A study on the energy transfer of a square prism under fluid-elastic galloping

H.G.K.G. Jayatunga, B.T. Tan, J. S. Leontini

Abstract

Extracting useful energy from flow induced vibrations has become a developing area of research in recent years. In this paper, we analyse power transfer of an elastically mounted body under the influence of aeroelastic galloping. The system and the power transfer is analysed by numerically integrating the quasi-steady state model equations. The power transfer is analysed for both high (Re = 22300) and low (Re = 165) Reynolds numbers cases, and the impact of the system mass is investigated for both.

At high mass ratios ($m^* > 50$), the power transfer is completely controlled by galloping and essentially independent of the mass. A combined massdamping coefficient, Π_2 , that can be derived from the equation of motion, is shown to be the parameter that governs power output. The system is a balance between the power delivered to the system due to hydrodynamic forcing and power removed through mechanical damping which are governed by the hydrodynamic forcing characteristics (i.e. the lift force as a function of incident angle) and mechanical damping coefficient respectively. The peak efficiency of 0.26% for Re = 165 and 6.7% for Re = 22300 were observed when the non-dimensionalised mass-damping factor becomes 0.314 and 1.04 respectively.

A contradictory behaviour is observed at low m^* between the low and high Re cases. The forcing due to vortex shedding at low Reynolds numbers suppresses the galloping excitation and results in a reduced power output. For the case with high Re power output increases as m^* is reduced . For this high Re case, at low m^* the reduction in inertia allows the body to accelerate faster and spend a larger portion of the period at relatively high transverse velocities. Extrapolating this trend, the limit to peak efficiency is found to be 13.5% and occurs when $m^* \to 0$ and $U^* \to \infty$ and $\Pi_2 = 1.22$

Keywords:

1. Introduction

Fluid-elastic galloping is one of the sub-areas of research in fluid structure interactions. This area has been of interest due to the vibrations crated by galloping on transmission lines and civil structures and leading them to failure. Therefore understanding this phenomenon in order to suppresses these vibrations was quite important. However, the search for alternate energy sources with minimal environmental impact has become an important area of research in the modern word. Therefore researchers are moving towards investigating the possibility of extracting useful energy from this vibrations rather than suppressing them. Thus, it is quite important to understand the governing parameters and analyse the influence of them on the energy transfer from the fluid to the structure, because this understanding will lead to develop better practical applications. Hence, in this paper we focus on understanding the energy transfer from the fluid to the body and isolate the governing parameters influencing it.

According to Païdoussis et al. (2010), Glauert (1919) provided a criterion for galloping by considering the auto-rotation of an aerofoil. Den Hartog (1956) provided a theoretical explanation for galloping for iced electric transmission lines. A weakly non-linear theoretical aeroelastic model to predict the response of galloping was developed by Parkinson and Smith (1964) based on the quasi-steady state hypothesis. Experimental lift and drag data on a fixed square prism at different angles of attack were used as an input for the theoretical model. It essentially used a curve fit of the transverse force to predict the galloping response. The study managed to achieve a good agreement with experimental data.

However, the QSS model equation when solved analytically using the sinusoidal solution, cannot predict the response for cases with low mass ratios. Joly et al. (2012) observed that finite element simulations show a sudden change in amplitude below a critical value of the mass ratio. The quasi-oscillator equation in Parkinson and Smith (1964) was altered to account for the vortex shedding and solved numerically to predict the reduced displacement amplitude at low mass ratios to the point where galloping is no longer present. Barrero-Gil et al. (2010) investigated the possibility of extracting power from vibrations caused by galloping using the quasi-steady state model. So far the studies on galloping using quasi-steady state assumption

has been mainly focused on understanding the behaviour of the displacement amplitude. Although, it is quite important to analyse the behaviour of the velocity when studying the power transfer from the fluid to the body. This is because power could be simply defined as the product the force and velocity. This study also focuses on how well the QSS model perform at high damping at low Reynolds numbers.

Here, the modified QSS model developed by Joly et al. (2012) is integrated numerically for low Reynolds numbers. The power transfer from the fluid to the structure and the influence of mechanical parameters was investigated (i.e. mass, stiffness and damping). To this end, a series of previously mentioned mechanical parameters are tested at two different values of Re: Re = 200, a case that should remain laminar and closer to two-dimensional behaviour; Re = 22300, a case where the flow is expected to be turbulent and three-dimensional. Both cases require the input of transverse force coefficients C_y as a function of angle of attack θ for a fixed body. These data are provided from direct numerical simulations for the Re = 200 case, while the data provided by Parkinson and Smith (1964) are used for the Re = 22300 case.

