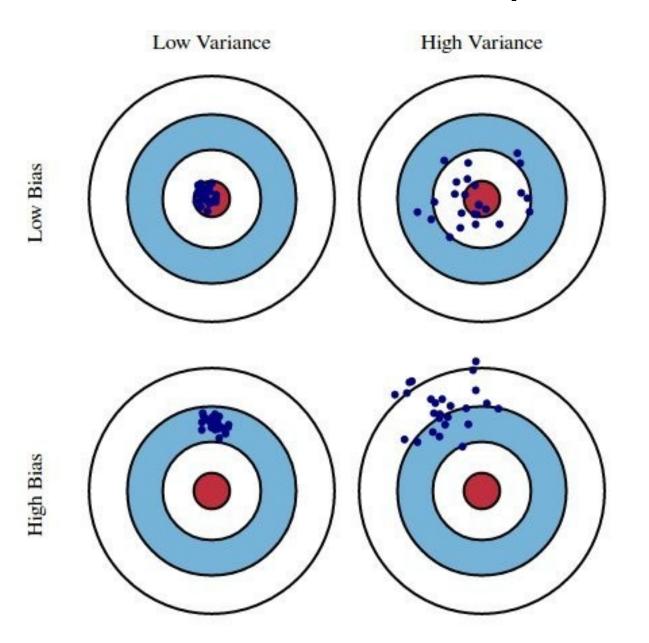
Bagging



Bagging

- Combining predictions by voting/averaging
 - Each model receives equal weight
- "Idealized" version:
 - Sample several training sets of size n
 (instead of just having one training set of size n)
 - Build a classifier for each training set
 - Combine the classifiers' predictions
- Learning scheme is unstable ⇒
 almost always improves performance
 - Unstable learner: small change in training data can make big change in model (e.g., when learning decision trees)

Bias-variance decomposition



Bias-variance decomposition

- The bias-variance decomposition is used to analyze how much restriction to a single training set affects performance
- Assume we have the idealized ensemble classifier discussed on the previous slide
- We can decompose the expected error of any individual ensemble member as follows:
 - Bias = expected error of the ensemble classifier on new data
 - Variance = component of the expected error due to the particular training set being used to built our classifier
 - Total expected error ⇒ bias + variance
- Note (A): we assume noise inherent in the data is part of the bias component as it cannot normally be measured
- Note (B): multiple versions of this decomposition exist for zero-one loss but the basic idea is always the same

More on bagging

- The idealized version of bagging improves performance because it eliminates the variance component of the error
 - Note: in some pathological hypothetical situations the overall error may increase when zero-one loss is used (i.e., there is negative "variance")
 - The bias-variance decomposition was originally only known for numeric prediction with squared error where the error never increases
- Problem: we only have one dataset!
- Solution: generate new datasets of size n by sampling from the original dataset with replacement
- This is what bagging does and even though the datasets are all dependent, bagging often reduces variance, and, thus, error
 - Can be applied to numeric prediction and classification
 - Can help a lot if the data is noisy
 - Usually, the more classifiers the better, with diminishing returns

Bagging classifiers

Model generation

```
Let n be the number of instances in the training data

For each of t iterations:

Sample n instances from training set

(with replacement)

Apply learning algorithm to the sample

Store resulting model
```

Classification

```
For each of the t models:

Predict class of instance using model
Return class that is predicted most often
```

Bagging with costs

- Bagging unpruned decision trees is known to produce good probability estimates
 - Where, instead of voting, the individual classifiers' probability estimates are averaged
 - Note: this can also improve the zero-one loss
- Can use this with the minimum-expected cost approach for learning problems with costs
 - Note that the minimum-expected cost approach requires accurate probabilities to work well
- Problem: ensemble classifier is not interpretable
 - MetaCost re-labels the training data using bagging with costs and then builds a single tree from this data

