# A Numerical Investigation of TBA.....!!!1

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### Chapter 1

# GOVERNING PARAMETERS OF FLUID-ELASTIC GALLOPING

### 1.1 Introduction

This chapter contains the formulation of non dimensional governing parameters namely, the combined mass-stiffness  $\Pi_1$  and the combined mass-damping  $\Pi_2$  and the results and discussion demonstrating the influence of them. These parameters are formulated by obtaining the relevant time-scales of the system followed by non-dimensionlising the governing QSS oscillator equation.

A comparison of Quasi-steady state data presented using the classical VIV parameters and the newly formulated  $\Pi_1$  and  $\Pi_2$  is presented and it is concluded that  $\Pi_2$  provides a better collapse for velocity amplitude and mean power compared the classical reduced velocity ( $U^*$ ) particularly because unlike  $U^*$ ,  $\Pi_2$  does not include a frequency component in it. This is followed by the presentation of QSS data and discussion on the influence of  $\Pi_1$  and  $\Pi_2$  on power, which concludes that the power transfer is a primary function of  $\Pi_2$  and a weak function of  $\Pi_1$ .

Following this, a comparison of the QSS data with Direct Numerical Simulations (DNS) is presented. This reveals that the power transfer of the DNS data is strongly influenced by both  $\Pi_1$  and  $\Pi_2$ . Further analysis reveals that there is a good agreement between QSS and DNS for velocity and power at substantially high  $\Pi_1\dot{A}s$   $\Pi_1$  decreases, the deviation

(between QSS simulations and DNS) increases. Power spectral analysis of the DNS data shows a significant response at the vortex shedding at low  $\Pi_1$ . The relative strength was found out to be an inverse function of  $\Pi_1$ , which provides a clear explanation for the deviation between QSS simulations and DNS data at low  $\Pi_1$ . This is primarily due to the influence of vortex shedding where this effect is not accounted in the QSS model.

# 1.2 Formulation of the non-dimensionalised parameters $\Pi_1$ and $\Pi_2$

The natural time scales of the system could be obtained by linearising the quasi-steady equation of motion. (Eq: \*\*KJ: equation of motion \*\*) and finding the eigenvalues. The non-linear terms of the forcing function are truncated and the equation of motion could be expressed as,

$$m\ddot{y} + c\dot{y} + ky = \frac{1}{2}\rho U^2 \mathcal{A}a_1\left(\frac{\dot{y}}{U}\right), \qquad (1.1)$$

After combining the  $\dot{y}$  terms and solving for eigenvalues the following solutions for the eigenvalues could be obtained.

$$\lambda_{1,2} = -\frac{1}{2} \frac{c - \frac{1}{2}\rho U \mathcal{A} a_1}{m} \pm \frac{1}{2} \sqrt{\left[\frac{c - \frac{1}{2}\rho U \mathcal{A} a_1}{(m)}\right]^2 - 4\frac{k}{m}}.$$
 (1.2)

Galloping essentially occurs at low frequencies therefore it can be assumed that the spring is relevantly weak and therefore,  $k \to 0$ . Hence a single non-zero eigenvalue remains which is,

$$\lambda = -\frac{c - \frac{1}{2}\rho U \mathcal{A}a_1}{m}.\tag{1.3}$$

Further, if it is assumed that the mechanical damping is weaker than the fluid dynamic forces on the body the non zero eigenvalue could be further simplified to,

$$\lambda = \frac{\frac{1}{2}\rho U \mathcal{A}a_1}{m}.\tag{1.4}$$

 $\Pi_2$ 

In this representation  $\lambda$  represents the inverse time scale of the motion of the body due to the effect of long-time fluid dynamic forces (or forced due to the induced velocity). This term could also be re-written and  $\lambda$  could be expressed as