Nomenclature

a_1, a_3, a_5, a_7	coefficients of the polynomial to determine C_y
A	displacement amplitude
c	damping constant
D	characteristic length (side length) of the cross section of the body
$f = \sqrt{k/m}/2\pi$	natural frequency of the system
F_y	instantaneous force normal to the flow
F_0	amplitude of the oscillatory force due to vortex shedding
k	spring constant
m	mass of the body
m_a	added mass
P_d	power dissipated due to mechanical damping
$P_{in} = \rho U^3 D/2$	Energy flux of the approaching flow
P_{mean}	mean power
P_t	power transferred to the body by the fluid
t	time
U	freestream velocity
U_i	Induced velocity
y,\dot{y},\ddot{y}	transverse displacement, velocity and acceleration of the body
$\mathcal{A} = DL$	frontal area of the body
λ	Inverse time scale of a galloping dominated flow
$\lambda_{1,2}$	Eigenvalues of linearized equation of motion
ho	fluid density
$\omega_n = 2\pi f$	natural angular frequency of the system
ω_s	vortex shedding angular frequency
$c^* = cD/mU$	non-dimensionalised damping factor
$C_y = F_y/0.5\rho U^2 DL$	normal (lift) force coefficient
$m^* = m/\rho D^2 L$	mass ratio
Re	Reynolds number
$U^* = U/fD$	reduced velocity
Y = y/D	non-dimensional transverse displacement
$Y = m^* \dot{y} / a_1 U$	non-dimensional transverse velocity
$\ddot{Y} = m^{*2}D/a_1^2U^2$	non-dimensional transverse acceleration
$\Gamma_1 = 4\pi^2 m^{*2} / U^{*2} a_1^2$	First dimensionless group arising from linearised, non-dimensionalise
$\Gamma_2 = c^* m^* / a_1$	Second dimensionless group arising from linearised, non-dimensional
$\zeta = c/2m\omega_n$	damping ratio
$\theta = \tan^{-1}\left(\dot{y}/U\right)$	instantaneous angle of incidence (angle of attack)
$\Pi_1 = 4\pi^2 m^{*2}/U^{*2}$	Combined mass-stiffness parameter
$\Pi_2 = c^* m^*$	Combined mass-damping parameter 4

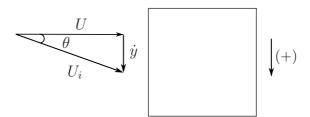


Figure 1: Induced angle of attack on the square prism due to the resultant of free-stream velocity of the fluid and transverse velocity of the body.

2. Problem formulation and methodology

2.1. The quasi-steady state (QSS) model

The equation of motion of the body is given by

$$(m)\ddot{y} + c\dot{y} + ky = F_y, \tag{1}$$

where the forcing term F_y is given by

$$F_y = \frac{1}{2}\rho U^2 \mathcal{A} C_y. \tag{2}$$

In the QSS model, it is assumed that the force on the body at a given instantaneous incident angle θ (defined in figure 1) is the same as the mean force on a static body at the same incident angle, or angle of attack. The instantaneous value of C_y is therefore determined by an interpolating polynomial based on the lift data for flow over a stationary body at various θ . Using the relationship between θ and the instantaneous transverse velocity of the body \dot{y} shown in figure 1, C_y can be written as a function of \dot{y} . The order of the interpolation polynomial used to define this function has varied from study to study. For example a 7^{th} order polynomial was used in Parkinson and Smith (1964) and 3^{rd} order polynomial was used in Barrero-Gil et al. (2009). Ng et al. (2005) concluded that using a 7^{th} order polynomial is sufficient and a polynomial higher than that of 7^{th} order doesn't provides a significantly better result. Thus a 7^{th} order interpolating polynomial is used in this present study. As a result, $C_y(\theta)$ (noting that theta is proportional to \dot{y}/U) is defined as

$$C_y(\theta) = a_1 \left(\frac{\dot{y}}{U}\right) + a_3 \left(\frac{\dot{y}}{U}\right)^3 + a_5 \left(\frac{\dot{y}}{U}\right)^5 + a_7 \left(\frac{\dot{y}}{U}\right)^7.$$
 (3)

