
Abstract

Keywords: Fluid-structure interaction, transverse galloping.

1. Selection of the cross section

The cross section selection process for this study was based to three key criteria

- The cross section should have a bluff front face with sharp upstream corners for the flow to separate at the leading edges;
- As the proximity of shear layers to the body plays a vital role in creating C_y (?), the cross section should have a basic level of streamlining.
- The cross section should consist of a geometric profile in the afterbody, to inhibit or delay the shear layer reattachment.

The square cross section which has been widely used in galloping studies satisfies the first two selection criteria. Thus, a modification to the square cross section was done in order to meet the third criterion. Therefore, in order to inhibit the shear layer reattachment, the top and bottom sides of the trailing edges of the square were tapered off and a hybrid cross section of a rectangle and a triangle (illustrated in figure 1), i.e, a pentagon was produced.

The inhibition of the shear layer can be varied systematically by varying one parameter, $\frac{d}{l}$; which was an advantage of this cross section. The ratio $\frac{d}{l}$ was varied from 1 to zero in increments of 0.25 where 1 is the square cross section and 0 is an isosceles triangle.

2. Static body results

Stationary time averaged C_y results were obtained for cross sections where $\frac{d}{l} = 1, 0.75, 0.5, 0.25$ and 0 using DNS at $Re = 200$. Table 1 shows the

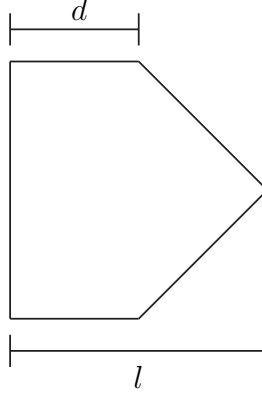


Figure 1: Illustration of the hybrid cross section (combination of a square and a triangle) obtained by tapering the afterbody of the square. The afterbody was changed by changing the ratio of $\frac{d}{l}$. Hence, data were obtained for $\frac{d}{l} = 1, 0.75, 0.5, 0.25$ and 0 were considered in this study.

coefficients of the 7th order curve fitting for each cross section. To achieve a better fit, piecewise interpolation using multiple 7th order polynomials were incorporated for a single cross section, giving more importance to accurately fitting the positive portion of the C_y curve; as the power transfer from the fluid to the body only occurs in this region.

The C_y vs. θ curves in figure 2 show the resultant of the piecewise curve-fits obtained for each cross section. A shift of the peak value of C_y to the right can be observed as the $\frac{d}{l}$ decreases therefore, the peak C_y occurs at higher induced angles. The overall trends of this behaviour agrees with trends of ? where the peak C_y value was shifted to higher induced angles when reattachment was delayed on a trapezoidal body. The peak value of C_y occurs at high induced velocities as $\frac{d}{l}$ is decreased because θ is proportional to the transverse velocity of the body via $\tan \theta = \frac{\dot{y}}{U}$. Thus, these bodies with a short straight section, or small $\frac{d}{l}$, satisfy one of the three conditions required to optimize the power transfer.

A negative region could be observed on the C_y vs. θ curves where $\frac{d}{l} \leq 0.25$. In this region C_y decreases as θ is increased and the increases after reaching a minimum, non-zero value of θ . The presence of this region indicates an unfavourable power transfer, i.e. power transferred from body to the fluid as the direction of the force and velocity vectors are out of phase. This implies that at low induced angles (when the \dot{y} is low), power transfer is from the body to the fluid and as the transverse velocity increases power transfers

