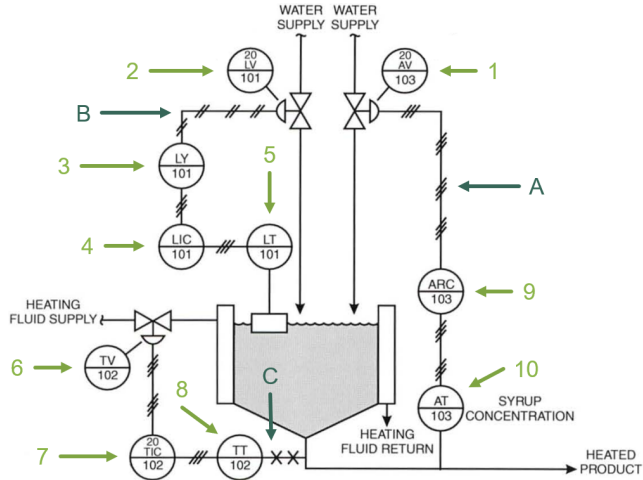


# Design of control systems

Kjartan Halvorsen

September 19, 2022

# Feedback control systems are ubiquitous



# Feedback control systems

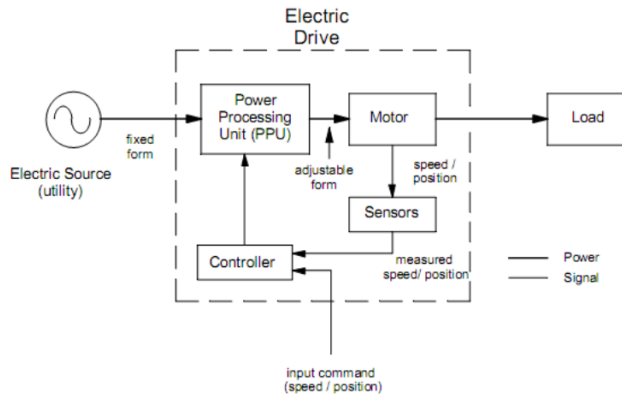
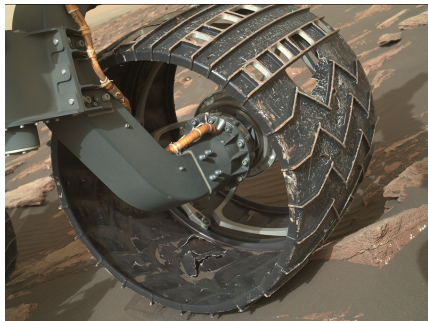
## The problem situation



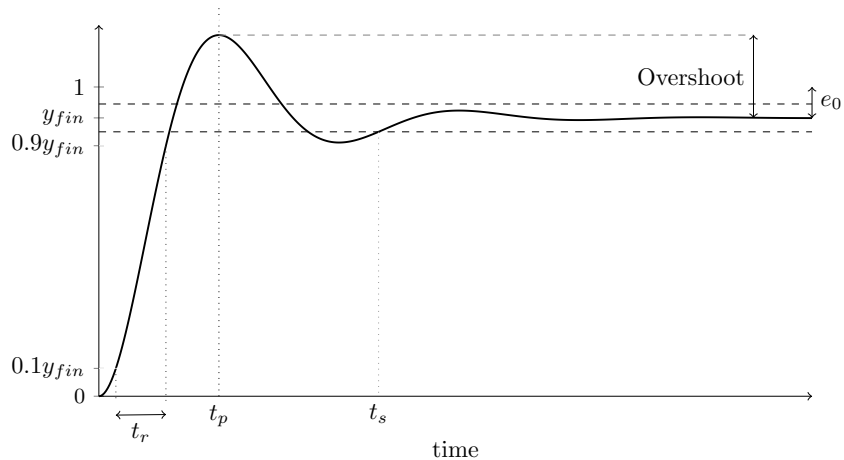
# Feedback control system



# Feedback control system



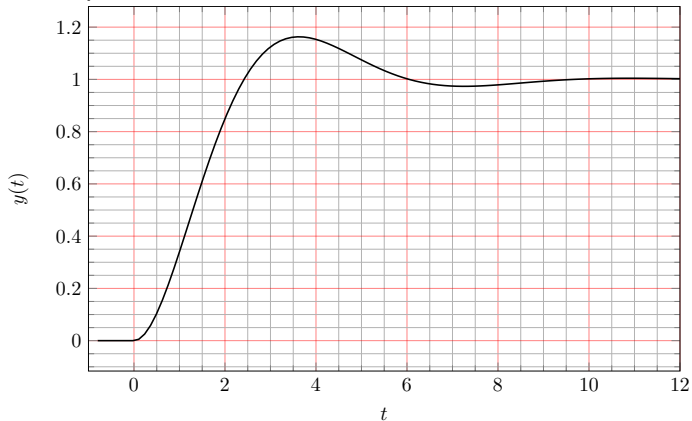
## Performance requirements - time domain