It is expected that vortex shedding will be well correlated along the span and provide significant forcing at low Re. Joly et al. (2012) introduced an additional sinusoidal forcing function to the hydrodynamic forcing to model this. This enables the model to provide accurate predictions even at low mass ratios where galloping excitation is suppressed or not present. However, in this study we also focus on isolating the regions where the QSS model predicts well and therefore the additional sinusoidal forcing function is disregarded.

$$m\ddot{y} + c\dot{y} + ky = \frac{1}{2}\rho U^2 \mathcal{A}\left(a_1\left(\frac{\dot{y}}{U}\right) + a_3\left(\frac{\dot{y}}{U}\right)^3 + a_5\left(\frac{\dot{y}}{U}\right)^5 + a_7\left(\frac{\dot{y}}{U}\right)^7. \tag{4}\right)$$

This equation can be solved using standard time integration methods. In this study the fourth-order Runge-Kutta scheme built in to the MATLAB routine 'ode45' was generally used to obtain the solutions.

2.2. Calculation of average power

The dissipated power due to the mechanical damping represents the ideal potential amount of harvested power output. Therefore, the mean power output can be given by

$$P_{mean} = \frac{1}{T} \int_{0}^{T} (c\dot{y})\dot{y}dt, \tag{5}$$

where T is the period of integration and c is the mechanical damping constant.

It should be noted that this quantity is equal to the work done on the body by the fluid, defined as

$$P_{mean} = \frac{1}{T} \int_0^T F_y \dot{y} dt, \tag{6}$$

where F_y is the transverse (lift) force.

have to repharase These two definitions show two important interpretations of the power with respect to any energy production device. The first shows that power will be high for situations where the damping coefficient is high, and the transverse velocity is consistently high. The second shows that power will be high for situations where the transverse force and the body velocity are in phase.

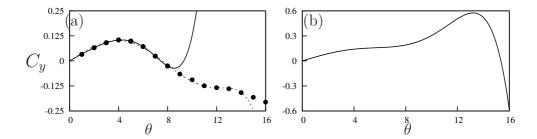


Figure 2: Lift coefficient, C_y , as a function of incidence angle θ , for a static square cross section. (a) Data from simulations at Re=200 (b) data from Parkinson and Smith (1964) at Re=22300. Points (\bullet) are measurements from the simulations. At Re=200 two interpolation polynomials are used where C_y where $\theta \leq 7^{\circ}$ is represented by (—) and $\theta \leq 7^{\circ}$ (---). All curves in both plots are 7th-order interpolating polynomials used to predict the fluid forcing for the QSS model. C_y is the force coefficient of the force which occurs normal to the induced velocity.

2.3. Validation

3. Results

The natural time scales of the system can be found by solving for the eigenvalues of the linearised equation of motion, namely

$$(m)\ddot{y} + c\dot{y} + ky = \frac{1}{2}\rho U^2 \mathcal{A}a_1\left(\frac{\dot{y}}{U}\right), \tag{7}$$

which is simply the equation of motion presented in equation 4 with the polynomial series for the lift force truncated at the linear term, and the forcing term representing vortex shedding removed.

Combining the \dot{y} terms and solving for eigenvalues gives

$$\lambda_{1,2} = -\frac{1}{2} \frac{c - \frac{1}{2}\rho U \mathcal{A} a_1}{(m)} \pm \frac{1}{2} \sqrt{\left[\frac{c - \frac{1}{2}\rho U \mathcal{A} a_1}{(m)}\right]^2 - 4\frac{k}{(m+m_a)}}.$$
 (8)

If it is assumed that the spring is relatively weak, $k \to 0$, a single non-zero eigenvalue remains. This eigenvalue is

$$\lambda = -\frac{c - \frac{1}{2}\rho U \mathcal{A} a_1}{(m)}. (9)$$

Further, if it is assumed that the mechanical damping is significantly weaker than the aerodynamic forces on the body, $c \to 0$ and

$$\lambda = \frac{\frac{1}{2}\rho U \mathcal{A}a_1}{(m)}.\tag{10}$$

Case	a_1	a_3	a_5	a_7
Re=200 (polynomial-1)	1.97	71.3	-6937	-254943
Re=200 (polynomial-2)	2.32	197.8	4301.7	30311.9
Re = 22300	2.69	168	1670	59900