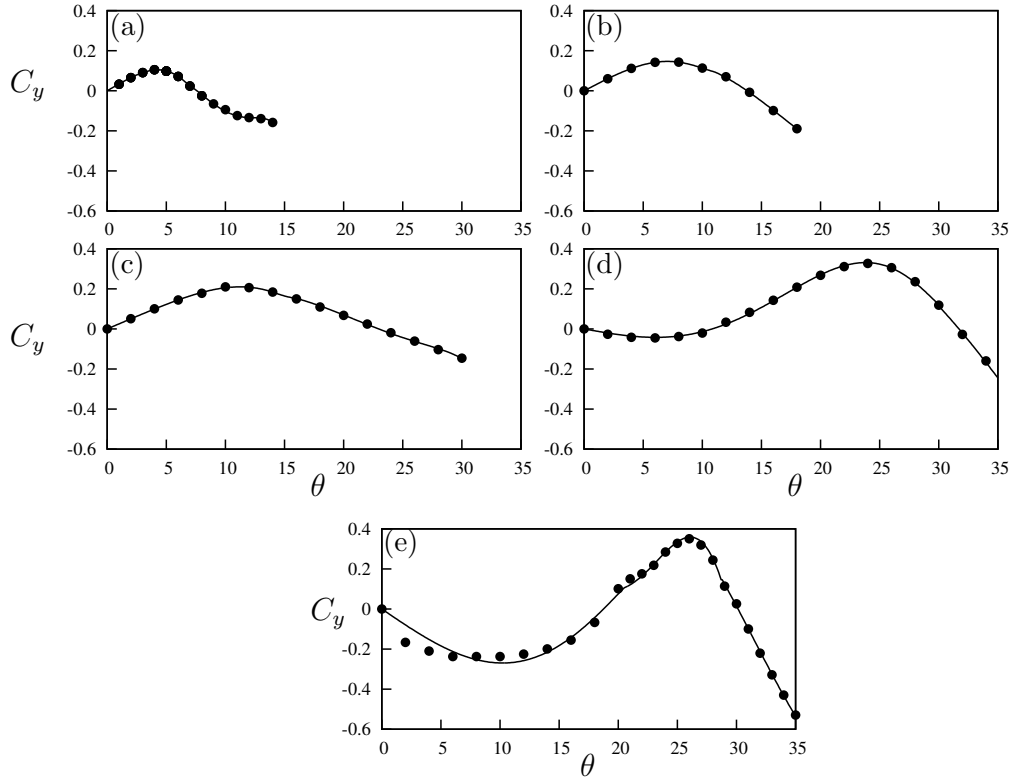


Figure 2: Induced lift coefficient C_y at different angles for selected cross sections. Data presented for cross sections, (a) square, (b) $\frac{d}{7} = 0.75$, (c) $\frac{d}{7} = 0.5$, (d) $\frac{d}{7} = 0.25$ and (e) triangle. Points (\bullet) are predicted from the static body simulations and the curves are the compound 7th order polynomials.

$\frac{d}{l}$	a_1	a_3	a_5	a_7	Overlap range
0	-2.30617	-269.075	-59.2929	4.74389	$20.5^\circ - 23.5^\circ$
	-5.08342	-56.5390	-160.505	-105.773	
	4.40685	19.9213	22.8894	7.68556	$28.6^\circ - 28.7^\circ$
0.25	-0.605146	-19.4346	-82.4463	-94.4226	$30.1^\circ - 30.2^\circ$
	2.50538	9.91021	10.2712	3.94112	
0.5	1.44734	4.83885	-166.900	-983.072	$14^\circ - 16^\circ$
	1.51455e	15.8476	52.5465	62.8067	
0.75	1.76938	35.2630	-345.562	-10072.7	$11.03^\circ - 11.11^\circ$
	1.77553	43.0120	262.983	638.484	

Table 1: Coefficient values used in the 7th order interpolation polynomial at $Re = 200$. Data present for $\frac{d}{l} = 0 - 0.75$ at increments of 0.25. Multiple polynomials were used to attain a better fit. The plot of the compound fit is presented in figure 2. The “Overlap” range refers to the range of angles which the transition of the two polynomials take place.

from fluid to the body. Thus, it means that the direction of power transfer can be different at different points in a particular oscillation cycle, which will be further discussed in section [Section](#).