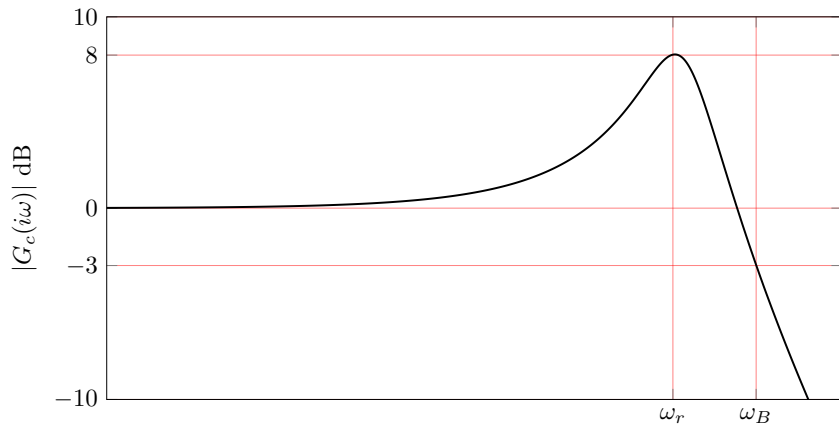
## Performance requirements - time domain

**Activity** Does the system satisfy the requirements?

Rise time  $< 1.5\text{s}$   
Overshoot  $< 18\%$

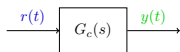


## Performance requirements - frequency domain

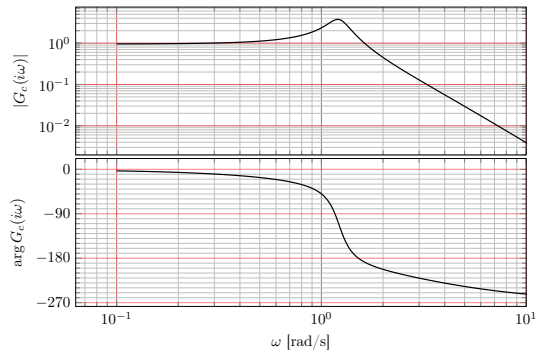




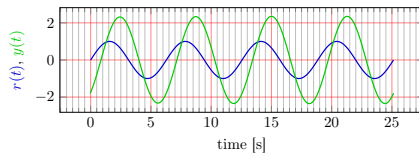
# Performance requirements - frequency domain



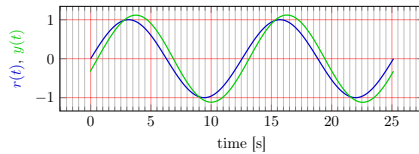
Bode plot



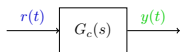
$r(t) = \sin(\omega t)$ ,  $\omega = 1$



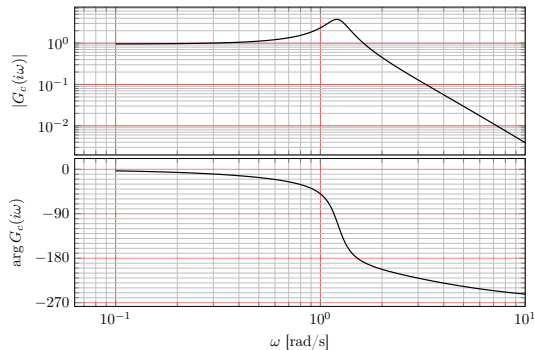
$r(t) = \sin(\omega t)$ ,  $\omega = 0.5$



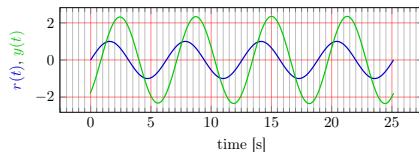
# Performance requirements - frequency domain