$$\lambda = \frac{a_1}{m^*} \frac{U}{D} \tag{1.5}$$

This form clearly shows the significant parameters that influences the inverse time scale of the system.  $\partial C_Y/\partial \alpha$ , the rate of change in the fluid dynamic force on the body, with respect to the induced angle of attack, is represented by  $a_1$ .  $\frac{U}{D}$  represents the inverse advective time scale of the incoming flow, and the mass ratio is resented by  $m^*$ . Increasing  $a_1$  would result in a rapid change of the fluid dynamic force with a small change of the induced angle  $\theta$ , which is proportional to transverse velocity  $\dot{y}$ . It can be seen in equation 1.5 that an increase of  $a_1$  would result in an increase of the inverse time scale or decrease the response time of the body. In contrast the mass ratio has the opposite effect where an increase in  $m^*$  will lead to a decrease in  $\lambda$ , since a heavier body (or a body with higher inertia) would have a slower response.

In order to find the relevant dimensionless groups of the problem, the time scale formulated could be used to non-dimensionalise the equation of motion. The equation of motion presented in Equation \*\*KJ: put final equation of motion \*\* can be non-dimensionalised using the non-dimensional time  $\tau$ , defined as  $\tau = t(a_1/m^*)(U/D)$ . The non-dimensional equation of motion could then be represented as,

$$\ddot{Y} + \frac{m^{*2}}{a_1^2} \frac{kD^2}{mU^2} Y = \left(\frac{1}{2} - \frac{m^*}{a_1} \frac{cD}{mU}\right) \dot{Y} - \frac{a_1 A_3}{m^{*2}} \dot{Y}^3 + \frac{a_1^3 a_5}{m^{*4}} \dot{Y}^5 - \frac{a_1^5 a_7}{m^{*6}} \dot{Y}^7.$$
 (1.6)

The equation could be further altered by regrouping the coefficients into non-dimensional groups and could be expressed as,

$$\ddot{Y} + \frac{4\pi^2 m^{*2}}{U^{*2} a_1^2} Y = \left(\frac{1}{2} - \frac{c^* m^*}{a_1}\right) \dot{Y} - \frac{a_1 A_3}{m^{*2}} \dot{Y}^3 + \frac{a_1^3 a_5}{m^{*4}} \dot{Y}^5 - \frac{a_1^5 a_7}{m^{*6}} \dot{Y}^7, \tag{1.7}$$

 $U^*$  is the reduced velocity which is the typical independent variable ussed in vortexinduced vibration studies.  $c^*$  is the non-dimensional damping parameter which is expressed as  $c^* = cD/mU$ .

By analysing equation 1.7 it is clear that five dimensionless parameters play a role in setting the response of the system. These are namely the stiffness, damping, mass ratio, the

geometry and the Reynolds number. The stiffness is repented by the reduced velocity  $U^*$ , the damping by  $c^*$  and the mass ratio by  $m^*$ . The geometry and the Reynolds number are represented by the coefficients  $a_n$ , of the polynomial fit to the  $C_y$  curve. Using the natural time scales of the system, grouping of these non-dimensional parameters into two groups in the non-dimensional equation of motion, suggests that there are two groups that governs the response which are:  $\Gamma_1 = 4\pi^2 m^{*2}/U^{*2} a_1^2$  and  $\Gamma_2 = c^* m^*/a_1$ .  $\Gamma_1$  could be described as a combined mass-stiffness, where  $\Gamma_2$  could be expressed as a combined mass-damping parameter for a given geometry and a Reynolds number. It is assumed that the stiffness plays a minor role,  $\Gamma_2$  seems more likely parameter to collapse the data. The wind tunnel data in the classic paper of galloping by (Parkinson and Smith, 1964) adopted a parameter similar to  $\Gamma_2$  to collapse the data.