3. QSS Mean power output

Predictions of the mean power output of these different cross sections were obtained using the QSS model using the curve fits presented in figure 2 as inputs. Figure 3 shows the mean power vs. Π_2 for different cross sections namely $\frac{d}{l} = 1, 0.75, 0.5, 0.25$ and 0. The cross sections are divided into two classes; high ($\frac{d}{l} > 0.25$) and low ($\frac{d}{l} \leq 0.25$). As Π_2 increases the mean power increases, peaks and reduces. For high $\frac{d}{l}$, the overall shape of the curves is

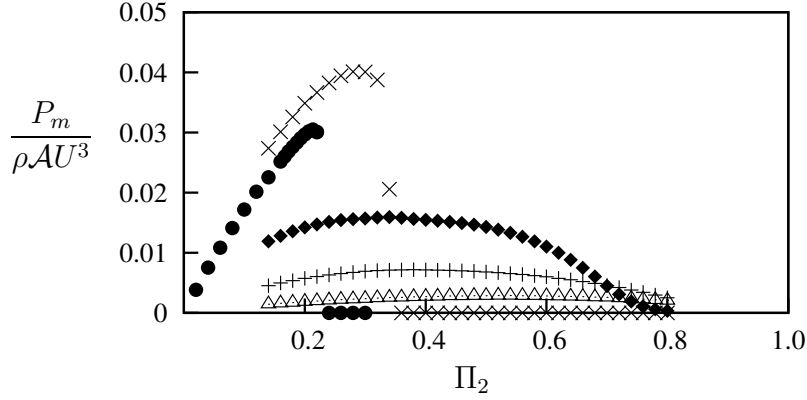


Figure 3: Dimensionless mean power obtained using QSS model as a function of Π_2 . Data presented for five selected cross sections, square (\triangle), $\frac{d}{l} = 0.75$ (+), $\frac{d}{l} = 0.5$ (\blacklozenge), $\frac{d}{l} = 0.25$ (\times) and triangle (\bullet) at $Re = 200$, $\Pi_1 = 100$.

similar, however as $\frac{d}{l}$ is decreased, the amount of power increases. For low $\frac{d}{l}$, the overall curve shape is markedly different; power first increases with Π_2 , then peaks, and then drops dramatically. The power extracted also appears to decrease with a decrease in $\frac{d}{l}$. Furthermore, negative regions of the C_y vs. θ curves in figure 2 appear in the low $\frac{d}{l}$ cases. The change in the trend of power, and the appearance of a negative region in the C_y , for the low $\frac{d}{l}$ cases clearly indicates that there is a distinct change in the flow structure for these cases which is discussed in section .

4. Flow characteristics at low $\frac{d}{l}$ cases

The analysis of the mean power and the static body results shows an indication of a significant change in the flow structure at low $\frac{d}{l}$ cases. As the variation of the mean C_y is the sole input of the fluid dynamics to the QSS model, the distinct features in the C_y vs. θ curves provides a good indication of the change in flow structure which results in the change in mean power discussed in section 3. The main distinct feature between the high and low $\frac{d}{l}$ cases is the negative region present at low $\frac{d}{l}$ in the C_y vs. θ curves. Therefore, it was of interest to investigate the cause of this region. The isosceles triangle ($\frac{d}{l} = 0$) is taken as the cross section of investigation as it produced the largest negative region out of the cross section considered in this study.

4.1. Surface pressure

The driving force of galloping F_y , which is the induced force is created as a result of the pressure difference created between the upper and lower sides of the body, due to the induced angle of attack occurred as a result of the horizontal movement of the flow and the transverse movement of the body. These pressure fields are created as a result of the relative proximities of the shear layer of the respective sides as discussed in ***KJ: Put the reference of the theory section ***. Hence, the pressure data of the time averaged flows of the stationary cross section ($\frac{d}{l} = 0$) is analysed here.

Time averaged surface pressure data on the top and bottom sides of the cross section were obtained at $\theta = 4^\circ$, $\theta = 16^\circ$ and $\theta = 21^\circ$ for the isosceles triangle. The specified angles corresponds to the key regions of the C_y vs. θ curve, i.e where the C_y is negative, but increasing in magnitude; C_y is negative, but decreasing in magnitude and C_y is significantly positive.

The surface pressure of the top and bottom surfaces of the body as a function of the distance from the leading edge is presented in figure 4. At $\theta = 4^\circ$, the pressure on the bottom of the body is greater than the top at practically all distances. Thus, a force is generated due to the pressure difference in the upward direction, which is against the velocity of the body according to the sign convention presented in ***KJ: Put the sign convention figure *** which results in a negative C_y .

The pressure difference between the top and bottom leading edges of the top and bottom sides reduces as θ is increased to 16° . For small distances downstream from the leading edge, the pressure on the top surface is greater than that on the bottom. This effect results in a reduction of the magnitude of C_y (although it is still negative).

