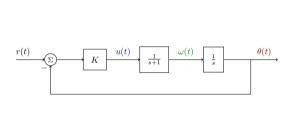
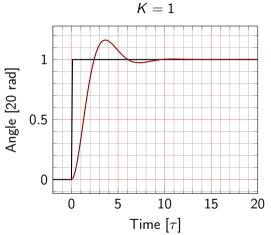
Compensator design - Loop shaping

Kjartan Halvorsen

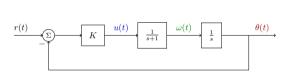
October 1, 2021

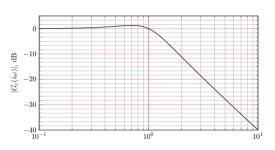
Proportional control of the normalized DC motor



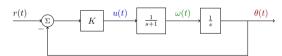


Proportional control of the normalized DC motor

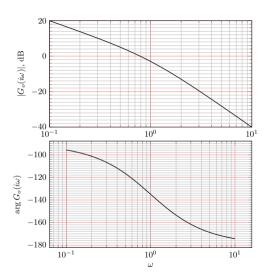




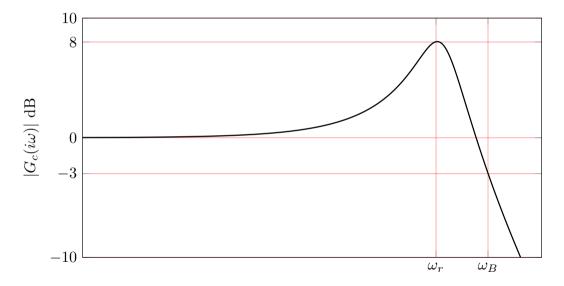
Proportional control of the normalized DC motor



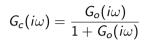
Activity Determine the cross-over frequency and the phase margin.

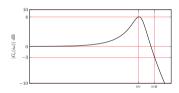


Specifications on the frequency properties of the closed-loop system



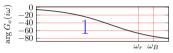
How to achieve the frequency-domain specifications





Activity Which of the Bode plots to the right shows the correct loop gain $G_o(i\omega)$?













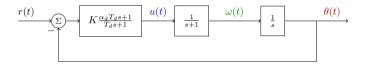




From specifications on G_c to specifications on G_o

Closed-loop specifications	Loop gain specifications
High bandwidth ω_B	High cross-over frequency ω_c
Low resonance peak M_p	Large phase margin φ_m
Static gain $\mathit{G}_{c}(0)pprox1$	static gain $G_o(0)$ high

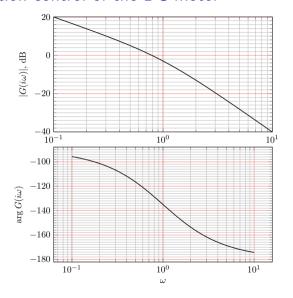
Position control of the DC motor



Specifications:

- 1. $\omega_B \approx \omega_c = 2 \text{ rad/s}$
- 2. $\varphi_m > 60^{\circ}$

Position control of the DC motor



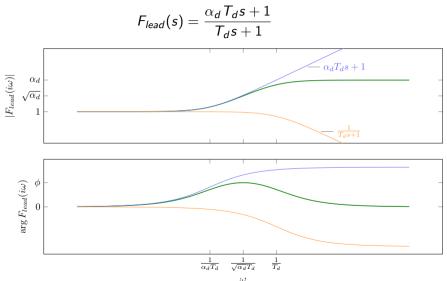
Specifications:

- 1. $\omega_B \approx \omega_c = 2 \text{ rad/s}$
- 2. $\varphi_m = \arg G_o(i\omega_c) (-180^\circ) > 60^\circ$

Activity

- 1. What is $|G(i\omega_c)|$?
- 2. What is arg $G(i\omega_c)$?
- 3. What should arg $G_o(i\omega_c)$ be to satisfy the phase margin requirement?
- 4. How much phase advance is needed at the desired cross-over frequency?

