

Frequently used bitwise operation tricks for competitive programming -
Along with intuition of why the trick works.

1) Check if the number is odd
 $X \& 1 = 1$

(Works because only the last bit remains after operation)

2) Same logic be extended to check if the kth bit is set
 $(X \gg k) \& 1 = 1$

3) Flip the kth bit
 $X = X \wedge (1 \ll k)$

4) Set and Unset Kth bit - Instead of XOR use OR/AND
 $X = X | (1 \ll k)$
 $X = X \& \sim(1 \ll k)$

5) Count set bits [Unlike other tips this one is C++ specific]
Use `__builtin_popcountll`, very fast.

6) Check if the number is a power of 2
 $X \& (X - 1) = 0$

(Power of 2 has only one bit set, what happens if we subtract one from such a number, think AND with that)

7) Super handy in solving problems many times
 $A + B = (A | B) + (A \& B)$

(Proof - OR counts every bit once, we want to count bit set in both twice, hence the additional AND too).