The surface pressure on the top side becomes greater than the bottom over a majority portion of the body when θ is further increased to 21° . Thus, the net effect of the pressure difference leads to a positive C_y which is the driving force of galloping F_y , which now in phase with the velocity of the body.

4.2. Velocity profiles at the points of flow separation

Flow separation at the leading edge of the body plays a vital part in galloping, as it creates the shear layer which sustains galloping. Two wall jets could be observed in the top and bottom leading edges. A comparison of the velocity profiles of these wall jets can gain a clearer explanation on the behaviour of the pressure at the leading edges.

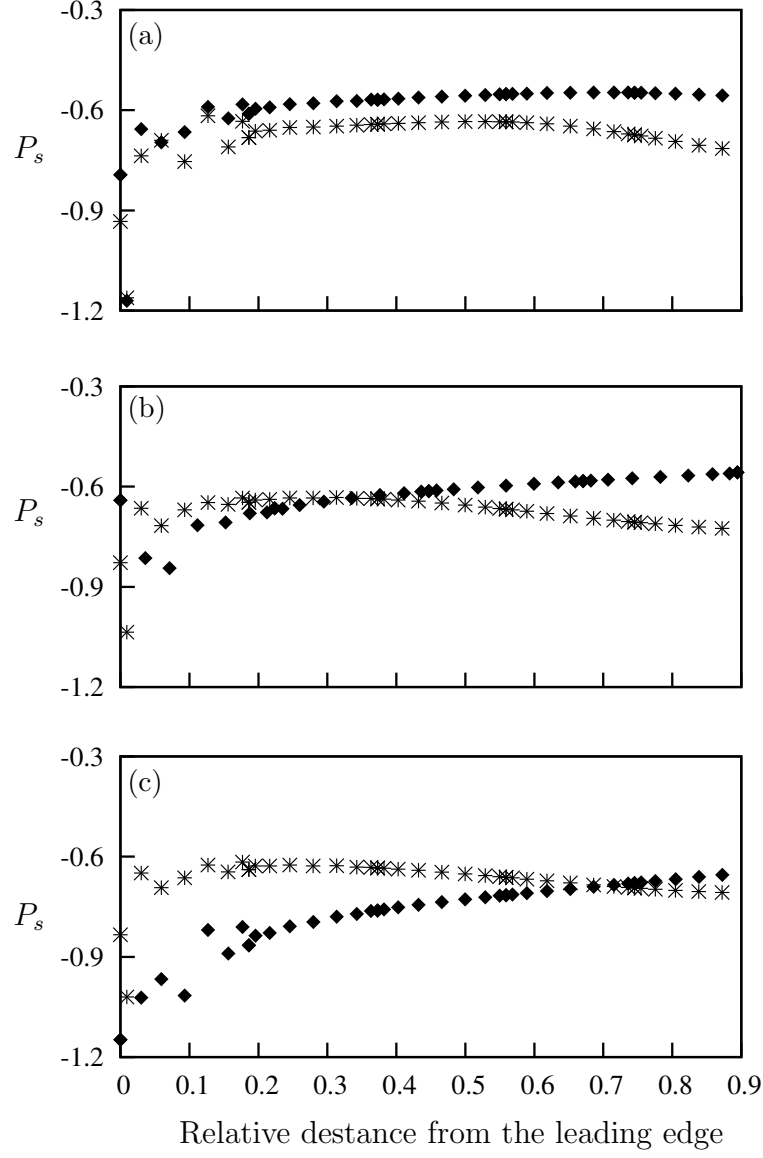


Figure 4: Surface pressure of top ($*$) and bottom (\blacklozenge) surfaces of the static triangular cross section at (a) $\theta = 4^\circ$, (b) $\theta = 16^\circ$ and (c) $\theta = 21^\circ$. A clear pressure difference is visible between the top and bottom surfaces. The top surface comparatively has more negative pressure compared to the bottom surface and reduces as θ is increased and vice versa occurs at the bottom surface. Thus, initially the effective force is upwards which results in a negative C_y . The effective C_y becomes positive as θ is increased.