All of the quantities that formulate  $\Gamma_1$  and  $\Gamma_2$  except  $a_1$  in theory, could be obtained before an experiment. However in order to obtain the value of  $a_1$  static body experiments are required making it relatively difficult to obtain. Here, the *Re*and the geometry remains constant and therefore multiplying  $\Gamma_1$  with  $a_1^2$  and  $\Gamma_2$  with  $a_1$  suitable parameters could be obtained, and formulate a mass-stiffness parameter  $\Pi_1 = 4\pi^2 m^{*2}/U^{*2}$ , and a mass-damping parameter defined as  $\Pi_2 = c^* m^*$ . Therefore equation 1.7 can be written in terms of  $\Pi_1$  and  $\Pi_2$ .

$$\ddot{Y} + \Pi_1 Y = \Pi_2 \dot{Y} - \frac{a_1 a_3}{m^{*2}} \dot{Y}^3 + \frac{a_1^3 a_5}{m^{*4}} \dot{Y}^5 - \frac{a_1^5 a_7}{m^{*6}} \dot{Y}^7, \tag{1.8}$$

From equation 1.8, it is clear that the governing parameters of the non dimensionlised equation are  $\Pi_1$   $\Pi_2$  and  $m^*$ . However, form closer inspection it is possible to see that  $m^*$  has an impact on the non-linear terms of the forcing function. The velocity pf the and hence the induced angle of attack needs to be very high in order for the non-linear terms to be applicable.

### 1.3 Quasi-stedady state results

### 1.3.1 Classical VIV parameters vs. $\Pi_1$ and $\Pi_2$ .

Vortex-induced vibrations being another form fluid-structure interaction which occurs in a slender structure, has been investigated as candidate for power extraction from external flows. Significant progress on this problem have been made by Bernitsas et al. (2008, 2009); Raghavan and Bernitsas (2011); Lee and Bernitsas (2011) and other colleagues in VIVCACE group in the University of Michigan. Hence, it may seem that it is reasonable to present the data in a fluid-elastic problem using the same parameters in a VIV problem.

QSS data presented in figure 1.1 at Re = 200, shows a comparison between classical VIV and the newly formulated parameters presented as independent variables. The displacement amplitude, velocity amplitude and the mean power is presented in sub-figures (a), (c) and (e), as functions of the classical VIV parameter  $U^*$  for different  $\zeta$ . The same data as functions of  $\Pi_2$ , are presented in sub-figures (b), (d) and (f), for various, reasonably high values of  $\Pi_1$  \*\*KJ: put the parameters used section \*\*. Sub-figure (e) shows a similar trend to Barrero-Gil et al. (2010). The Value of the peak power remains constant. However, the power curve shifts to the right as  $\zeta$  is increased. Here, in figure 1.1 the maximum dimensionless power is achieved at two times the velocity at which the galloping starts, which is similar to the observations made by Barrero-Gil et al. (2010); Vicente-Ludlam et al. (2014). An excellent collapse for velocity amplitude and mean power could be observed on the data, presented using the dimensionless group  $\Pi_2$ , formulated using the natural time scales of the system. This implies that essentially velocity amplitude and the mean power is dictated by  $\Pi_2$  which furthermore, implies that the natural frequency of the system which is used to scale  $U^*$ ,  $\zeta$  and  $\Pi_1$ does not have a significant influence on the behaviour of the system, unlike VIV, which is a resonant phenomenon.

#### 1.3.2 High and low Re data

The successful collapse of data, mean power in particular using  $\Pi_2$  for low Reynolds number (Re=200), could be replicated at high Reynolds numbers. An example case is presented in figure 1.1 at Re=22300 for selected vales of  $\Pi_1$ . The successful collapse of mean power data at high Reynolds numbers shows that suitability of using  $\Pi_2$  as an independent variable across a large range of Reynolds numbers.

Hysteresis is evident in the high Reynolds number case (Re = 22300). Manipulating the initial condition (initial displacement) lead to obtaining different solutions for the same  $\Pi_2$  value. The upper and lower branch were obtained by giving an initial displacement which was higher than the expected amplitude and providing a lower initial displacement

