

Data Science Final Project

MODEL 3: CLUSTERING TECHNIQUE

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Helper Packages And Modeling Packages

```
library(dplyr)

##
## Attaching package: 'dplyr'

## The following objects are masked from 'package:stats':
##
##     filter, lag

## The following objects are masked from 'package:base':
##
##     intersect, setdiff, setequal, union

library(ggplot2)
library(stringr)
library(cluster)
library(factoextra)

## Welcome! Want to learn more? See two factoextra-related books at https://goo.gl/ve3WBa

library(gridExtra)

##
## Attaching package: 'gridExtra'

## The following object is masked from 'package:dplyr':
##
##     combine

library(tidyverse)

## -- Attaching packages ----- tidyverse 1.3.2 --
```

```

## v tibble 3.1.8      v purrr   0.3.5
## v tidyverse 1.2.1    v forcats 0.5.2
## v readr   2.1.3

## -- Conflicts ----- tidyverse_conflicts() --
## x gridExtra::combine() masks dplyr::combine()
## x dplyr::filter()     masks stats::filter()
## x dplyr::lag()       masks stats::lag()

library(readr)
library(mclust)

## Package 'mclust' version 6.0.0
## Type 'citation("mclust")' for citing this R package in publications.
##
## Attaching package: 'mclust'
##
## The following object is masked from 'package:purrr':
##
##     map

```

IMPORTING THE DATA

```

set.seed(123)
radiomics_data <- read_csv("D:/1 MASTERS/STAT225/FINAL PROJECT/STAT 325 _FINAL PROJECT_/Normalize Radionics.csv")

## Rows: 197 Columns: 431
## -- Column specification -----
## Delimiter: ","
## chr  (1): Institution
## dbl (430): Failure.binary, Failure, Entropy_cooc.W.ADC, GLNU_align.H.PET, Mi...
##
## i Use 'spec()' to retrieve the full column specification for this data.
## i Specify the column types or set 'show_col_types = FALSE' to quiet this message.

```

Below are the first 6 of the data.

```
head(radiomics_data)
```

```

## # A tibble: 6 x 431
##   Institution Failure..1 Failure..2 Entropy..3 GLNU..4 Min_h..4 Max_h..5 Mean_h..6 Variance..7
##   <chr>          <dbl>     <dbl>     <dbl>     <dbl>     <dbl>     <dbl>     <dbl>
## 1 A              0     1.15     12.9    -0.433    -0.270    -0.257    -0.192    0.0509
## 2 A              1    -0.533     12.2     -1.02     0.671     0.405     0.490    0.687
## 3 A              0     2.24     12.8     0.179     -1.41     -1.57     -1.53    -1.57
## 4 A              1    -0.140     13.5     2.00     -0.218     0.0764    -0.153    0.0127
## 5 A              0     0.787     12.6     0.153     -1.06     -1.15     -1.45    -1.91
## 6 A              1    -2.80      13.2     0.391     -1.57     -1.91     -1.72    -1.84
## # ... with 422 more variables: Standard_Deviation_hist.PET <dbl>,
## #   Skewness_hist.PET <dbl>, Kurtosis_hist.PET <dbl>, Energy_hist.PET <dbl>,
## #   Entropy_hist.PET <dbl>, AUC_hist.PET <dbl>, H_suv.PET <dbl>,

```

```

## #  Volume.PET <dbl>, X3D_surface.PET <dbl>, ratio_3ds_vol.PET <dbl>,
## #  ratio_3ds_vol_norm.PET <dbl>, irregularity.PET <dbl>,
## #  tumor_length.PET <dbl>, Compactness_v1.PET <dbl>, Compactness_v2.PET <dbl>,
## #  Spherical_disproportion.PET <dbl>, Sphericity.PET <dbl>, ...

```

scaling/standardizing the data

```
radiomics_data <- radiomics_data[c(3:431)]
```

```
sum(is.na(radiomics_data))
```

```
## [1] 0
```

Since there is no N/A's, we can proceed with the clustering.

```
#CLUSTERS
```

K means clustering

```
kmeans(radiomics_data, centers = 3, iter.max = 100, nstart = 100)
```

```

## K-means clustering with 3 clusters of sizes 44, 103, 50
##
## Cluster means:
##           Failure Entropy_cooc.W.ADC GLNU_align.H.PET Min_hist.PET Max_hist.PET
## 1  -0.24619905          12.33268     0.126606986   0.04582414  0.08498506
## 2   0.06533738          12.23104    -0.009427189  -0.43614178 -0.46164331
## 3   0.08209356          12.32898    -0.091994139   0.85812682  0.87619837
##           Mean_hist.PET Variance_hist.PET Standard_Deviation_hist.PET Skewness_hist.PET
## 1      0.08473313        0.2277805            0.04100243   -0.5424529
## 2     -0.45835946       -0.3328592            -0.43567962  -0.1562938
## 3      0.86965533        0.4852431            0.86141787   0.7993239
##           Kurtosis_hist.PET Energy_hist.PET Entropy_hist.PET AUC_hist.PET H_suv.PET
## 1     -0.06873937       -1.2397463            -0.1534404  -1.20290321 -0.1720189
## 2      0.04875016        0.1318335            -0.5421416  -0.09783915 -0.3528293
## 3     -0.03993469       0.8193998            1.2518393   1.26010348  0.8782050
##           Volume.PET X3D_surface.PET ratio_3ds_vol.PET ratio_3ds_vol_norm.PET
## 1      0.4515175        0.1228859            -1.031642260  -0.9243764
## 2     -0.4469966       -0.3135307            -0.002503013  -0.0514460
## 3      0.5234776        0.5377336            0.913001395   0.9194300
##           irregularity.PET tumor_length.PET Compactness_v1.PET Compactness_v2.PET
## 1     -0.9580603        -0.3146062            -1.06054229  0.0007560935
## 2     -0.2024322        -0.3575160            -0.04050121  -0.3312421924
## 3      1.2601035        1.0133370            1.01671038   0.6816947970
##           Spherical_disproportion.PET Sphericity.PET Asphericity.PET Center_of_mass.PET
## 1                  -0.9243764        0.008385093   -0.92270228  -0.1662871
## 2                  -0.0514460        -0.408748277  -0.04630539  -0.2828044
## 3                  0.9194300        0.834642568   0.90736711   0.7289097
##           Max_3D_diam.PET Major_axis_length.PET Minor_axis_length.PET

```

```

## 1      0.4046184      0.2921464      0.09507154
## 2     -0.5662795     -0.5482485     -0.54506409
## 3      0.8104716      0.8723031      1.03916907
## Least_axis_length.PET Elongation.PET Flatness.PET Max_cooc.L.PET
## 1      0.2609288     -0.8077720     -0.5658959     -1.2368186
## 2     -0.5442359     -0.2537675     -0.3405795      0.1175010
## 3      0.8915085      1.2336004      1.1995823      0.8463483
## Average_cooc.L.PET Variance_cooc.L.PET Entropy_cooc.L.PET DAVE_cooc.L.PET
## 1     -0.4955642     -0.6734268     -0.2683455     -0.6448461
## 2     -0.3623110     -0.1757674     -0.4970677     -0.2723810
## 3      1.1824572      0.9546964      1.2601035      1.1285694
## DVAR_cooc.L.PET DENT_cooc.L.PET SAVE_cooc.L.PET SVAR_cooc.L.PET
## 1     -0.6762875     -0.7051941     -0.4938394     -0.6635562
## 2     -0.1908866     -0.3104527     -0.3629185     -0.1976191
## 3      0.9883594      1.2601035      1.1821908      0.9910248
## SENT_cooc.L.PET ASM_cooc.L.PET Contrast_cooc.L.PET Dissimilarity_cooc.L.PET
## 1     -0.9310482     -1.2286049     -0.5543879     -0.6448461
## 2     -0.2139714      0.1318891     -0.1506873     -0.2723810
## 3      1.2601035      0.8094807      0.7982773      1.1285694
## Inv_diff_cooc.L.PET Inv_diff_norm_cooc.L.PET IDM_cooc.L.PET
## 1     -0.7769917      -0.8136118     -0.8851310
## 2     -0.2737576      -0.2641384     -0.1967642
## 3      1.2476933      1.2601035      1.1842495
## IDM_norm_cooc.L.PET Inv_var_cooc.L.PET Correlation_cooc.L.PET
## 1     -0.9668136     -0.9006801     -0.3583977
## 2     -0.1986930     -0.1926182     -0.3347999
## 3      1.2601035      1.1893919      1.0050778
## Autocorrelation_cooc.L.PET Tendency_cooc.L.PET Shade_cooc.L.PET
## 1     -0.4279069     -0.6635562     -0.37662109
## 2     -0.2521613     -0.1976191     -0.06384699
## 3      0.8960104      0.9910248      0.46295135
## Prominence_cooc.L.PET IC1_.L.PET IC2_.L.PET Coarseness_vdif_.L.PET
## 1     -0.64429095    -0.02864872    -1.0005069     -1.2467745
## 2     -0.06485971    0.28929559    -0.1824053      0.1388886
## 3      0.70058703    -0.57073804    1.2562010      0.8110514
## Contrast_vdif_.L.PET Busyness_vdif_.L.PET Complexity_vdif_.L.PET
## 1     -0.70538289     0.2285534     -0.8090014
## 2     -0.02509042     -0.3707759     -0.1974261
## 3      0.67242321     0.5626713      1.1186189
## Strength_vdif_.L.PET SRE_align.L.PET LRE_align.L.PET GLNU_align.L.PET
## 1     -0.8797615     -1.28600130    -0.7769197      0.4271735
## 2      0.1337268     -0.06234094    -0.2798127     -0.3993524
## 3      0.4987130      1.26010348    1.2601035      0.4467533
## RLNU_align.L.PET RP_align.L.PET LGRE_align.L.PET HGRE_align.L.PET
## 1      0.4741659     -1.27752719    -1.1293148105   -0.4397308
## 2     -0.4020416     -0.06596095     0.0003066527   -0.2605452
## 3      0.4109397      1.26010348     0.9931653287   0.9236862
## LGSRE_align.L.PET HGSRE_align.L.PET LGHRE_align.L.PET HGLRE_align.L.PET
## 1     -1.13704860    -0.4544490     -1.0938526389   -0.3818739
## 2      0.00150105    -0.2532377     -0.0002880775   -0.2914542
## 3      0.99751061    0.9215848      0.9631837619   0.9364447
## GLNU_norm_align.L.PET RLNU_norm_align.L.PET GLVAR_align.L.PET
## 1     -1.28913655     -1.22301869   -0.6236610
## 2      0.05022954     -0.08924613   -0.2126497