Hence, mean velocity magnitude data of the flow were obtained along two lines parallel to the front wall of the cross section, one starting at the top and the other starting at the bottom leading edges of the cross section, spreading outward as illustrated in figure 5. The lengths of these lines were equal to the width of the cross section. Data were obtained for the same cases presented earlier i.e. isosceles triangle ($\frac{d}{l} = 0$) at $\theta = 4^\circ$, $\theta = 16^\circ$ and $\theta = 21^\circ$.

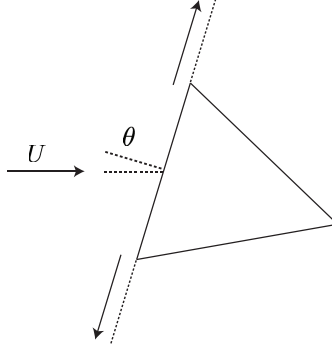


Figure 5: Illustration of the lines along which the flow velocity magnitudes have been extracted. The data have been extracted along a line starting from the separation points in the outward direction (shown with arrows) for the top and bottom surfaces.

The maximum velocity magnitude in the top wall jet at $\theta = 4^\circ$ (figure 6 (a)) is higher than that in the corresponding bottom wall jet, leading to a lower pressure at the top edge. However, the velocity magnitude in the bottom wall jet becomes greater than that in the top wall jet at $\theta = 16^\circ$. The difference between the top and bottom velocity magnitude in these wall jets tends to increase as θ is increased to 21° , where the velocity magnitude at the bottom is greater than at the top (figure 6 (c)). This effectively creates the pressure difference (according to the Bernoulli's principle) shown in figure 4 (c), which leads to a positive C_y and results in a forcing which is in phase with the velocity of the body.

4.3. Mean streamlines

The magnitude of the strain rate tensor is an excellent way of the visualising the shear layers as the strain rate is directly proportional to the shear stress and hence, will be high in the shear layers. The instantaneous flow-field data consists of vortex shedding on top of the shear layers. Therefore,

