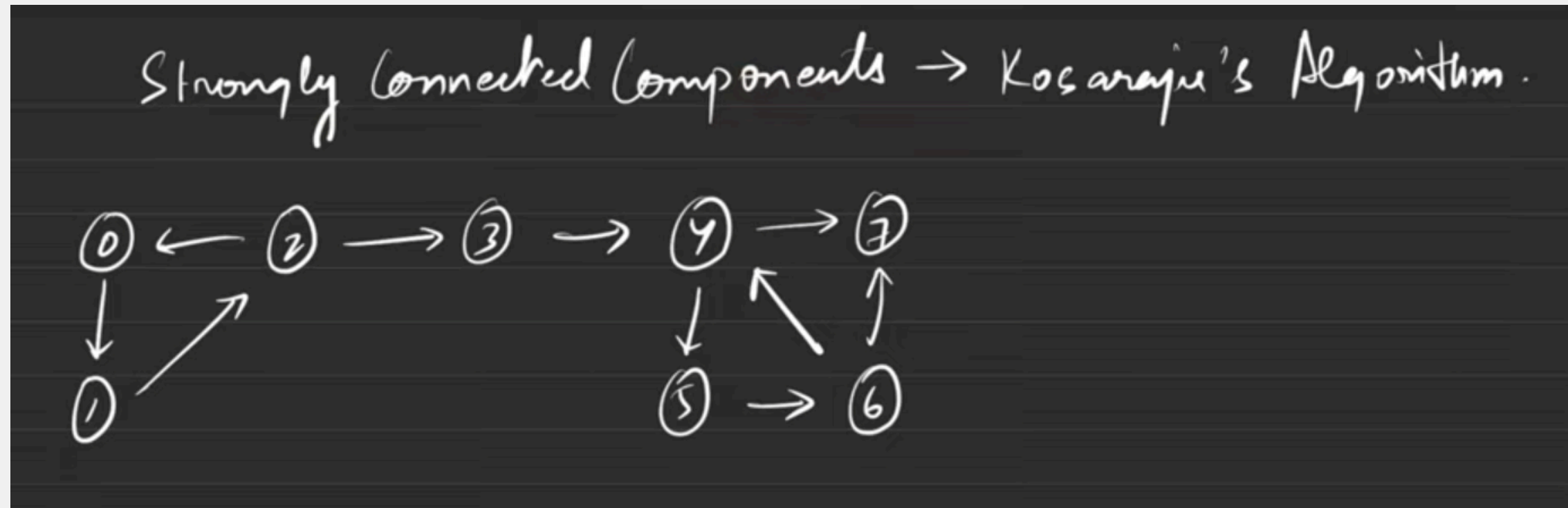
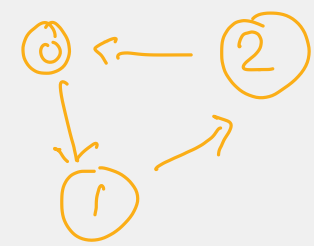


Strongly connected graphs are only valid for directed graphs.



Strongly connected component means for every edge if we can go from node 1 to node 2 we should be able to go from node 2 to node 1 like if we consider below component it is a strongly connected component.



Below are strongly connected components from above example

$(0, 1, 2)$, (3) , $(4, 5, 6)$, (7)

The thought process behind this algorithm is that if we reverse the edges we won't be able to visit the other strongly connected components.

- 1> Sort all the edges according to finishing time.
- 2> Reverse the graph
- 3> Do a DFS

```

class Solution
{
    //Function to find number of strongly connected components in the graph.
    public int kosaraju(int V, ArrayList<ArrayList<Integer>> adj)
    {
        // Step 1: Sort all the edges according to finish time (Storing in stack)
        boolean[] visited = new boolean[V];
        Stack<Integer> stk = new Stack<>();
        for (int node = 0; node < V; node++) {
            if (visited[node])
                continue;
            dfs(node, visited, adj, stk);
        }

        // Step 2: Reversing the edges
        List<List<Integer>> reverse = new ArrayList<>();
        for (int i = 0; i < V; i++)
            reverse.add(new ArrayList<>());

        for (int i = 0; i < V; i++) {
            for (int ng: adj.get(i)) {
                reverse.get(ng).add(i);
            }
        }

        // Step 3: Perform DFS and counts strongly connected components
        int scc = 0;
        visited = new boolean[V];
        while (!stk.isEmpty()) {
            int topNode = stk.pop();
            if (visited[topNode])
                continue;
            scc++;
            dfsForReverse(topNode, reverse, visited);
        }

        return scc;
    }

    private void dfsForReverse(int node, List<List<Integer>> adj, boolean[] visited) {
        visited[node] = true;
        for (int ng: adj.get(node)) {
            if (visited[ng])
                continue;
            dfsForReverse(ng, adj, visited);
        }
    }

    private void dfs(int node, boolean[] visited, ArrayList<ArrayList<Integer>> adj, Stack<Integer> stk) {
        visited[node] = true;

        for (int ng: adj.get(node)) {
            if (visited[ng])
                continue;
            dfs(ng, visited, adj, stk);
        }

        stk.push(node);
    }
}
  
```

TC - $O(V+E)$
 SC - $O(V) + O(V+E)$ \leftarrow This is for reverse graph.