```

```

## 3          1.03096731          1.26010348          0.9868800
##   RLVAR_align.L.PET Entropy_align.L.PET SZSE.L.PET LZSE.L.PET LGLZE.L.PET
## 1      -1.10120014       -0.3046051 -1.1695429 -0.2558248 -1.140945043
## 2      -0.02323398       -0.4815782 -0.1120901 -0.4485566 -0.002220365
## 3      1.01691811       1.2601035  1.2601035  1.1491524  1.008605590
##   HGLZE.L.PET SZLGE.L.PET SZHGE.L.PET LZLGE.L.PET LZHGE.L.PET GLNU_area.L.PET
## 1     -0.4543853 -1.169002746 -0.5172963 -0.92951089 -0.2704267      0.4164200
## 2     -0.2601593  0.001671419 -0.2327100 -0.02472047 -0.3085215      -0.4001837
## 3     0.9357872  1.025279294  0.9346034  0.86889376  0.8735299      0.4579289
##   ZSNU.L.PET ZSP.L.PET GLNU_norm.L.PET ZSNU_norm.L.PET GLVAR_area.L.PET
## 1     0.4712947 -1.0700979       -1.28758586      -1.0104268      -0.6375918
## 2    -0.4102506 -0.1545715       0.04986928      -0.1800621      -0.2146953
## 3     0.4303770  1.2601035       1.03034483      1.2601035      1.0033531
##   ZSVAR.L.PET Entropy_area.L.PET Max_cooc.H.PET Average_cooc.H.PET
## 1     -0.5201697       -0.2298400      -1.0439220      -0.8667845
## 2    -0.2132431       -0.5135166       0.1787787      -0.2414238
## 3     0.8970301       1.2601035       0.5503672      1.2601035
##   Variance_cooc.H.PET Entropy_cooc.H.PET DAVE_cooc.H.PET DVAR_cooc.H.PET
## 1     -0.1075906       -0.1512476      -0.3368512      -0.3489379
## 2     -0.5534078       -0.5127561      -0.4670489      -0.4579410
## 3     1.2346999       1.1893755       1.2585499      1.2504238
##   DENT_cooc.H.PET SAVE_cooc.H.PET SVAR_cooc.H.PET SENT_cooc.H.PET
## 1     -0.1765452       -0.7370141      -0.2179443      -0.7925095
## 2     -0.5101347       -0.2968597      -0.5086056      -0.1373389
## 3     1.2062372       1.2601035       1.2395185      0.9803265
##   ASM_cooc.H.PET Contrast_cooc.H.PET Dissimilarity_cooc.H.PET
## 1     -1.1500618       -0.3225785      -0.3368512
## 2     0.2172291       -0.4438519      -0.4670489
## 3     0.5645624       1.1982041       1.2585499
##   Inv_diff_cooc.H.PET Inv_diff_norm_cooc.H.PET IDM_cooc.H.PET
## 1     -0.9444524       -0.1622969      -0.92210693
## 2     -0.1145474       -0.1151856      -0.05599947
## 3     1.0670858       1.2601035       0.92681301
##   IDM_norm_cooc.H.PET Inv_var_cooc_.H.PET Correlation_cooc.H.PET
## 1     -1.23089598      -1.13861682      -0.2937629
## 2     -0.08588108       0.03014244      -0.3674791
## 3     1.26010348      0.93988938      1.0155183
##   Autocorrelation_cooc.H.PET Tendency_cooc.H.PET Shade_cooc.H.PET
## 1     -0.8758287      -0.08212314      0.01301747
## 2     -0.2311291      -0.55484894      0.28955287
## 3     1.2468553       1.21525719      -0.60793428
##   Prominence_cooc.H.PET IC1_d.H.PET IC2_d.H.PET Coarseness_vdif.H.PET
## 1     0.05657518      -0.5767901      -0.3672377      -1.2288138
## 2     -0.47574640      0.3320062      -0.4234805      0.1365392
## 3     0.93025143      -0.1763575      1.1955390      0.8000853
##   Contrast_vdif.H.PET Busyness_vdif.H.PET Complexity_vdif.H.PET
## 1     -0.56946460      0.5441468      -0.91557198
## 2     -0.05874494      -0.4356625      -0.07505258
## 3     0.62214341      0.4186155      0.96031165
##   Strength_vdif.H.PET SRE_align.H.PET LRE_align.H.PET RLNU_align.H.PET
## 1     -0.9370565      -0.5654173      -0.7052421      0.5000366
## 2     0.2374769       -0.3701632      -0.2153213      -0.4136037
## 3     0.3354073       1.2601035      1.0641749      0.4119913
##   RP_align.H.PET LGRE_align.H.PET HGRE_align.H.PET LGSRE_align.H.PET

```

```

## 1      -0.5198775      -1.1991256      -0.7736121      -1.1999048
## 2      -0.3896171       0.1184110      -0.2735091       0.1187439
## 3      1.2601035       0.8113038      1.2442073       0.8113038
##   HGSRE_align.H.PET LGHRE_align.H.PET HGLRE_align.H.PET GLNU_norm_align.H.PET
## 1      -0.6712253      -1.1990100      -0.5793873      -1.02059613
## 2      -0.3249637       0.1172528      -0.1800196       0.03756653
## 3      1.2601035       0.8135873      0.8807012       0.82073753
##   RLNU_norm_align.H.PET GLVAR_align.H.PET RLVAR_align.H.PET Entropy_align.H.PET
## 1      -0.4211417      -0.07605649     -0.66403304     -0.09440151
## 2      -0.4317955      -0.54757978     -0.01909491     -0.57137386
## 3      1.2601035       1.19494406     0.62368460     1.26010348
##   SZSE.H.PET LZSE.H.PET LGLZE.H.PET HGLZE.H.PET SZLGE.H.PET SZHGE.H.PET
## 1      -0.4467099      -0.27138729     -1.1989792     -0.6197406     -1.2012727     -0.4710644
## 2      -0.4030065      -0.07461144     0.1185232     -0.3368316     0.1195423     -0.3805777
## 3      1.2232981      0.39252039     0.8109439     1.2392449     0.8108628     1.1985268
##   LZLGE.H.PET LZHGE.H.PET GLNU_area.H.PET ZSNU.H.PET ZSP.H.PET
## 1      -0.9505149      -0.403462890    0.4027853     0.4708721     -0.2761913
## 2      0.1834368      0.002522648    -0.4063182     -0.3657920     -0.3878684
## 3      0.4585734      0.349850687    0.4825644     0.3391641     1.0420572
##   GLNU_norm.H.PET ZSNU_norm.H.PET GLVAR_area.H.PET ZSVAR_H.PET
## 1      -1.00764207    -0.3164794      -0.1075251     -0.40788949
## 2      0.01917366    -0.3840552      -0.5267189     0.02642073
## 3      0.84722728    1.0696557      1.1796629     0.30451604
##   Entropy_area.H.PET Max_cooc.W.PET Average_cooc.W.PET Variance_cooc.W.PET
## 1      -0.05105993    -1.2459112      0.1121741      0.2335546
## 2      -0.58988871    0.2202280      -0.4613212     -0.3253769
## 3      1.26010348    0.6427321      0.8516085      0.4647485
##   Entropy_cooc.W.PET DAVE_cooc.W.PET DVAR_cooc.W.PET DENT_cooc.W.PET
## 1      -0.1072905     0.006738718    0.1970246     -0.1803521
## 2      -0.5584923     -0.424119492    -0.3222303     -0.5229929
## 3      1.2449097     0.867756082    0.4904128     1.2360752
##   SAVE_cooc.W.PET SVAR_cooc.W.PET SENT_cooc.W.PET ASM_cooc.W.PET
## 1      0.1156181      0.2549118      -0.3617410     -1.2634130
## 2      -0.4622211     -0.3284163      -0.4561071     0.1984999
## 3      0.8504316      0.4522152      1.2579126     0.7028941
##   Contrast_cooc.W.PET Dissimilarity_cooc.W.PET Inv_diff_cooc.W.PET
## 1      0.1721288      0.006738718    -0.9375557
## 2      -0.3223858     -0.424119492    -0.1655483
## 3      0.5126415      0.867756082    1.1660786
##   Inv_diff_norm_cooc.W.PET IDM_cooc.W.PET IDM_norm_cooc.W.PET
## 1      -0.8558238     -0.90988988    -0.9828363
## 2      -0.2461061     -0.08797305    -0.1918482
## 3      1.2601035     0.98192759     1.2601035
##   Inv_var_cooc.W.PET Correlation_cooc.W.PET Autocorrelation_cooc.W.PET
## 1      -0.9370922     -0.3426602      0.3143182
## 2      -0.1190777     -0.3422077      -0.3619782
## 3      1.0699412      1.0064888      0.4690750
##   Tendency_cooc.W.PET Shade_cooc.W.PET Prominence_cooc.W.PET IC1_d.W.PET
## 1      0.2549118      0.2259899      0.3337971     -0.6258080
## 2      -0.3284163     -0.1930359      -0.2585297     0.3870571
## 3      0.4522152      0.1987828      0.2388296     -0.2466266
##   IC2_d.W.PET Coarseness_vdif.W.PET Contrast_vdif.W.PET Busyness_vdif.W.PET
## 1      -0.4866597     -1.2485044     -0.3595673     -0.1344966
## 2      -0.3970734     0.1742902     -0.2217484     -0.1646606

```

```

## 3 1.2462317          0.7396460          0.7732209          0.4575578
## Complexity_vdif.W.PET Strength_vdif.W.PET SRE_align.W.PET LRE_align.W.PET
## 1          0.2966242          -0.41636860         -0.7713867         -0.7984492
## 2          -0.3064288         -0.09767275         -0.2821763         -0.2476012
## 3          0.3702140          0.56761023         1.2601035         1.2126937
## GLNU_align.W.PET RLUU_align.W.PET RP_align.W.PET LGRE_align.W.PET
## 1          0.2964473          0.4903783          -0.6838744         -0.99421758
## 2          -0.3661553          -0.4103442          -0.3195602          0.04873235
## 3          0.4934063          0.4137762          1.2601035          0.77452284
## HGRE_align.W.PET LGSRE_align.W.PET HGSRE_align.W.PET LGHRE_align.W.PET
## 1          0.3171582          -1.01360410         0.3118848         -0.89164937
## 2          -0.3648013          0.03592996         -0.3575084          0.07771776
## 3          0.4723914          0.81795589         0.4620087          0.62455287
## HGLRE_align.W.PET GLNU_norm_align.W.PET RLUU_norm_align.W.PET
## 1          0.3285020          -1.14436073         -0.5348833
## 2          -0.3794703          0.09070163         -0.3832069
## 3          0.4926271          0.82019209         1.2601035
## GLVAR_align.W.PET RLVAR_align.W.PET Entropy_align.W.PET SZSE.W.PET
## 1          0.2469658          -0.88171590         -0.08897816        -0.5458488
## 2          -0.3400889          0.03912658         -0.57369063        -0.3785226
## 3          0.4832532          0.69530904         1.26010348        1.2601035
## LZSE.W.PET LGLZE.W.PET HGLZE.W.PET SZLGE.W.PET SZHGE.W.PET LZLGE.W.PET
## 1 -0.57423830 -1.00060806          0.3030741         -1.08553622         0.2676319        -0.7098443
## 2 -0.05493204          0.03609125         -0.3612973          0.01377567        -0.3411788        0.1221971
## 3 0.61848970          0.80618711         0.4775674          0.92689401         0.4673123        0.3729370
## LZHGE.W.PET GLNU_area.W.PET ZSNU.W.PET ZSP.W.PET GLNU_norm.W.PET
## 1 0.2910763          0.3497735          0.4790935        -0.4311684         -1.14171833
## 2 -0.3855402          -0.3914134         -0.3951841        -0.4241199         0.07906742
## 3 0.5380657          0.4985108          0.3924770         1.2531151         0.84183325
## ZSNU_norm.W.PET GLVAR_area.W.PET ZSVAR.W.PET Entropy_area.W.PET Min_hist.ADC
## 1 -0.3987918          0.2290786         -0.57384578        -0.05587383        -0.2839460
## 2 -0.4342701          -0.3293288         0.05364306        -0.58783229        -0.1360750
## 3 1.2455332          0.4768281          0.39447957         1.26010348        0.5356019
## Max_hist.ADC Mean_hist.ADC Variance_hist.ADC Standard_Deviation_hist.ADC
## 1 -0.4635840          -0.3889453         -0.57324808        -0.6677390
## 2 -0.4109585          -0.4404749         -0.09465534        -0.2637073
## 3 1.2549000          1.2496503          0.69944832         1.1308474
## Skewness_hist.ADC Kurtosis_hist.ADC Energy_hist.ADC Entropy_hist.ADC
## 1 -0.06412824          0.05489374         -1.2248338        -0.4447917
## 2 -0.18754348          -0.16659367         0.1306280        -0.4216926
## 3 0.44277242          0.29487646         0.8087608         1.2601035
## AUC_hist.ADC Volume.ADC X3D_surface.ADC ratio_3ds_vol.ADC
## 1 -0.8187563          0.4137352          -0.06062747         -0.7495328
## 2 -0.2619403          -0.4230570         -0.27514913         -0.1973241
## 3 1.2601035          0.5074105          0.62015938         1.0660761
## ratio_3ds_vol_norm.ADC irregularity.ADC Compactness_v1.ADC Compactness_v2.ADC
## 1 -0.5665482          -0.6588633         -1.27996576        -0.7091030
## 2 -0.3696801          -0.3302445          0.03139817        -0.2320236
## 3 1.2601035          1.2601035          1.06168964         1.1019793
## Spherical_disproportion.ADC Sphericity.ADC Asphericity.ADC Center_of_mass.ADC
## 1 -0.5665482          -0.8263138         -0.4562283        -0.30889853
## 2 -0.3696801          -0.2587123         -0.3555244        -0.08723432
## 3 1.2601035          1.2601035          1.1338612         0.45153340
## Max_3D_diam.ADC Major_axis_length.ADC Minor_axis_length.ADC