Table 1: Coefficient values used in the 7th order interpolation polynomial for high (Re = 22300) and low (Re = 200) Reynolds numbers. Polynomial-1 was used to predict the C_y at $\theta \leq 7^{\circ}$ while polynomial-2 was used to predict the C_y where $\theta > 7^{\circ}irc$ in order to obtain a better fit. These data are used as input data to calculate the right-hand side of Eq. 4 throughout this study.

In this form, λ represents the inverse time scale of the motion of the body due to the negative damping effect of the long-time aerodynamic forces. In fact, the terms can be regrouped and λ written as

$$\lambda = \frac{a_1}{m^*} \frac{U}{D} \tag{11}$$

Written this way, the important parameters that dictate this inverse time scale are clear. The rate of change in the aerodynamic force with respect to angle of attack when the body is at the equilibrium position, $\partial C_y/\partial \alpha$, is represented by a_1 . The mass ratio is represented by m^* . The inverse advective time scale of the incoming flow is represented by the ratio U/D. Increasing a_1 would mean the force on the body would increase more rapidly with small changes in the angle of attack, θ , or transverse velocity. Equation 11 shows that such a change will increase the inverse time scale, or analogously decrease the response time of the body. Increasing the mass of the body, thereby increasing m^* , has the opposite effect. The inverse time scale is decreased, or as might be expected, a heavier body will take longer to respond.

This timescale can then be used to non-dimensionalize the equation of motion, and to find the relevant dimensionless groups of the problem. If the non-dimensional time, τ , is defined such that $\tau = t(a_1/m^*)(U/D)$, the

equation of motion presented in equation 4 can be non-dimensionalized as

$$\ddot{Y} + \frac{m^{*2}}{a_1^2} \frac{kD^2}{mU^2} Y = \left(\frac{1}{2} - \frac{m^*}{a_1} \frac{cD}{mU}\right) \dot{Y} + H.O.T., \tag{12}$$

where H.O.T. represents the higher order terms in \dot{Y} . The coefficients can be regrouped into combinations of non-dimensional groups, and rewritten as

$$\ddot{Y} + \frac{4\pi^2 m^{*2}}{U^{*2} a_1^2} Y = \left(\frac{1}{2} - \frac{c^* m^*}{a_1}\right) \dot{Y} + H.O.T, \tag{13}$$

where $c^* = cD/mU$ is a non-dimensional damping parameter.

Equation 13 shows there are four non-dimensional parameters that play a role in setting the response of the system. These are the stiffness (represented by the reduced velocity U^*), the damping c^* , the mass ratio m^* , and the geometry, represented by the rate of change in the aerodynamic force with respect to angle of attack when the body is at the equilibrium position, a_1 . The grouping of these parameters into two groups in equation 13 which arise by non-dimensionalising using the natural time scale of the galloping system, suggests there are two groups that dictate the response: $\Gamma_1 = 4\pi^2 m^{*2}/U^{*2}a_1^2$ and $\Gamma_2 = c^*m^*/a_1$. For a given geometry and Reynolds number, Γ_1 can be thought of as a combined mass-stiffness, whereas Γ_2 can be thought of a a combined mass-damping parameter. As it is assumed that during galloping the stiffness plays only a minor role, Γ_2 seems a likely parameter to collapse the data presented in figure 3. In fact, in the classic paper on galloping from Parkinson and Smith (1964), galloping data from wind tunnel tests is presented in terms of a parameter that can be shown to be the same as Γ_2 .

All of the quantities that make up Γ_1 and Γ_2 can, in theory, be known before an experiment is conducted. However, the quantity a_1 is a relatively difficult one to determine, requiring static body experiments or simulations. Here, the geometry is unchanged and results are only being compared at the same Re. Hence, suitable parameters can be formed by multiplying Γ_1 and Γ_2 by a_1^2 and a_1 respectively, to arrive at a mass-stiffness parameter $\Pi_1 = 4\pi^2 m^{*2}/U^{*2}$, and a mass-damping parameter defined as $\Pi_2 = c^* m^*$.

there are several differences that can be observed when the low Re data are compared with the 7^{th} order polynomial curve at Re=22300 shown in figure 3(b). The peak value of C_y is significantly lower at Re=200 ($C_y=0.12$ at 5°) in comparison with Re=22300 ($C_y=0.57$ at 13°). The inflection point present around 8° for Re=22300 is not observed at Re=200. This

agrees with the findings of Luo et al. (2003). It was concluded by Luo et al. (2003) that hysteresis in the system response occurs due to the inflection point in the C_y curve. Therefore hysteresis is not expected at Re = 165.