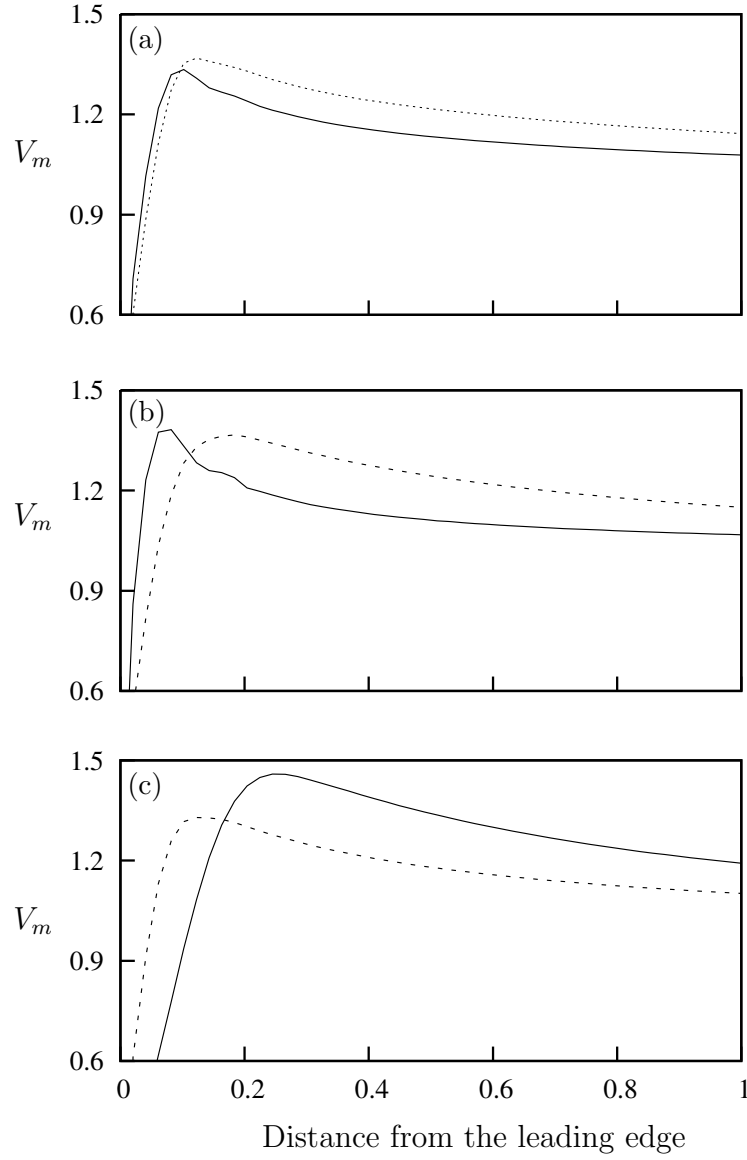


Figure 6: Velocity magnitudes of the flow along a line parallel to the front surface spreading towards top (---) and bottom (—) boundaries (figure 5). These two lines (for the top and bottom surfaces) start from the top and bottom leading edges of the triangular cross section. Data present (a) $\alpha = 4^\circ$, (b) $\alpha = 16^\circ$ and (c) $\alpha = 21^\circ$.

the flow-field data are time averaged over a vortex shedding cycle to filter out the vortex shedding .

The strain rate tensor of the flow can be expressed as,

$$\varphi = \frac{1}{2} \begin{bmatrix} 2\frac{\partial u}{\partial x} & \frac{\partial u}{\partial y} + \frac{\partial v}{\partial x} \\ \frac{\partial v}{\partial x} + \frac{\partial u}{\partial y} & 2\frac{\partial v}{\partial y} \end{bmatrix} \quad (1)$$

thus the magnitude of the strain rate tensor becomes,

$$|\varphi| = \frac{1}{2} \left(4\frac{\partial u}{\partial x}\frac{\partial v}{\partial y} + \left(\frac{\partial u}{\partial y} + \frac{\partial v}{\partial x} \right)^2 \right) \quad (2)$$

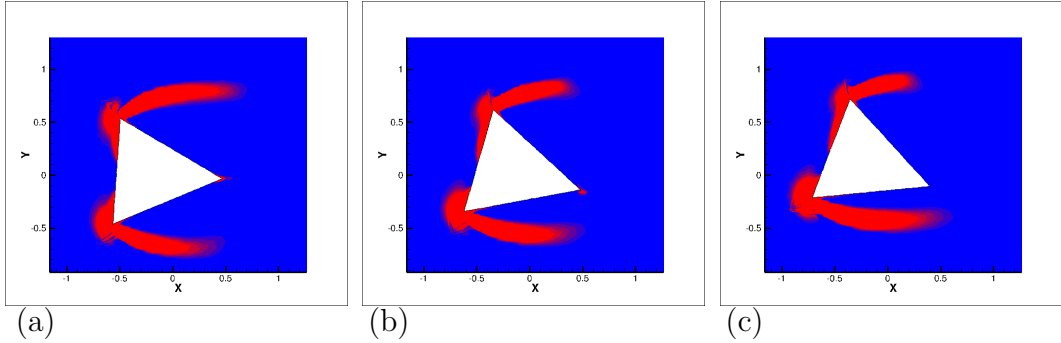


Figure 7: Contours of the magnitude of the shear strain rate of time averaged flow field on the stationary isosceles triangle ($\frac{d}{l} = 0$) at $Re = 200$ at different incidence angles. (a) 4° (negative value of C_y that is further decreasing with increasing θ), (b) 16° (negative value of C_y that is increasing with increasing θ) and (c) 21° (a significantly positive value of C_y). The bottom shear layer comes closer to the bottom wall and as the angle of incidence increases.

Contours of the magnitude of the strain rate tensor of the time-averaged flow-fields of the stationary isosceles triangle are presented in figure 7. Data present at $\theta = 4^\circ$, $\theta = 16^\circ$ and $\theta = 21^\circ$. It can be observed that the proximity of the bottom shear layer increases as θ is increased from $4^\circ - 21^\circ$.