```

```

## 1      -0.2272466      -0.3096826      -0.2273920
## 2      -0.3641393      -0.4002567      -0.3810801
## 3       0.9501040      1.0970495      0.9851300
## Least_axis_length.ADC Elongation.ADC Flatness.ADC Max_cooc.L.ADC
## 1      -0.1584101      -0.4555603      -0.4352743      -1.21898466
## 2      -0.3766661      -0.4154356      -0.4102787      0.08247576
## 3       0.9153330      1.2566904      1.2282154      0.90280642
## Average_cooc.L.ADC Variance_cooc.L.ADC Entropy_cooc.L.ADC DAVE_cooc.L.ADC
## 1      -0.3334022      -0.6739796      -0.6246132      -0.6275483
## 2      -0.4657713      -0.1418733      -0.3448756      -0.2975032
## 3       1.2528828      0.8853611      1.2601035      1.1650991
## DVAR_cooc.L.ADC DENT_cooc.L.ADC SAVE_cooc.L.ADC SVAR_cooc.L.ADC
## 1      -0.6792861      -0.7163919      -0.3331065      -0.6644654
## 2      -0.1346799      -0.3056692      -0.4658976      -0.1328135
## 3       0.8752124      1.2601035      1.2528828      0.8583253
## SENT_cooc.L.ADC ASM_cooc.L.ADC Contrast_cooc.L.ADC Dissimilarity_cooc.L.ADC
## 1      -0.3986302      -1.2078330      -0.5907004      -0.6275483
## 2      -0.3227867      0.1096301      -0.1425577      -0.2975032
## 3       1.0157352      0.8370442      0.8134852      1.1650991
## Inv_diff_cooc.L.ADC Inv_diff_norm_cooc.L.ADC IDM_cooc.L.ADC
## 1      -0.8106287      -1.033224      -0.8257846
## 2      -0.2643399      -0.170323      -0.2353613
## 3       1.2578935      1.260102      1.2115347
## IDM_norm_cooc.L.ADC Inv_var_cooc.L.ADC Correlation_cooc.L.ADC
## 1      -1.1864475      -0.8125180      -0.6732339
## 2      -0.1048688      -0.2448072      -0.2079255
## 3       1.2601035      1.2193186      1.0207723
## Autocorrelation_.L.ADC Tendency_cooc.L.ADC Shade_.L.ADC Prominence_cooc.L.ADC
## 1      -0.3096152      -0.6644654      -0.06131213      -0.632012951
## 2      -0.3806305      -0.1328135      -0.08926511      0.009639142
## 3       1.0565602      0.8583253      0.23784081      0.536314765
## IC1_.L.ADC IC2_.L.ADC Coarseness_vdif_.L.ADC Contrast_vdif_.L.ADC
## 1      -0.3286775      -0.8504159      -1.2306293      -0.75531507
## 2       0.4221620      -0.2429369      0.1831016      -0.00426411
## 3      -0.5804176      1.2488160      0.7057617      0.67346133
## Busyness_vdif_.L.ADC Complexity_vdif_.L.ADC Strength_vdif_.L.ADC
## 1      -0.4833384      -0.6202209      -0.35760129
## 2      -0.1266996      -0.2878726      -0.04138263
## 3       0.6863390      1.1388120      0.39993735
## SRE_align.L.ADC LRE_align.L.ADC GLNU_align.L.ADC RLNU_align.L.ADC
## 1      -1.22833517     -0.7704476      0.009702583      -0.04684558
## 2      -0.08697493     -0.2825775      -0.240760507      -0.22537592
## 3       1.26010162     1.2601035      0.487428372      0.50549851
## RP_align.L.ADC LGRE_align.L.ADC HGRE_align.L.ADC LGSRE_align.L.ADC
## 1      -1.1846756      -1.2386718      -0.3621041      -1.2384754
## 2      -0.1056257      0.1448884      -0.3944579      0.1441628
## 3       1.2601035      0.7915610      1.1312349      0.7928837
## HGSRE_align.L.ADC LGHRE_align.L.ADC HGLRE_align.L.ADC GLNU_norm_align.L.ADC
## 1      -0.3718172      -1.2402380      -0.3207144      -1.22633549
## 2      -0.3912582      0.1518783      -0.4119247      -0.04113242
## 3       1.1331911      0.7785402      1.1307935      1.16390802
## RLNU_norm_align.L.ADC GLVAR_align.L.ADC RLVAR_align.L.ADC Entropy_align.L.ADC
## 1      -1.0564678      -0.6883319      -0.9937756      -0.7413903
## 2      -0.1603942      -0.1602669      -0.0982178      -0.2949903

```

```

## 3          1.2601035      0.9358820      1.0768529      1.2601035
## SZSE.L.ADC LZSE.L.ADC LGLZE.L.ADC HGLZE.L.ADC SZLGE.L.ADC SZHGE.L.ADC
## 1 -1.0514733 -0.4386766 -1.2381380 -0.3641634 -1.2347891 -0.3747242
## 2 -0.1625277 -0.3953429  0.1399974 -0.4018017  0.1376303 -0.3949377
## 3  1.2601035  1.2004418  0.8011667  1.1481754  0.8030950  1.1433289
## LZLGE.L.ADC LZHGE.L.ADC GLNU_area.L.ADC ZSNU.L.ADC ZSP.L.ADC
## 1 -1.2331796 -0.2671294 -0.003032553 -0.04621719 -0.8812271
## 2  0.1872096 -0.4080677 -0.238004422 -0.22780845 -0.2352542
## 3  0.6995465  1.0756933  0.492957756  0.50995654  1.2601035
## GLNU_norm.L.ADC ZSNU_norm.L.ADC GLVAR_area.L.ADC ZSVAR.L.ADC
## 1 -1.24380273 -0.8418370 -0.6976156 -0.3886638
## 2 -0.03057441 -0.2520807 -0.1626997 -0.1999883
## 3  1.15753016  1.2601012  0.9490632  0.7539999
## Entropy_area.L.ADC Max_cooc.H.ADC Average_cooc.H.ADC Variance_cooc.H.ADC
## 1 -0.6968516 -1.2195763 -0.4648233 -0.3952568
## 2 -0.3140165  0.1226214 -0.4131354 -0.4428532
## 3  1.2601035  0.8206280  1.2601035  1.2601035
## Entropy_cooc.H.ADC DAVE_cooc.H.ADC DVAR_cooc.H.ADC DENT_cooc.H.ADC
## 1 -0.2456499 -0.4106896 -0.4407048 -0.4873658
## 2 -0.5067629 -0.4362605 -0.4222198 -0.4035056
## 3  1.2601035  1.2601035  1.2575931  1.2600955
## SAVE_cooc.H.ADC SVAR_cooc.H.ADC SENT_cooc.H.ADC ASM_cooc.H.ADC
## 1 -0.4574294 -0.5523827 -0.4826353 -1.2187170
## 2 -0.4162940 -0.3757314 -0.4055264  0.1276736
## 3  1.2601035  1.2601035  1.2601035  0.8094090
## Contrast_cooc.H.ADC Dissimilarity_cooc.H.ADC Inv_diff_cooc.H.ADC
## 1 -0.3609737 -0.4106896 -1.1798197
## 2 -0.4341280 -0.4362605 -0.1075456
## 3  1.2119605  1.2601035  1.2597865
## Inv_diff_norm_cooc.H.ADC IDM_cooc.H.ADC IDM_norm_cooc.H.ADC
## 1 -1.1769913 -1.20553484 -1.21238942
## 2 -0.1089083 -0.08629617 -0.09378679
## 3  1.2601035  1.23864077  1.26010348
## Inv_var_cooc.H.ADC Correlation_cooc.H.ADC Autocorrelation_cooc.H.ADC
## 1 -1.2362039 -0.6754567 -0.5592331
## 2 -0.0746561 -0.2053340 -0.3728050
## 3  1.2416511  1.0173899  1.2601035
## Tendency_cooc.H.ADC Shade_cooc.H.ADC Prominence_cooc.H.ADC IC1_d.H.ADC
## 1 -0.5523827 -0.04021948 -0.5274542 -0.2930730
## 2 -0.3757314 -0.17187278 -0.3863805  0.3516626
## 3  1.2601035  0.38945107  1.2601035 -0.4665213
## IC2_d.H.ADC Coarseness_vdif.H.ADC Contrast_vdif.H.ADC Busyness_vdif.H.ADC
## 1 -0.7745696 -1.2274857 -0.4516339 -0.2332118
## 2 -0.2794834  0.1822561 -0.4186159 -0.1961535
## 3  1.2573571  0.7047403  1.2597865  0.6093025
## Complexity_vdif.H.ADC Strength_vdif.H.ADC SRE_align.H.ADC LRE_align.H.ADC
## 1 -0.3776594 -0.31448595 -1.28508015 -1.0977408
## 2 -0.4475287 -0.03715531 -0.06273425 -0.1427629
## 3  1.2542493  0.35328758  1.26010348  1.2601035
## GLNU_align.H.ADC RLNU_align.H.ADC RP_align.H.ADC LGRE_align.H.ADC
## 1 -0.05169972 -0.04863572 -1.27270722 -1.27672651
## 2 -0.22752508 -0.22997103 -0.06802005  0.03984021
## 3  0.51419743  0.51653976  1.26010348  1.04142924
## HGRE_align.H.ADC LGSRE_align.H.ADC HGSRE_align.H.ADC LGHRE_align.H.ADC