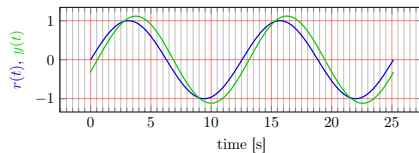
Bode plot



$r(t) = \sin(\omega t)$ ,  $\omega = 1$

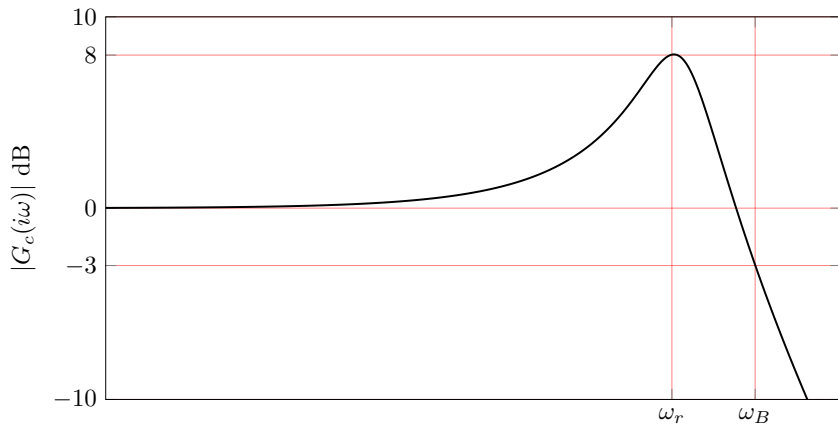


$r(t) = \sin(\omega t)$ ,  $\omega = 0.5$



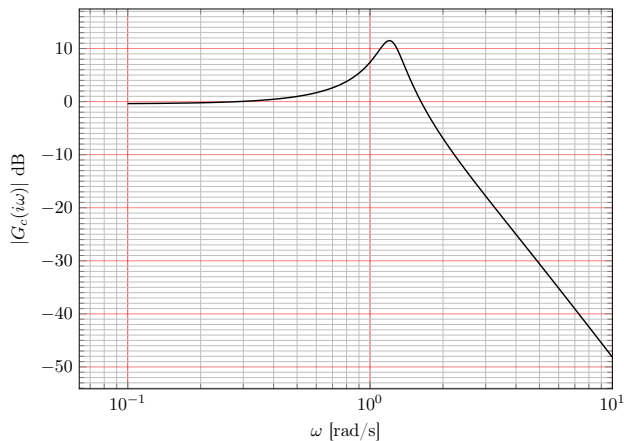
**Activity** What is the gain and phase shift at  $\omega = 2$  rad/s?

## Performance requirements - frequency domain



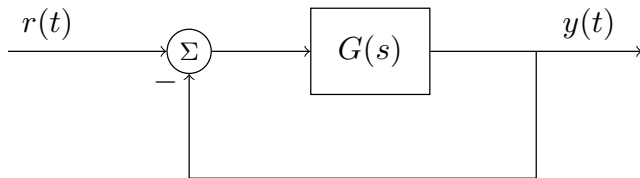
# Performance requirements - frequency domain

**Activity** Does the system satisfy the requirements?



Bandwidth  $> 3$  rad/s  
Resonance peak  $< 9$  dB

## Block diagram algebra



Transfer function from  $r(t)$  to  $y(t)$ :

$$\frac{Y(s)}{R(s)} = \frac{G(s)}{1 + G(s)}$$

# Block diagram algebra

**Activity** Pair the block-diagram with the correct closed-loop transfer function!

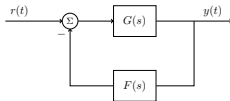
A



I

$$\frac{Y(s)}{R(s)} = \frac{G(s)F(s)}{1+G(s)}$$

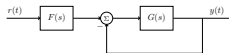
B



II

$$\frac{Y(s)}{R(s)} = \frac{G(s)}{1+G(s)F(s)}$$

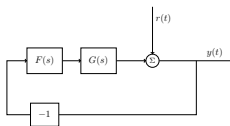
C



III

$$\frac{Y(s)}{R(s)} = \frac{1}{1+G(s)F(s)}$$

D



IV

$$\frac{Y(s)}{R(s)} = \frac{G(s)F(s)}{1+G(s)F(s)}$$