Randomization and random forests

- Can randomize learning algorithm instead of input
- Some algorithms already have a random component: e.g., initial weights in a neural net
- Most algorithms can be randomized, e.g., greedy algorithms:
 - Pick N options at random from the full set of options, then choose the best of those N choices
 - E.g.: attribute selection in decision trees
- More generally applicable than bagging: e.g., we can use random subsets in a nearest-neighbor classifier
 - Bagging does not work with stable classifiers such as nearest neighbour classifiers
- Can be combined with bagging
 - When using decision trees, this yields the famous random forest method for building ensemble classifiers

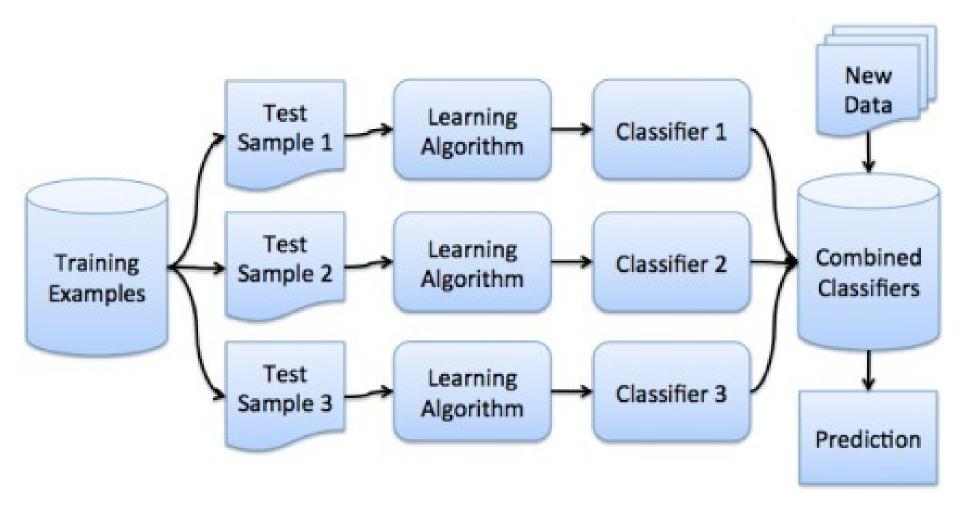
Rotation forests: motivation

- Bagging creates ensembles of accurate classifiers with relatively low diversity
 - Bootstrap sampling creates training sets with a distribution that resembles the original data
- Randomness in the learning algorithm increases diversity but sacrifices accuracy of individual ensemble members
 - This is why random forests normally require hundreds or thousands of ensemble members to achieve their best performance
- So-called *rotation forests* have the goal of creating accurate **and** diverse ensemble members

Rotation forests

- Combine random attribute sets, bagging and principal components to generate an ensemble of decision trees
- An iteration of the algorithm for creating rotation forests, building k ensemble members, involves
 - Randomly dividing the input attributes into k disjoint subsets
 - Applying PCA to each of the k subsets in turn
 - Learning a decision tree from the k sets of PCA directions
- Further increases in diversity can be achieved by creating a bootstrap sample in each iteration before applying PCA
- Performance of this method compares favorably to that of random forests on many practical datasets

Boosting



Boosting

- Bagging can easily be parallelized because ensemble members are created independently
- Boosting is an alternative approach
- Also uses voting/averaging
- But: weights models according to performance
- Iterative: new models are influenced by performance of previously built ones
 - Encourage new model to become an "expert" for instances misclassified by earlier models
 - Intuitive justification: models should be experts that complement each other
- Many variants of boosting exist, we cover a couple

Boosting using AdaBoost.M1

Model generation

```
Assign equal weight to each training instance
For t iterations:

Apply learning algorithm to weighted dataset,
store resulting model

Compute model's error e on weighted dataset

If e = 0 or e > 0.5:
Terminate model generation

For each instance in dataset:
If classified correctly by model:
Multiply instance's weight by e/(1-e)

Normalize weight of all instances
```

Classification

```
Assign weight = 0 to all classes

For each of the t (or less) models:

For the class this model predicts

add -log e/(1-e) to this class's weight

Return class with highest weight
```