```

```

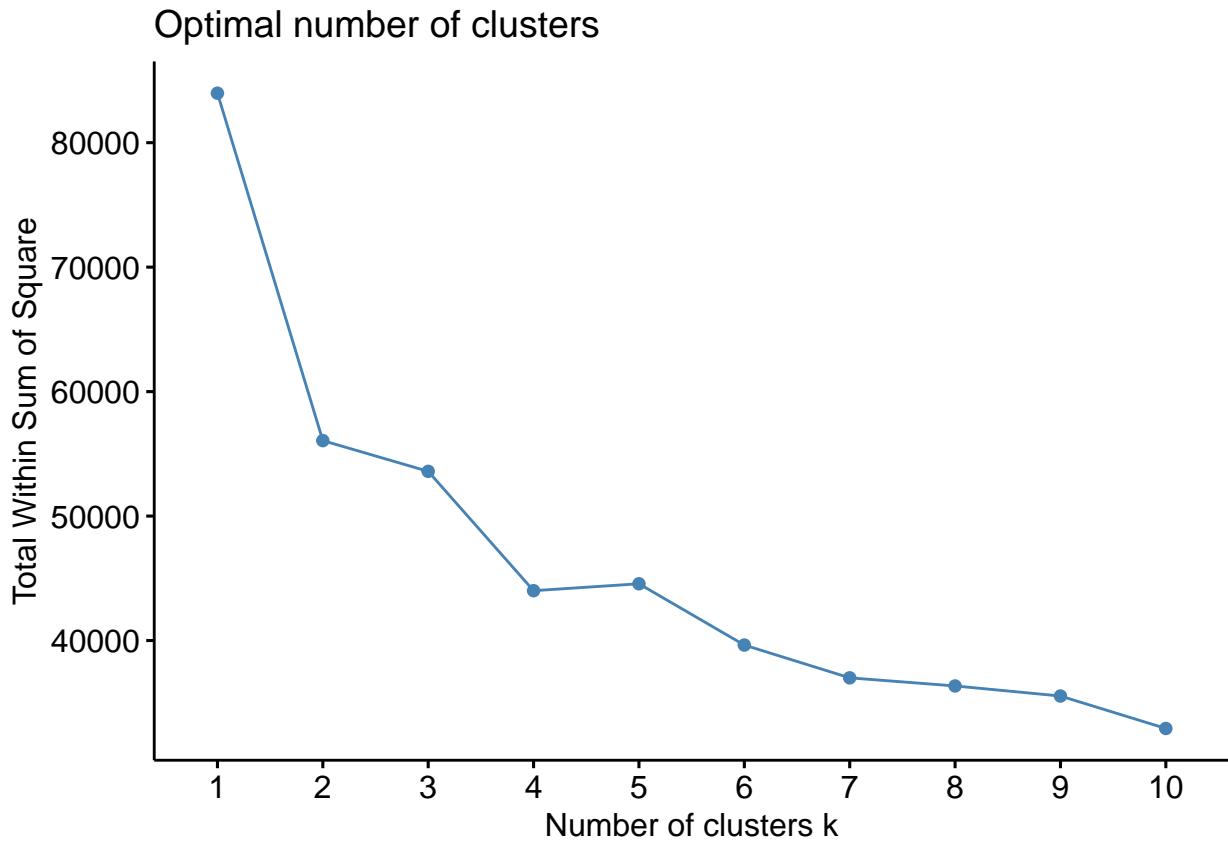
## 1      -0.5635528      -1.27571074      -0.4692509      -1.271448876
## 2      -0.3709597      0.04334384      -0.4112440      0.007470147
## 3      1.2601035      1.03332111      1.2601035      1.103486399
## HGLRE_align.H.ADC GLNU_norm_align.H.ADC RLNU_norm_align.H.ADC
## 1      -0.3916857      -1.25710430      -1.20154494
## 2      -0.4443787      0.05815368      -0.09841951
## 3      1.2601035      0.98645175      1.26010348
## GLVAR_align.H.ADC RLVAR_align.H.ADC Entropy_align.H.ADC SZSE.H.ADC LZSE.H.ADC
## 1      -0.4584233      -1.233836931     -0.7044152      -1.1327756      -0.7274341
## 2      -0.4158694      0.006015476     -0.3107856      -0.1277969      -0.3008986
## 3      1.2601035      1.073384619     1.2601035      1.2601035      1.2601035
## LGLZE.H.ADC HGLZE.H.ADC SZLGE.H.ADC SZHGE.H.ADC LZLGE.H.ADC LZHGE.H.ADC
## 1      -1.26419521     -0.6234993      -1.25631169     -0.4625418      -1.17805121     -0.5641318
## 2      0.04239107     -0.3453515      0.05393276     -0.4141100      -0.00305751     -0.3702458
## 3      1.02516668     1.2601035      0.99445300     1.2601035      1.04298353     1.2591423
## GLNU_area.H.ADC ZSNU.H.ADC ZSP.H.ADC GLNU_norm.H.ADC ZSNU_norm.H.ADC
## 1      -0.04629173     -0.0380691     -0.9989990     -1.25998052    -0.8734469
## 2      -0.22985144     -0.2346340     -0.1849442     0.05936074     -0.2385781
## 3      0.51423069     0.5168978     1.2601035      0.98604257     1.2601035
## GLVAR_area.H.ADC ZSVAR.H.ADC Entropy_area.H.ADC Max_cooc.W.ADC
## 1      -0.3959549      -0.86964158    -0.6175828      -1.2227040
## 2      -0.4425550      -0.02618112    -0.3478789      0.1289851
## 3      1.2601035      0.81922296    1.2601035      0.8102563
## Average_cooc.W.ADC Variance_cooc.W.ADC DAVE_cooc.W.ADC DVAR_cooc.W.ADC
## 1      -0.3004989      -0.57373994    -0.6384395      -0.6111998
## 2      -0.3720482      -0.08003143    -0.2959584      -0.0907048
## 3      1.0308583      0.66975588    1.1715010      0.7247077
## DENT_cooc.W.ADC SAVE_cooc.W.ADC SVAR_cooc.W.ADC SENT_cooc.W.ADC
## 1      -0.7144191      -0.3119314      -0.52193538     -0.3570017
## 2      -0.3065120      -0.3678297      -0.07787238     -0.3281686
## 3      1.2601035      1.0322287      0.61972023     0.9901887
## ASM_cooc.W.ADC Contrast_cooc.W.ADC Dissimilarity_cooc.W.ADC
## 1      -1.2185004      -0.5848798      -0.6384395
## 2      0.1275774      -0.1101784      -0.2959584
## 3      0.8094624      0.7416618      1.1715010
## Inv_diff_cooc.W.ADC Inv_diff_norm_cooc.W.ADC IDM_cooc.W.ADC
## 1      -1.0933303      -1.0324694      -1.15112454
## 2      -0.1118448      -0.1706458      -0.09016671
## 3      1.1925307      1.2601035      1.19873300
## IDM_norm_cooc.W.ADC Inv_var_cooc.W.ADC Correlation_cooc.W.ADC
## 1      -1.183584       -1.12975006    -0.6710596
## 2      -0.106092       -0.09544937    -0.2087147
## 3      1.260103       1.19080576    1.0204847
## Autocorrelation_cooc.W.ADC Tendency_cooc.W.ADC Shade_cooc.W.ADC
## 1      -0.2373656      -0.52193538     -0.01897833
## 2      -0.2456825      -0.07787238     -0.08227907
## 3      0.7149876      0.61972023     0.18619581
## Prominence_cooc.W.ADC IC1_d.W.ADC IC2_d.W.ADC Coarseness_vdif.W.ADC
## 1      -0.41203710     -0.09221458    -0.8157384      -1.2311552
## 2      0.02841938     0.32916605     -0.2632300      0.1693522
## 3      0.30404482     -0.59693323    1.2601035      0.7345515
## Contrast_vdif.W.ADC Busyness_vdif.W.ADC Complexity_vdif.W.ADC
## 1      -0.67751125     -1.09459202    -0.2913541
## 2      -0.03593965     -0.01151753    -0.1147268

```

Clustering using kmeans has 41.9 percent with k = 3.

K means clustering using WSS

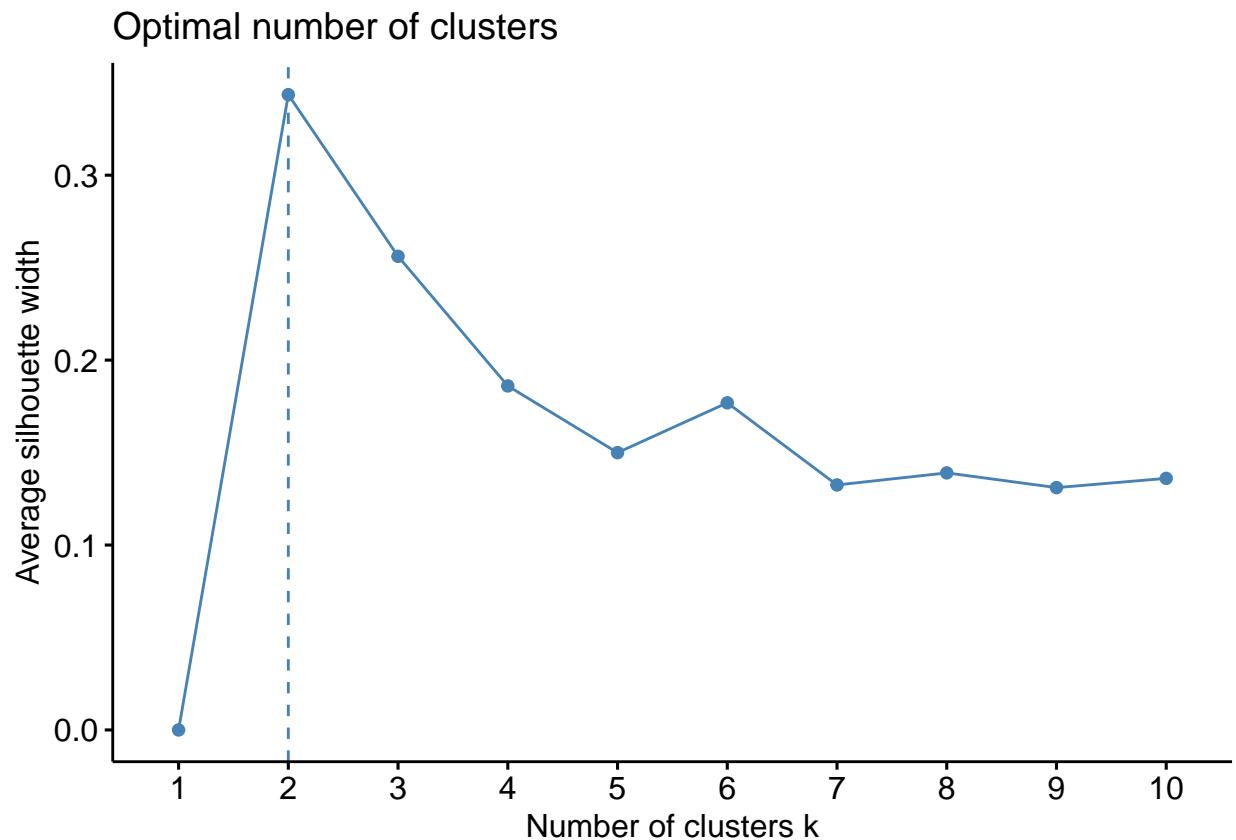
```
fviz_nbclust(radiomics_data, kmeans, method = "wss")
```



Using elbow method to identify k, k=2.