The range of incident flow angles where C_y remains positive is narrow at $Re = 200 \ (0^{\circ} < \theta \le 7^{\circ})$ compared to $Re = 22300 \ (0^{\circ} < \theta \le 15^{\circ})$. This feature is what sustains galloping. Power is only transferred from the fluid to the supporting structure within this range of incident angles because fluid forces are acting in the direction of travel of the oscillating body, as demonstrated by equation 6. Incident angles beyond this range actually suppress the galloping and power goes in the opposite direction, i.e; from body to fluid. Therefore due to the overall smaller C_y and narrow range of angles where C_y is positive for Re = 200 compared to Re = 22300, it is expected that the transferred power at Re = 200 is significantly lower than at Re = 22300.

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The quasi-steady analysis data reveal that the displacement amplitude grows with increasing U^* . This is shown for both the high and low Re cases in figures 3 (a) and (b). The onset of galloping is delayed with increasing damping ratio ζ for both high and low Reynolds numbers. This echos the findings of previous studies by Parkinson and Smith (1964) and Barrero-Gil et al. (2010). Hysteresis could be observed for the case with a higher Reynolds number. Different solutions could be obtained by manipulating the initial conditions (initial displacement) of the system. The upper branch was obtained by giving an initial displacement which was higher than the expected amplitude while the lower branch was obtained by providing a lower initial displacement than the expected amplitude. Although theory shows a possible third state, it is an unstable branch and as such it could not be achieved numerically. This was also observed by Vio et al. (2007).

The data presented in figure 3 show that, regardless of the damping ratio ζ , the trend of the response with U^* is similar, suggesting the data can be collapsed by a suitable choice of parameters. These parameters can be found by considering the natural time scales which was mentioned earlier. Figure 4 presents the same data as shown in figure 3, but in terms of the parameter Π_2 . The collapse, especially of the velocity amplitude and power output data, is excellent. This result shows that it is possible to obtain a similar power output at different values of U^* or ζ when the mass-damping constant, Π_2 , is kept fixed.

Figure 2 shows the plots of the interpolation polynomials as a function of

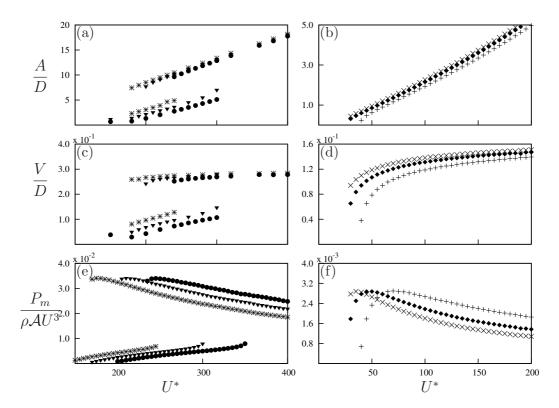


Figure 3: Velocity amplitude, displacement amplitude and mean power as functions of U^* . Data presented in (a), (c) and (e) were calculated using input data at Re=22300 and $m^*=1163$ obtained by Parkinson and Smith (1964) at three different damping ratios: $\zeta=0.0125$ (\circledast), $\zeta=0.015$ (\blacktriangledown) and $\zeta=0.0175$ (\bullet). Data presented in (b),(d) and (f) were obtained using input data at Re=200 and $m^*=20$ at three different damping ratios: $\zeta=0.075$ (\times), $\zeta=0.1$ (\bullet) and $\zeta=0.15$ (+). The multiple branches for the higher Re are due to the hysteresis between two solutions.