Comments on AdaBoost.M1

- Boosting needs weights ... but
- can adapt learning algorithm ... or
- can apply boosting without weights:
 - Resample data with probability determined by weights
 - Disadvantage: not all instances are used
 - Advantage: if error > 0.5, can resample again
- The AdaBoost.M1 boosting algorithm stems from work in computational learning theory
- Theoretical result:
 - Training error decreases exponentially as iterations are performed
- Other theoretical results:
 - Works well if base classifiers are not too complex and
 - their error does not become too large too quickly as more iterations are performed

More comments on boosting

- Continue boosting after training error = 0?
- Puzzling fact: generalization error continues to decrease!
 - Seems to contradict Occam's Razor
- Possible explanation: consider margin (confidence), not just error
 - A possible definition of *margin*: difference between estimated probability for true class and nearest other class (between -1 and 1)
 - Margin continues to increase with more iterations
- AdaBoost.M1 works well with so-called weak learners; only condition: error does not exceed 0.5
 - Example of weak learner: decision stump
- In practice, boosting sometimes overfits if too many iterations are performed (in contrast to bagging)

Additive regression

- Using statistical terminology, boosting is a greedy algorithm for fitting an additive model
- More specifically, it implements forward stagewise additive modeling
- Forward stagewise additive modeling for numeric prediction:
 - 1. Build standard regression model (e.g., regression tree)
 - Gather residuals, learn model predicting residuals (e.g. another regression tree), and repeat
- To predict, simply sum up individual predictions from all regression models

Comments on additive regression

- Additive regression greedily minimizes squared error of ensemble if base learner minimizes squared error
- Note that it does not make sense to use additive regression with standard multiple linear regression
 - Why? Sum of linear regression models is a linear regression model and linear regression already minimizes squared error
- But: can use forward stagewise additive modeling with *simple* linear regression to implement multiple linear regression
 - Idea: build simple (i.e., one-attribute) linear regression models in each iteration of additive regression, pick attribute that yields lowest error
 - Use cross-validation to decide when to stop performing iterations
 - Automatically performs attribute selection!
- A trick to combat overfitting in additive regression: shrink predictions of base models by multiplying with pos. constant < 1
 - Caveat: need to start additive regression with initial model that predicts the mean, in order to shrink towards the mean, not 0

Additive logistic regression

- Can apply additive regression in conjunction with the logit transformation to get an algorithm for classification
 - More precisely, an algorithm for class probability estimation
 - Probability estimation problem is transformed into a regression problem
 - Regression scheme is used as base learner (e.g., regression tree learner)
- Implemented using forward stagewise algorithm: at each stage, add base model that maximizes the probability of the data
- We consider two-class classification in the following
- If f_j is the jth regression model, and \mathbf{a} is an instance, the ensemble predicts probability $p(1|\vec{a}) = \frac{1}{1 + \exp(-\sum f_j(\vec{a}))}$

LogitBoost

Model generation

```
For j = 1 to t iterations:
   For each instance a[i]:
     Set the target value for the regression to
     z[i] = (y[i] - p(1|a[i])) / [p(1|a[i]) × (1-p(1|a[i])]
     Set the weight of instance a[i] to p(1|a[i]) × (1-p(1|a[i])
     Fit a regression model f[j] to the data with class
     values z[i] and weights w[i]
```

Classification

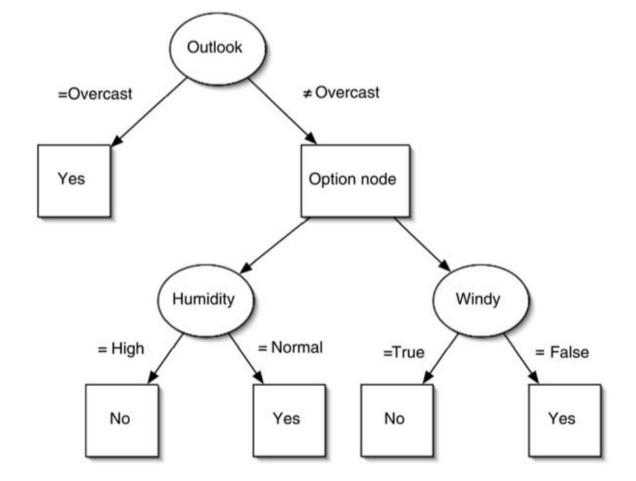
```
Predict 1^{st} class if p(1 \mid a) > 0.5, otherwise predict 2^{nd} class
```