K means clustering using silhouette

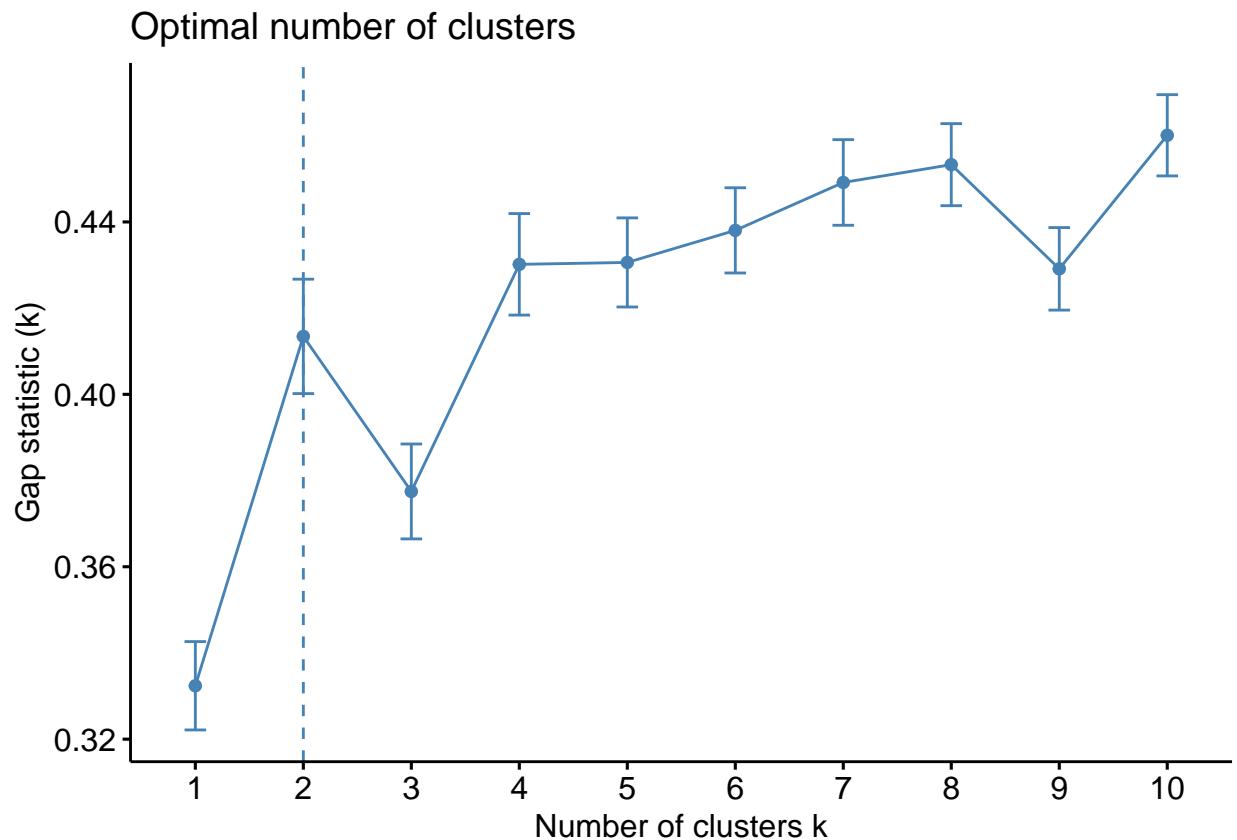
```
fviz_nbclust(radiomics_data, kmeans, method = "silhouette")
```



Silhouette suggest that number of cluster is 2.

K means clustering using gap_stat

```
fviz_nbclust(radiomics_data, kmeans, method = "gap_stat")
```



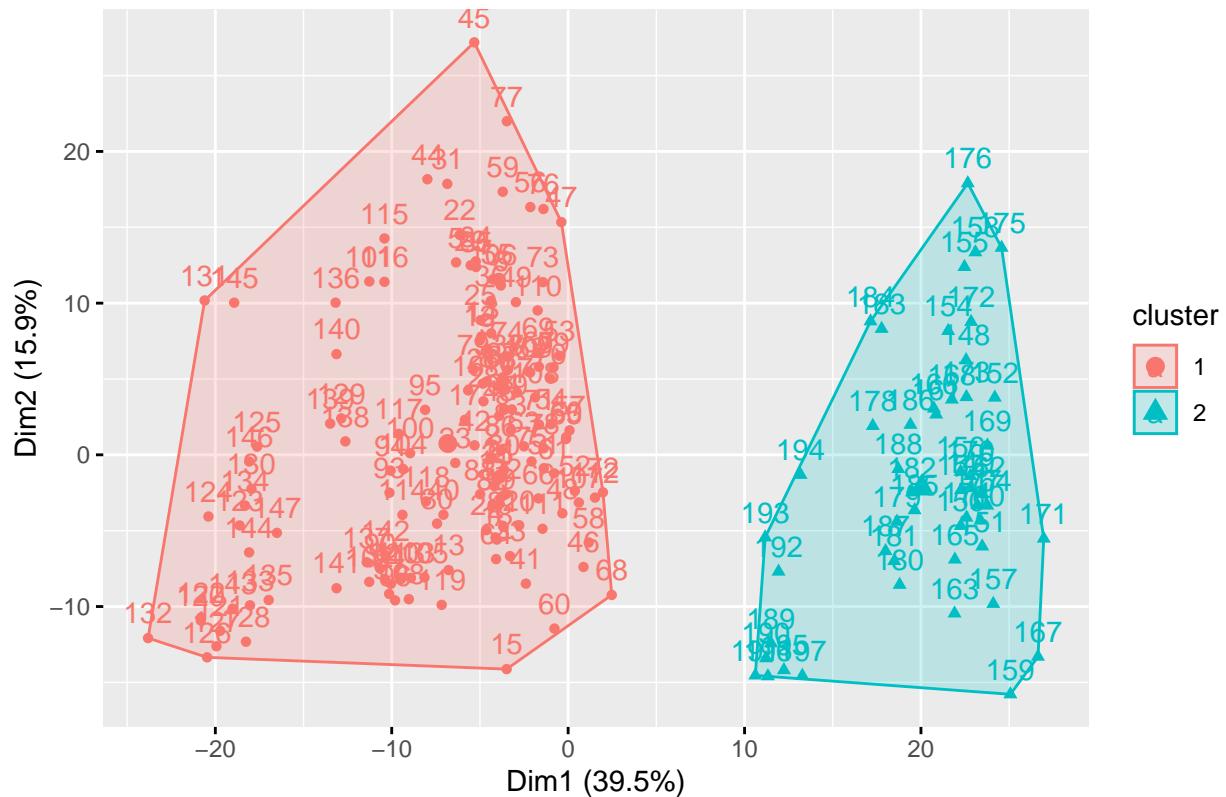
Gap-stat suggest that the number of cluster is 2.

Since cluster is equal to 2, the number of cluster is 2. Below is the cluster using 2 cluster.

```
clusters <- kmeans(radiomics_data, centers = 2, iter.max = 100, nstart = 100)
```

```
fviz_cluster(kmeans(radiomics_data, centers = 2, iter.max = 100, nstart = 100), data = radiomics_data)
```

Cluster plot



Above image shows the cluster structure using 2 number of clusters.

The quality of a k-means partition.

```
clusters$betweenss / clusters$totss
```

```
## [1] 0.3324189
```

The quality of k means partition is 0.4192 or 41.92 percent.

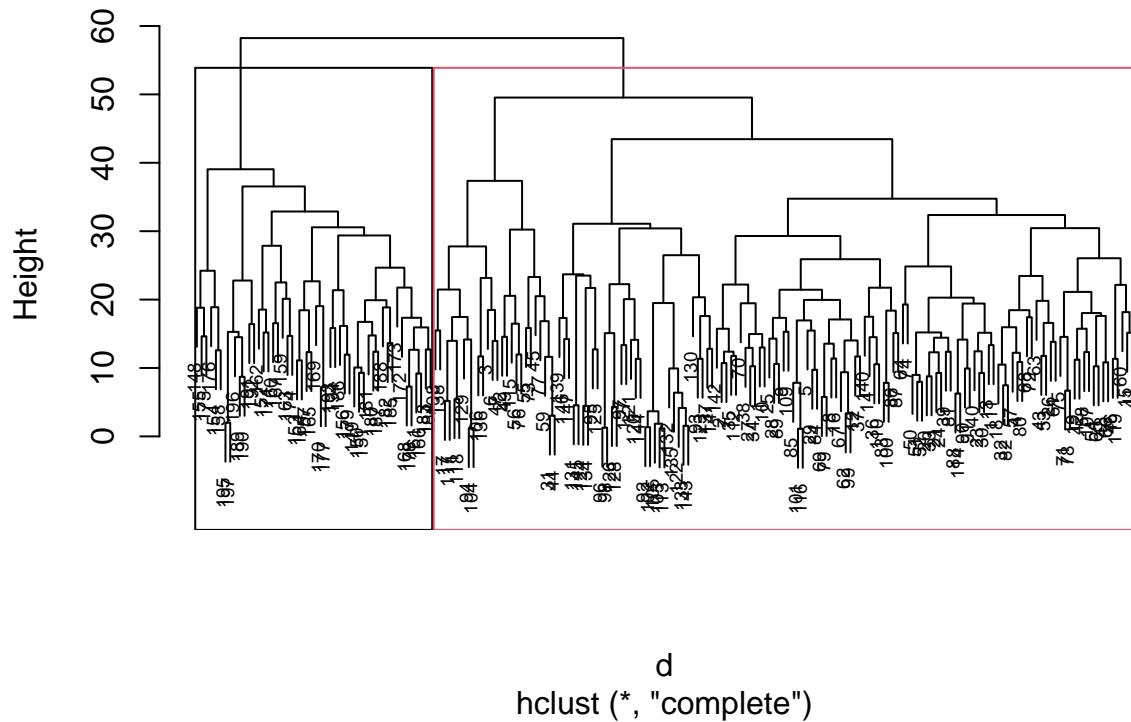
2. Heirarchical Clustering

```
radiomics_data <- radiomics_data %>%
  select_if(is.numeric) %>% # select numeric columns
  mutate_all(as.double) %>% # coerce to double type
  scale()
d <- dist(radiomics_data, method = "euclidean")
```

Hierarchical clustering using Complete Linkage

```
hc1 <- hclust(d, method = "complete")
plot(hc1, cex = 0.6)
rect.hclust(hc1, k = 2, border = 1:4)
```

Cluster Dendrogram



Hierarchical clustering using AGNES

```
set.seed(123)
hc2 <- agnes(radiomics_data, method = "complete")
hc2$ac

## [1] 0.8076961
```

Using the AGNES, it has 80.77 percent quality of partition.