Through a comparison of the pressure and velocity plot together with the flow-field data, it is clearly evident that two mechanisms govern the transverse forcing. The first mechanism is the pressure difference in each shear layer, created as a result of the uneven distribution of the flow created due to the profile and positioning (angle of attack) of the geometry. This uneven distribution creates a different speed wall jet on either side, and a simple consideration of Bernoulli's equation suggests the higher speed jet

will have a lower pressure. This forcing occurs out of phase or in the opposite direction of the transverse velocity of the body, as the lower speed (higher pressure) jet is formed on the lower side of the body (when the body is travelling down). The second mechanism is the relative proximity of the top and bottom shear layers. Regardless of the pressure in each shear layer, that pressure will have a larger influence on the force on the body the closer the shear layer is to the body. So, there are two ways to manipulate the force from the shear layers; increase the pressure difference between the shear layers by increasing the difference between the flow in each shear layer (a “streaming effect”); move the shear layers closer or further from the body (the “proximity effect”).

In the initial stage at $\theta = 4^\circ$ the streaming effect dominates. This can be clearly observed through a comparison of figures 7 (a) to (b) and (c). As the bottom shear layer is far from the body as $\theta = 4^\circ$ the proximity effect is low and hence, results in negative C_y .

As θ is increased first to $\theta = 16^\circ$ and then to 21° , the proximity effect becomes more dominant, as the proximity of the bottom shear layer to the wall of the body increases (figure 7 (b) and (c)). At least for the $\theta = 21^\circ$ case, this creates the positive region of the C_y vs. θ curve.

5. Fluid-structure interaction (DNS) results

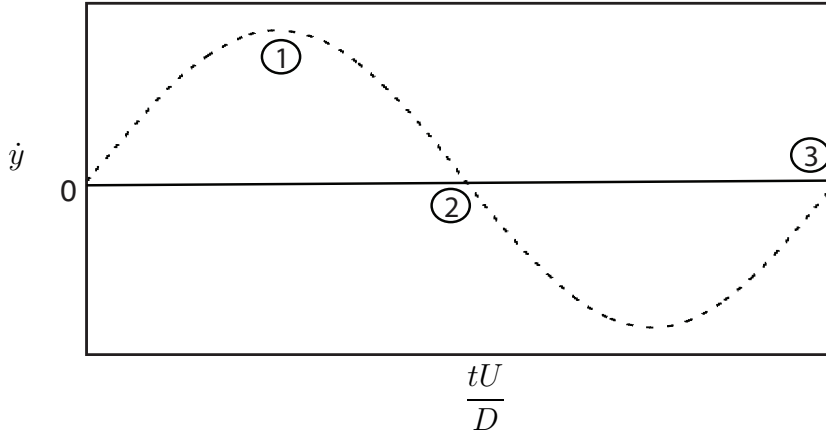


Figure 8: Illustration of the time history of velocity depicting the points considered to obtain time averaged stream traces. The points considered are: point 1 where \dot{y} is maximum, point 2 where \dot{y} is close to zero with a negative gradient and point 3 where \dot{y} is close to zero with a positive gradient.

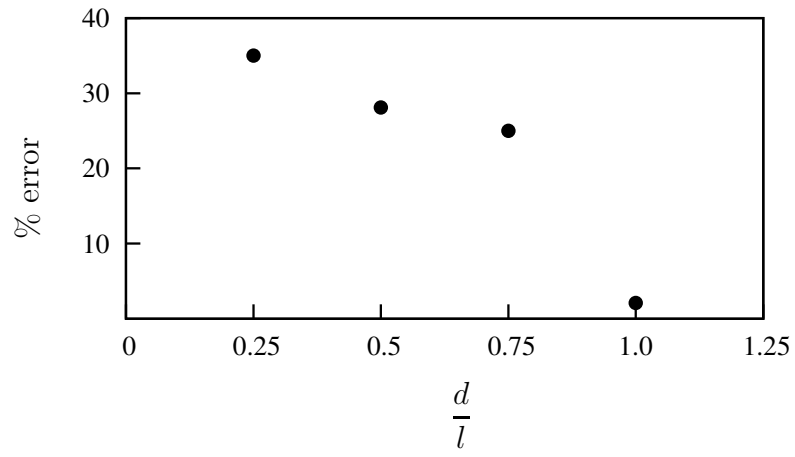


Figure 9: The percentage error calculated using equation ?? between the maximum power obtained using DNS data and predicted by QSS model as a function of $\frac{d}{l}$. The error reduces significantly as $\frac{d}{l} \rightarrow 1$.