- Greedily maximizes probability if base learner minimizes squared error
- Difference to AdaBoost.M1: optimizes probability/likelihood instead of a special loss function called exponential loss
- Can be extended to multi-class problems
- Overfitting avoidance: shrinking and cross-validation-based selection of the number of iterations apply

Option trees

- Ensembles are not easily interpretable
- Can we generate a single model?
 - One possibility: "cloning" the ensemble by using large amounts of artificial data that is labeled by the ensemble
 - Another possibility: generating a single structure that represents an ensemble in a compact fashion
- Option tree: decision tree with option nodes
 - Idea: follow all possible branches at option node
 - Predictions from different branches are merged using voting or by averaging probability estimates

Example



- Can be learned by modifying a standard decision tree learner:
 - Create option node if there are several equally promising splits (within a user-specified interval)
 - When pruning, error at option node is average error of options

Alternating decision trees

- Can also grow an option tree by incrementally adding nodes to it using a boosting algorithm
- The resulting structure is called an alternating decision tree, with splitter nodes and prediction nodes
 - Prediction nodes are leaf nodes if no splitter nodes have been added to them yet
 - Standard alternating tree applies to 2-class problems but the algorithm can be extended to multi-class problems
 - To obtain a prediction from an alternating tree, filter the instance down all applicable branches and sum the predictions
 - Predictions from all relevant predictions nodes need to be used, whether those nodes are leaves or not
 - Predict one class or the other depending on whether the sum is positive or negative