Hierarchical clustering using DIANA

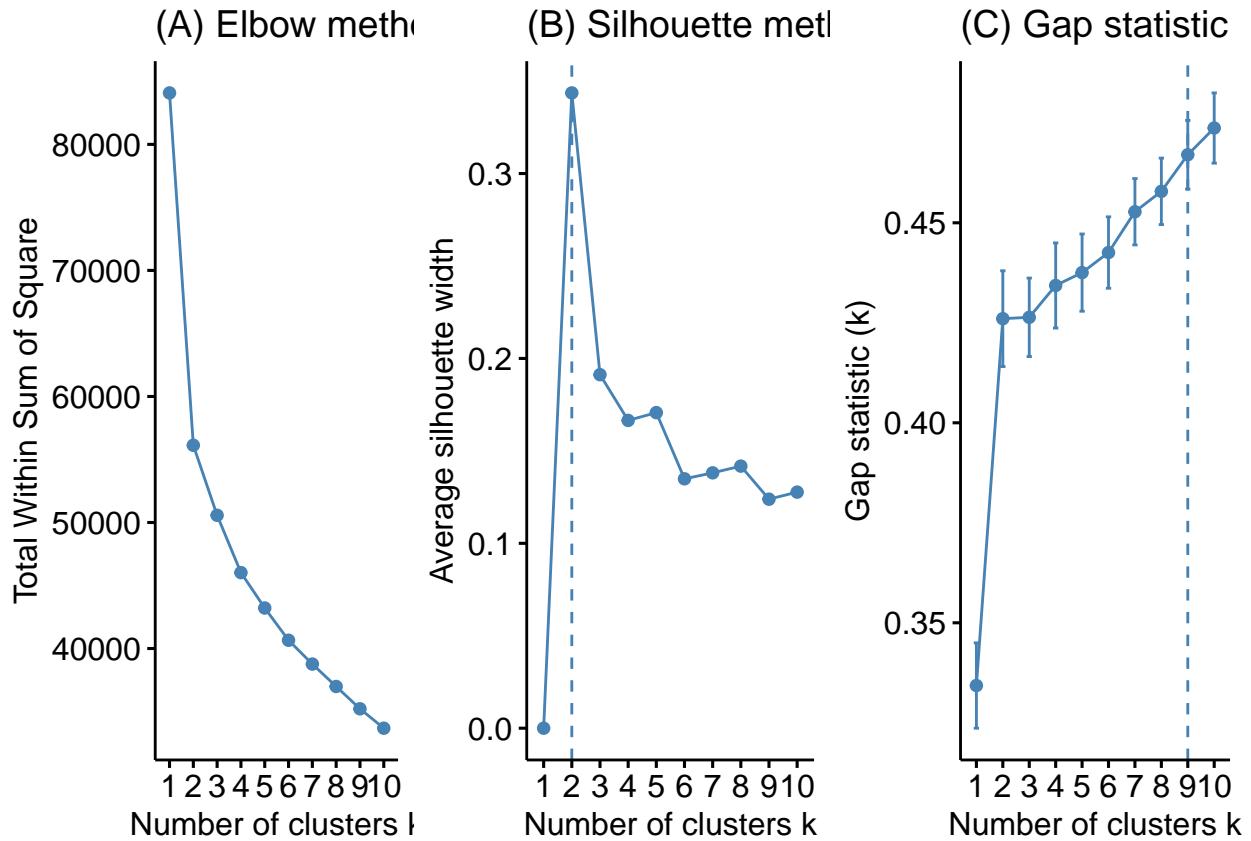
```
hc4 <- diana(radiomics_data)
hc4$dc
```

```
## [1] 0.7919039
```

Using the DIANA, it has 79.19 percent quality of partition.

```
wss_plot <- fviz_nbclust(radiomics_data, FUN = hcut, method = "wss",
  k.max = 10) +
  ggtitle("(A) Elbow method")
silhouette_plot <- fviz_nbclust(radiomics_data, FUN = hcut, method = "silhouette",
  k.max = 10) +
  ggtitle("(B) Silhouette method")
gapstat_plot <- fviz_nbclust(radiomics_data, FUN = hcut, method = "gap_stat",
  k.max = 10) +
  ggtitle("(C) Gap statistic")
```

```
gridExtra::grid.arrange(wss_plot, silhouette_plot, gapstat_plot, nrow = 1)
```



The result of the graph shows that they give different number of cluster in each method. Elbow method gives 3, silhouette gives 2 and gap stat gives 9. The difference between heirarchical and k means is that k means gives the same number of cluster in gap stat, silhouette and elbow method. While in heirarchical does not.

Ward's method

```
hc5 <- hclust(d, method = "ward.D2" )
sub_grp <- cutree(hc5, k = 9)
table(sub_grp)
```

```
## sub_grp
##  1  2  3  4  5  6  7  8  9
## 25 33 46 12 21 10 19 22  9
```

Above is the number of sample in each cluster. If number of cluster is 8, the member of cluster is 22.

3. Model Based

```
set.seed(123)
model_based3 <- Mclust(radiomics_data[,1:10], G=3)
summary(model_based3)

##
## Gaussian finite mixture model fitted by EM algorithm
##
## Mclust VEE (ellipsoidal, equal shape and orientation) model with 3 components:
##
## log-likelihood   n  df      BIC      ICL
##           -1074.583 197 89 -2619.371 -2638.94
##
## Clustering table:
##   1  2  3
## 111 50 36
```

The result shows 3 optimal number of clusters with BIC -2632.206. A negative zone with the highest value indicates the preferred model, In general, the lower the BIC value, the better. Plot the results with BIC, density and uncertainty.

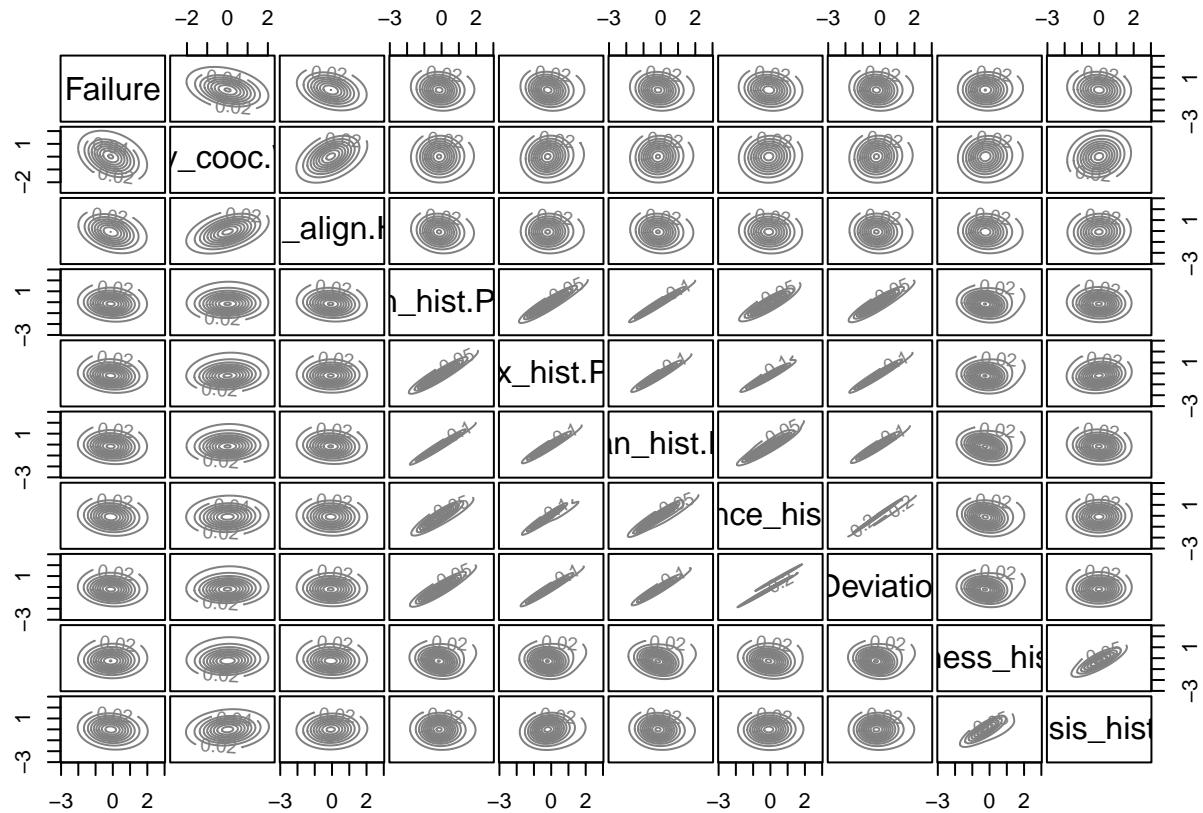
```
set.seed(123)
model_based4 = Mclust(radiomics_data, 1:9)
summary(model_based4)

##
## Gaussian finite mixture model fitted by EM algorithm
##
## Mclust VEI (diagonal, equal shape) model with 9 components:
##
## log-likelihood   n  df      BIC      ICL
##           -77829.42 197 4306 -178408.3 -178408.3
##
## Clustering table:
##   1  2  3  4  5  6  7  8  9
## 32 29 25 11 21 41 19 10  9
```

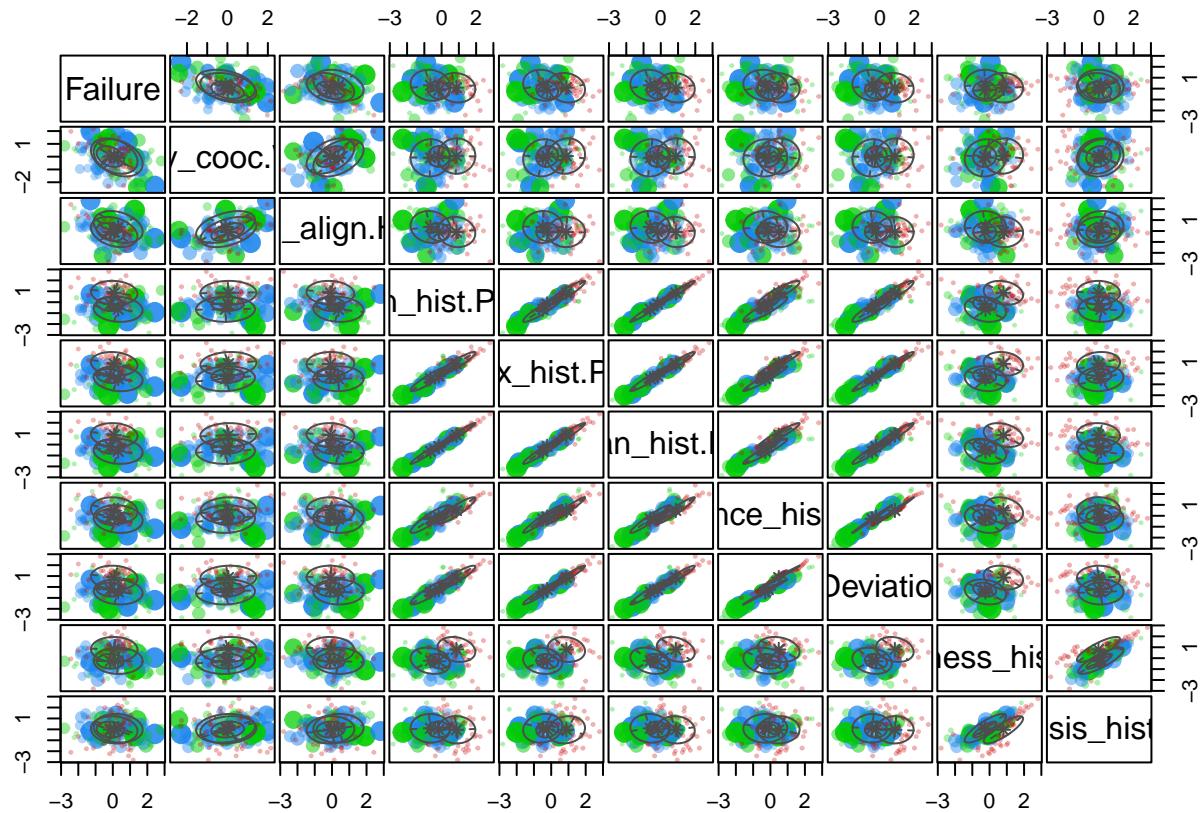
The result shows 3 optimal number of clusters with BIC -178301. A negative zone with the highest value indicates the preferred model, In general, the lower the BIC value, the better. Plot the results with BIC, density and uncertainty.