Position control of the DC motor - obtaining the phase advance



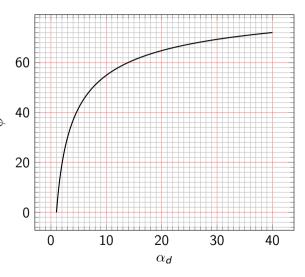
The maximum phase advance of the lead compensator

$$F_{lead}(s) = rac{lpha_d T_d s + 1}{T_d s + 1}$$

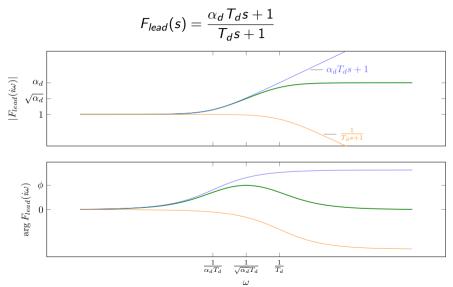
$$\phi = \max \arg F_{lead}(i\omega)$$

$$\sin \phi = rac{lpha_d - 1}{lpha_d + 1} \quad \Leftrightarrow \quad lpha_d = rac{1 + \sin \phi}{1 - \sin \phi}$$

Activity Find the value of α_d that gives the necessary maximum positive phase arg $F_{lead}(i\omega_c) = 34^{\circ}$.

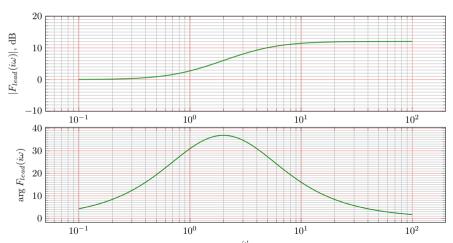


Position control of the DC motor - placing the phase peak

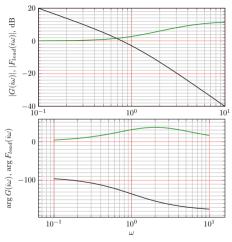


Position control of the DC motor - The resulting lead compensator

$$F_{lead}(s) = rac{lpha_d T_d s + 1}{T_d s + 1} = rac{s + 1}{0.25 s + 1}$$



Position control of the DC motor - Getting the gain right



Specifications

1.
$$\omega_B = \approx \omega_c = 2 \text{ rad/s}$$

2.
$$\varphi_m = \arg G_o(i\omega_c) - (-180^\circ) > 60^\circ$$

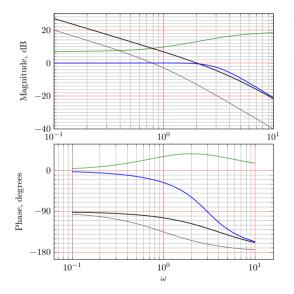
Activity

$$20 \log G_o(i\omega) = 20 \log KF(i\omega)G(i\omega)$$
$$= 20 \log K + 20 \log F(i\omega) + 20 \log G(i\omega)$$

so, what should the gain K be to obtain

$$|G_o(i2)| = 1 = 0$$
dB?

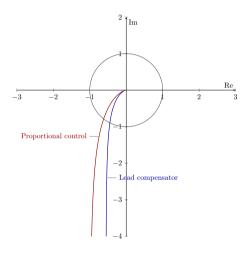
Position control of the DC motor - Results

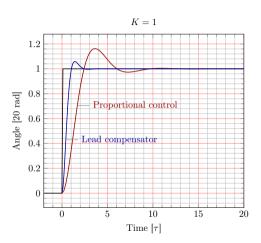




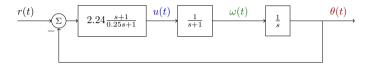
Activity Identify the frequency responses of: 1) The plant, 2) The compensator, 3) The loop gain, and 4) The closed-loop system.

Position control of the DC motor - Results

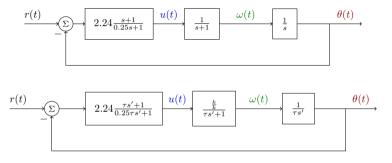




Applying the compensator design to a particular motor



Applying the compensator design to a particular motor



Applying the compensator design to a particular motor

