

Printing count of primes in range  $[L-R]$

There can be multiple ranges(queries)

We can use isPrime helper method with  $\sqrt{n}$  complexity for each range.

$$T.C (Q \times (R-L+1) \times \sqrt{n})$$

This is naive approach and not acceptable.

One step in improving T.C. is converting check of isPrime to constant by pre-computing all primes till max possible value of query boundary. This computation takes  $\log(\log n)$

Still we only improve  $\sqrt{n}$  to one pre-calculation of  $\log(\log n)$ .

For most optimal solution we can pre-compute the number of primes till  $j^{th}$  idx. Prefix sum.

Now, for each query we can check

$$queryResult[i] = primeCount[R] - primeCount[L-1] \leftarrow \text{check boundary here}$$

```
func (list <> queries)
{
    prime[] = getSieve( $10^6$ )  $\rightarrow n \log(\log n)$ 
    cut = 0
    for (i = 2  $\rightarrow$   $10^6$ )  $\rightarrow 0$ 
    {
        cut = cut + prime[i];
        prime[i] = cut;
    }

    for (i = 0  $\rightarrow$  queries.size)
    {
        l = queries[i][0]  m = queries[i][1]
        print (prime[m] - prime[l-1])
    }
}
```

Annotations for T.C. analysis:

- $list \rightarrow$   $\log(\log 10^6)$
- $for(i = 2 \rightarrow 10^6)$   $\rightarrow 10^6$
- $return list$   $\rightarrow Q$

Total T.C. =  $\log(\log 10^6) + 10^6 + Q$