Example

Ex.: -overcast, high, false

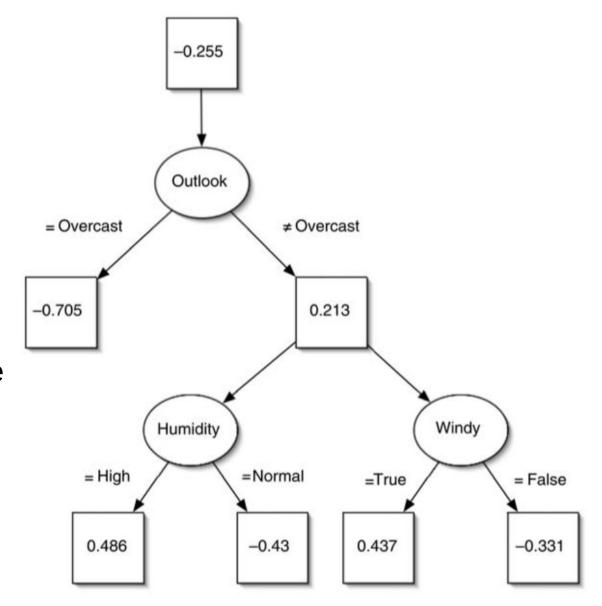
-0.255

+0.213

+0.486

-0.331

=0.113



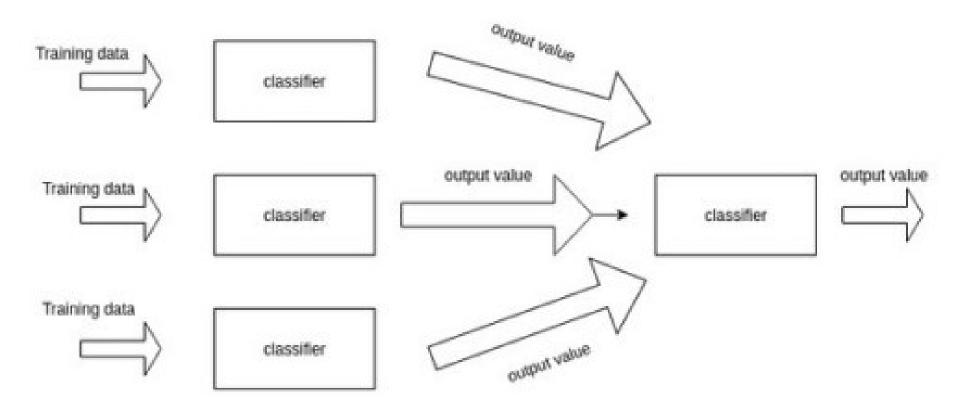
Growing alternating trees

- An alternating tree is grown using a boosting algorithm,
 e.g., the LogitBoost algorithm described earlier:
 - Assume that the base learner used for boosting produces a single conjunctive if-then rule in each boosting iteration (an if-then rule for least-squares regression if LogitBoost is used)
 - Each rule could simply be added into the current alternating tree, including the numeric prediction obtained from the rule
 - Problem: tree would grow very large very quickly
 - Solution: base learner should only consider candidate regression rules that extend existing branches in the alternating tree
 - An extension of a branch adds a splitter node and two prediction nodes (assuming binary splits)
 - The standard approach chooses the best extension among all possible extensions applicable to the tree, according to the loss function used
 - More efficient heuristics can be employed instead

Logistic model trees

- Alternating decision trees may still be difficult to interpret
 - The number of prediction nodes that need to be considered for any individual test instance increases exponentially with the depth of tree in the worst case
- But: can also use boosting to build decision trees with linear models at the leaves (trees without options)
 - These trees are often more accurate than standard decision trees but remain easily interpretable because they lack options
- Algorithm for building logistic model trees using LogitBoost:
 - Run LogitBoost with simple linear regression as the base learner (choosing the best attribute for linear regression in each iteration)
 - Interrupt boosting when the cross-validated accuracy of the additive model no longer increases
 - Once that happens, split the data (e.g., as in the C4.5 decision tree learner) and resume boosting in the subsets of data that are generated by the split
 - This generates a decision tree with logistic regression models at the leaves
 - Additional overfitting avoidance: prune tree using cross-validation-based cost-complexity pruning strategy from CART tree learner

Stacking



Stacking

- Question: how to build a <u>heterogeneous</u> ensemble consisting of different types of models (e.g., decision tree and neural network)
 - Problem: models can be vastly different in accuracy
- Idea: to combine predictions of base learners, do not just vote, instead, use meta learner
 - In stacking, the base learners are also called level-0 models
 - Meta learner is called level-1 model
 - Predictions of base learners are input to meta learner
- Base learners are usually different learning schemes
- Caveat: cannot use predictions on training data to generate data for level-1 model!
 - Instead use scheme based on cross-validation

Generating the level-1 training data

- Training data for level-1 model contains predictions of level-0 models as attributes; class attribute remains the same
- Problem: we cannot use the level-0 models predictions on their training data to obtain attribute values for the level-1 data
 - Assume we have a perfect rote learner as one of the level-0 learner
 - Then, the level-1 learner will learn to simply predict this level-0's learners predictions, rendering the ensemble pointless
- To solve this, we generate the level-1 training data by running a cross-validation for each of the level-0 algorithms
 - Then, the predictions (and actual class values) obtained for the test instances encountered during the cross-validation are collected
 - This pooled data obtained from the cross-validation for each level-0 model is used to train the level-1 model

More on stacking

- Stacking is hard to analyze theoretically: "black magic"
- If the base learners can output class probabilities, use those as input to meta learner instead of plain classifications
 - Makes more information available to the level-1 learner
- Important question: which algorithm to use as the metallearner (aka level-1 learner)?
 - In principle, any learning scheme
 - In practice, prefer "relatively global, smooth" models because
 - base learners do most of the work and
 - this reduces the risk of overfitting
- Note that stacking can be trivially applied to numeric prediction too