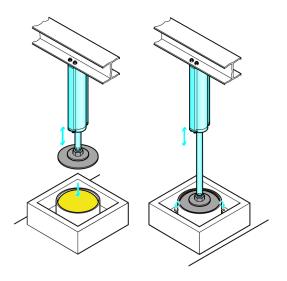
## Logic control of electro-pneumatic systems

Kjartan Halvorsen

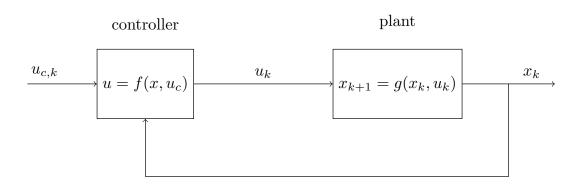
May 14, 2020

# Cheese pressing example, sequence A+A-



From FESTO Didactic

### A logic control loop



#### Cheese pressing example - Variables

Activating solenoid UA+ extends the cylinder, activating UA- retracts the cylinder.

#### State variable

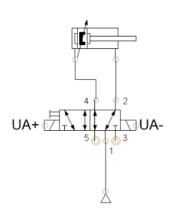
$$x = \begin{cases} 0 & \text{Cylinder retracted} \\ 1 & \text{Cylinder extended} \end{cases}$$

## Control signal

$$u = \begin{bmatrix} u_1 \\ u_2 \end{bmatrix},$$

with

$$u_1 = egin{cases} 0 & ext{Don't activate UA+} \ 1 & ext{Activate UA+} \ u_2 = egin{cases} 0 & ext{Don't activate UA-} \ 1 & ext{Activate UA-} \end{cases}$$



## Command signal

$$u_{c} = \begin{cases} 0 & \text{Button unpushed} \\ 1 & \text{Button pushed} \end{cases}.$$

# Cheese pressing example - Plant dynamics and control law

Activating solenoid UA+ extends the cylinder, activating UA- retracts the cylinder.

### Plant dynamics $x_{k+1} = g(x_k, u_k)$

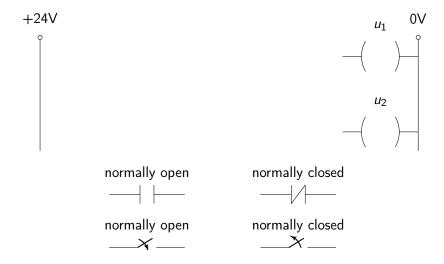
		state		
$u_{1,k}$	$u_{2,k}$	$x_k$	$x_{k+1}$	
0	0	0	0	
0	1	0	0	
1	0	0	1	
1	1	0	0	
0	0	1	1	
0	1	1	0	
1	0	1	1	
1	1	1	1	

## Control law $u_k = f(x, u_c)$

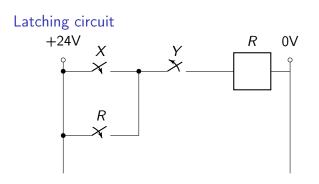
Χ	Иc	$u_1$	<i>u</i> <sub>2</sub>
0	0	0	0
1	0	0	1
0	1	1	0
1	1	0	1

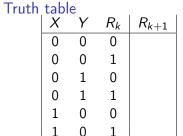
$$u_1 = u_2 = u_2 = u_3 = u_3$$

## Cheese pressing example - implementing the control law

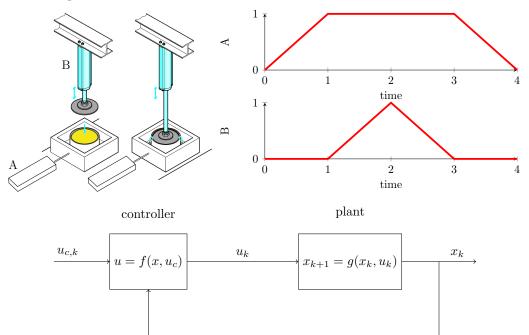


## Intermezzo - An electrical circuit with memory

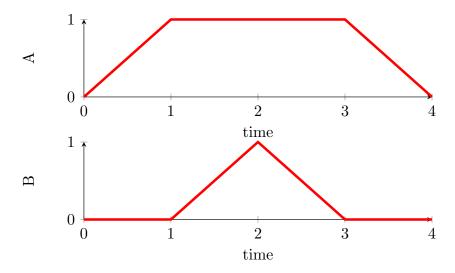




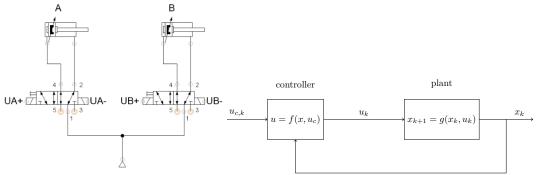
## The lab assignment



## Implementing the sequence A+B+B-A-



## Implementing the sequence A+B+B-A-, control signal



#### Control signal

$$u = \begin{bmatrix} u_A + & u_A - & u_B + & u_B - \end{bmatrix}^T$$

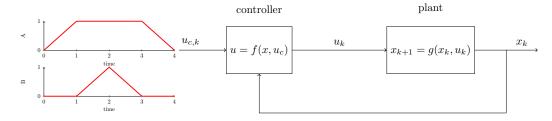
with

$$u_A + = \begin{cases} 0 & \text{Solenoid extending A is not activated} \\ 1 & \text{Solenoid extending A is activated} \end{cases}$$

etc.