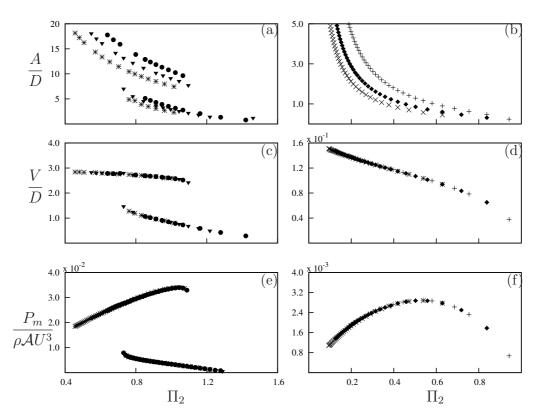


Figure 4: Displacement amplitude, velocity amplitude and mean power as functions of the mass-damping Π_2 . Data presented in (a),(c) and (e) were calculated using input data at Re=22300 obtained by Parkinson and Smith (1964) at three different damping ratios: $\zeta=0.0125$ (**), $\zeta=0.015$ (**) and $\zeta=0.0175$ (•*). Data presented in (b), (d) and (f) were obtained using input data at Re=200 at three different damping ratios: $\zeta=0.075$ (×), $\zeta=0.1$ (•*) and $\zeta=0.15$ (+). The collapsed data implies that there is no frequency selection and the tuning parameter of the mechanical side of the system is the damping constant to obtain an optimum power output.

 θ . For high Rethe polynomial incorporated by Parkinson and Smith (1964) was used. For low Retwo polynomials were used to obtain a better fit to the data. One to fit data from $\theta = 0^0 \rightarrow 7^0$ and the other $\theta > 7^0$

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3.1. Displacement, velocity and power

Power can be expressed as the product of force and velocity. Therefore the instantaneous power from the fluid to the body can be expressed as $P_t = F_y \dot{y}$. Similarly the dissipated power due to the mechanical damping can be expressed as $P_d = (c\dot{y})\dot{y}$. The time average of these two quantities, described in equations 5 and 6 should be equal due to energy conservation, provided that the mechanical friction losses are neglected. The mean power vs Π_2 provides a detailed explanation for the variation of the output power when Π_2 is increased. The key regions consists of region 1 where the P_{mean} increases with Π_2 , region 2 where P_{mean} becomes maximum and region 3 where P_{mean} decreases with Π_2 . Time histories of P_t and P_d at each of these key regions are presented in figure 6.

Figure 2(a) shows that C_y and therefore instantaneous force rises until 4° where it peaks and then falls, and at around 6° becomes negative. The maximum amount of power that can be transferred occurs when \dot{y} is such that θ is near the peak region. At the region where the instantaneous force becomes negative it will be opposing the velocity \dot{y} . Data at $\Pi_1 = 10$, $m^* = 20$ and Re = 200 are shown in figure 6 and are analysed as an example.

At region 1 ($\Pi_2 = 0.3$) the damping is low in comparison with region 1 and 2. While this may lead to larger oscillations, damping is required to dissipate power according to equation 5. Therefore, the low damping in this region leads to a low mean power output. Fig.6 (a) shows that P_t becomes negative over some portion of the cycle. This is caused by the high velocity amplitude leading to the equivalent incident angle θ to exceed the range where C_y is positive (i.e. $0 < \theta < 6^{\circ}$ as shown in figure3(a)). In this portion of the cycle the hydrodynamic force actually opposes the direction of travel and power is transferred from the structure to the fluid during those times. From an energy perspective, the mechanical damping is not sufficient to remover the energy transferred from the fluid to the structure during other times of the cycle because Γ_2 is substantially low. Therefore this excess energy is transferred back to the fluid as depicted by the negative region of P_d in Fig.6(a).

iiiiiii HEAD At region 2 where $\Pi_2 = 0.8$ the damping constant is high and a clear sinusoidal signal is observed for both P_d and P_t in figure 6(c). Figures 6(f) and 6(i) show that equivalent incident angle θ (which for small values, is proportional to the transverse velocity of the body) is in phase with F_y . The velocity amplitude in this case is small and θ is within the range where the hydrodynamic force increases with the incident angle (i.e. $0 < \theta \le 5^{\circ}$ as shown in figure 2(a)). According to equation 6, these conditions are suitable for high power output. However in this case, the power output is limited by the high damping which limits the amplitude of the oscillation.