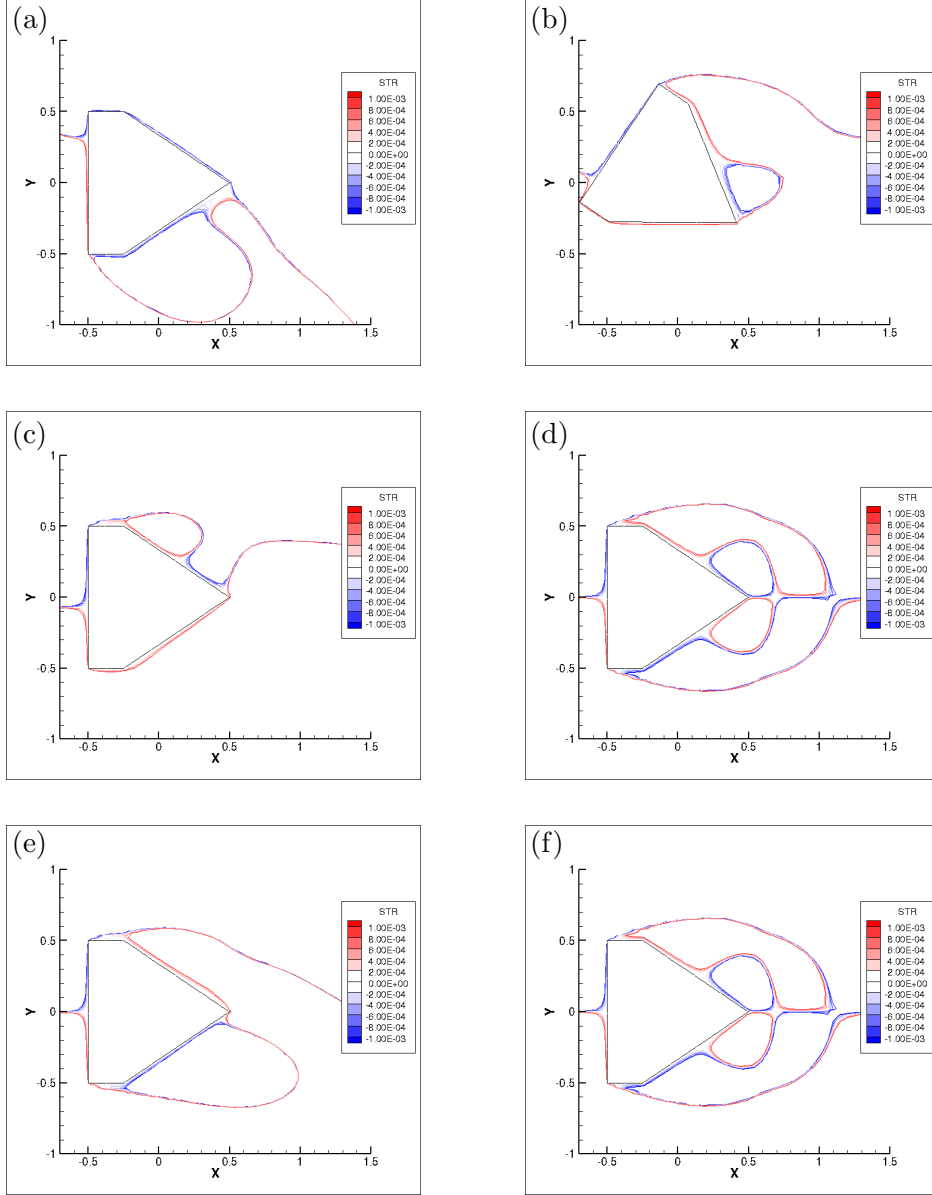


Figure 10: Time averaged stream functions of stationary and oscillating flow-fields of the hybrid cross section ($\frac{d}{l} = 0.25$), averaged over a vortex shedding cycle. (a), (c) and (e) are the averaged stream functions of the oscillating case at $\frac{tU}{D} = 2295.763$ (point 1), $\frac{tU}{D} = 2305.897$ (point 2) and $\frac{tU}{D} = 2325.870$ (point 3) . (b), (d) and (f) are the stream functions of the flow field of the stationary body corresponding to the induced angles of (a), (c) and (e).

References