

# DSA Mids Lab exam

## Section B

May 18, 2022

### Instructions for the exam

1. This is a 2 hour exam.
2. You will be submitting your problems on the OJ
3. All the data structures will be provided in a .c file. You can copy them into your code and use them as required. You can modify them as well. Please go through the template code before using it (at-least the function definitions).
4. Problems A and B are worth **100 points** each, and Problem C is worth **200** points.
5. Refer to the time limit and memory limit of each problem on OJ.

## Problem A

**Definition.** Two words are said to be anagrams of each other if they can be obtained from each other by rearranging the letters of the words. For example "see", "ese" and "ees" are anagrams of each other, but "show" and "wash" are not anagrams of each other.

Given two linked lists  $ll1$ ,  $ll2$  with character values and  $n$  elements each, you have to implement the function `int ans(LL* ll1, LL* ll2)`, which **returns 1 if the strings formed by these linked lists are anagrams of each other, and 0 otherwise.**

For this question, you will be provided the template code in file `a.c` which will contain the ADT for linked list. You can write additional methods to solve this problem, but **ONLY** inside the designated area specified by comments. **Any change in code outside designated area will lead to a straight 0 in this problem.**

## Constraints

Number of test cases  $1 \leq T \leq 10^3$   
 $1 \leq n \leq 10^3$

## Input format

- First line contains an integer  $T$ , the number of test cases.
- For every test case the first line contains an integer  $n$ , the number elements in the linked lists.
- Then the next two lines contain  $n$  character strings each denoting the strings formed by the two linked lists. The strings contain lowercase Latin alphabets (a-z) ONLY.

## Examples

### Sample Testcase 1

#### Input

```
2
8
triangle
integral
5
house
mouse
```

#### Output

```
Yes
No
```

**Explanation**

The two words triangle and integral are anagrams of each other, so the function *int ans(LL\* ll1, LL\* ll2)* should return 1

The two words house and mouse are not anagrams of each other, so the function *int ans(LL\* ll1, LL\* ll2)* should return 0

## Problem B

**Definition.** A balanced binary tree is a binary search tree where for each of its node, the height of its left child and right child differs by at most 1.

Or in simpler words, a balanced binary search tree of  $N$  nodes has height of  $\log N$

**Definition.** The lowest common ancestor of two nodes  $u, v$  in a tree is the lowest node in the tree  $r$  such that  $u$  and  $v$  are in the subtree rooted at  $r$ .

Given a balanced binary search tree (BST) with  $N$  nodes, print the lowest common ancestor (LCA) of two given nodes in the BST. (*Note that the LCA of two nodes in a tree always exists*)

## Constraints

$$1 \leq N \leq 10^6$$

$$1 \leq Q \leq 10^6$$

$$-10^8 \leq \text{node values} \leq 10^8$$

All node values are distinct

## Input format

- First line contains  $N$  and  $Q$ , the number of nodes in the balanced binary search tree and the number of queries.
- Then  $N$  lines follow that contain three integers;  $p, wc$  and  $val$ .  $p$  ( $-1 \leq p < n$ ) denotes the parent of the current node (-1 if it is the root). If  $wc$  ( $-1 \leq wc \leq 1$ ) is 0, then the current node is the left child of the parent, and if it is 1, then the current node is the right child of the parent (It is -1 when the node is the root).  $val$  ( $-10^8 \leq val \leq 10^8$ ) is the value of the node. (*Note that  $p$  is zero-indexed*)
- No two nodes will have the same value
- The input is a valid balanced binary search tree.
- Next  $Q$  lines contain two integers,  $a$  ( $-10^8 \leq a \leq 10^8$ ) and  $b$  ( $-10^8 \leq b \leq 10^8$ ), the values of the nodes whose LCA you have to find. (*There will always exist a node with node value  $a$ , and same for  $b$* )

In the binary tree template file, a function `BT create_BT(int **arr, int n)` is included. The template has the code for taking input of the specified format and creating a binary tree from the input. Use it to construct the binary tree.

## Output format

Output  $Q$  lines,  $i^{\text{th}}$  of which has the answer for the  $i^{\text{th}}$  query, which is the value stored in the LCA of the queried nodes.

## Example

### Sample Test case 1

#### Input

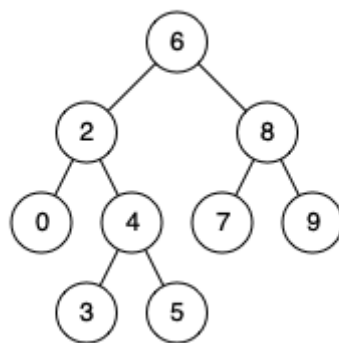
```
9 4
-1 -1 6
0 0 2
1 0 0
1 1 4
3 0 3
3 1 5
0 1 8
6 0 7
6 1 9
0 4
7 5
2 5
7 9
```

#### Output

```
2
6
2
8
```

#### Explanation

The tree in this test case is depicted as



Note the third query in particular, LCA of two nodes can be one of the nodes itself

## Problem C

**Definition.** A binary string is a string whose characters can only be one of '0' or '1'. For example "01001" is a binary string, but "0120", "010a" are not binary strings.

**Definition.** A string  $a$  is a prefix of string  $b$  if there exists some string  $c$  such that  $a$  concatenated with  $c$  forms  $b$ . For example "abc" is a prefix of "abcde", but "abd" is not a prefix of "abcd".

For a binary string  $s$ , you can split it into 2 parts  $s_1$  and  $s_2$  only if the ratio  $\frac{\text{number of 1s}}{\text{number of 0s}}$  for both  $s_1$  and  $s_2$  is equal. (If there are no 0s, then we consider the ratios  $\frac{1}{0}$  and  $\frac{2}{0}$  to be equal)

Now for every prefix of a given binary string  $s$  you need to print the maximum number of parts the prefix string can be split into following previously mentioned constraint.

## Constraints

### Subtask 1 (20 points)

$$1 \leq n \leq 10^3$$

### Subtask 2 (80 points)

$$1 \leq n \leq 2 \times 10^5$$

## Input format

- First line contains an integer  $n$  which is the length of the string  $s$ .
- Second line contains an  $n$  character binary string  $s$ .

## Output format

One line with  $n$  space separated numbers, where the  $i^{th}$  number denotes the maximum number of parts the prefix string consisting of the first  $i$  characters can be split into following the constraint mentioned in the problem statement.

## Example

### Sample Testcase 1

**Input**

3  
001

**Output**

1 2 1

**Explanation**

There is no way to partition "0" or "001" into more than one block with equal ratios of numbers of 0s and 1s, while you can split "00" into "0" and "0".

**Sample Testcase 2****Input**

6  
000000

**Output**

1 2 3 4 5 6

**Explanation**

you can split each prefix of length  $i$  into  $i$  blocks "0".