Plot results

```
plot(model_based3, what = "density")
```



```
plot(model_based3, what = "uncertainty")
```



Observations with high uncertainty

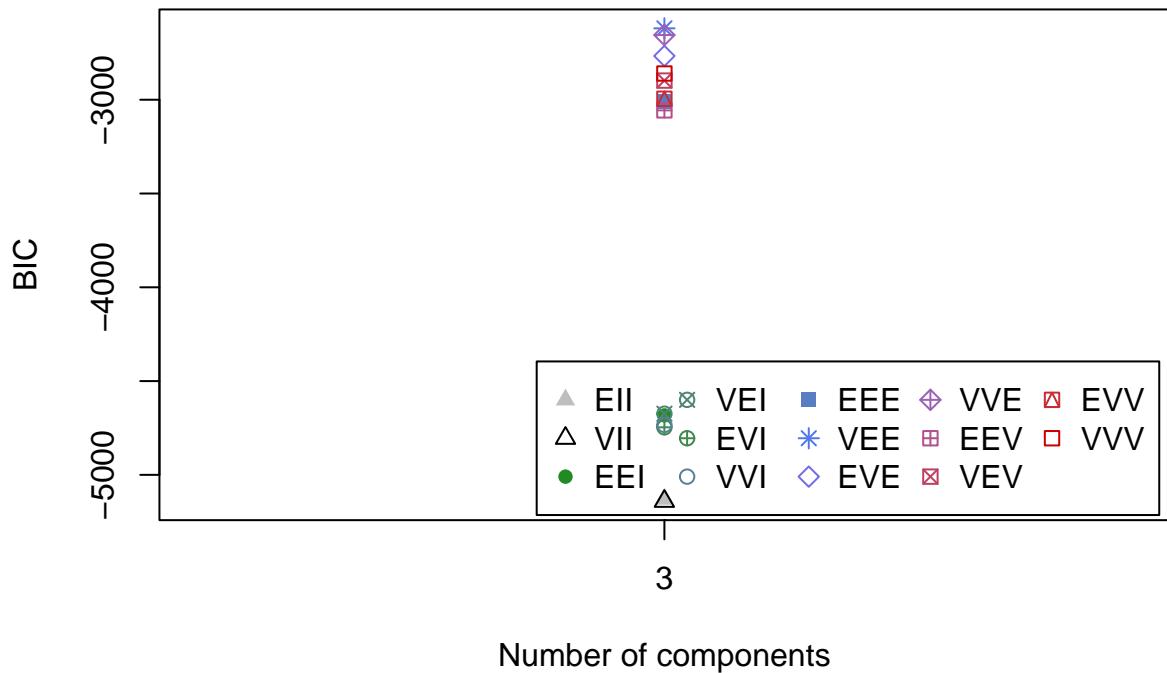
```

sort(model_based3$uncertainty, decreasing = TRUE) %>% head()

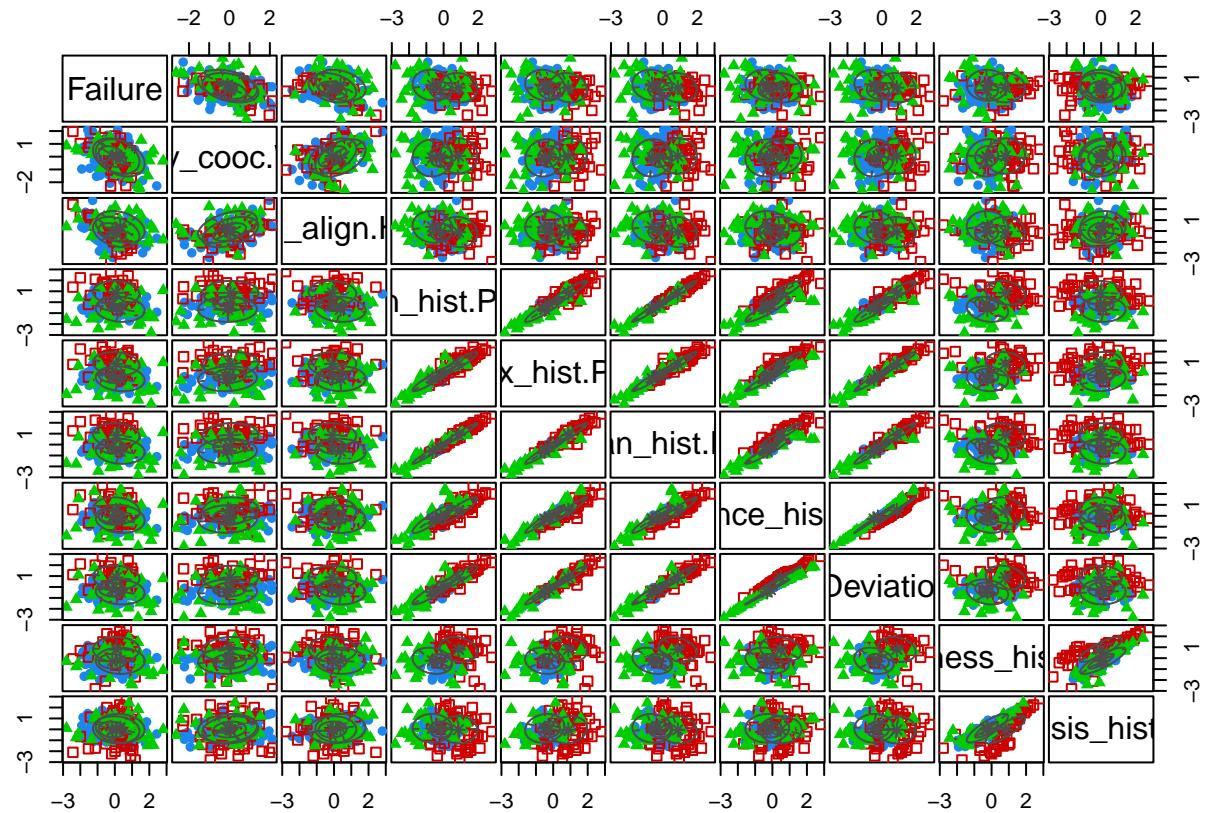
## [1] 0.4896053 0.4872327 0.4812039 0.4638017 0.4255382 0.3886809

legend_args <- list(x = "bottomright", ncol = 5)
plot(model_based3, what = 'BIC', legendArgs = legend_args)

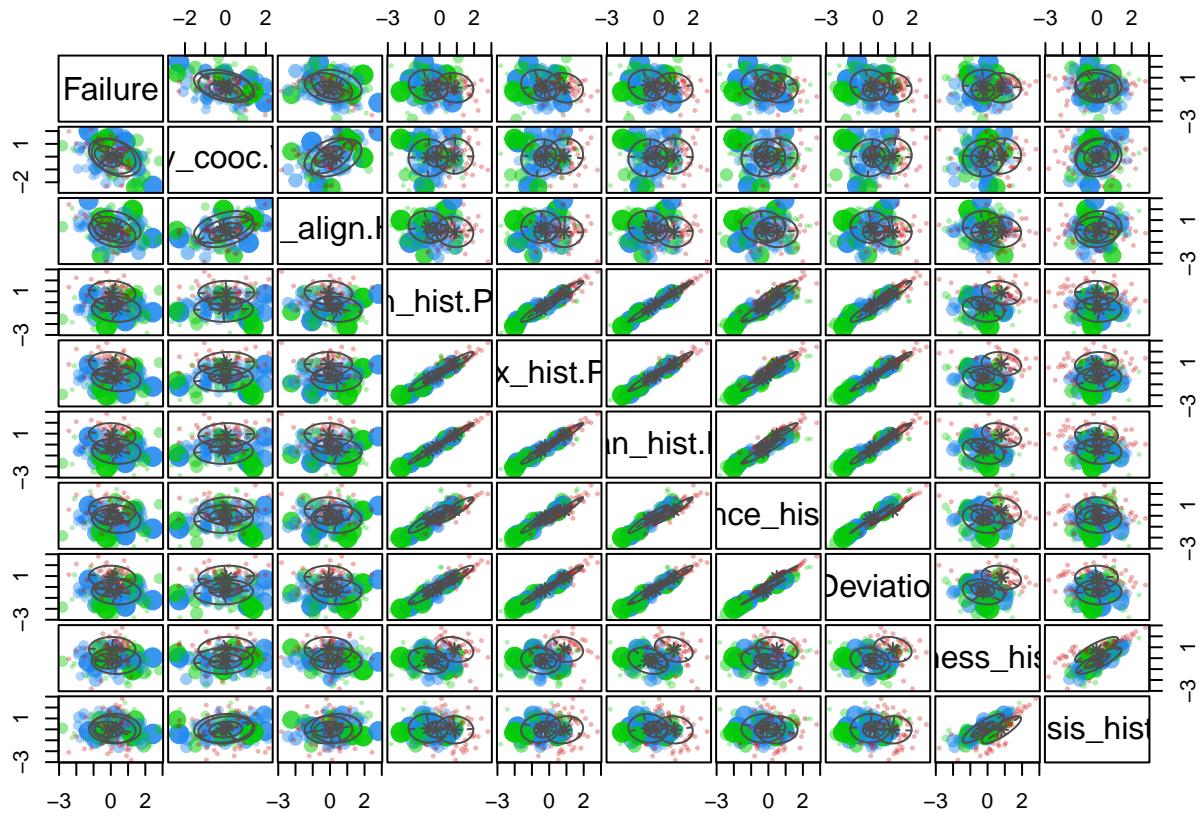
```



```
plot(model_based3, what = 'classification')
```



```
plot(model_based3, what = 'uncertainty')
```