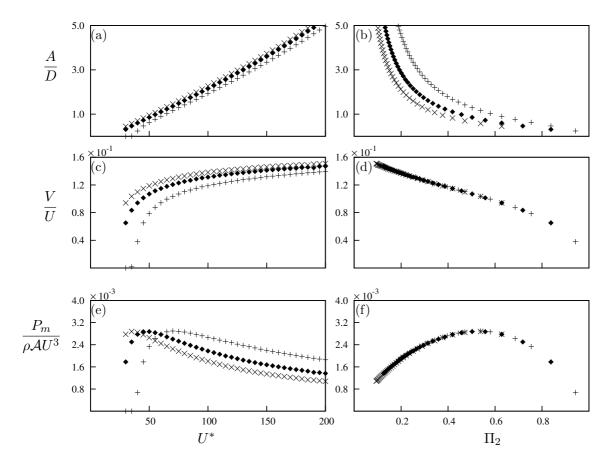


Figure 1.1: Displacement amplitude, velocity amplitude and dimensionless mean power data as functions of two different independent variables. Data presented in (a), (c) and (e) using the classical VIV parameter  $U^*$ , obtained at Re = 200 and  $m^* = 20$  at three different damping ratios:  $\zeta = 0.075$  (×),  $\zeta = 0.1$  ( $\spadesuit$ ) and  $\zeta = 0.15$  (+). (b) (d) and (f) are the same data presented using the combined mass-damping parameter ( $\Pi_2$ ) as the independent variable. Even though  $\Pi_1$  varies in the range of  $0.4 \le \Pi_1 \le 17.5$ , it is clear that the power is a function of  $\Pi_2$  only.

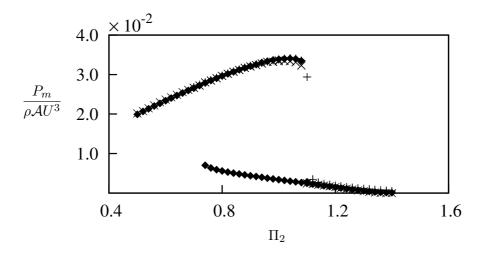


Figure 1.2: Dimensionless mean power as a function of  $\Pi_2$ . Data presented at (a) Re = 22300,  $\Pi_1 = 200$  (×),  $\Pi_1 = 2000$  ( $\spadesuit$ ) and  $\Pi_1 = 10000$  (+). Hysteresis could be observed at high Re.

respectively. Even though in theory, there is a possibility of a third state, this unstable branch could not be achieved with a time integration method (also observed by (Vio et al., 2007)) such as the one employed in this study.

### 1.3.3 Dependence on mass-stiffness, $\Pi_1$

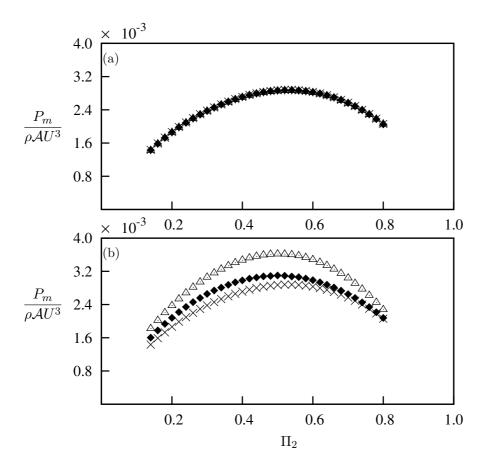


Figure 1.3: Dimensionless mean power as a function of  $\Pi_2$  obtained using the QSS model at Re = 200. (a) High  $\Pi_1$ ; data presented at four different combined mass-stiffness levels.  $\Pi_1 = 10 \ (m^* = 20, \ U^* = 40) \ (\times), \ \Pi_1 = 100 \ (m^* = 80, \ U^* = 50) \ (+), \ \Pi_1 = 500 \ (m^* = 220, \ U^* = 60) \ (\spadesuit)$  and  $\Pi_1 = 1000 \ (m^* = 400, \ U^* = 40) \ (\triangle)$ . (b) Low  $\Pi_1$ ; data presented at  $\Pi_1 = 10 \ (\times), \ \Pi_1 = 0.1 \ (\spadesuit)$ , and  $\Pi_1 = 0.01 \ (\triangle)$ .

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