At region 2 ($\Pi_2 = 0.54$), a balance is found between high and low values of damping. P_t is not a pure sinusoidal signal, however the signal remains periodic. From the time history graph of P_t , two 'peaks' are present in a single half cycle as shown if figure 6(b). In this case, the velocity amplitude actually exceeds the equivalent incident angle where the hydrodynamic forces peaks (i.e. $\theta = 5^{\circ}$ in 3 (a)). The dips in P_d between the two peaks approximately correspond to the time where the transverse velocity is higher than 0.09 and F_y is decreasing with increasing transverse velocity. The mean power output is at its maximum. This is due to the fact that this region is the best compromise between region 1 and 3. The damping is high enough to obtain a high power output while not too high to allow the induced angle of attack to enter the region where the forcing opposes the direction of travel.

- 3.2. limitations of the quasi-steady hypothesis at low Reynolds numbers
- 3.3. Comparison between QSS and DNS results

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3.4. limitation of the quasi-steady hypothesis at low Reynolds numbers

The QSS hypothesis assumes that the only force driving the system is the instantaneous lift generated by the induced velocity. However, vortex shedding is also present in this system. Therefore, an essential assumption when this model is used is that the effect of vortex shedding is minimal. Hence, the model has been always used at high Reand high mass ratios. The present study is focused on quantifying the limiting parameters of the QSS model at low Reynolds numbers by providing a comparison with DNS results.

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Joly et al. (2012) showed that the displacement data obtained using the QSS assumption and DNS agree well at low Reynolds numbers, with the modification implemented to the oscillator equation which accounts for the

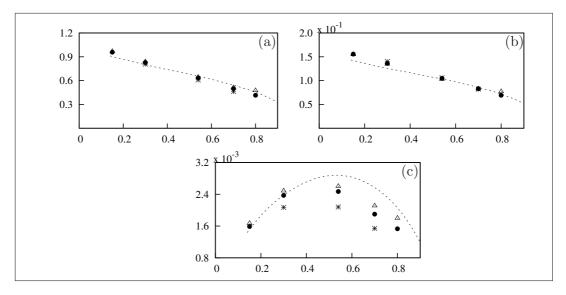


Figure 5: Comparison of data generated using the quasi-static theory and full DNS simulations. (a) Displacement amplitude, (b) velocity amplitude and (c) mean power as functions of Π_2 . Data were obtained at Re = 200 and pi2 values

vortex shedding. These data were obtained at zero damping levels. Since the current study was focused on the power transfer, more focus was put on analysing he behaviour od the velocity as the damping is increased. The comparison between the QSS and the DNS results revealed that the discrepancy of the power data increases significantly as Π_2 is increased. From figure ?? (powers spectrum analysis done on the DNS results) it is evident that the relative strength of the galloping signal decreases as the Π_2 is increased from $0 \to 0.7$. Therefore the influence of the vortex shedding becomes more significant and the interactions between galloping and shedding become more complex as the damping is increased.

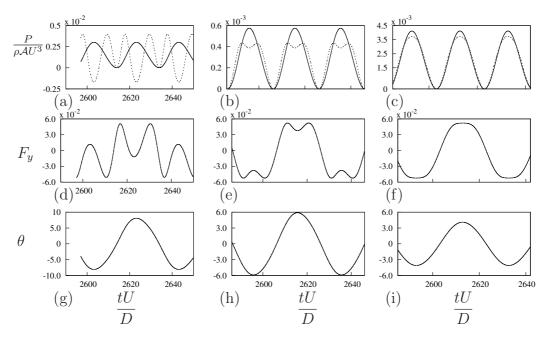


Figure 6: Time histories of P_t , P_d , F_y and θ at $\Pi_2=0.15$, 0.54 and 0.8. Data was obtained at $m^*=20$, $\Pi_1=10$ and Re=200. The time histories of P_t (—) and P_d (---) are presented for: (a) $\Pi_2=0.15$; (b) $\Pi_2=0.54$; (c) $\Pi_2=0.8$. Time histories of the instantaneous force F_y for: (d) $\Pi_2=0.15$; (e $\Pi_2=0.54$; (f) $\Pi_2=0.8$. Time histories of the instantaneous angle θ for: (g) $\Pi_2=0.15$; (h) $\Pi_2=0.55$; (i) $\Pi_2=0.8$.

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