## Implementing the sequence A+B+B-A-, state variables



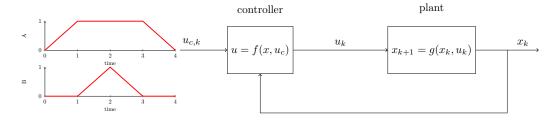
#### State variables (naive)

$$x = \begin{bmatrix} x_A & x_B \end{bmatrix}^T,$$

with

$$x_{\{A,B\}} = \begin{cases} 0 & \text{Cylinder } \{A,B\} \text{ retracted} \\ 1 & \text{Cylinder } \{A,B\} \text{ extended} \end{cases}$$

#### Implementing the sequence A+B+B-A-, control law

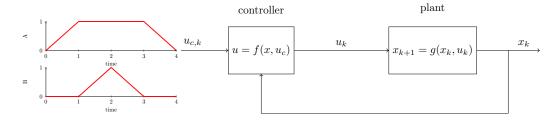


#### Control law (problematic)

Ignoring input signal  $u_c$  (no start/stop buttons). Movement should be cyclic

XA	ХB	$u_A+$	$u_A-$	$u_B+$	u <sub>B</sub> -
0	0				
1	0				
1	1				
0	1				

## Implementing the sequence A+B+B-A-, control law



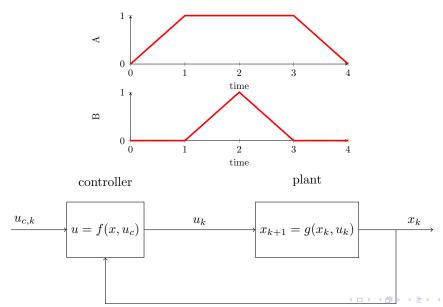
#### Control law (problematic)

Ignoring input signal  $u_c$ . Movement should be cyclic

$x_A$	$x_B$	$u_A+$	$u_A-$	$u_B +$	u <sub>B</sub> -
0	0	1	0	0	0
1	0	0	1 or 0	0 or 1	0
1	1	0	0	0	1
(0)	(1)	0	0	0	1

#### Implementing the sequence A+B+B-A-, the problem

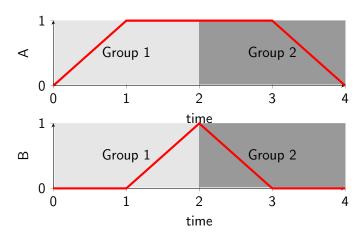
The correct control signal (action) is not uniquely defined by the position of the cylinders



### Implementing the sequence A+B+|B-A-

Dividing the sequence into groups (a.k.a. cascade method)

$$A+B+$$
 | B-A-  
Group 1 Group 2



## Implementing the sequence A+B+|B-A-|, state variables

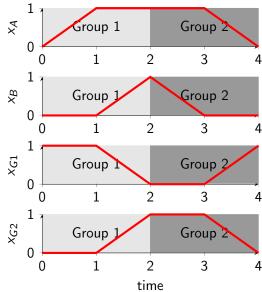
#### State variables (better)

$$x = \begin{bmatrix} x_A & x_B & x_{G1} & x_{G2} \end{bmatrix}^T$$

with

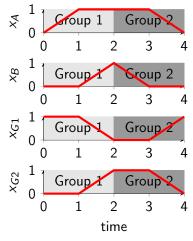
$$x_{\{A,B\}} = \begin{cases} 0 & \text{Cylinder } \{A,B\} \text{ retracted} \\ 1 & \text{Cylinder } \{A,B\} \text{ extended} \end{cases}$$
 $x_{Gi} = \begin{cases} 0 & \text{Group } i \text{ not active} \\ 1 & \text{Group } i \text{ active} \end{cases}$ 

#### State transitions



## Implementing the sequence A+B+|B-A-, control law

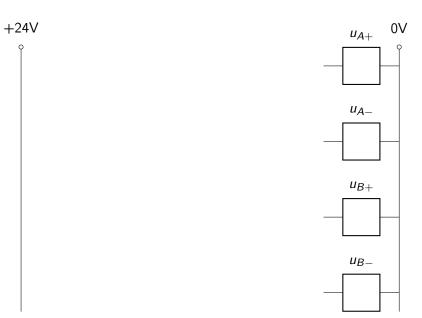
#### State transitions



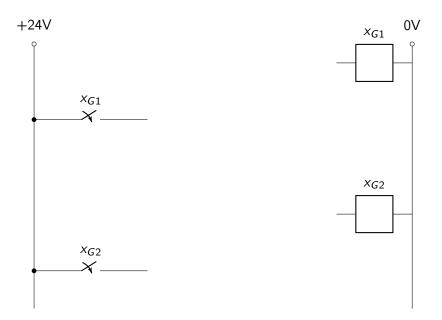
#### Control law

$x_A$	$x_B$	$x_{G1}$	$x_{G2}$	$u_A+$	$u_A-$	$u_B +$	$u_B-$
0	0	1	0				
1	0	1	0				
1	1	0	1				
1	0	0	1				

# Implementing the control law



## Implementing the group transitions



## Implementing the proximity sensor circuit