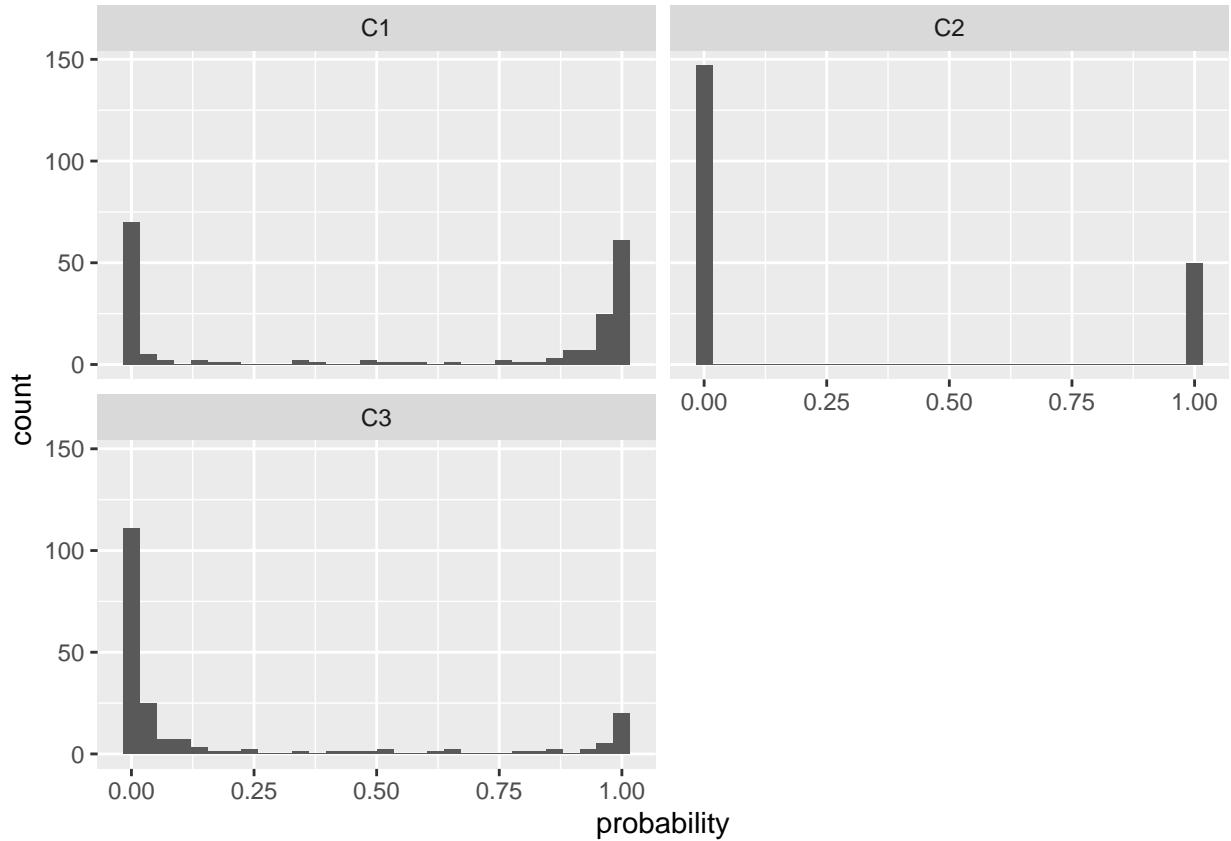
```
probabilities <- model_based3$z
colnames(probabilities) <- paste0('C', 1:3)
```

```
probabilities <- probabilities %>%
  as.data.frame() %>%
  mutate(id = row_number()) %>%
  tidyr::gather(cluster, probability, -id)
```

Plot the observations that are aligned to each cluster but their uncertainty of membership is greater than 0.25.

```
ggplot(probabilities, aes(probability)) +
  geom_histogram() +
  facet_wrap(~ cluster, nrow = 2)

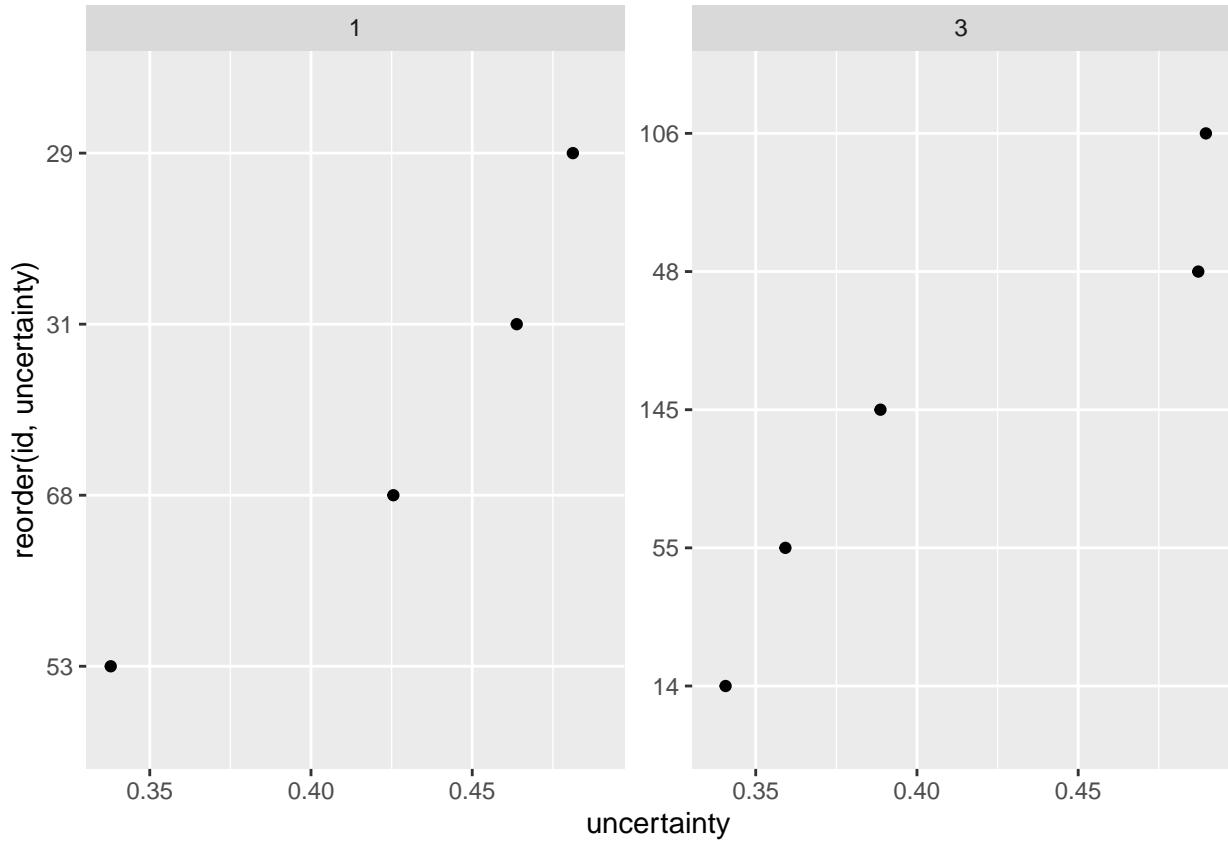
## 'stat_bin()' using 'bins = 30'. Pick better value with 'binwidth'.
```



```
uncertainty <- data.frame(
  id = 1:nrow(radiomics_data),
  cluster = model_based3$classification,
  uncertainty = model_based3$uncertainty
)
```

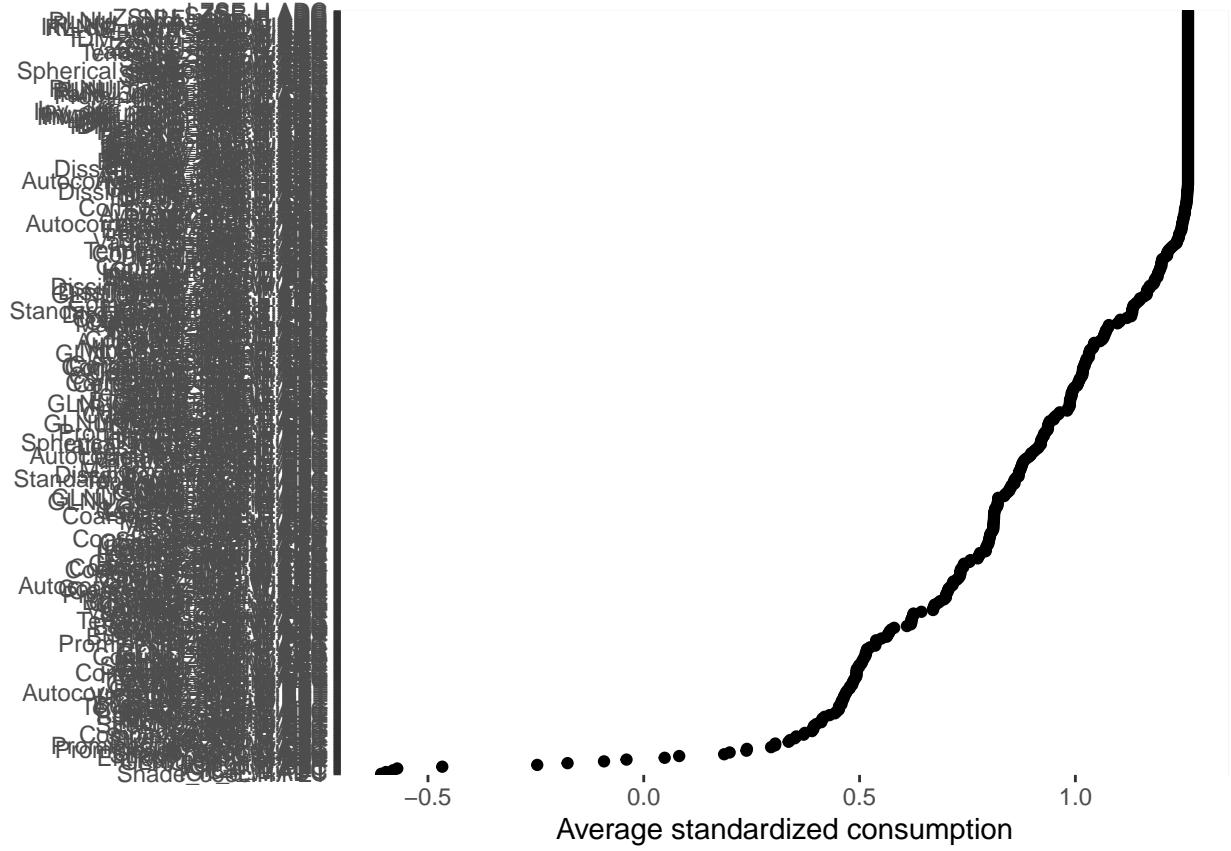
Plot the average standardized consumption for cluster 2 observations compared to all observations.

```
uncertainty %>%
  group_by(cluster) %>%
  filter(uncertainty > 0.25) %>%
  ggplot(aes(uncertainty, reorder(id, uncertainty))) +
  geom_point() +
  facet_wrap(~ cluster, scales = 'free_y', nrow = 1)
```



```
cluster2 <- radiomics_data %>%
  scale() %>%
  as.data.frame() %>%
  mutate(cluster = model_based3$classification) %>%
  filter(cluster == 2) %>%
  select(-cluster)
```

```
cluster2 %>%
  tidyrr::gather(product, std_count) %>%
  group_by(product) %>%
  summarize(avg = mean(std_count)) %>%
  ggplot(aes(avg, reorder(product, avg))) +
  geom_point() +
  labs(x = "Average standardized consumption", y = NULL)
```



The advantage of model-based clustering over K-means and hierarchical clustering is that it automatically determines the ideal number of clusters. In this clustering, Gaussian mixture models is applied, which are one of the most popular model-based clustering approaches available. Using df values in k-means clustering since it is already standardized, we can use `Mclust()` function. Leaving G = NULL forces `Mclust()` to evaluate 1–9 clusters and select the optimal number of components based on BIC.